Probabilistic indicators for soil and groundwater contamination risk assessment

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Abstract

Deterministic assessments of whether, when, and where environmental safety thresholds are exceeded by pollutants are often unreliable due to uncertainty stemming from incomplete knowledge of the properties of environmental systems and limited sampling. We present a global sensitivity analysis to rank the contribution of uncertain parameters to the probability, $P$, of a target quantity to exceed user-defined environmental safety thresholds. To this end, we propose a new index ($AMAP$) which quantifies the impact of a parameter on $P$ and can be readily employed in probabilistic risk assessment. We apply $AMAP$, along with existing moment-based sensitivity indices, to quantify the sensitivity of soil and aquifer contamination following herbicide glyphosate (GLP) dispersal to soil hydraulic parameters. Target quantities are GLP and its toxic metabolite aminomethylphosphonic acid (AMPA) concentrations in the top soil as well as their leaching below the root zone. The global sensitivity analysis encompasses six scenarios of managed water amendments and rainfall events. The biodegradation of GLP and AMPA varies slightly across scenarios, while leaching below the root zone is greatly affected by the assumed hydrologic boundary conditions. $AMAP$ shows that, among the tested uncertain parameters, absolute permeability, air-entry suction, and porosity have the greatest impact on GLP and AMPA probability to pollute the aquifer by exceeding the aqueous concentration thresholds. Our results show that $AMAP$ is effective to thoroughly explore time histories arising from model-based predictions of environmental pollution hazards.
The proposed methodology may support informed decision making in risk assessments and help assessing ecological indicators through threshold-based analyses.

**Keywords:** global sensitivity analysis; uncertainty quantification; modeling; pollution; soil; groundwater; glyphosate; AMPA; environmental risk assessment

1. **Introduction**

Surface waters and aquifers are the recipients of contaminants resulting from anthropogenic activities such as agriculture, industry and waste treatment. According to the Lancet Commission on Pollution and Health, more than 140,000 synthetic molecules have been developed since 1950; of those, the 5,000 most produced molecules can be found in the environment worldwide (Landrigan *et al.*, 2018). These molecules and their metabolites can be persistent in the environment and, therefore, their detrimental effects can dramatically extend over space and time, thus harming not only humans and other living organisms but also their descendants (Kubsad *et al.*, 2019). In order to minimize and control harmful impacts, the use of these molecules has to be properly planned, managed, and regulated, thus requiring a good understanding of their dynamics in the environment.

Mathematical models are often used as decision support tools to evaluate contaminant degradation and transport (e.g., EPA, 2008; Porta *et al.*, 2018; Manheim *et al.*, 2019). Predictive models are also employed to carry out assessments on future scenarios such as climate change, land-use change, and global environmental change (e.g., Hiscock *et al.*, 2007; Armitage *et al.*, 2011; Brack *et al.*, 2015). Processes and environmental factors controlling contaminant dynamics (e.g., soil-water dynamics, contaminant sorption to soil minerals and organic matter, biochemical degradation, microbial-nutrient interactions, and soil-plant interactions) are described and coupled in models through mathematical equations with parameters often sourced from literature or estimated against laboratory or field experiments (Jackson *et al.*, 2000; Barrios *et al.*, 2019). Since environmental systems are complex and open to energy and mass flows, it is difficult to constrain and
model all controlling processes (Oreskes et al., 1994). Deterministic models neglect the inherent uncertainty associated with model structure and parameters (Uusitalo et al., 2015).

To overcome the shortcoming of deterministic models, uncertainty quantification and sensitivity analysis methods are used within a stochastic framework to provide decision makers with estimates of the potential outcomes of tested scenarios (e.g., Bates et al., 2003; Walker et al., 2003; Uusitalo et al., 2015). There exist many different approaches for sensitivity analysis (e.g., Razavi & Gupta, 2015; Pianosi et al., 2016; Ceriotti et al., 2018). Among these, global sensitivity analysis (GSA) is one of the most comprehensive approaches because it allows (a) quantifying sensitivity across the entire parameter space and (b) accounting for the joint effects resulting from the uncertainty in diverse parameters even in nonlinear models. Output sensitivity to model parameters is commonly quantified using variance-based techniques such as the Sobol’s indices (Sobol’, 1993); more recently, the AMA family of indices was introduced (Dell’Oca et al., 2017) to quantify sensitivity in terms of any statistical moment of the probability density function (pdf) of the model outputs. Available sensitivity indices do not provide a straightforward assessment of how a parameter influences the probability for a model output (e.g., the concentration of a contaminant) to exceed a user-defined threshold value. In environmental risk assessment and management, the policies and protection strategies often rely on regulatory guidelines that specify a safety limit for a certain contaminant. For example, the European Commission has set two severe safety limits to protect water resources quality from pesticide contamination: (a) the concentration of single pesticides and their relevant metabolites must not exceed 0.1 µg l\(^{-1}\); and (b) the sum of pesticides and their metabolites concentration must not exceed 0.5 µg l\(^{-1}\) (2006/118/EC, 2006).

In this study we introduce a new global sensitivity index (AMAP) to rank parameters based on their impact on the probability to exceed a defined safety limit for single contaminants and mixtures. AMAP complements the available AMA moment-based indices by targeting sensitivity with respect to the exceedance probability rather than the statistical moments of the output.
We demonstrate the use of AMAP to the case study of dispersal of the herbicide glyphosate (GLP) throughout a soil profile in an irrigated winter wheat field, using the results of la Cecilia et al. (2018) as a reference. The case study selection is motivated by the observation that GLP is currently the most widely used herbicide worldwide (Maggi et al., 2019). Modeling GLP biodegradation pathways requires a complex network of bioreactive processes coupled to water flow and solute transport. Hence, quantitative indicators that can identify relevant parameters and processes are important to reduce the uncertainty involved in risk assessment and help constraining the whole decision-making process. Societal implications of the uncertainties underlying environmental risk assessment of GLP have been widely discussed in the recent literature (e.g., Van Straalen & Legler, 2018). The relevance of hydraulic parameters on the fate of GLP and AMPA in soil has been documented in field experiments (e.g. Soracco et al., 2018; Lupi et al., 2019), as well as in numerical studies (Heuvelink et al., 2010). In this work we analyze the impact of uncertainty in soil hydraulic parameters on risk assessment of GLP and AMPA accumulation and leaching. We apply a number of different boundary conditions affecting transport and biodegradation processes to gain a wider understanding of how (i) AMAP informs on the effects of parameter uncertainty within pollution risk assessment and (ii) GLP and AMPA biodegradation predicted by the model is affected by the assumed boundary water fluxes. We designed such specific scenarios to represent managed (irrigated) and unmanaged (not irrigated) cropping. Analyses are also accompanied by specific robustness tests of the proposed AMAP index to show limits and advantages of its generalized application beyond the test case presented here. While we focus on soil and water contamination risk assessment, we emphasize that the proposed sensitivity index is readily applicable in other contexts, such as to assess the response of ecological and environmental systems, and particularly within threshold-based analysis of ecological indicators reported in recent literature (e.g., Libralato et al., 2019; Fu et al., 2019).
2. Materials and Methods

We introduce here the definition of the sensitivity indices (or metrics) as well as the approach we employ for their application within contamination risk assessments. In Section 2.1 we introduce the proposed sensitivity metrics and provide an operational framework for their application in a generic environmental problem. Next, we illustrate the application of our method to soil contamination as a result of glyphosate (GLP) dispersal. We start by presenting an overview of the kinetic model used to describe GLP contamination in a winter wheat field (Section 2.2). Target outputs for risk analysis and their corresponding safety thresholds are identified in Section 2.3. In Section 2.4, six scenarios with different ecohydrological boundary conditions are designed to be used in GSA. Finally, we select the uncertain parameters and describe the sampling methodology in Section 2.5.

2.1. Sensitivity indices and application to environmental problems

The AMA sensitivity indices (Dell’Oca et al., 2017) quantify the impact of each uncertain parameter on the statistical moments of the pdf of the target model outputs. Let \( g(p) \) be an output of interest, and \( p = (p_1, \ldots, p_i, \ldots, p_N) \) a vector gathering \( N \) uncertain parameters. The \( AMAM_i \) indices quantify the impact of variability in parameter \( p_i \) on the statistical moment \( M_i \) of \( g(p) \) (e.g., \( AMAE \) for the expected value \( E \) and \( AMAV \) for the variance \( V \)). \( AMAM_i \) is defined as

\[
AMAM_i = \begin{cases} 
\int_{\Gamma_i} \frac{|M[g(p|p_i)] - M[g(p)]| \rho(p_i) dp_i}{|M[g(p)]|} & \text{if } M[g(p)] \neq 0 \\
\int_{\Gamma_i} |M[g(p|p_i)]| \rho(p_i) dp_i & \text{if } M[g(p)] = 0
\end{cases}
\]

(1)

where \( \rho(p_i) \) is the pdf of \( p_i \) defined in the parameter space \( \Gamma_i \). Along with Eq. (1), and to cast our work within a risk assessment framework, we introduce the new index \( AMAP \), which allows quantifying the expected variation of the probability of exceedance of a threshold value \( thr \) as

\[
AMAP_i = \int_{\Gamma_i} \left| P_{thr} - P[g(p|p_i) > thr] \right| \rho(p_i) dp_i,
\]

(2)
where $P_{thr} = P[g(p) > thr]$ is the unconditional probability that the quantity $g(p)$ exceeds the threshold $thr$ and $P[g(p)|p_i]$ indicates the same probability conditional to parameter $p_i$. Note that $AMAP$ provides the probability-weighted average distance between conditional and unconditional exceedance probability within $\Gamma_i$ and is limited between 0 and 1. The output $g(p)$ and its related threshold $thr$ can be any quantity of interest, including a contaminant concentration, and can be used in a generalized way for the purpose of, but not limited to, risk analysis as shown later in this work.

A flowchart is presented in Figure 1 to illustrate the workflow for the $AMAP$ application within model-based environmental pollution assessment. First, prior information needs to be collected to define (i) a model structure and reference values of model parameters, and (ii) target outputs of interest and the related safety thresholds, where the latter can be user-defined or taken from guidelines. Additionally, various scenarios can be selected to explore the system response in diverse conditions (e.g., diverse hydrologic or climatic regimes, socio-economic and/or legislative constraints). As environmental models typically embed a large number of parameters, a subset of these is selected to conduct sensitivity analysis. The latter may be then used to (a) rank parameter importance (b) design and prioritize experimental campaigns aimed at constraining the uncertainty of the selected output. A pdf $\rho(p_i)$ must be defined for each uncertain input to compute $AMAP_i$ through Eq. (2). This can be determined from available prior information through empirically defined frequency distributions or according to general pdf models (e.g., Gaussian or uniform distributions), thus defining a probability space for the selected parameters set. Different choices for the input pdfs $\rho(p_i)$ can be performed and the results of the analyses may depend on the chosen input distribution. Therefore, the chosen $\rho(p_i)$ should reflect available information as closely as possible. Stochastic sampling of the parameters within this set is then performed $N$ times, rendering $N$ values of the output $g(p)$. These latter are employed to evaluate the conditional and unconditional probability to exceed a given threshold needed in (2) to compute $AMAP$. The work-
flow is replicated for each of the selected scenarios, thus providing a scenario-dependent sensitivity ranking that can guide in implementing strategies to reduce uncertainty.

Prior Information

- Development of deterministic model and reference model parameters
- Determination of target outputs for risk analysis and selection of safety limit threshold
- Selection of scenarios

Selection of uncertain parameters for global sensitivity analysis (GSA)

Determination of parameter probability distributions

Evaluate conditional and unconditional probability to exceed thresholds

Compute AMAP index and rank parameter impact on target outputs

Figure 1: Flowchart of the steps used in this study for the application of AMAP index.

2.2. Reference site and modeling description

We apply the framework introduced in Sec. 2.1 to the case of GLP biodegradation considered in la Cecilia et al. (2018). The reference winter wheat field is located in the Modena Municipality, Italy (44°40'57"N; 10°57'48"E). The soil is a typical alluvial deposit of the Po Valley region characterized by a silt loam and loam layers (SGSS, 2016). Two regions of interest were identified along the soil profile: the root zone (RZ) with thickness $h_{RZ} = 1$ m and the soil below RZ (BRZ) with thickness $h_{BRZ} = 4$ m.

Rainfall data in the period 2006-2016 were collected (Arpae-Simc, 2016) and post-processed to compute the water infiltration after assuming a 20% rainfall interception by the crop. The actual
crop evapotranspiration was calculated from data in Arpae-Simc (2016) with the time-varying crop coefficient $K_C$ in Allen et al. (1998). Irrigation was estimated to match groundwater table depth observations in Chiari et al. (2016) as described in la Cecilia et al. (2018). The 11 year precipitation, actual evapotranspiration, and irrigation time series were repeated periodically to build 50 years of daily boundary conditions. GLP was applied annually at rate $1.2 \times 10^{-3}$ mol m$^{-2}$ (i.e., 2 kg ha$^{-1}$ year$^{-1}$) in a single application event. An interception fraction of 0.2 and a drift fraction of 0.2 for post-emergence pesticide application on winter wheat (Trevisan et al., 2009) were accounted for as losses of the applied GLP rate, thus resulting in a net application rate $A = 7.2 \times 10^{-4}$ mol m$^{-2}$ (i.e., 1.2 kg ha$^{-1}$ year$^{-1}$).

The GLP reaction network includes GLP and AMPA biodegradation and neglects chemical degradation because it has been shown to only occur in soils rich in Mn oxides (e.g., birnessite mineral, la Cecilia & Maggi, 2018). Inhibition of the reaction by heavy metals (e.g., Cu$^{2+}$)(Barrett & McBride, 2005; la Cecilia & Maggi, 2018; la Cecilia et al., 2018; Li et al., 2015) is also not considered. GLP and AMPA degradation is tightly coupled with the nitrogen (N) cycle and a pool of soil organic matter, which releases ammonium ($\text{NH}_4^+$), orthophosphate ($\text{PO}_4^{3-}$), and monomeric organic carbon (represented by CH$_2$O) for microbial metabolic purposes (Maggi et al., 2008). Six microbial functional groups describe the soil microbial ecology and include: GLP and AMPA hydrolizing and oxidizing bacteria ($B_{\text{HyO}}$), and aerobic and anaerobic bacteria ($B_{\text{AER}}$ and $B_{\text{ANAER}}$) that consume organic carbon (la Cecilia & Maggi, 2018; la Cecilia et al., 2018), and $\text{NH}_4^+$ and $\text{NO}_2^-$ oxidizing bacteria ($B_{\text{AOB}}$ and $B_{\text{NOB}}$) that mediate a two-steps nitrification, and denitrifying bacteria ($B_{\text{DEN}}$) that perform a three-step $\text{NO}_3^-$ denitrification reduction to $\text{N}_2$ (Maggi et al., 2008).

Dynamic stability of soil microbial ecology resorts to group-specific biomass background recovery rates after Porta et al. (2018) showed that some functional groups can be outcompeted for some parameter combinations. Inhibition on various reactions include O$_2$ effects to anaerobic reactions and pH below 6 and above 8 for microbial activity (Boon & Laudelout, 1962). Protection of
aqueous species, including GLP and AMPA, to the mineral phase is modeled as a linear equilibrium process. Biodegradation neglects the protected phase because it is assumed to not be accessible to exoenzymes as suggested in Riley et al. (2014). Benchmarking of the reaction network has been performed in Maggi et al. (2020) against field measurements of GLP and AMPA concentrations reported in the literature. All the details of the biodegradation reaction network used in this work are available in la Cecilia et al. (2018).

Deterministic simulations of GLP biodegradation were conducted using the BRTSim-v3.1a general-purpose solver for reaction-advection-diffusion processes in variably saturated soils (Maggi, 2019). BRTSim numerically resolves the mass, momentum and energy conservation laws, biochemical kinetics, and equilibrium reactions using hybrid explicit-implicit finite volumes solvers, which are described in detail in the User Guide and Technical Manual (Maggi, 2018). Under the assumption that the gas phase undergoes negligible pressure gradients, advection was neglected here for gaseous species while diffusion of gaseous species was explicitly included. A steady temperature profile was assigned linearly changing from 20 °C at the top soil to 14 °C at 5 m depth.

In the following we describe the key equations used to describe flow and transport processes, i.e. where the investigated uncertain parameters are directly involved (see Section 2.5). We indicate variables dimensions using the notation \([M,L,T,\Theta]\) for mass, length, time and temperature, respectively. The mass and momentum conservation laws for water in a one dimensional variably saturated soil with constant porosity \(\phi\) can be written as (Richards, 1931)

\[
\phi \frac{\partial S_I}{\partial t} = -\frac{\partial q}{\partial z} - ET(z,t) - \Delta B(z,t), \quad \text{with} \quad q = -\frac{\rho_l g k_r(S_I)}{\mu} \left(\frac{\partial \psi(S_I)}{\partial z} - 1\right),
\]

where \(t\) [T] is time, \(S_I\) [-] is water saturation, \(z\) [L] is the vertical coordinate, \(k\) [L^2] and \(k_r\) are the absolute and relative permeabilities, \(g\) [LT^{-2}] is the gravitational acceleration, \(q\) [LT^{-1}] is the Darcy’s velocity, \(\psi\) [L] is the water potential, and \(\rho_l\) [ML^{-3}] and \(\mu\) [ML^{-1}T^{-1}] are the water density and viscosity, respectively.
and viscosity, respectively. Terms $ET(z, t)$ and $\Delta B(z, t)$ [T$^{-1}$] describe contributions to the soil water saturation due to actual evapotranspiration and immobilization in the microbial biomass, respectively. Precipitations $P(t)$ and irrigation $I(t)$ [LT$^{-1}$] per unit planar surface are assigned at the soil surface. Eq. (3) was solved assuming the following empirical formulations for $k_r$ and $\psi$ proposed by Brooks & Corey (1964)

$$k_r = S_{le}^{2b+3},$$

(4a)

$$\psi = \psi_s S_{le}^{-b},$$

(4b)

where $b$ [-] is the pore volume distribution index, $\psi_s$ [L] is the air-entry suction at water saturation, and $S_{le}$ is the effective water saturation defined as

$$S_{le} = \frac{S_l - S_{lr}}{1 - S_{lr} - S_{gr}},$$

(5)

$S_{lr}$ and $S_{gr}$ indicate the water and gas residual saturations, respectively.

Mass balance of chemical species is expressed by

$$\phi \frac{\partial X^i}{\partial t} = \frac{\partial J_{X^i}}{\partial z} + \hat{r}^i \quad J_{X^i} = -qX^i + \phi D_m \frac{\partial X^i}{\partial z},$$

(6)

where $X^i$ [ML$^{-3}$] is aqueous concentration, $D_m$ [L$^2$T$^{-1}$] is molecular diffusion, $J_{X^i}$ [ML$^{-2}$T$^{-1}$] is the advective diffusive solute flux, $\hat{r}^i$ [ML$^{-3}$T$^{-1}$] lumps the contribution from all chemical and biochemical reactions.

Chemical and biochemical kinetic reactions are assumed to occur only in the aqueous phase. The modelling approach employed to represent the feedbacks between water stress, temperature and bioreactive processes is detailed in Appendix A.

The microbial biomass was initialized with a simulation of 100 years to allow the water flow
and microbial processes related to GLP and the N cycle reaching a stationary state. The initialized system was then used repeatedly for the purpose of GSA to simulate a period of $T_s = 50$ years, setting GLP and AMPA initial concentrations to zero in each realization. As a consequence, this initialization presumed the ecological capability to degrade GLP, i.e., the microbial functional groups have already adapted to degrade GLP when they receive the first application. Recent experiments show that adaptation may imply a time lag in the order of months before soil microorganisms can effectively degrade GLP (Tang et al., 2019a), or in the order of hours due to catabolite repression mechanisms triggered by substrate preference and memory of previous growth conditions (la Ceccilia et al., 2019). As these observed adaptation times are significantly smaller than the considered time window of 50 years we neglect these effects in our analysis. This assumption may generally be reasonable because agricultural soils have typically been exposed to a wide suite of xenobiotics before the application of GLP.

2.3. Target quantities and thresholds for pollution assessment

The target quantities selected for risk analysis are (see also Figure 2):

- the depth-averaged aqueous concentration of GLP and the mixture $\text{MXT} = \text{GLP} + \text{AMPA}$ in BRZ (1 to 5 m depth), labeled as $C_{\text{GLP}}|_{\text{BRZ}}$ and $C_{\text{MXT}}|_{\text{BRZ}}$. The threshold values used are 0.1 µg l$^{-1}$ for GLP and 0.5 µg l$^{-1}$ for MXT, as prescribed by the Directive 2006/118/EC (2006) for the tolerable contamination of groundwater.

- GLP and AMPA mass in the top 30 cm of soil. These variables are indicated as $M_{\text{GLP}}|_{\text{TOP}}$ and $M_{\text{AMPA}}|_{\text{TOP}}$. We used the ecotoxicological concentration (i.e., LC$_{50}$) of GLP and AMPA mass fractions to earthworms as thresholds, which are set to $M_{\text{thr,GLP}} = 5,600$ mg kg-soil$^{-1}$ and $M_{\text{thr,AMPA}} = 1,000$ mg kg-soil$^{-1}$ for GLP and AMPA, respectively (Lewis et al., 2006).

- the yearly cumulative leaching rate of GLP and MXT between RZ and BRZ soil, $F_{\text{GLP}}$ and $F_{\text{MXT}}$, corresponding to advective-diffusive fluxes between the two soil regions, defined pos-
itive for downward fluxes (i.e., from RZ to BRZ). As threshold fluxes we set 0.02 mg m$^{-2}$ y$^{-1}$ and 0.1 mg m$^{-2}$ y$^{-1}$ for GLP and MXT, respectively. These values correspond to the 0.01% and 0.05% of the gross GLP application rate $A_{GLP} = 2$ kg ha$^{-1}$ y$^{-1}$, following the rationale employed in 2006/118/EC (2006). We explore here the impact of using a threshold mass rate to reflect the risk of aquifer contamination and pollution. This definition is motivated by the possibility of direct comparison with application and biodegradation rates, and detachment from water saturation-dependent assessment indicators.

Figure 2: Graphical representation of the outputs considered for pollution and contamination risk analysis

In the following, we employ the term ‘contamination’ for a non-negligible concentration of a molecule in an environmental compartment where it should not exist, and ‘pollution’ when a given quantity exceeds a prescribed safety threshold following Rodriguez Eugenio et al. (2018). Therefore, contamination refers here to any positive level of concentration or flux detected below the root zone.

$AMAP_i$ indices were calculated considering all the selected outputs within the simulation time window $T_s = 50$ y. Results obtained at year 15 are emphasized in the discussion because 15 y is the maximum approval period for pesticides in the EU. Note that while concentrations and top soil masses of contaminants are considered as continuous functions of time, fluxes are annual averages.
used to detect persistent contaminant leaching.

Finally, we calculated the annual biodegradation efficiency in RZ of GLP

\[
E_{\text{GLP}}(n) = \frac{1}{n} \sum_{j=1}^{n} \frac{1}{A \Delta t} \int_{h_{\text{RZ}}}^{\int_{(n-1)\Delta t}} \left[ R_{\text{GLP}}^{\text{Oxi}}(z, t) + R_{\text{GLP}}^{\text{Hyd}}(z, t) \right] dz dt
\]  

(7)

as the ratio of biodegraded GLP through oxidation \( R_{\text{GLP}}^{\text{Oxi}} \) and hydrolysis \( R_{\text{GLP}}^{\text{Hyd}} \) calculated as in Eq. A.1 relative to the GLP application rate \( A \) in year \( n \). Similarly, the biodegradation efficiency of AMPA is defined as

\[
E_{\text{AMPA}}(n) = \frac{1}{n} \sum_{j=1}^{n} \int_{h_{\text{RZ}}}^{\int_{(n-1)\Delta t}} \frac{R_{\text{AMPA}}(z, t)}{R_{\text{GLP}}^{\text{Oxi}}(z, t)} dz dt
\]  

(8)

where \( R_{\text{AMPA}} \) is biodegraded AMPA. In both (7)-(8) we set \( \Delta t = 1 \) year. Note that Eq. (8) measures the ratio between biodegraded and produced AMPA, where the latter is a metabolite of GLP biodegradation through oxidation, see la Cecilia & Maggi (2018) for details. The biodegradation efficiencies in Eqs. (7)-(8) are not used for AMAM or AMAP analyses because there is no legislation that recommends threshold biodegradation efficiencies in field applications. However, Eq. (7)-(8) were used to interpret how parameter uncertainty affected GLP and AMPA biodegradation across different scenarios.

2.4. Selection of scenarios

We consider six hydrometeorological scenarios (Table 1). The first scenario corresponds to the reference (REF) case study described in la Cecilia et al. (2018), where the precipitation \( P = P_{\text{REF}} \) and actual evapotranspiration \( ET = ET_{\text{C,REF}} \) are used to estimate irrigation rates \( I = I_{\text{REF}} \) necessary to match locally-measured water table depths. This case study is representative of managed agricultural crops. In the second and third scenarios, \( P \) is decreased and increased by 20% of \( P_{\text{REF}} \) to simulate drier (DRY) and wetter (WET) conditions, respectively, while irrigation is maintained as in the REF scenario. In the fourth scenario, steady state (SS) boundary conditions are set equal
to time-averaged fluxes $P = \overline{P}_{\text{REF}}, ET = \overline{ET}_{\text{C, REF}}, I = \overline{I}_{\text{REF}}$ calculated over the whole simulation time and applied as constant boundary flows. In this case, the GLP application rate is also time-averaged and applied throughout the simulated time period as $A = \overline{A}_{\text{REF}}$. DRY and SS unmanaged scenarios without irrigation are also considered.

The managed and unmanaged SS scenarios are tested to investigate the extent to which accounting of time-resolved as compared to constant hydrological fluxes can influence the prediction of GLP and AMPA biodegradation.

<table>
<thead>
<tr>
<th>Boundary conditions</th>
<th>Managed (REF)</th>
<th>(DRY)</th>
<th>(WET)</th>
<th>(SS)</th>
<th>Unmanaged (DRY)</th>
<th>(SS)</th>
</tr>
</thead>
<tbody>
<tr>
<td>$P$</td>
<td>$P_{\text{REF}}$</td>
<td>$P_{\text{REF}} \times 0.8$</td>
<td>$P_{\text{REF}} \times 1.2$</td>
<td>$P_{\text{REF}}$</td>
<td>$P_{\text{REF}}$</td>
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<td>$I$</td>
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Table 1: Boundary conditions applied in the tested scenarios. REF, DRY, WET and SS indicate the reference scenario, dry and wet scenarios, and steady state scenarios, respectively.

2.5. Selection of uncertain parameters

To illustrate the use of the sensitivity metrics defined in Section 2.1, we analyze here the impact of uncertainty related to soil hydraulic properties on the target quantities defined in Section 2.3. We consider a total of six uncertain parameters indicated in Eqs (3)-(4), i.e. $k$, $b$, $\psi_s$, $\phi$, $S_{lr}$ and $S_{gr}$. In principle, permeability $k$ can be expressed as a function of the other parameters by means of empirical or semi-empirical correlations (e.g. Brutsaert, 2000). However, we have included $k$ within the set of uncertain parameters because of the reported non-exact dependence between $\phi$ and $k$ (e.g., Maggi & Porporato, 2007). These parameters are assumed to be mutually independent and uniformly distributed within given ranges $\delta(p)$. Our choice of using a uniform pdf to characterize the uncertain model inputs rests on the idea of assigning equal weight to each value of the distribution (i.e., an equal prior probability). The range $\delta(p_i)$ associated with $k$, $b$, $\psi_s$ and $\phi$ (Table 2) is retrieved from naturally occurring soils, i.e., from hydrothermal properties database by Dai
et al. (2013) and the SoilGrids database in Hengl et al. (2017). Measured residual liquid saturation $S_{lr}$ range from 0.046 to 0.31 (Ghanbarian-Alavijeh et al., 2010), while $S_{gr}$ observations vary between 0.092 and 0.22 (Smith & Browning, 1943; Peck, 1969). Based on these observations, $S_{lr}$ and $S_{gr}$ are here considered as uniformly distributed parameters with values comprised between 0.05 and 0.2 (Table 2). Our analysis neglects vertical heterogeneity of soil properties. We solve one-dimensional flow and transport along a vertical soil column. This choice is consistent with models used for assessing pesticide leaching in regulatory frameworks (Jene, 1998; Carsel et al., 1985; Van den Berg et al., 2012; Carsel et al., 1985; 2006/118/EC, 2006). The assumed uncertainty in the soil hydraulic parameters can be used to assess the impact of their spatial variability, such as rendered by geo-referenced databases discussed in Heuvelink et al. (2010).

Sampling of the parameters space was conducted using a quasi Monte Carlo (QMC) technique (Sobol’, 1998). In total, 5,000 parameter realizations were generated and applied to each scenario. Upon performing a forward modeling run for each of the selected sampling points, we obtain a QMC ensemble of our target outputs of interest that is next used to conduct the sensitivity analysis. We verified the convergence of the QMC samples in terms of the outputs sample pdfs, see Appendix B. The CPU time for each QMC flow and transport simulation is 600 s (Intel Xeon Platinum 8160 @ 2.10 GHz).

<table>
<thead>
<tr>
<th>$k$ ($\times 10^{-13}$ [m$^2$])</th>
<th>$b$ [-]</th>
<th>$\psi_s$ [m water]</th>
<th>$\phi$ [-]</th>
<th>$S_{lr}$ [-]</th>
<th>$S_{gr}$ [-]</th>
</tr>
</thead>
<tbody>
<tr>
<td>(0.50, 10)</td>
<td>(3.7)</td>
<td>(-0.6, -0.1)</td>
<td>(0.4, 0.5)</td>
<td>(0.05, 0.2)</td>
<td>(0.05, 0.2)</td>
</tr>
</tbody>
</table>

Table 2: Parameter value ranges.

3. Results and discussions

In the following we apply the global sensitivity indices $AMAM$ and $AMAP$ introduced in Section 2 to the reference scenario and we then analyze the impact of the considered hydrological and management regime on the system response. Finally we consider the impact of the selected scenar-
ios on the biodegradation efficiency, to assess the relevance of the hydrologic boundary conditions on the GLP biodegradation reaction network.

3.1. Global sensitivity indices in the reference (REF) scenario

Figure 3 reports $AMAE_i$, $AMAV_i$ and $AMAP_i$ computed for all uncertain parameters $p_i$ and for all target quantities evaluated at the time corresponding to the maximum approval period for pesticides in the EU, i.e. at $t = 15$ y.

$AMAE_i$ (Figure 3a-d) suggests that the soil permeability $k$ has the greatest influence on the sample average of all target quantities analyzed followed by (a) $\psi_s$ and $\phi$ for the concentration targets and (b) by the gas residual saturation $S_{gr}$ and $\psi_s$ for the flux targets. Other parameters display moderate to minor effects. Similar results have been obtained for $AMAV_i$ for the two concentrations (Figure 3e-f), while the fluxes variances are also greatly influenced by the pore volume distribution index $b$ (Figure 3g-h).

$AMAP_i$ (Figure 3i to l) shows that the probability of $C_{GLP}$ and (to a lesser extent) $F_{MXT}$ to exceed their thresholds are impacted by the variability of the uncertain parameters at $t = 15$ y. Otherwise, $AMAP_i$ obtained for $C_{MXT|BRZ}$ and $F_{GLP}$ are negligible. This result is explained observing that the threshold MXT concentration/GLP flux is never or always exceeded in the investigated sample regardless of the parameters’ values (see also Sections 3.4 and 3.3). The investigated parameters have then a negligible influence on the probability of exceeding the threshold, while they still influence the outputs mean and variance as shown by the corresponding $AMAE_i$ and $AMAV_i$ values.

Overall Figure 3 suggests that an accurate characterization of $k$, $\psi_s$, $\phi$ should be prioritized to predict agrochemicals’ concentrations in the aquifer. In addition, estimating agrochemical fluxes from the root zone to the aquifer would benefit from an accurate knowledge of $S_{gr}$ and $b$. 

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3.2. Range Impact Analysis - RIA

In this section, we quantify the variability of $AMAP_i$ with respect to the level of uncertainty assumed for each parameter $p_i$ upon considering GLP concentration $C_{GLPBRZ}(t = 15y)$. We keep the average value for each parameter probability distribution constant and we increase/decrease the ranges of variability in $\delta(p_i)$ by a prescribed factor comprised between 0.7 and 1.1. This allows testing the robustness of parameter ranking upon maintaining uniformly distributed parameters and without violating physical constraints (i.e., positive permeability and porosity comprised between zero and one).
Figure 4 shows that the $AMAP_i$ indices smoothly vary. The ranking of parameters importance is also consistent for all the investigated ranges with $k$, $\psi_s$ and $\phi$ chiefly influencing the system response, while the effect of $b$ and $S_{lr}$ and $S_{gr}$ appears negligible. Increasing values of $AMAP_i$ are obtained for increasing parameters ranges, which reflects the increase of assumed uncertainty in the parameter values.

![Graph showing $AMAP_i$ variations with parameters](image)

**Figure 4: AMAP - Range Impact Analysis for $C_{GLP|BRZ}(t=15y)$**

### 3.3. Analysis of contamination and pollution

Figure 5a-b displays the temporal evolution of the expected values (or sample-averages) $E[M_{GLP|TOP}]$ and $E[M_{AMPA|TOP}]$, respectively. Both quantities are significantly smaller (by three orders of magnitude) than their ecotoxicological threshold (i.e., LC$_{50}$ for earthworms) and the probability to exceed the thresholds is negligible across the whole sample. Managed and unmanaged steady state scenarios result in the largest $E[M_{GLP|TOP}]$ and $E[M_{AMPA|TOP}]$ values, which are likely caused by re-
duced flushing as compared to scenarios where intense precipitations caused fast GLP and AMPA transport to BRZ.

The sample-averaged aqueous concentrations $E[C_{GLP}|BRZ]$ and $E[C_{MXT}|BRZ]$ (Figure 5c and d) increase over time in the aquifer. Wet scenarios (REF and WET) lead to faster increase in $E[C_{GLP}|BRZ]$ and $E[C_{MXT}|BRZ]$ as compared to dry scenarios (DRY). Our results also suggest that pollution may occur at substantially longer time scales in steady state conditions, i.e., SS scenarios do not cause any significant contamination within the investigated 50-year time period.

Figure 5e and f show the relative frequency (or sample probability) of the exceedance time $\hat{t}$, i.e., the time at which $C_{GLP}|BRZ$ and $C_{MXT}|BRZ$ exceed the corresponding threshold concentrations. All transient scenarios showed more than 95% probability for $C_{GLP}|BRZ$ and $C_{MXT}|BRZ$ to exceed the threshold concentrations within a time frame of 50 years. On the other hand, considering the EU maximum approval period for pesticides of 15 years, the probability to exceed the threshold concentrations is smaller than 20% for $C_{GLP}|BRZ$ and negligible for $C_{MXT}|BRZ$. This result is consistent with Figure 3j, showing negligible $AMAP_i$ values (for all parameters) for $C_{MXT}|BRZ$. We further note that the probability distributions of $\hat{t}$ display heavier right tails for DRY than for WET scenarios, i.e., GLP and MXT arrival times to BRZ are characterized by larger uncertainty in DRY than in WET scenarios. This result quantifies a delay in the occurrence of water pollution BRZ in DRY conditions.

The mean GLP and MXT leaching rates from RZ to BRZ (Figure 6a-b) vary significantly across all scenarios. As expected, WET scenarios lead to higher leaching rates than DRY ones. Soil BRZ can undergo pollution after 4 years since the first GLP application in both WET and DRY scenarios. Figure 6a and b also show that upward (negative) fluxes occur from BRZ to RZ in dry scenarios. These instances are driven by particularly dry periods and elevated $ET_C$, which result in high water suction in TOP and RZ from BRZ. Upward fluxes are consistent with previous observations of herbicide transport during capillary driven groundwater rise (Arjoon et al., 1998). This result may
Figure 5: Average GLP and AMPA mass in RZ (a-b) and aqueous concentrations in BRZ (c-d); (e)-(f) represent the corresponding probability distribution of exceedance time \( \hat{t} \), i.e., the time at which contaminant concentrations exceeded threshold concentrations.

The recontamination does not occur in the SS scenarios because the saturation profile is constant in time. This result confirms our interpretation that unsteady water inputs due to precipitations can cause rapid contaminant flushes (i.e., positive fluxes) to BRZ as compared to SS scenarios.
Figures 6c and d show that the probability to exceed $F_{\text{thr}}$ is very high ($P_{\text{thr}} \approx 1$) within 15 years for both GLP and MXT in all scenarios except SS. Comparing Figures 6c and d with Figure 5e and f, one can conclude that the time scale associated to pollution observed in leaching rate (from RZ to BRZ) is significantly smaller than the time scale linked to resident agrochemical concentrations in BRZ. Therefore, measurements and modeling predictions of leaching rates would provide a more conservative indicator than concentration data within a contaminant risk assessment framework.

Figure 6: Sample-averaged GLP ($F_{\text{GLP}}$) (a) and MXT ($F_{\text{MXT}}$)(b) leaching rate from RZ to BRZ, respectively; (c) and (d) represent the relative frequency of the exceedance time $\hat{t}$, i.e., the first time at which $F_{\text{GLP}}$ and $F_{\text{MXT}}$ exceeded the threshold values.
3.4. AMAP and scenario analyses

AMAP\textsubscript{i} can be used as a time dependent sensitivity measure as illustrated in Figure 7. We observe that parameter ranking is consistent across different outputs for the same scenario because the selected outputs are inherently linked between each other. Significant differences in ranking are conversely observed across scenarios. For example, parameter \( b \) has an important influence on the probability that both \( C_{\text{GLP}}|\text{BRZ} \) and \( C_{\text{MXT}}|\text{BRZ} \) exceed the related thresholds in DRY scenarios (Figure 7b,f,d,h). On the other hand, the parameter \( \psi_s \) is predominant over \( b \) in assessing \( C_{\text{GLP}}|\text{BRZ} \) and \( C_{\text{MXT}}|\text{BRZ} \) in wet scenarios (WET and REF). This result is consistent with Eq. (4), showing that the impact of \( b \) decreases as the water saturation increases.

Figure 8 displays AMAP\textsubscript{i} values evaluated for the transient scenarios and considering \( C_{\text{GLP}}|\text{BRZ} \) and \( F_{\text{MXT}} \) after 15 years from the first GLP application. Analogous results for \( C_{\text{MXT}} \) and \( F_{\text{GLP}} \) in the transient conditions as well as for all target quantities in the SS scenarios are not reported since negligible values of AMAP\textsubscript{i} have been obtained for all parameters.

Parameters \( k \) and \( \psi_s \) are the most influential parameters on \( C_{\text{GLP}}|\text{BRZ} \) and \( F_{\text{GLP}} \). These results are consistent with Eq. (3); that is, (i) increasing \( k \) promotes faster water flows, and thereby solute transport; (ii) decreasing \( \psi_s \) promotes higher water capillary rise from BRZ to RZ contrasting leaching. Figures 7-8 allow identifying which parameters should be further constrained, such as through measurement campaigns, to reduce the uncertainty associated with probabilistic groundwater or soil contamination risk assessment.

3.5. Biodegradation and flow regime

Mean biodegradation efficiencies \( E[E_{\text{GLP}}] \) and \( E[E_{\text{AMPA}}] \) indicate that biodegradation starts as soon as GLP is applied and increases over time (see Figure 9). Sample-averaged GLP biodegradation efficiency does not change significantly among all investigated scenarios, because \( E[E_{\text{GLP}}] \) varies only between 0.85 and 0.9. The variability slightly increases when AMPA is considered, values of \( E[E_{\text{AMPA}}] \) ranging between 0.24 and 0.32. Therefore, the sensitivity of microbial activity
Figure 7: Time evolution of AMAP values: each row of plots is associated with a single output, columns distinguish the different scenarios.

and biodegradation to soil water availability is not particularly relevant in the selected scenarios even though water availability is explicitly considered in the model via Eq. (A.3).

This result suggests that simplified SS models as compared to time-resolved hydrologic boundary conditions may be used to predict overall contaminant mass budgets and is in line with previous numerical results by Tang et al. (2019b). However, SS scenarios do not yield accurate predictions of contaminants concentrations and leaching rates, which are instead driven by hydrological fluc-
Figure 8: AMAP values of the uncertain soil hydraulic parameters relative to (a) GLP aqueous concentration BRZ and (b) MXT fluxes from RZ to BRZ. Analyses were carried out at time $t = 15$ years and results are grouped and colored according to each one of the six scenarios.

3.6. Final remarks

Our results demonstrate that probabilistic indicators allow identifying the impact of soil hydraulic properties on pesticide contamination and leaching. In particular, we show that leaching is highly variable depending on soil properties, hydrological boundary conditions, and land management practices. In previous studies, Stenemo & Jarvis (2007) showed that the ranking of parameters may change according to soil texture, while Jury & Gruber (1989) showed that the persistence of pesticides with residence times longer than one year is more affected by soil rather than climatic variability. A number of studies have investigated uncertainty quantification and sensitivity analysis of agrochemical biodegradation and leaching (Dubus et al., 2003; Stenemo & Jarvis, 2007; Heuvelink et al., 2010). These modeling works assumed first order decay of pesticides in soil in
contrast with our approach that uses Michaelis-Menten-Monod kinetics. Some of these studies suggest that soil hydraulics has a smaller impact on pesticide fate as compared to half life and sorption properties, yet our results demonstrate that soil hydraulic properties have a relevant impact on threshold exceedance probability. In particular, the AMAP time series demonstrate the impact of soil hydraulic parameters appears to be more persistent in dry than wet scenarios. We emphasize that the above mentioned studies typically rely on a single output statistics for parameter ranking in pesticide leaching (Heuvelink et al., 2010) or quantify sensitivity by changing parameters one at a time (Dubus et al., 2003). Conversely, our results advocate for the use of a suite of global sensitivity indicators to thoroughly test the system response, and are in line with recent studies (Borgonovo et al., 2017; Ceriotti et al., 2018). Hence AMAP can complement moment-based sensitivity indicators that do not account for safety threshold considered in risk assessment protocols. Likewise moment-based indicators, AMAP can be used with any input parameter distribution, model formulation and dimensionality. The present work considers only scenario and parametric uncertainty. Model structure and dimensionality has been identified as another possible relevant source of uncertainty. Different results may be obtained upon considering diverse flow and transport formulations as well as alternative biogeochemical reaction networks. Future work is en-
visaged to provide a formal derivation of model structure sensitivity indices within a probabilistic risk assessment framework, as recently discussed in Dell’Oca et al. (2020).

4. Conclusions

Our work leads to the following major conclusions:

- We test the use of a suite of sensitivity indicators for soil and groundwater environmental risk assessment. To this end, we introduce a new sensitivity index (AMAP) and we show its application to contamination and pollution following glyphosate (GLP) herbicide dispersion in an agricultural soil column. AMAP provides a time dependent indication of the relevance of each parameter on the probability for a given output to exceed a user defined threshold and complements available moment-based sensitivity metrics. The index developed here can be readily applied to rank uncertain parameters with respect to any arbitrary threshold related to the quality of any environmental sphere (e.g., water, air, soil, and their combinations) and to inform appropriate management and restoration strategies.

- We quantify the impact of uncertainty in soil hydraulic parameters on the time required for the concentration of GLP and its toxic metabolite AMPA to exceed pollution thresholds in the top soil, below the root zone and for the fluxes measured at 1 m depth. We repeated these analyses in different scenarios of managed and unmanaged water budgets. When concentration thresholds are considered, dry scenarios result in larger uncertainty in terms of exceedance time as compared to wet ones. Measurements of contaminant fluxes reduce such uncertainty.

- Parameter ranking varies with ecohydrological scenarios of precipitations and irrigation practice. Permeability ($k$) and air-entry suction ($\psi_s$) have the greatest effect on exceedance of water quality safety limits in the reference scenario as well as in the wet scenario. The
influence of the pore volume distribution index $b$ emerges in dry conditions, probably due to its relation with the relative permeability. Gas residual saturation may play an important role in contaminant transport in some scenarios, however it has shown a relatively minor role on pollution assessment. Porosity appears to have a minor effect on pollution risk as compared to permeability, except in the driest investigated conditions. These results suggest that $AMAP$ can be used to refine uncertainty quantification in hazard assessment through measurements campaigns or to design risk management strategies, which can be specialized to local ecohydrological boundary conditions.

- Steady state scenarios do not allow assessing contamination and pollution and overpredict pollution time scales if compared with time-resolved simulations. Remarkably the sample-averaged GLP and AMPA biodegradation efficiencies show only minor differences across the tested scenarios. This result shows that steady state simulation may be able to match biodegradation efficiency yielded by time-resolved boundary conditions, but are not effective in rendering contamination hazards. Average flow conditions neglect the impact of short range fluctuations that play a predominant role in triggering contamination and pollution.

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have contributed to the research results reported within this paper.
Appendix A. Modelling of feedbacks between water saturation and biodegradation rates

The rate of change of an aqueous species for a given reaction in (6) is \( \dot{r}^i = \frac{dX^i}{dt} = x_i R^i \), where \( x_i \) is the stoichiometric number for species \( i \) and \( R^i \) [ML\(^{-3}\)T\(^{-1}\)] is the reaction velocity. For a generic reaction with \( n_O \) order kinetic products, \( n_{MM} \) Michaelis-Menten-Monod terms with concentration \( X_{n_{MM}} \), \( n_{COM} \) competitive reactants \( (X_{n_{COM}}) \), and \( n_{INB} \) inhibition terms \( (X_{n_{INB}}) \), the reaction velocity \( R \) is written as

\[
R^i = r_f B \prod_{n_O} X_{nO}^{x_i} \cdot \prod_{n_{MM}} \frac{X_{nMM}}{X_{nMM} + K_{nMM}} \left(1 + \sum_{n_{COM}} \frac{X_{nCOM}}{K_{nCOM}} \right) \prod_{n_{INB}} \frac{X_{nINB}}{X_{nINB} + K_{nINB}},
\]  

(A.1)

where \( r \) [T\(^{-1}\)] is the reaction rate constant, \( K_{n_{MM}}, K_{n_{INB}}, K_{n_{COM}} \) are the Michaelis-Menten half saturation, competition and inhibition constants, respectively, \( f_B = 1 \) if the reaction is chemical or if the reaction is biochemical.

\[
f_B = \min \{ f(S_B), f(\Theta), f(S_I)/\max\{f(S_I)\}\},
\]  

(A.2)

where \( f(S_B) \), \( f(\Theta) \) and \( f(S_I) \) are the specific microbial response functions to space availability, temperature and water saturation, respectively. These terms are evaluated as

\[
f(S_B) = \min \left\{ 1 - \frac{S_B - S_{lr}}{1 - S_{gr} - S_{lr}}, 1 - \frac{f_1 S_B}{S_I}, 1 - \frac{(1 - f_I) S_B}{S_g} \right\},
\]  

(A.3a)

\[
f(\Theta) = \left( \frac{e^{\theta}}{e^{\theta_{LB}} + e^{\theta}} \right)^n \cdot \left( \frac{e^{\theta_{UB}}}{e^{\theta_{UB}} + e^{\theta}} \right)^m,
\]  

(A.3b)

\[
f(S_I) = \frac{S_I}{S_{I,UB} + S_I} \cdot \frac{S_{I,UB}}{S_{I,UB} + S_I},
\]  

(A.3c)

where \( f_1 \) is the biomass water fraction, \( S_B \) is the biomass saturation, \( \theta_{LB} \) and \( \theta_{UB} \) [\( \Theta \)] and \( S_{I,LB} \) and \( S_{I,UB} \) are the lower and upper temperature (in Kelvin) and liquid saturation response
parameters. The three functions in (A.3) introduce a limitation to microbially driven reactions as a function of environmental factors that may limit the bacterial growth and/or activity.

The function \( f(S_B) \) implies that microbial functional groups can grow as long as there is enough free water to immobilize, or gas space available for the cell solid fraction \((1 - f)\) to occupy, or there is enough pore volume to host the total microbial biomass volume. Following the scheme in Maggi & Porporato (2007), the function \( f(S_B) \) also implies that the total water saturation includes the free (mobile) water saturation \( S_l \) and the immobilized water saturation \( S_{IB} = f_l S_B \). As a consequence, the term \( \Delta B \) in Eq. (3) accounts for the rate of change in mobile water saturation \( S_l \) when the total microbial biomass increases (i.e., \( \Delta B > 0 \) expresses water immobilization) or decreases (i.e., \( \Delta B < 0 \) expresses water remobilization). Hence, Eq. (3) is subject to the constraint \( S_l + S_g + S_B = 1 \).

Function \( f(T) \) limits \( R \) when temperature is below \( \theta_{LB} \) and above \( \theta_{UB} \). Finally, function \( f(S_l) \) limits \( R \) when \( S_l \) is below \( S_{l,LB} \) or above \( S_{l,UB} \).

The response function \( f(\Theta) \) appearing in (A.1)-(A.2) was calculated with \( m = 0.1, n = 0.5 \), \( \theta_{LB} = 6 \, ^\circ C \) and \( \theta_{UB} = 45 \, ^\circ C \) to return the microbial activity curve typical of mesophiles documented in (Rittmann & McCarty, 2001) (Figure A.1a), while \( f(S_l) \) was implemented with \( S_{l,LB} = S_{l,UB} = 0.46 \) to represent typical water stresses (e.g., Moyano et al., 2012; Yan et al., 2018) (Figure A.1b). The response function \( f(S_B) \) was implemented with \( f_l = 0.85 \) after Rockhold et al. (2005) and varies with \( S_B \) and therefore with \( t \) and over \( z \).

![Figure A.1](image_url)

Figure A.1: Microbial response functions for (a) temperature stress \( f(\Theta) \), and (b) water stress \( f(S_l) \) as a function of temperature and mobile water saturation, respectively. Functions apply to all microbial functional groups accounted for in the GLP biogeochemical reaction network. The curve for mesophiles (left panel) is from Rittmann & McCarty, 2001; experiments in the right panel are from Wickland & Neff (2008).
Appendix B. Stability of QMC sampling

Results in Figure B.2 shows that 5,000 stochastic realizations resulted in stable relative frequency in the target outputs. The results also allow appreciating that different scenarios resulted in different frequencies.

![Figure B.2: Relative frequency of $M_{GLP}$, $C_{GLP}$, $F_{GLP}$ at increasing number of QMC realizations (from 1,000 in light to 5,000 in dark, grey, red and blue, respectively).](image)

Figure B.2: Relative frequency of $M_{GLP}$, $C_{GLP}$, $F_{GLP}$ at increasing number of QMC realizations (from 1,000 in light to 5,000 in dark, grey, red and blue, respectively).
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