

# Assessment of membrane plants for biogas upgrading to biomethane at zero methane emission

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## Abstract

In the future energy infrastructure there is a considerable potential for biogas and, in particular, for biomethane as a natural gas substitute. Among the alternatives of upgrading biogas to biomethane, this work focuses on membrane permeation. Taking cellulose acetate as membrane material and spiral-wound as membrane configuration, five layouts are assessed. All layouts have the same biogas plant rated at 500 m<sup>3</sup>/h (STP), yet they may adopt: (i) one- or two-stage permeation, (ii) permeate or residue recycle, and (iii) a water heater or a prime mover (internal combustion engine or a micro gas turbine) to exploit residues as fuel gas. Since residues are consumed, all layouts have zero emission of methane into the atmosphere. The membrane material is modeled considering the phenomenon of plasticization; the membrane modules are described by a crossflow permeation patterns without pressure drops. The results indicates that specific membrane areas range from 1.1 to 2.4 m<sup>2</sup>h/m<sup>3</sup> (STP), specific energy from 0.33 to 0.47 kWh/m<sup>3</sup> (STP), and exergy efficiencies from 57.6% to 88.9%. The splitting of permeation over two stages and the adoption of water heater instead of prime movers is a convenient option. The preferred layout employs a single compressor, a two-stage membrane permeation at 26 bar, a water heater fueled by the first-stage permeate, and a second-stage permeate recycle. Assuming a biomethane incentive of 80 €/MWh<sub>LHV</sub> and a project life of 15 years, the total investment of this plant is 2.9 M€, the payback time 5 years and the net present value 3.5 M€.

*Keywords: biomethane; biogas upgrading; membrane; natural gas substitute; process simulation.*

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## 24 **1 Introduction**

25 The future energy infrastructure will be based likely and largely on renewable sources. In this scenario,  
26 there is a considerable potential for biogas production from anaerobic digestion of agricultural byproducts,  
27 animal manure and slurry. Holm et al. [1] estimate that at least 25% of the whole bioenergy produced in  
28 Europe can originate from the digestion of wet biological materials.

29 The composition of a biogas depends strongly on the organic substrate and the digestion conditions.  
30 Typically, biogas has two main constituents, methane and carbon dioxide, and other minor components,  
31 water, hydrogen sulfide, nitrogen and oxygen, as well as ammonia and other organic components in very  
32 low quantities. The bulk presence of carbon dioxide reduces significantly the calorific value of the gas,  
33 whereas the minor components may lead to critical operational problems, like corrosion and clogging.  
34 Thus, biogas upgrading to a higher quality combustible gas, the so-called biomethane, requires removing  
35 most of that carbon dioxide and of the minor components. Their removal may be achieved by a variety of  
36 processes. Ryckebosch et al. [2] provide an accurate review of a large number of these processes, including  
37 the membrane systems that are the focus of this assessment. According to the review, the main advantages  
38 of the membrane technology are simple construction, easy operation and high reliability, while the general  
39 disadvantages are a low selectivity and the possibility of requiring multiple stages.

40 Technologies for the carbon dioxide separation differ by physical principle, plant layout, removal  
41 effectiveness, energy requirements, investment costs, operational efforts as well as the amount of  
42 methane that may be unrecovered. Among these technologies, membranes are recognized to be simple,  
43 reliable and modular. However, they may require multiple stages to achieve high purities at low methane  
44 losses, they cannot recover completely the methane, and they have not found yet a large market diffusion.  
45 Nevertheless, market share will predictably increase as membrane materials are improving.

46 The present paper focuses specifically on agricultural biogas due to the larger potential of this substrate  
47 compared to others. Agricultural biogas plants are usually small, located in rural areas, and operated by

48 very few technicians.<sup>†</sup> In this rural context, the biogas upgrading process must be simple and reliable.  
49 Naturally, the membrane technology is chosen for the scope. Among all possible materials and modules,  
50 cellulose acetate spiral-wound membranes are selected because, despite they are not the best performing  
51 option, they are common and robust, as demonstrated by UOP Separex™ and former Grace Membrane  
52 Systems technologies [3, Table 2], meeting the mentioned requirement of simplicity and reliability set for  
53 the installation in the agricultural sites.

54 Five layouts of the membrane plant, alternatively connected to the same biogas plant, are assessed here  
55 from energy, economic and exergy perspectives. All plants produce pipeline-quality biomethane, inject it  
56 into a mid-pressure (5-10 bar) natural gas pipeline, and avoid emitting methane into the atmosphere. The  
57 plants differ by:

- 58 • number of membrane stages (one or two),
- 59 • presence and type of recycles (permeate or residue),
- 60 • type of system utilizing the residue gas as fuel gas to avoid the methane emission (internal  
61 combustion engine, micro turbine and heater).

62 All layouts are first optimized economically, as a function of the operational parameters, and then  
63 compared against each other. The objective is to determine the strategic layout with the best overall  
64 performances. The exergy analysis is employed to identify the major sources of thermodynamic losses.

65 Methodologically, all layouts are modeled with a bottom-up approach through three levels:

- 66 • membrane material (here cellulose acetate as said),
- 67 • membrane module (spiral-wound),
- 68 • membrane process (five alternative layouts).

69 The models of membrane plants include all the necessary operational units (compressors, air coolers, and  
70 fuel gas utilizers) that constitute the upgrading process. The biogas plant is instead defined in an

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<sup>†</sup> Here biogas plant refers to the system that converts wet biomass into dehumidified and desulfurized biogas, which could be used in internal combustion engines, while membrane plant to the system that upgrades that biogas into biomethane by membrane technology.

71 approximate manner because of its minor interest from the overall process perspective. All models are  
72 implemented in a Matlab code developed for the purpose.

73 To the best knowledge of the authors, the novelty of this paper resides first in the types of considered  
74 layouts, which may employ a micro gas turbines as opposed to the commonly considered internal  
75 combustion engines or which may combine multiple membrane stages with a heater. Moreover, the biogas  
76 plant and the membrane plant are simulated altogether, while most of the studies focus only on the latter.  
77 Finally, the simulations do not consider only mass and energy balances, but also an economic assessment  
78 over the entire plant lifetime and an exergy evaluation, both of which are original.

79 The following sections provide in sequence: a general bibliographic review on membrane materials,  
80 modules and processes; a description of the considered plants as well as of the numerical models; the  
81 numerical results along with their discussion and, ultimately, the conclusions and the future developments.

## 82 **2 Bibliographic review**

83 The next paragraphs review those studies that provide an overview on the topic or that focus on the three  
84 scales of the problem: materials, modules and process. For completeness, the sections include cellulose  
85 acetate and polyimide as well as spiral-wound and hollow-fiber membranes, despite this assessment covers  
86 solely cellulose acetate spiral-wound membranes.

### 87 **2.1 Overview**

88 Baker [4] describes the membranes from the lower scale of solution-diffusion mechanism to the larger  
89 scale of commercial plants. Membrane modules for carbon dioxide removal from methane-rich streams are  
90 technically viable. They turn economically competitive for flow rates smaller than 3,500 m<sup>3</sup>/h at the  
91 Standard Temperature and Pressure (STP) conditions of 0°C and 1 bar. This statement is in agreement with  
92 the plant size adopted in this work of 500 m<sup>3</sup>/h (STP), as outlined in Section 3.

93 A review of biogas upgrading by membrane technology is provided by Scholz et al. [5]. According to the  
94 authors, available materials are suitable for harsh working conditions of high pressure (around 25 bar) and

95 of chemically aggressive components ( $H_2S$ , in particular when  $H_2O$  is also present). Single-stage permeation  
96 processes are not able to simultaneously produce a high  $CH_4$  purity and obtain a high  $CH_4$  recovery. Hence,  
97 multistage layouts become mandatory. Both Baker [4] and Scholz et al. [5] highlight the need for utilizing or  
98 even flaring the permeate gas. Sharing this observation, the present work considers only layouts that utilize  
99 entirely the permeate.

## 100 **2.2 Materials**

101 There are many materials proposed for biogas upgrading. According to Basu et al. [6], the most common for  
102 commercial applications are polymeric materials, in particular cellulose acetate and polyimide.  
103 Harasimowicz et al. [7] report that the high permeability of the polyimide membranes to  $H_2O$  and  $H_2S$   
104 makes them useful for biogas processing without special pre-treatment, while cellulose acetate  
105 membranes, which are sensitive to water vapor, require water removal. The biogas upgrading layouts  
106 considered here comprise both  $H_2O$  and  $H_2S$  abatements.

107 A problem of polymeric membrane is plasticization, which is the sorption of  $CO_2$  in the polymer matrix that  
108 causes a higher polymer chain mobility and, ultimately, a higher mass transport of all gases. Lee et al. [8]  
109 describe the effect of plasticization in cellulose acetate membranes by a modified dual-mode theory with  
110 concentration-dependent diffusivities, whereas Kanehashi et al. [9] illustrate the plasticization in a  
111 polyimide membrane. Both these materials show an appreciable plasticization at pressures above the  
112 threshold of 10 atm, which can be raised to 30 atm by special material treatment. The work of Lee et al. [8]  
113 is taken as reference for the material modeling (Section 4.1).

## 114 **2.3 Modules**

115 Commercial membranes for gas separation applications are usually spiral-wound or hollow-fiber modules.  
116 The later modules can be designed in coflow, counterflow and crossflow arrangement, while the former in  
117 crossflow. Their mathematical models can be solved analytically for simplified cases or numerically for  
118 general applications. The analytical solution for crossflow gas permeation of binary mixtures under  
119 simplifying condition is presented first by Weller and Steiner in 1950 [10], and extended by Stern and

120 Walavender in 1969 [11], who also correct the membrane area calculation for the crossflow case. These  
121 analytical solutions are used here to verify the correct model implementation under simplifying  
122 assumptions, as noted in Section 4.2.

123 A simple yet robust numerical solution for multicomponent crossflow systems is outlined by  
124 Kohl and Nielsen [12, Ch. 15]. This solution considers small incremental areas of the membrane (namely,  
125 succession of stages): a permeation analysis and a material balance are performed on the first incremental  
126 area, the residue gas from this area is treated then as the feed to the next area and the operation is  
127 repeated iteratively. Thundyl and Koros [13], Tessendorf et al. [14], as well as Makaruk and Harasek [15]  
128 present optimal algorithms for multicomponent gas separation in coflow, counterflow and crossflow  
129 configurations, proving that crossflow is more effective than coflow always and than counterflow in some  
130 cases. Despite the simplicity, the approach by Kohl and Nielsen [12, Ch. 15] is adapt for this study.

## 131 **2.4 Processes**

132 Membrane plants for natural gas and biogas upgrading share the feature of separating carbon dioxide from  
133 a methane-rich stream. Hao et al. [16,17] describe technically and economically polyimide membranes for  
134 both CO<sub>2</sub> and H<sub>2</sub>S separation in single- and multi-stage layouts with various recycle options.

135 Qi and Henson [18] describe different layouts based on spiral-wound modules for natural gas treatment  
136 and enhanced oil recovery. The most promising schemes by Hao et al. [16,17] and Qi and Henson [18] are  
137 taken as reference in this assessment.

138 Makaruk et al. [19] investigate diverse membrane systems for biomethane production, including single- and  
139 double-stage arrangements. The authors state that single-stage and double-stage cascade with permeate  
140 recycle provide good flexibility for the integration with biogas plants and that the specific electric  
141 consumption for biogas upgrading is about 0.3 kWh/m<sup>3</sup> (STP). In addition, they propose the use of the  
142 permeate gas as a fuel for either an internal combustion engine, in single-stage layouts, or a  
143 porous/catalytic burner, in double-stage layouts.

144 Finally, Deng and Hägg [20] study an efficient CO<sub>2</sub>-selective polyvinylamine/polyvinylalcohol (PVAm/PVA)  
145 blend membrane by conducting an experimental analysis of the material and, then, a numerical simulation  
146 of a whole plant. They consider a farm-scale system rated at 1000 m<sup>3</sup>/h (STP) and four layouts. The double-  
147 stage cascade layout with residue recycle is proven optimal among the four processes with an area,  
148 expressed in specific terms with respect to the produced biomethane, of 1.69 m<sup>2</sup>h/m<sup>3</sup> (STP) and a specific  
149 electric consumption of 0.29 kWh/m<sup>3</sup> (STP) [20, Table 6 – case c]. The investment of the optimal membrane  
150 plant is 3.06 M\$. The energy and economic results by Makaruk et al. [19] and by Deng and Hägg [20] are  
151 taken as reference for the present work (Section 5.3).

### 152 **3 Plant description**

153 The present work assumes a biogas plant rated at 500 m<sup>3</sup>/h (STP). The raw biogas is treated to separate  
154 water by condensation and adsorption on silica and hydrogen sulfide by adsorption on “iron sponges” prior  
155 to entering the membrane plant. The adsorption cartridges are replaced periodically and regenerated  
156 externally from the plant. The biogas plant is connected to a membrane plant, which may have five  
157 alternative layouts. Membrane material is cellulose acetate, while module is spiral-wound. The five plant  
158 layouts include single- and double-stage arrangements, residue and permeate recycles, and diverse residue  
159 utilizations as fuel gas as describe in the following sections.

#### 160 **3.1 Biogas plant**

161 The biogas plant has three main electrical power consumptions for: (i) the biomass handling and conveying  
162 to the digester, (ii) the mixing of the biomass within the digester and (iii) the drying of the biogas prior to  
163 entering the membrane plant. In addition, it has a thermal power utilization to keep the digesters at the  
164 optimal temperature (35 to 55°C). Electrical and thermal power requirements are treated as lumped sums.

#### 165 **3.2 Membrane plants: the five layouts**

166 The membrane plants differ by type, number and arrangement of the operational units. They may employ a  
167 diverse number of air-cooled oil-free reciprocating compressors (indicated by the acronym CMP). They may

168 have one or two membrane stages (MBR). Membranes operate at a pressure higher than the 5-10 bar grid  
169 assumed here, so that biomethane is throttled into the pipeline. Because it is not possible to recover the  
170 whole of the methane, all membrane layouts adopt a way to utilize the permeate as a fuel gas in a  
171 combustion process. This way may be an internal combustion engine (ICE), a micro gas turbine (MGT), or  
172 simply a conventional water heater (HTR). Engine, turbine and heater work at the minimum methane  
173 fraction in the fuel gas allowed by the technology. Moreover, internal combustion engines and micro gas  
174 turbines produce electrical power that is partly consumed on-site and partly exported to grid, and thermal  
175 power that is partly consumed on-site and partly dissipated into the ambient. The conventional water  
176 heater produces thermal power that is consumed on-site and partly dissipated when in excess. The five  
177 layouts are as follows.

178 Layout 1 Single-stage permeation and internal combustion engine (Figure 1).

179 Layout 2 Single-stage permeation and micro gas turbine (Figure 2).

180 Layout 3 Double-stage permeation with second-stage permeate recycle, single-stage compression and  
181 heater (Figure 3).

182 Layout 4 Double-stage permeation with second-stage residue recycle, first-stage permeate recompression  
183 and heater (Figure 4).

184 Layout 5 Double-stage permeation with second-stage permeate recycle, two-stage compression and micro  
185 gas turbine (Figure 5).

186 Layout 1 and Layout 2 are the basic membrane layouts in which the permeate is used as a fuel gas in a  
187 power cycle. Layout 1 adopts an internal combustion engine as power cycle because it is the most common  
188 technology in the biogas sector. In contrast, Layout 2 adopts a micro gas turbine that can work on a poorer  
189 fuel gas (lower methane content) because it utilizes a dedicated component, the combustor, to burn the  
190 gas. As a positive consequence, Layout 2 allows for a higher biomethane production. However, the micro



191 gas turbine requires a compressor to increase the pressure of the fuel gas.<sup>‡</sup> In both layouts a biogas bypass  
192 is necessary to increase the methane content in the permeate.

193 Layout 3 is an evolution of the previous two layouts in which the fuel gas utilizer is a water heater that can  
194 work on an even poorer gas than the micro gas turbine. Given typical values of membrane selectivity, it is  
195 impossible to achieve a very high methane content in the residue and, simultaneously, a low content in the  
196 permeate. Therefore, a second stage of permeation is needed. In Layout 3, this second stage processes the  
197 residue from the first stage in order to produce the biomethane for the grid. In its turn, the permeate from  
198 the second stage, which has a high methane content, is recycled back to the compressor.

199 Layout 4 is an alternative to Layout 3 in which the second stage of permeation processes the permeate (not  
200 the residue) from the first stage in order to produce the fuel gas for the heater (not the biomethane for the  
201 grid). A second compressor is required for increasing the permeate pressure to the same level as the first  
202 compressor (in other words, the two compressors have the same discharge pressure). In its turn, the  
203 residue from the second stage is recycled back to the first membrane.

204 Finally, Layout 5 is an evolution of Layout 2, inspired by Layout 3, in which there are two permeation stages  
205 working at two different pressure levels. The second permeation stage processes the residue from the first  
206 stage (similarly to Layout 3), but it operates at a higher pressure (contrarily to Layout 3). Compared to the  
207 compressor of Layout 2, the compressors of Layout 5 work at lower pressure ratios and flow rates. The  
208 permeate from the second stage is recycled to the first compressor (similarly to Layout 3).

## 209 **4 Plant simulations**

210 The mathematical model developed for the analysis of the membrane plants is based on the following  
211 general assumptions:

- 212 • water and hydrogen sulfide are not considered because separated prior to the membrane plant,

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<sup>‡</sup> In general, packaged micro gas turbines working on natural gas from the grid are equipped with a gas compressor; nevertheless, it is preferred here to keep the compressor separated from the package because the flow rate of the fuel gas is higher than the natural gas case given that the methane content is lower.

- 213 • biogas consists exclusively in methane and carbon dioxide,
- 214 • both gases behaves as ideal gases,
- 215 • their heat capacities at constant pressure in the ideal gas stated are described via the Shomate
- 216 equation with coefficients derived from the NIST Webbook [21],
- 217 • cellulose acetate is taken as membrane material,
- 218 • plasticization is taken into consideration,
- 219 • spiral-wound is taken as membrane modules,
- 220 • pressure drops are neglected,
- 221 • membranes are operated at a pressure higher than the natural gas pipeline pressure (biomethane
- 222 is then throttled easily to pipeline pressure),
- 223 • the requirement on methane content for injection into pipelines is typical for European countries,
- 224 • the economical analysis is based on a conventional Net Present Value (NPV) analysis.

225 Concerning thermodynamic properties, specific enthalpy, entropy and exergy of any CO<sub>2</sub>-CH<sub>4</sub> mixture at any  
 226 state derive from the proper integration of the equation of the heat capacity. Reference conditions are of  
 227 minor importance for energy, entropy and (physical) exergy balances because the flows are non-reactive.  
 228 Only the reference chemical exergy of methane is important for the exergy assessment.

#### 229 **4.1 Material**

230 The expression of the permeance of CO<sub>2</sub> (component 1) and of CH<sub>4</sub> (component 2) through the material as  
 231 a function of their partial pressures in presence of plasticization is taken from Lee et al. [8]. The permeance  
 232 of CO<sub>2</sub>,  $P_1$ , turns to be:

$$P_1 = \frac{D_1^\circ/\delta}{(\beta_1 + \beta_2 B)(p_{h_1} - p_{l_1})} \left\{ \exp \left[ (\beta_1 + \beta_2 B) \left( k_{D_1} p_1 + \frac{C'_H b_1 p_1}{1 + b_1 p_1 + b_2 p_2} \right) \right] \right\}_{p_l}^{p_h} \quad (1)$$

233 while the permeance of CH<sub>4</sub>,  $P_2$ :

$$P_2 = \frac{D_2^\circ/\delta}{\left(\frac{\beta_1}{B} + \beta_2\right)(p_{h_2} - p_{l_2})} \left\{ \exp \left[ \left( \frac{\beta_1}{B} + \beta_2 \right) \left( k_{D_2} p_2 + \frac{C'_H b_2 p_2}{1 + b_1 p_1 + b_2 p_2} \right) \right] \right\}_{p_l}^{p_h} \quad (2)$$

234 where  $\delta$  is the membrane thickness,  $D_i^\circ$  is the effective diffusivity of the  $i$ -th component at infinitely dilute  
 235 concentration,  $\beta_i$  a parameter related to the effective diffusivity to be determined by nonlinear regression,  
 236  $k_{D_i}$  the dissolution coefficient,  $C'_H$  the saturated concentration of adsorbed gas,  $b_i$  the adsorption  
 237 equilibrium constant,  $p_{h_i}$  and  $p_{l_i}$  the partial pressures in the high pressure side and in the low pressure side  
 238 respectively. The braces contain the difference of the exponentials evaluated at the high- and the low-  
 239 pressure sides. Lastly, the parameter  $B$  is:

$$B = \frac{k_{D_2} p_{h_2} (1 + b_1 p_{h_1} + b_2 p_{h_2}) + C'_H b_2 p_{h_2}}{k_{D_1} p_{h_1} (1 + b_1 p_{h_1} + b_2 p_{h_2}) + C'_H b_1 p_{h_1}} \quad (3)$$

## 240 4.2 Module

241 The spiral-wound modules adopted in this work are modeled as crossflow systems. The analytical solution  
 242 proposed by Weller and Steiner [10], later corrected by Stern and Walawender [11], cannot be employed  
 243 because the permeance of the components are not constant, but affected by the concentration through  
 244 the plasticization equations 1 and 2.<sup>§</sup> The simple and robust iterative approach illustrated by Kohl and  
 245 Nielsen [12] is simplified from the multicomponent case to this binary problem. According to their  
 246 approach, a process simulation can be made by considering small incremental areas of the membrane. A  
 247 permeation analysis and a material balance are performed on the first incremental area. The residue gas  
 248 from this area is treated as the feed to the next area, and the operation is repeated sequentially.

249 For the  $k$ -th incremental area, the composition of the permeate side, i.e. the low-pressure side, for a binary  
 250 mixture in a crossflow membrane can be expressed as [4]:

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<sup>§</sup> The analytical model is utilized anyhow to validate the numerical model imposing constant values for the component permeances.

$$x_{l_i}^{(k)} = \frac{\varphi}{2} \left[ x_{h_i}^{(k)} + \frac{1}{\varphi} + \frac{1}{\alpha^{(k)} - 1} - \sqrt{\left( x_{h_i}^{(k)} + \frac{1}{\varphi} + \frac{1}{\alpha^{(k)} - 1} \right)^2 - \frac{4\alpha^{(k)} x_{h_i}^{(k)}}{(\alpha^{(k)} - 1)\varphi}} \right] \quad (4)$$

251 where  $x_{h_i}^{(k)}$  and  $x_{l_i}^{(k)}$  are the  $i$ -th component feed and permeate compositions respectively,  $\alpha^{(k)}$  the  
 252 selectivity ( $P_1/P_2$ ), and  $\varphi$  is the pressure ratio ( $p_h/p_l$ ), which is the only parameter independent from  $k$ .  
 253 For the particular case of crossflow pattern,  $x_{l_i}^{(k)}$  is only dependent on  $x_{h_i}^{(k)}$  and  $\varphi$ , but not on  $x_{l_i}^{(k-1)}$ .  
 254 Because the calculation of permeances is a function of CO<sub>2</sub> and CH<sub>4</sub> partial pressures at each  $k$ -th  
 255 incremental area, the resulting set of equations at any incremental area comprises the three implicit  
 256 equations 1, 2 and 4. The set of equations must be solved iteratively by direct substitution at each  
 257 incremental area in sequence. Once the  $k-1$  incremental area is solved, the high-pressure composition of  
 258 the  $k$ -th area is known (thanks to equation 8 reported below). Next, the permeances of  $k$ -th area are taken  
 259 equal to those of  $k-1$  area as a first guest. At this point the iterative procedure starts: the low-pressure  
 260 composition is computed according to equation 4 and the new permeances according to equation 1 and 2.  
 261 These new values of permeances are substituted over the previous values iteratively until the maximum  
 262 variation among new and old values is below a desired tolerance.  
 263 Once the permeate composition is solved, the molar flow of the  $i$ -th component through the  $k$ -th small  
 264 incremental area is (see Figure 6):

$$M_i^{(k)} = P_i^{(k)} \left( x_{h_i}^{(k)} p_h - x_{l_i}^{(k)} p_l \right) \Delta A \quad (5)$$

265 where  $M_i^{(k)}$  is the  $i$ -th component molar flow across the membrane and  $\Delta A$  is the small incremental area,  
 266 chosen arbitrarily. The increase in permeate molar flow of the  $i$ -th component,  $O_i^{(k+1)}$ , at each  $\Delta A$  is:

$$O_i^{(k+1)} = O_i^{(k)} + M_i^{(k)} \quad (6)$$

267 whereas the corresponding decrease in residue molar flow,  $N_i^{(k+1)}$ , is:

$$N_i^{(k+1)} = N_i^{(k)} - M_i^{(k)} \quad (7)$$

268 and the boundary conditions are as follows:  $O_i^{(1)}$  is null and  $N_i^{(1)}$  is equal to the  $i$ -th component molar flow  
 269 in the feed.

270 The residue molar composition is updated as:

$$x_{h_i}^{(k+1)} = \frac{N_i^{(k+1)}}{\sum_i N_i^{(k+1)}} \quad (8)$$

271 while the membrane area as:

$$A^{(k+1)} = A^{(k)} + \Delta A \quad (9)$$

272 The procedure is repeated until the desired residue molar composition is met. Each increment of area is  
 273 accumulated so that total area required is known, as well as the gas compositions and flows in the residue  
 274 and in the permeate. The smaller the taken value of incremental area, the more accurate the result.

### 275 4.3 Process

276 In a membrane plant at least three operational units are required in addition to the membrane modules:  
 277 gas compressors, gas coolers, and utilizer of the permeate gas as a fuel gas. In this work, compressors and  
 278 coolers are combined in electric air-cooled oil-free reciprocating packages; compressors are characterized  
 279 by constant isentropic and electric efficiencies, while coolers by a constant electric consumption per unit of  
 280 heat dissipated. Concerning the permeate utilizers, internal combustion engines, micro gas turbines and  
 281 water heaters are modeled with constant electrical and thermal efficiencies. The three utilizers differ in the  
 282 value of the efficiencies and, importantly, in the minimum methane content in the fuel gas.

283 Mass, energy and exergy balances of the single units and the overall plant are executed by way of Classical  
 284 Thermodynamics. In particular, the exergy efficiency of whole plant is defined as the ratio of the exiting  
 285 exergy flow (biomethane from the membrane plant and electricity if produced) and the entering exergy  
 286 flow (biomass to the biogas plant and electricity if consumed). For simplicity, the exergy flow of the

287 entering biomass is taken equal to the exergy flow of the biogas to the membrane plant. Electrical and  
288 thermal powers consumed within the biogas plant are treated as wasted.

289 Biogas upgrading plants are assessed economically by way of the conventional Net Present Value (NPV)  
290 analysis. It is assumed that the total investment is paid in full at the instant “present”, which is the moment  
291 the plant goes into operation. Cash flows are transacted at the end of each operation year for the total  
292 duration of the project lifetime.

293 The total investment is the sum of the biogas plant and the membrane plant costs. The biogas plant cost is  
294 treated as a constant lumped sum. In contrast, the membrane plant cost is estimated from the total base  
295 equipment cost, which is the sum of the costs of the main operational units (membranes, compressors,  
296 coolers, and permeate utilizers), following the single-factor method of Perry’s Handbook [22, Ch. 9]. The  
297 cost of each unit, but the membrane modules, is evaluated by the exponential method [22]; the membrane  
298 module cost is simply linear with the membrane area. Ultimately, the total base equipment cost is  
299 increased by the single factor to yield the membrane plant investment. This factor is referred to as Balance  
300 of Plant (BOP) and expressed as a percentage.\*\*

301 Cash flows comprise yearly incomes, expenditures and taxes, which are all assumed to be constant over the  
302 project lifetime. Incomes include the sale of biomethane. Electricity may be purchased or sold to the grid,  
303 depending on the plant layout, and thus may fall among expenditures or incomes. Yearly amounts of  
304 biomethane and electricity are computed via the capacity factor. Expenditures include also the cost of the  
305 biomass supplied to the biogas plant as well as the cost of the Operation and Maintenance (O&M). In its  
306 turn, O&M cost is the sum of the costs for all the operational units and the cost for the remainder of the  
307 plant. The latter O&M cost is estimated as a fraction of the total investment. Taxes are computed as a  
308 fraction of the earnings, while earnings are simply the incomes subtracted by expenditures and by  
309 amortization. The amortization is calculated as the total investment divided by the project lifetime.

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\*\* For example, if the total base equipment cost for the membrane plant is 100 k€ and the BOP is 200%, the membrane plant investment is  $100 \cdot (1 + 200\%) = 300$  k€.

310 Ultimately, the NPV of each plant is determined discounting the yearly cash flows to the instant “present”  
311 by a weighted average cost of the capital.

#### 312 **4.4 Assumed parameters**

313 Several parameters are employed in the simulations. The parameters for equations from 1 to 3 referring  
314 specifically to the adopted material, cellulose acetate, are listed in Table 1. All other parameters can be  
315 divided into two major groups: technical parameters (mostly on the left side of Table 2) and economical  
316 parameters (right side). The technical parameters include: the characteristics of the dried gas from the  
317 biogas plant to the membrane plant as well as the characteristics of the biomethane injected into the grid;  
318 technical specifications of compressors, coolers, internal combustion engines, micro gas turbines, heaters;  
319 and references for the energy and the exergy analyses. The economical parameters include: fixed costs,  
320 cash flow parameters, and NPV factors. In particular, the dried biogas composition adopted here is typical  
321 of the anaerobic digestion of a mixture containing mainly animal manure and partly energy crops.

#### 322 **4.5 Free parameters and their optimization**

323 The free parameter for Layout 1 thru Layout 3 is the discharge pressure of the compressor. Similarly, the  
324 only free parameter for Layout 4 is the discharge pressure of the first compressor, as the second one has  
325 the same pressure level. Lastly, the free parameters of Layout 5 are the discharge pressures of both  
326 compressors as well as the carbon dioxide content in the permeate from the first permeation stage. The  
327 mentioned free parameters of each layout are optimized in order to maximize the NPV of that layout over  
328 its lifetime.

### 329 **5 Plant results and discussion**

330 Model and assumptions are benchmarked with respect to a conventional biogas plant, in which biogas itself  
331 is utilized totally in an internal combustion engine to produce electricity. The code is employed then to  
332 optimize the five layouts of the membrane plant in order to, as explained above, maximize the NPV of all  
333 layouts. The optimal results are reported in Table 3 and discussed below. Subsequently, a sensitivity

334 analysis of the biomethane incentive, which is a fundamental parameter, is executed and, lastly, an insight  
335 into the exergy and economic analyses of the preferred layout is provided.

## 336 **5.1 Methodology benchmark**

337 The methodology is benchmarked by assessing a conventional biogas plant that exports only electricity  
338 produced via an internal combustion engine. In this case, the BOP is taken equal to 100%, in contrast to the  
339 value reported in Table 2 for the membrane plant, because it is a consolidated technology. For this  
340 validation plant, the assessment returns that the engine is rated at 1094 kW<sub>e</sub>, the thermal power exceeds  
341 by far the biogas plant requirement, the net electrical power to the grid is 994 kW<sub>e</sub> and the exergy  
342 efficiency 35.1%. From the economical perspective, the total investment is about 4.0 M€, which is  
343 equivalent to a specific cost of 4024 €/kW<sub>e</sub>, the yearly cash flow is 730 k€, the payback time is about 8 years  
344 and the NPV about 2.2 M€. These values are in good agreement with the study by Walla et al. [23] and the  
345 current state of the art.

## 346 **5.2 Layout optimization**

347 The NPV is related linearly with the biomethane incentive through the amount of produced biomethane.  
348 For each layout, the amount of produced biomethane is given by the overall mass balance and, thus, it is  
349 independent from the compressor discharge pressure. Consequently, biomethane incentive and  
350 compressor discharge pressure influence independently the NPV. In other words, the NPV is a linear  
351 combination of two functions, one dependent on the incentive (income) and the other on pressure (total  
352 investment and expenditures). Therefore, the compressor discharge pressure at which the NPV is maximum  
353 is independent from the incentive, as demonstrated numerically below.

354 For Layout 1 to 4, Figure 7 shows the normalized NPV as a function of the pressure for three diverse  
355 incentives (80, 100 and 120 €/MWh<sub>LHV</sub>). Each incentive curve is normalized with respect to its maximum. As  
356 reasoned above, the optimal pressure is independent from the incentive value. The optimal pressures,  
357 ranging from 24 to 26 bar, are slightly higher than 20 bar determined by Deng and Hägg [20]. The  
358 difference is related to the fact that the economical optimization favors higher compressor ratios, and thus



359 more expensive compressors, reducing on the other hand the membrane surface, and thus their  
360 investment and maintenance costs. For Layout 5, Figure 7 shows the normalized NPV as a function of the  
361 second compressor discharge pressure and the CO<sub>2</sub> content in the permeate. The surface is drawn for a  
362 single incentive value (80 €/MWh<sub>LHV</sub>). The optimal pressure is 46 bar, which leads to a first compressor  
363 discharge pressure of 6.8 bar, while the optimal carbon dioxide content in the permeate from the first  
364 stage is 92%. These optimal pressures are achievable via conventional compressors and bearable by  
365 common membranes. The only exception is the second stage of Layout 5, which is relatively high; however,  
366 this layout will not turn to be the preferred one, as reported below.

### 367 **5.3 Overall performances of the optimized layouts**

368 The prediction of membrane areas, compressor sizes, prime mover as well as water heater sizes,  
369 biomethane flow rates and electricity (produced or consumed) of the optimized layouts are included  
370 in Table 3. In specific terms with respect to the produced biomethane, membrane extensions are around  
371 1.1-1.2 m<sup>2</sup>h/m<sup>3</sup> (STP) for Layout 1 to 3, 1.4 for Layout 4 and 2.4 for Layout 5. Layout 4 shows a modestly  
372 larger membrane extension than Layout 1 and 2 because its first membrane stage operates on a greater  
373 flow rate as it adopts a recycle instead of a bypass of the biogas. Moreover, it shows a larger extension than  
374 Layout 3 because its first stage must achieve directly grid-quality requirements, whereas Layout 3 employs  
375 two stages to do so. Layout 5 requires the greatest membrane area because its first stage operates at low  
376 pressure. All layouts, but Layout 5, show lower membrane extensions than those predicted by Deng and  
377 Hägg [20] in strict agreement with the fact that, as reasoned previously, the maximization of NPV favors  
378 larger compressors and smaller modules.

379 The specific separation energy of Table 3 includes only the work for the separation compressors, not the  
380 fuel gas compressor of the micro gas turbine, nor the air-cooler, nor the electricity production when  
381 present in order to make the results comparable with other studies. These three items (fuel gas  
382 compressor, air-coolers and electricity production) are though included in the economic calculations. All  
383 layouts, but Layout 4, have a specific separation energy of 0.33-0.38 kWh/m<sup>3</sup> (STP), which are slightly  
384 higher than the 0.29-0.30 value by Makaruk et al. [19] and by Deng and Hägg [20]. This result is again in

385 strict agreement with the fact that the maximization of the NPV favors larger compressors and smaller  
386 modules. Secondly, the lower compressor efficiency assumed here because biogas flow rate and, thus,  
387 compressor sizes are smaller in this work yielding higher specific energies. The specific separation energy  
388 for Layout 4 is  $0.47 \text{ kWh/m}^3$  that is the highest because the second-stage compressors processes the  
389 permeate, which is at low pressure.

390 Exergy efficiencies of all layouts are appreciable higher than that of the conventional biogas plant, equal to  
391 35.1% (see Section 5.1). The exergy efficiency follow closely the biomethane production. Layout 1 shows  
392 the lowest value of almost 58% with a biomethane production of  $928 \text{ kW}_{\text{LHV}}$ , Layout 2 and 5 a value of  
393 about 67% with a production of  $1556 \text{ kW}_{\text{LHV}}$ , and Layout 3 and 4 around 88% with a production of  
394  $2496 \text{ kW}_{\text{LHV}}$ . Layout 3 has a modestly lower electricity consumption than Layout 4, and thus a modestly  
395 higher exergy efficiency. The most interesting outcome of the exergy analysis is, anyhow, the indication of  
396 which processes generates the largest irreversibilities. As reported later in Section 5.5, the most irreversible  
397 processes, which shall be addressed if possible, are fuel gas combustion and electrical consumption.  
398 Interestingly, air-cooling turns to be more irreversible than biogas compressing and separating.

399 From the economical perspective, Layout 3 and 4 have the lowest total investment (about 2.9-3.0 M€)  
400 because they do not employ prime movers, which are expensive technologies. All others exceed 4.0 M€.  
401 Total investments include the biogas plant cost of 2.5 M€. In other words, the membrane plant cost ranges  
402 from 0.4 to over 1.5 M€, which are values lower than those computed by Deng and Hägg [20] because of  
403 the much lower plant size and the lower single factor assumed in this work. Cash flows and, thus, payback  
404 times as well as NPVs are computed with a biomethane incentive value of  $80 \text{ €/MWh}_{\text{LHV}}$  (the sensitivity  
405 analysis on the incentive is illustrated below). Layouts employing a micro gas turbine (2 and 5) yield the  
406 lowest cash flows because of the lower electrical efficiency. Among the others, Layout 4 is intermediate  
407 because of its high specific separation energy, while Layout 1 and 3 allow for the highest cash flows due to  
408 the highest electricity production and highest biomethane production, respectively. Similarly to the total  
409 investment, Layout 3 and 4 have the best payback time (5 and 6 years) and NPVs (3.5 and 3.1 M€) because,

410 again, they do not employ prime movers. In essence, the economical optimization favors the layouts that  
411 do not employ prime movers because they are expensive technologies.

412 For completeness, Figure 8 illustrates the CO<sub>2</sub>/CH<sub>4</sub> selectivity as well as the CO<sub>2</sub> permeance for Layout 1 as a  
413 function of the membrane incremental area, which is expressed in specific terms with respect to the  
414 produced biomethane at STP conditions (CH<sub>4</sub> permeance is not depicted, but it may be derived). The  
415 specific membrane area for Layout 1 is 1.23 m<sup>2</sup>h/m<sup>3</sup> (STP), as reported in Table 3. Along the membrane, the  
416 selectivity is around 29, in agreement with the data reported by Lee et al. [8], and shows a maximum of  
417 almost 31. The maximum exists due to the relative variations of the CO<sub>2</sub> permeance and of the CH<sub>4</sub>  
418 permeance. Both permeances decrease monotonically. At low incremental areas the permeance of CO<sub>2</sub>  
419 diminishes more gently than that of CH<sub>4</sub> due to the positive effect of a lowering plasticization of the  
420 material thanks to a lowering CO<sub>2</sub> concentration in the residue. Thus, the selectivity increases. However, at  
421 higher incremental areas the plasticization reduction becomes marginal and the permeance of CO<sub>2</sub>  
422 diminishes more steeply than that of CH<sub>4</sub>. Thus, the selectivity decreases. These results are in agreement  
423 with similar ones in the literature (for instance Baker [4] or Kohl and Nielsen [12]); they indicate that  
424 material plasticization has an appreciable effect over the selectivity and, thus, it shall be included in the  
425 material modeling.

#### 426 **5.4 Sensitivity analysis of biomethane incentive**

427 The biomethane incentive is a crucial parameter for the economical analysis. It varies among countries  
428 worldwide. For completeness, a sensitivity analysis on the incentive is conducted in the wide range from 40  
429 to 120 €/MWh<sub>LHV</sub>. Figure 9 shows the NPV as a function of the biomethane incentive for the five layouts  
430 and, in addition, for the conventional biogas plant. The NPV of the conventional plant is, of course,  
431 independent from the incentive and it is equal to about 2.2 M€. The curve for Layout 1 is the less steep,  
432 while those for Layout 2 and 5 are intermediate, and Layout 3 and 4 are the steepest. In fact, the higher the  
433 biomethane production the higher the curve slope. Below 70 €/MWh<sub>LHV</sub> none of the layouts is competitive  
434 compared to the conventional biogas plant; in the rough range between 70 and 80 €/MWh<sub>LHV</sub> only Layout 3  
435 and 4 become more convenient than conventional; and above 85 €/MWh<sub>LHV</sub> all are economically attractive.

436 In particular, Layout 3 and 4 are favored over a wide range of the incentives thanks to a higher biomethane  
437 production and a lower initial cost (as mentioned, they do not employ prime movers). From an investment  
438 perspective, they are the safest operation, even in the case of incentives varying over time.

## 439 **5.5 Insight in the preferred plant**

440 Layout 3 turns to be the preferred layout from both technical and economical perspectives, as it is rather  
441 simple and cost effective. Figure 10 visualizes its exergy efficiency and exergy losses. As explained in  
442 Section 4.3, the biomass exergy flow entering the biogas plant is taken numerically equal to the biogas  
443 exergy flow entering the membrane plant. The exergy efficiency is 88.9%, which is a high value because  
444 most of the methane content in the biogas is converted into the biomethane. The larger exergy losses are  
445 related to the permeate use in the water heater (5.4%) to keep the digester warm and to the electrical  
446 consumption (3.5%) in the biogas plant, because both thermal and electrical powers are considered as lost  
447 (Section 4.3). Losses due to the compressor and its air-cooler are appreciable (0.4% and 0.9% respectively),  
448 while losses due to permeation in the two membrane stages are lower (0.6% and 0.2%). Biogas mixing with  
449 the permeate from the second membrane is negligible. Therefore, the water heater consumption shall be  
450 reduced to the amount strictly required by the digester for improving the overall performance, for instance  
451 by adopting catalytic burners that can operate on very poor fuel gas and, hence, with lower flow rates than  
452 the layouts considered here.

453 The annualized cash flows for Layout 3 are depicted in Figure 11. They decrease over the years due to the  
454 effect of the weighted average cost of capital. The NPV for a given year is the cumulative sum of the cash  
455 flows up to that year. The NPV turns from negative to positive in the 5<sup>th</sup> year and, by the end of project,  
456 exceeds the total investment cost. A payback time of 5 years may be considered an interesting yet not  
457 outstanding result because energy supply from renewable sources is an increasing market in many  
458 Countries.

## 459 **6 Conclusions**

460 The present work assesses technologically, energetically, exergetically and economically, five layouts for  
461 biogas upgrading to biomethane via membrane technology. These layouts are optimized maximizing their  
462 Net Present Value (NPV).The work draws the conclusions as reported in the following.

- 463 • Membrane biogas separation via cellulose acetate spiral-wound modules is technologically a viable  
464 option for biomethane production.
- 465 • Layouts that employ two-stage permeation and utilize a water heater instead of a prime mover  
466 (internal combustion engine or micro gas turbine) allow for the maximum biomethane production.  
467 Considering cellulose acetate as membrane material and spiral-wound as module configuration,  
468 permeation is to be operated optimally at about 26 bar.
- 469 • The optimal values of membrane areas expressed in specific terms with respect to the produced  
470 biomethane range from 1.1 to 2.4 m<sup>2</sup>h/m<sup>3</sup> (STP) and the optimal values of specific energy from 0.33  
471 to 0.47 kWh/m<sup>3</sup> (STP), depending on the layout.
- 472 • The maximization of the NPV appears to favor larger compressors and smaller modules with  
473 respect to other studies in the literature that optimize in general the energy consumption.
- 474 • Biogas upgrading represents an appreciable improvement from an exergy perspective: in general,  
475 the higher the biomethane production the higher the exergy efficiency. Exergy efficiencies are in  
476 the range 57.7%-88.9%, compared to 35.1% of the conventional biogas plant.
- 477 • For membrane plants connected to a biogas plant producing 500 m<sup>3</sup>/h (STP), total investment span  
478 from 2.9 to 4.4 M€, of which 2.5 M€ are due to the biogas plant. Assuming a biomethane incentive  
479 of 80 €/MWh<sub>LHV</sub> and a project life of 15 years, payback times fall in the 5-9 year range while Net  
480 Present Values in 1.8-3.5 M€.
- 481 • The economic feasibility of biogas upgrading via membrane technology is strictly dependent on the  
482 biomethane incentive: below 70 €/MWh<sub>LHV</sub> none of the layouts is viable; up to 85 €/MWh<sub>LHV</sub> only  
483 the layouts employing water heaters instead of prime movers are viable; above 85 €/MWh<sub>LHV</sub> all  
484 layout are viable.

485 • The preferred layout (Layout 3) employs a single compressor, a two-stage membrane permeation  
486 operating at about 26 bar and a permeate-fueled water heater: its plant simplicity and the prime  
487 mover exclusion are the winning factors.

488 The future work will focus on simulating hollow-fiber polyimide modules, which require pressure drop  
489 models, and on investigating the use of catalytic heaters that can operate at low methane content.

## 490 **Acknowledgement**

491 The authors are very grateful to Mr. Luca Talia and Mr. Alberto Giannone from Sebigas S.p.a. for the fruitful  
492 exchange of opinions.

## 493 **Nomenclature**

### 494 **Acronyms**

BOP	Balance Of Plant
CMP	Compressor
DRY	Dryer
HTR	Heater
ICE	Internal Combustion Engine
LHV	Lower Heating Value
MBR	Membrane
MGT	Micro Gas Turbine
NIST	National Institute of Standards and Technology
NPV	Net Present Value
O&M	Operation and Maintenance
PSA	Pressure Swing Adsorption
STP	Standard Temperature (0°C) and Pressure (1 bar) in agreement with the definition of “standard conditions of gases” in IUPAC Compendium of Chemical Terminology

## 495 **Symbols**

$\Delta A$	Small increment of membrane area [m <sup>2</sup> ]
$\alpha$	Selectivity
$\beta$	Concentration-dependent parameter [m <sup>3</sup> /mol]
$\delta$	Membrane thickness [m]
$\varphi$	Pressure ratio
$A$	Membrane area [m <sup>2</sup> ]
$C'_H$	Saturated concentration of adsorbed gas [mol/m <sup>3</sup> ]
$D^\circ$	Effective diffusivity of penetrant gas at infinitely dilute concentration [m <sup>2</sup> /s]
$M$	Molar flow across the membrane [mol/s]
$N$	Permeate molar flow [mol/s]
$O$	Residue molar flow [mol/s]
$P$	Permeance [mol/m <sup>2</sup> s bar]
$b$	Adsorption equilibrium constant [bar <sup>-1</sup> ]
$k_D$	Dissolution coefficient [mol/m <sup>3</sup> bar]
$p_h$	High pressure or partial pressure [bar]
$p_l$	Low pressure or partial pressure [bar]
$x_h$	Molar concentration in the high pressure side
$x_l$	Molar concentration in the low pressure side

## 496 **Subscript and superscript**

$k$	$k$ -th incremental area
$i$	$i$ -th component

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546 **Table captions**

547 **Table 1. Assumed values for the cellulose acetate membrane parameters, converted from [8].**

548

549 **Table 2. Assumed values for the technical and economical parameters (for membrane parameters see Table 1).**

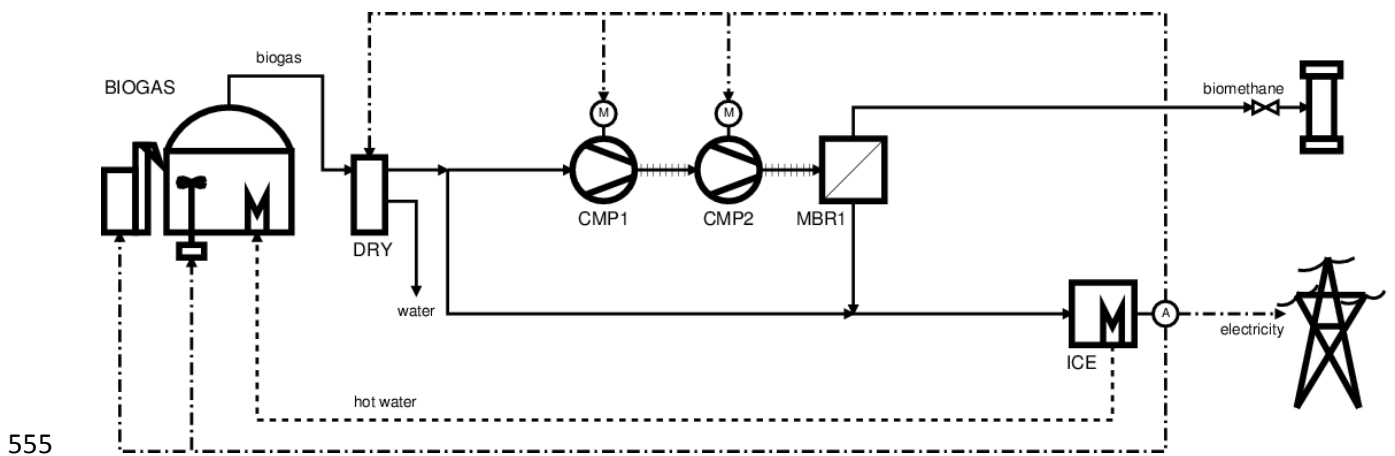
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551 **Table 3. Overall performances of the optimized layouts from the energy, exergy and economical perspectives.**

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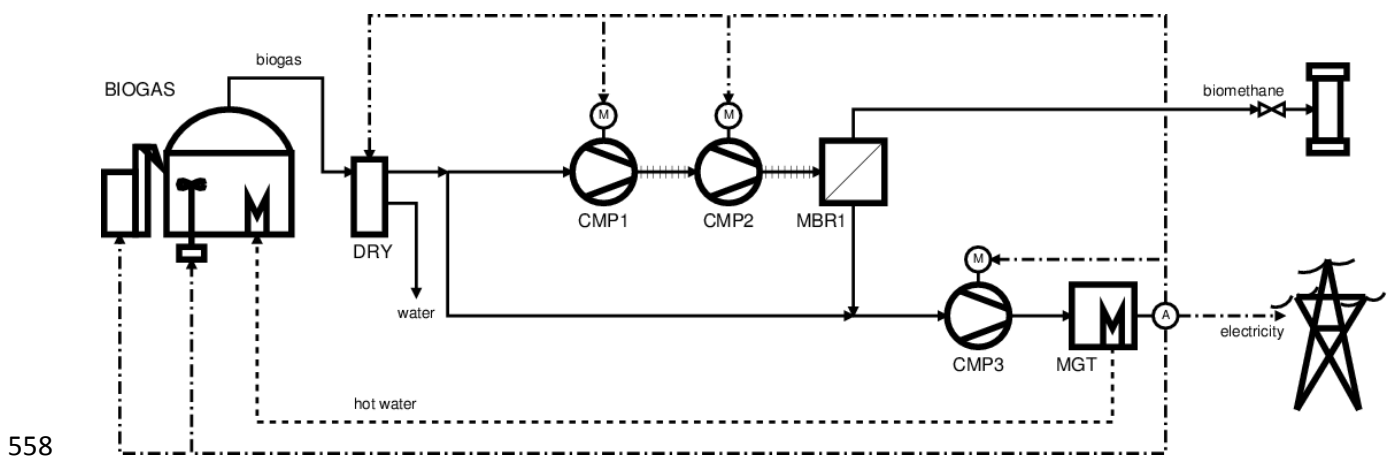
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554 **Figures**



556 **Figure 1. Single-stage permeation and internal combustion engine (Layout 1).**

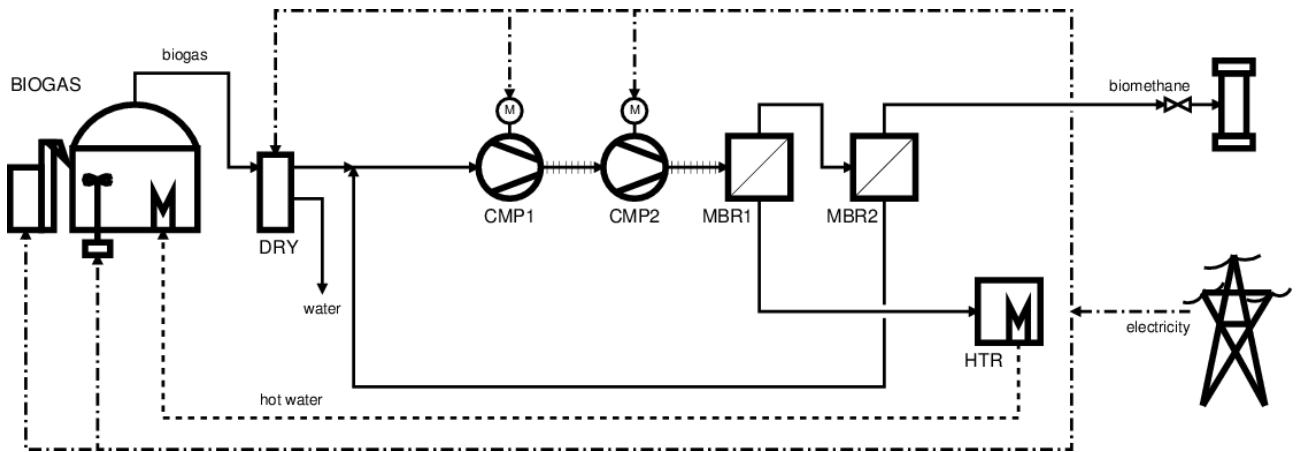
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559 **Figure 2. Single-stage permeation and micro gas turbine (Layout 2).**

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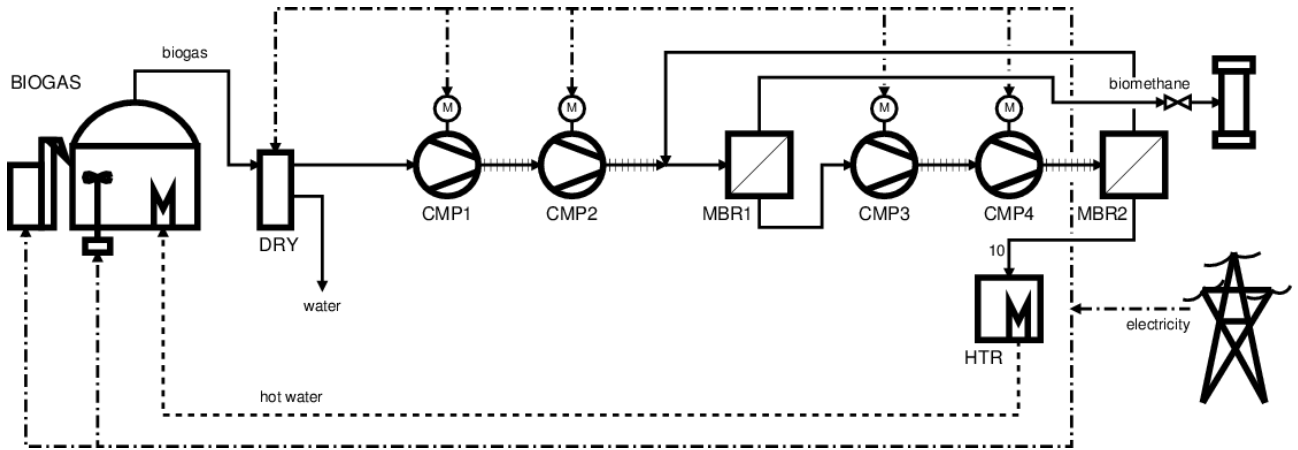


562 **Figure 3. Double-stage permeation with second-stage permeate recycle, single-stage compression and heater (Layout 3).**

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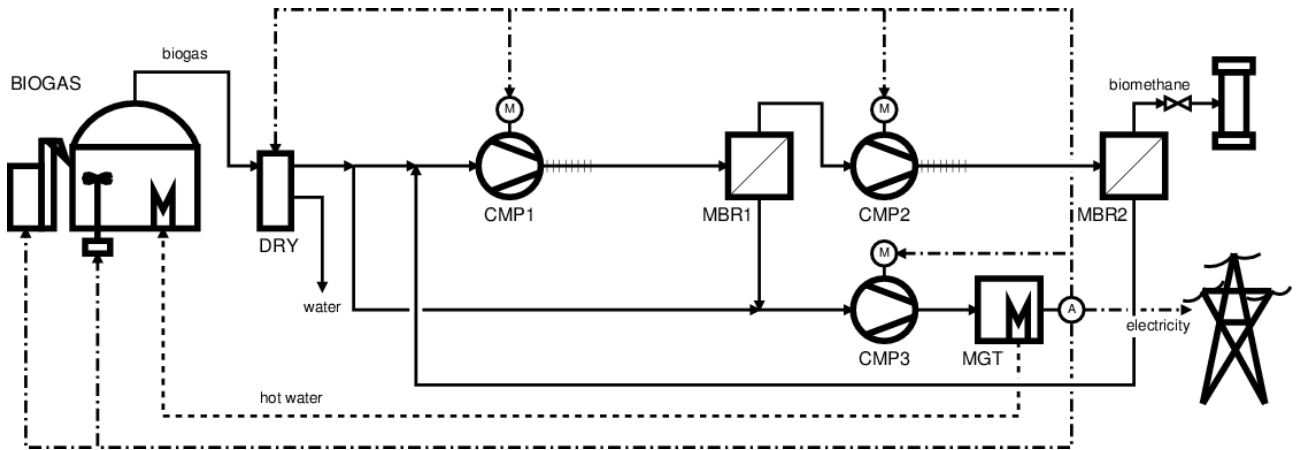


566 **Figure 4. Double-stage permeation with second-stage residue recycle, first-stage permeate recompression and heater (Layout 4).**

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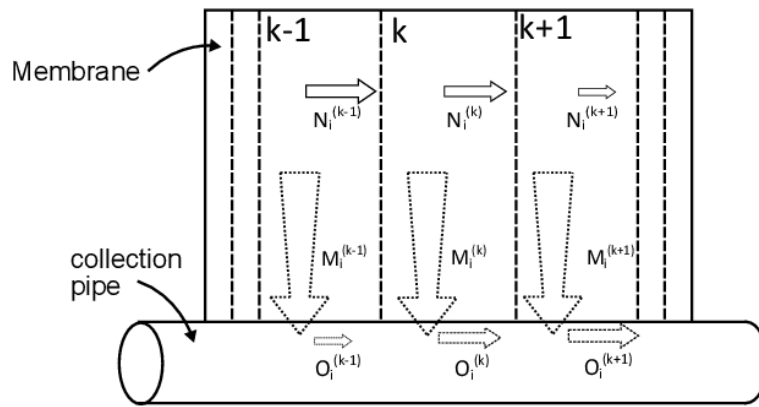
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570 **Figure 5. Double-stage permeation with second-stage permeate recycle, two-stage compression and micro gas turbine (Layout 5).**

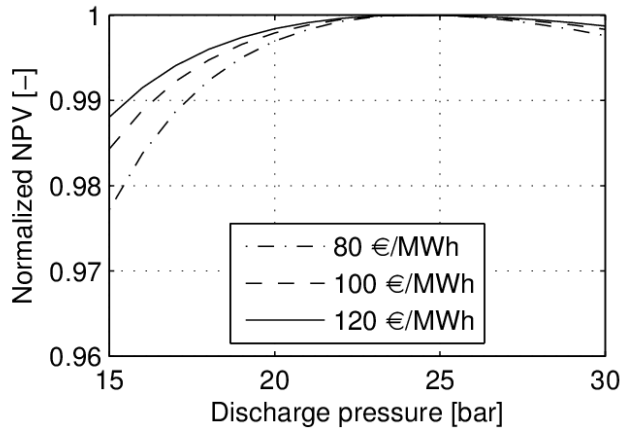
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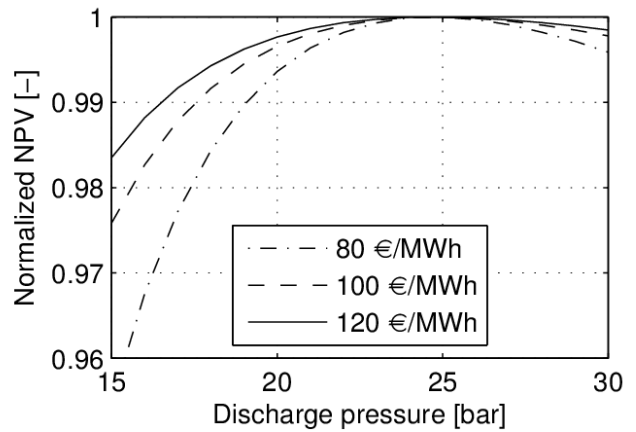
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573 **Figure 6. Schematic of the numerical solution of the crossflow pattern.**

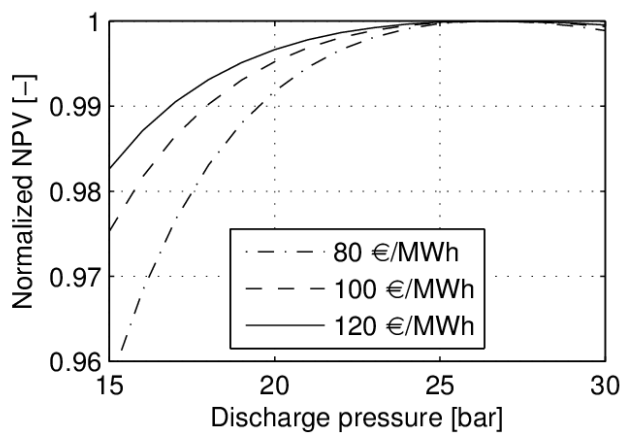
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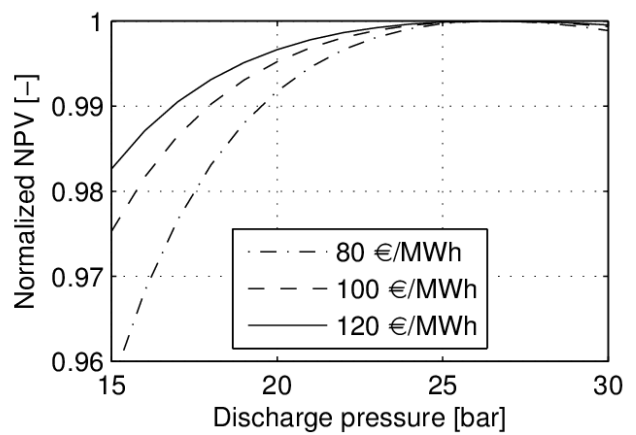
a. Layout 1



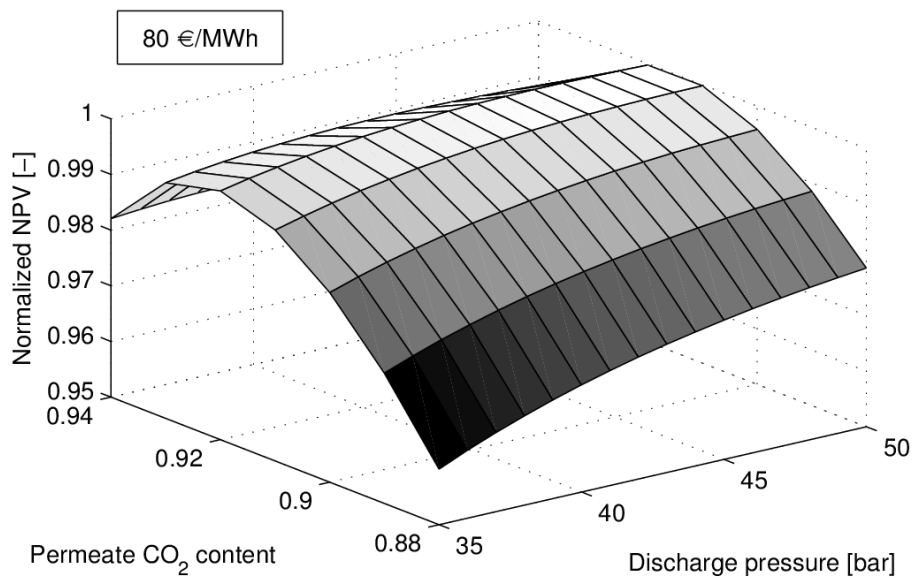
b. Layout 2



c. Layout 3

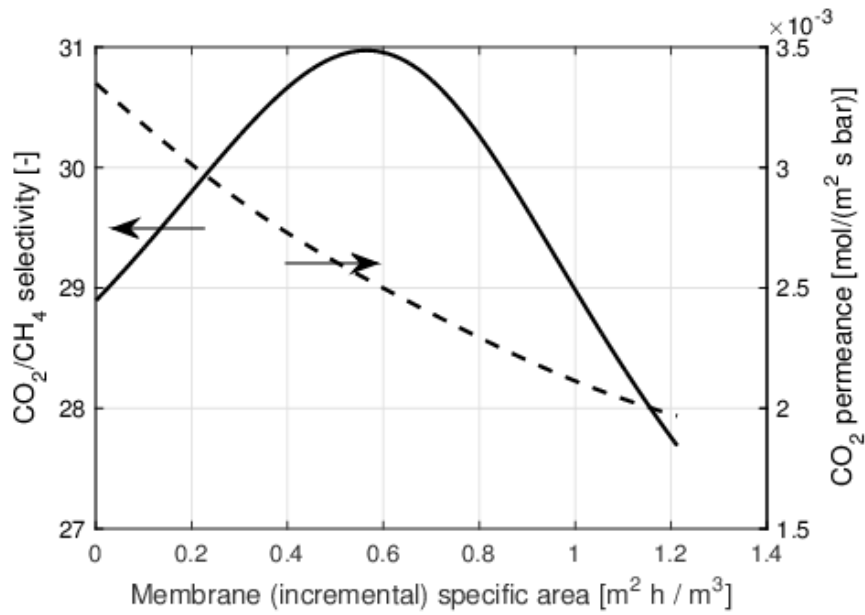


d. Layout 4



e. Layout 5

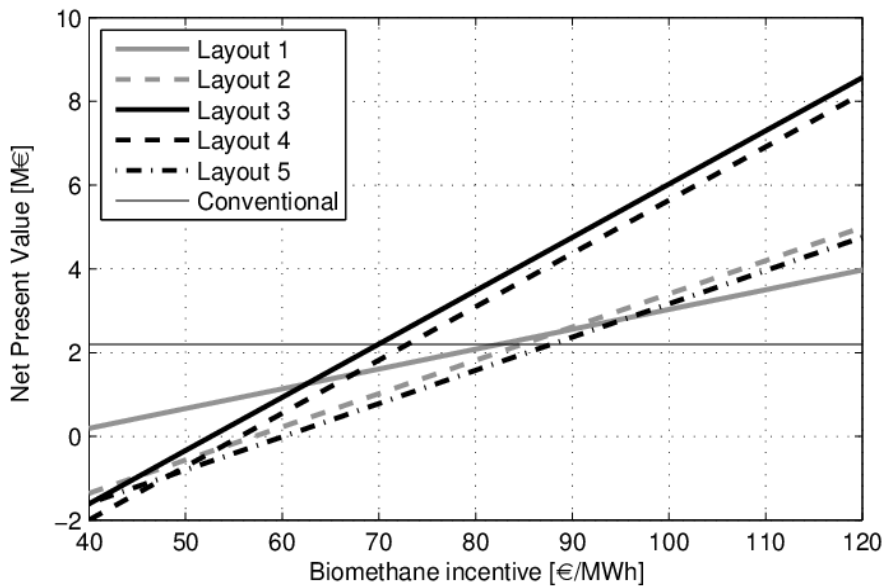
575 **Figure 7. Normalized Net Present Value (NPV) [-] as a function of the free parameters for the five layouts:**  
 576 **compressor discharge pressure for Layout 1 to 5, and of permeate CO<sub>2</sub> content for just Layout 5. Curves for Layout 1**  
 577 **to 4 are drawn for three biomethane incentive values. Curve for Layout 5 is drawn for only one value. Normalization**  
 578 **of NPV is executed with respect to the maximum of each curve.**



579

580 Figure 8. CO<sub>2</sub>/CH<sub>4</sub> selectivity (solid line) [-] and CO<sub>2</sub> permeance (dashed line) [mol/(m<sup>2</sup> s bar)] for Layout 1 as  
 581 a function of the membrane incremental area, which is expressed in specific terms with respect to the produced  
 582 biomethane (STP conditions) [m<sup>2</sup>h/m<sup>3</sup>]. The total specific area for Layout 1 is 1.23 m<sup>2</sup>h/m<sup>3</sup> as reported in Table 3.

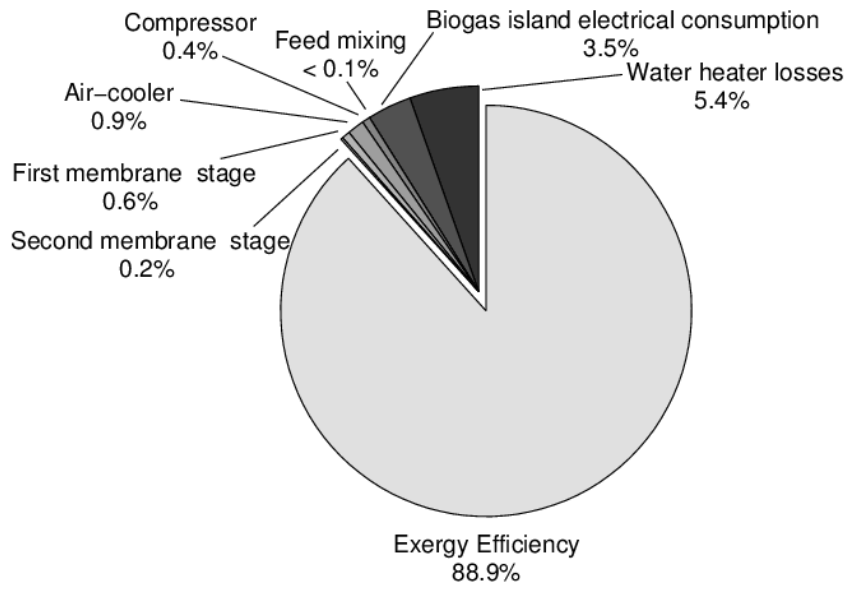
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584

585 Figure 9. Net Present Value (NPV) [M€] as a function of the biomethane incentive [€/MWh] for the five layouts and  
 586 for the conventional biogas plant taken in the methodology validation (Sec. 5.1).

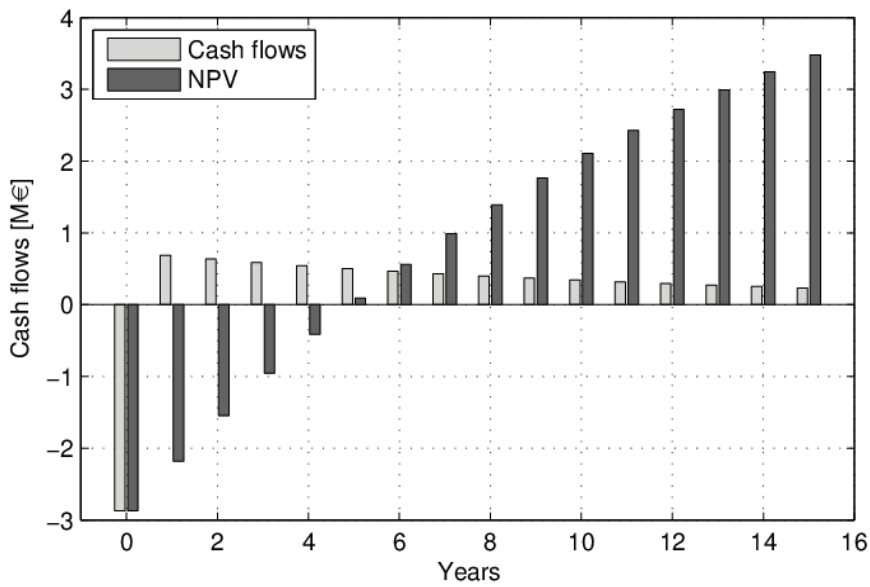
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588

589 **Figure 10. Pie diagram of the exergy losses for the preferred layout (Layout 3).**

590



591

592 **Figure 11. Cash flows over the project lifetime for the preferred layout (Layout 3).**

593



## Tables

**Table 1. Assumed values for the cellulose acetate membrane parameters, converted from [8].**

Cellulose acetate parameter	Unit	Symbol	Value	
			CO <sub>2</sub>	CH <sub>4</sub>
Concentration-dependent parameter	m <sup>3</sup> /mol	$\beta_i$	0.0018	0.0016
Effective diffusivity of penetrant gas at infinitely dilute concentration	m/s	$D_i^0/\delta$	4.420e-06	1.120e-06
Saturated concentration of adsorbed gas	mol/m <sup>3</sup>	$C'_H$	1629.2	1629.2
Adsorption equilibrium constant	bar <sup>-1</sup>	$b_i$	0.1900	0.0219
Dissolution coefficient	mol/m <sup>3</sup> bar	$k_{D_i}$	36.3701	7.6615

**Table 2. Assumed values for the technical and economical parameters (for membrane parameters see Table 1).**

Parameter	Unit	Value	Parameter	Unit	Value
<i>Dry biogas to membrane plant</i>			<i>Energy and exergy references</i>		
Composition			Pressure	atm	1
CH <sub>4</sub>	%	55	Temperature	K	298.15
CO <sub>2</sub>	%	45	CH <sub>4</sub> Lower Heating Value (LHV)	kJ/mol	802.3
Pressure	bar	1	CH <sub>4</sub> chemical exergy	kJ/mol	830.2
Temperature	K	273.15	<i>Investment</i>		
Flow rate	mol/s	6.2 <sup>a</sup>	Biogas plant cost	M€	2.5
<i>Biomethane to grid</i>			Exponential method factor		0.7
Composition			<i>Exponential method references</i>		
CH <sub>4</sub>	%	97	Compressor size	kW <sub>e</sub>	25 <sup>d</sup>
CO <sub>2</sub>	%	3	Compressor specific cost	€/kW	900 <sup>d</sup>
<i>Biogas plant</i>			ICE size	kW <sub>e</sub>	500
Electrical power requirement	kW <sub>e</sub>	100	ICE specific cost	€/kW <sub>e</sub>	900 <sup>e</sup>
Thermal power requirement	kW <sub>th</sub>	200	MGT size	kW <sub>e</sub>	65
<i>Air-cooled compressors</i>			MGT specific cost	€/kW <sub>e</sub>	1800 <sup>e</sup>
Isentropic efficiency	%	75	Heater size	kW <sub>th</sub>	100
Electric efficiency	%	95	Heater specific cost	€/kW <sub>th</sub>	60
Fan electric consumption	kW <sub>e</sub> /kW <sub>th</sub>	0.002	Membrane specific cost	€/m <sup>2</sup>	150
<i>Internal Combustion Engine (ICE)</i>			Balance Of Plant (BOP)	%	200
Net electrical efficiency	%	40 <sup>b</sup>	<i>Yearly cash flows</i>		
Max thermal efficiency	%	45	Capacity factor	%	85
Fuel gas			Biomass cost	k€/year	350
Min CH <sub>4</sub> content	%	45	<i>Operation &amp; Maintenance costs</i>		
Inlet pressure	bar	1	Compressor	€/MWh <sub>e</sub>	5
<i>Micro Gas Turbine (MGT)</i>			ICE	€/MWh <sub>e</sub>	30
Net electrical efficiency	%	33 <sup>c</sup>	MGT	€/MWh <sub>e</sub>	15
Max thermal efficiency	%	50	Membrane	€/m <sup>2</sup> /year	30
Fuel gas			Other w/r/t total investment	%	1
Min CH <sub>4</sub> content	%	35	<i>Electricity</i>		
Inlet pressure	bar	6	Purchased from grid	€/MWh <sub>e</sub>	150
<i>Heater</i>			Sold to grid with incentives	€/MWh <sub>e</sub>	200
Max thermal efficiency	%	90	Tax rate	%	20
Fuel gas			<i>Net Present Value analysis</i>		
MinCH <sub>4</sub> content	%	10	Project lifetime	years	15
Inlet pressure	bar	1	Weighted average cost of capital	%	8

<sup>a</sup> equivalent to 500 m<sup>3</sup>/h STP

<sup>b</sup> typical for an internal combustion engine rated at an electrical power from 500 to 800 kW<sub>e</sub>

<sup>c</sup> typical for a micro gas turbine rated at an electrical power of 200 kW<sub>e</sub> excluding the fuel compressor power requirement

<sup>d</sup> includes the cost for the corresponding air cooler

<sup>e</sup> includes the exhausts heat exchanger

**Table 3. Overall performances of the optimized layouts from the energy, exergy and economical perspectives.**

Optimal parameter	Unit	Layouts				
		1	2	3	4	5
Compressor discharge pressure <sup>a</sup>	Bar	24	24	26	24 / 24	6.8 / 46
Permeate CO <sub>2</sub> content	%	NA	NA	NA	NA	0.92
Membrane area (MBR1)	m <sup>2</sup>	118.2	198.3	121.0	313.0	340.7
Membrane area (MBR2)	m <sup>2</sup>	NA	NA	165.8	54.2	49.2
Compressor size (CMP1)	kW <sub>e</sub>	15.0	25.1	44.2	37.8	38.3
Compressor size (CMP2)	kW <sub>e</sub>	16.3	27.4	48.3	41.2	23.5
Compressor size (CMP3)	kW <sub>e</sub>	NA	32.1	NA	21.6	32.1
Compressor size (CMP4)	kW <sub>e</sub>	NA	NA	NA	21.6	NA
Prime mover size (ICE or MGT)	kW <sub>e</sub>	723.2	389.2	NA	NA	389.2
Water heater size (HTR)	kW <sub>th</sub>	NA	NA	216.1	216.1	NA
Biomethane flow rate	kW <sub>LHV</sub>	927.9	1556	2496	2496	1556
Methane recovery	%	33.9	56.9	91.2	91.2	56.9
Electricity <sup>b</sup>	kW <sub>e</sub>	591.3	203.5	-194.4	-224.4	193.9
Specific area	m <sup>2</sup> h/m <sup>3</sup> (STP)	1.23	1.23	1.11	1.42	2.42
Specific separation energy <sup>c</sup>	kWh/m <sup>3</sup> (STP)	0.33	0.33	0.36	0.47	0.38
Exergy efficiency	%	57.7	67.1	88.9	87.9	67.0
Total investment	M€	4.40	4.04	2.87	3.00	4.14
Yearly cash flow <sup>d</sup>	k€/year	757	684	741	712	668
Payback time <sup>d</sup>	Years	9	9	5	6	9
Net Present Value <sup>d</sup>	M€	2.08	1.81	3.48	3.09	1.58

<sup>a</sup> the compressor for the micro gas turbine in Layout 2 and 5 has a discharge pressure defined in Table 2

<sup>b</sup> positive if sold to the grid, negative if purchased from the grid

<sup>c</sup> the specific separation energy includes only the work for the separation compressors

<sup>d</sup> computed with a biomethane incentive of 80 €/MWh<sub>LHV</sub>