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An unsupervised learning schema for seeking patterns in rms voltage variations at the sub-10-minute time scale

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a r t i c l e i n f o

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A B S T R A C T

This paper proposes an unsupervised learning schema for seeking the patterns in rms voltage variations at the time scale between 1 s and 10 min, a rarely considered time scale in studies but could be relevant for incorrect operation of end-user equipment. The proposed framework employs a Kernel Principal Component Analysis (KPCA) followed by a k-means clustering. The schema is applied on 10-min time series with a 1-s time resolution obtained from 44 different periods of a location south of Sweden. Then, ten patterns are obtained by reconstructing the 10-min time series from each cluster center. The results of the proposed schema show a good separation of cluster centers. Moreover, some statistical power-quality indices are applied to the whole dataset, showing voltage variation between (0.5–3) V over a 10-min window. Obtaining the most suitable indices and applying them to the ten obtained cluster centers and their belonging time series shows that the existing statistical indices may not be enough to show a complete picture of the sub-10 min actual variations. This outcome shows the necessity of extracting 10-min patterns through our proposed schema besides the existing statistics to quantify the voltage variations, levels, and patterns together. Findings of this paper are: Not forgetting the sub-10-min time scale; The necessity of employing both statistics and the proposed schema; Extraction of ten typical patterns; The need for the statistics and patterns that are justified as changes in equipment connected to the grid; and compressing a huge amount of data from powerquality monitoring. The proposed schema is applied to a much less understood phenomena/disturbance type so that this work will result in general knowledge beyond the specific case study.

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1. Introduction

Voltage magnitude (rms value) deviation from its nominal voltage varies over a range of time scales. Power-quality monitoring (collecting measurement data) is an important part of the performance evaluation of power systems and a significant aspect of power-quality studies for network operators. An agreement for data collection with limited capacity has been restricted to 10-min values as defined in the IEC 61000-4-30 standard [\[1,](#page-10-0)[2\]](#page-10-1). The overview of voltage-quality regulation in [\[3\]](#page-10-2) also shows that 10 min is the most common value used. Moreover, there is a lack of performance necessities for voltage quality and knowledge on the levels for sub-10-min values (a time scale between 1 s and 10 min), and power-quality monitoring programs seldom include it. In contrast, this time scale should not be neglected because equipment susceptibility to sub-10-min variations changes.

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Moreover, tripping of PV installations due to overvoltages is seen for the values belonging to the 10-min time scale. Fast voltage variations and light flicker are also due to variations in this time scale [\[4](#page-10-3)–[7\]](#page-10-4). Besides, many different types of equipment (generation or load) show voltage variations in this time scale: PV power installation $[6,8,9]$ $[6,8,9]$ $[6,8,9]$ $[6,8,9]$ $[6,8,9]$, wind power installations $[10,11]$ $[10,11]$ $[10,11]$, EV charging [[12](#page-11-2)], and electric heat pumps [\[13\]](#page-11-3).

A very short variation (VSV) index over the 10-min widow was calculated for a single-customer nanogrid in [\[14\]](#page-11-4). The measurement-based definition of individual rapid voltage changes (voltage steps) as standardized by IEC 61000-4-30 resulted in a number of publications discussing this voltage-quality event [[8](#page-10-6)[,15\]](#page-11-5). However, voltage steps are only one aspect of the sub-10 min variations. Later, some research has been done on statistical indices and actual levels for quantifying variations of rms voltage $[6,16]$ $[6,16]$ and harmonic voltage $[17]$ $[17]$ $[17]$ in a sub-10-min time scale. Such statistics are defined, for example, the 95th percentile of 1-s values of the rms or harmonic voltage over the 10-min window minus a 10-min rms value. As single-window or singlesite, these statistical indices are appropriate for quantifying some

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kind of voltage variations but do not result in typical patterns of variations versus a 10-min time window. A complete picture of the sub-10-min time range needs to quantify not only the levels but also the patterns.

Power-quality monitoring can result in large amounts of data, especially where it concerns measurements at multiple locations over a long period. For example, one year of monitoring rms values (3 voltages, 3 currents, 1 s values) results in about 190 million data points per location, which will take a very high amount of data. Although manual analysis is possible, it is too time-consuming for multiple location measurements. Automatic analysis methods enable a continuous assessment of the power quality and other operational aspects without timeconsuming human intervention. Recent developments in machine learning could identify such hidden patterns. In general, two sets of methods can be used for training as supervised and unsupervised [\[18,](#page-11-8)[19](#page-11-9)]. The initial approaches, as supervised, needed a pre-labeled dataset. In [\[20–](#page-11-10)[22](#page-11-11)], expert systems classify powerquality disturbances. Artificial intelligent-based methods used expert classifiers like support vector machines [[23](#page-11-12)[–25\]](#page-11-13), ensemble learnings [[26](#page-11-14)], and neural networks [[27](#page-11-15)[,28\]](#page-11-16). Automatic extraction of input features has been done as one step before the supervised classifiers in literature [[29](#page-11-17)[,30\]](#page-11-18). Seeking patterns, socalled time series clustering is part of unsupervised problems since labeling/assigning cluster numbers to the input dataset (e.g., time series of signal variations) is not possible/too timeconsuming along with the errors. As observed in [[29](#page-11-17)[,30\]](#page-11-18), the automatic extraction of principal features has a normally better role than manually extracted features (e.g., statistical indices) [[1,](#page-10-8) [31](#page-11-19)[,32\]](#page-11-20) to group a dataset. There are many works done on time series clustering. e.g., clustering on the areas of big data in [\[33\]](#page-11-21), multivariable time series clustering in [\[34–](#page-11-22)[36](#page-11-23)], and clustering by using different tools than k-means and the Euclidean distance measurement criterion addressed in [\[37\]](#page-11-24) as shape-based clustering and in [[38](#page-11-25)] as fuzzy-based by using Distance Time Wrapping (DTW) as similarity measure criteria. However, a limited number of applications in power quality data measurement analysis have been found, e.g., a time-series clustering methodology for knowledge extraction in energy consumption data in [\[39\]](#page-11-26), a clustering method for probabilistic evaluation of harmonic load flow in [\[40\]](#page-11-27) and in [\[41\]](#page-11-28) a k-means clustering for identification of distributed generation contribution. A deep autoencoder followed by a kmeans clustering was applied in voltage harmonics with a 1-day time window by a 10-min resolution in $[42-44]$ $[42-44]$ $[42-44]$ $[42-44]$ to seek the daily patterns. They are concerned with a rather well-understood phenomenon (daily variation in harmonic voltage) so that their method did not create any new general knowledge. Among the few unsupervised machine learning schemas applicable for power quality measurement analysis, none of them have been applied

yet to seek patterns for rms/harmonic voltage fast variations in the sub-10-min scale, which is different from daily variational patterns.

On following the refs. [[6,](#page-10-9)[7,](#page-10-10)[16](#page-11-31),[17\]](#page-11-32) to learn more about the sub-10-min time scale, this paper proposes an unsupervised learning schema, scalable and computationally cheap, to seek the sub-10 min patterns in rms voltage variations at the time scale between 1 s and 10 min. The upper limit of the window (10 min) is defined in the power-quality monitoring standard, IEC61000-4-30, and is commonly used in power quality monitoring. The lower limit of the window (1 s) is not part of any standard nor commonly used. The 1-s period is partly set by the available measurement data, partly by the computation effort needed, and partly by the fact that standards and regulations exist for time scales below a few seconds. In this paper, it was decided to go for unsupervised learning because (a) the time window 1 s-10 min is still largely unexplored, (b) there is still a lack of knowledge and insight about the window (c) relevant information for labeling is missing. The unsupervised schema employs a Kernel Principal Component Analysis (KPCA) to automatically reduce the input feature size and generate principal features. A k-means clustering is employed to distinguish between the principal features into *K* clusters. A t-SNE (t-Distributed Stochastic Neighbor Embedding) is employed to visualize the principal and clustered feature vectors into two dimensions. The method is applied to measured 10 min time series with a 1-s time resolution obtained from 44 different periods of an apartment in a city in southern Sweden. The apartment is part of a 12-story apartment building with two elevators, 230-kV, and 50 Hz. Then, ten typical 10-min patterns are obtained by reconstructing the cluster centers. A statistical analysis of the obtained results shows that the proposed schema is effective in seeking sub-10-min patterns and confirms that a full representation of voltage variations at the sub-10-min scale needs both results of statistical indices and extracted patterns. In comparison with $[42-44]$ $[42-44]$ $[42-44]$, our proposed schema is applied to a much less understood phenomena/disturbance type so that the work will result in general knowledge beyond the specific case study.

Section [2](#page-2-0) of this paper presents the single-window existing statistical indices shortly. Section [3](#page-2-1) describes our unsupervised learning schema in detail. Section [4](#page-3-0) presents the measurement dataset and shows some examples of variations on the time scale below 10 min. A statistical analysis of the whole dataset, the results of the proposed schema, and statistical analysis of obtained cluster centers and their belonging samples are given in Section [5](#page-3-1). Section [6](#page-7-0) discusses the paper and suggests future works, and finally, Section [7](#page-10-11) concludes the paper.

Fig. 1. Process of the proposed unsupervised learning schema for clustering 10-min time series.

2. Single-window existing statistical indices

In order to confirm the further results of our unsupervised schema and to have a full picture of the variations of rms voltage in a sub-10-min time scale, [Table](#page-1-0) [1](#page-1-0) explains the single-window existing indices [\[16](#page-11-31)[,17\]](#page-11-32) used in this paper. The indices quantify the range of 1-s values within a 10-min window and somehow show a picture of the variation of values. 1-s very short variations are a difference between 1-s rms voltages and the 10-min rms voltage. Also, a 10-min rms voltage is the rms of 1-s values within the 10-min window.

3. Proposed unsupervised learning schema

The process of the proposed unsupervised learning scheme consists of four modules optimized by the grid search, as shown in [Fig.](#page-2-2) [1.](#page-2-2)

(a) Pre-processing measurement dataset; (b) KPCA on the feature vectors (normalized high-dimensional) *xⁱ* , which results in the vectors h_i with p principal features; (c) Using k-means clustering to group the principal features *hi*; (d) Reconstruction of cluster centers using an inverse KPCA; (e) Visualizing the size reduced principal and clustered features in 2D space using t-SNE.

(a) Pre-processing the measurement dataset

The initial part of the proposed methodology is pre-processing of the dataset. First, the 1-s rms voltages are shaped within 10-min windows. Therefore, an input dataset matrix *X m*×n ([1\)](#page-2-3) concludes, in which each row *xⁱ* includes a 10-min feature vector with 1-s resolution including $n = 600$ dimensions (600×1 $s = 600$ s/10 min).

$$
X^{m \times n} = [x_1, x_2, \dots, x_m]^T,
$$

\n
$$
x_i = [x_{i1}, x_{i2}, \dots, x_{in}], \quad i = 1, 2, \dots, m, n = 600
$$
\n(1)

n is the dimension of each sample (time series or 10-min windows) and *m* is the number of samples. Second, the windows including missing data (NaN values), are managed by two different removing, and replacing actions. In this way, the windows with a high number ($\geq 50\% \times 600 = 300$ values) of NaN values are removed (24 windows equal to 0.32% of all windows in our measurement dataset), and the NaN values in windows with NaN values less than 300 are replaced to the window' mean value.

The proposed model is based on unsupervised learning algorithms (KPCA+k-means), which use the distance between data

points to determine the similarity between samples. Considering a not normalized dataset, the higher weightage may be given to higher-magnitude features; consequently, the ML-based model will be biased toward such features, and the performance deteriorates. Hence, a Min-Max normalization ([2](#page-2-4)) is applied to each column of matrix *X* from several possible approaches. In this way, each of the 600 features is considered as an independent coordinate which means that those samples with very high (low) 1s rms voltages will have values close to 1 (0). Each time series is scaled between [0,1] at the end of this operation. x_{ii} − min(x_{ii})

$$
x_{ij[0,1]} = \frac{x_{ij} \cdot \min(x_{ij})}{\max(x_{ij}) - \min(x_{ij})},
$$
\n(2)

$$
j = 1, 2, ..., 600, i = 1, 2, ..., m
$$
 for each j

(b) KPCA

After using Principal Component Analysis (PCA) [\[45\]](#page-11-33) and sparse PCA [[46](#page-11-34)] on the dataset, a KPCA algorithm was chosen and employed as a non-linear method. KPCA takes high-dimensional data sequences (x_i^{600D}) from $X^{m\times600}$, maps data space $x_i(i)$ = 1, 2, ..., *m*) to a higher dimension space $\Phi(x_i)$, $(i = 1, 2, \ldots, m)$ and makes a non-linear function (kernel matrix *K* (3)). After checking the results of different kernels (Polynomial, RBF, Cosine, and sigmoid) $[47]$, this study chose a cosine kernel (4) . The next step is reducing dimension linearly. Hence, KPCA does an eigen analysis and projects the feature vectors on the first *p* dominant eigenvectors (principal components). Finally, the output of KPCA is determined to map the input to low-dimensional principal feature vectors $(h_i^{pD} = f_{for}(x_i))$ into $H^{m \times p}$ [\(5](#page-2-6)).

$$
\boldsymbol{K}^{m \times m} = \begin{bmatrix} [\boldsymbol{\Phi}(x_1), \boldsymbol{\Phi}(x_1)], & \cdots & [\boldsymbol{\Phi}(x_1), \boldsymbol{\Phi}(x_m)] \\ \vdots & \ddots & \vdots \\ [\boldsymbol{\Phi}(x_m), \boldsymbol{\Phi}(x_1)] & \cdots & [\boldsymbol{\Phi}(x_m), \boldsymbol{\Phi}(x_m)] \end{bmatrix}
$$
(3)

$$
[\Phi(x_i), \Phi(x_j)] = \frac{\Phi(x_i)\Phi(x_j)^T}{\|\Phi(x_i)\| \|\Phi(x_j)\|}
$$
\n(4)

$$
H^{m \times p} = [h_1, h_2, \dots, h_m]^T, h_i = [h_{i1}, h_{i2}, \dots, h_{ip}], i = 1, 2, \dots, m
$$
\n(5)

In addition to the size feature reduction, this step may help in better initialization of centroids for k-means clustering [\[48\]](#page-11-36). The best mapping from the input of KPCA to the output is obtained after many runs of the function of *KernelPCA* by the *''cosine''* kernel in *Phyton* under parameter settings, where the best mapping is found as a minimum loss.

Fig. 2. Four examples of variations in rms voltage within a 10-minute window.

(c) K-means clustering

Principal feature vectors (h_i^{pD}) from the output of KPCA are inputted to the k-means clustering block. The *k-means++* initialization scheme [\[49\]](#page-11-37) finds out *K* initial centroids (cluster centers) μ_j in an effective way. The k-means clustering aims to group the vectors h_i into *K* clusters (in our case, $K = 10$). Each feature vector is assigned to the cluster with the shortest 'distance' to one of the cluster centers. Centroids are then updated once all feature vectors are assigned. The k-means minimizes (6) (6) the sum of the Euclidian distances of each *hⁱ* to its cluster centroid. This inertia is then trained by alternatively applying the following steps ([7\)](#page-3-3) until convergence:

$$
\min \sum_{j=1}^{K} \sum_{i=1}^{m} \omega_{ij} \|h_i - \mu_j\|^2
$$
\n(6)

$$
\omega_{ij} = \begin{cases} 1, & \text{if } j = \text{argmin}_j \left\| h_i - \mu_j \right\|^2, \\ 0, & \text{otherwise} \end{cases}, \quad \mu_j = \frac{\sum_{i=1}^m \omega_{ij} h_i}{\sum_{i=1}^m \omega_{ij}} \tag{7}
$$

where the first part of (7) (7) (7) assigns each feature vector h_i to its closest μ_j , and the second part updates the μ_j by averaging all feature vectors within the *j*th cluster.

(d) Reconstruction of cluster centers

To further analyze the properties of clustered feature vectors, especially the representative data from each cluster, feature vectors from the centroids are fed to the inverse KPCA function to reconstruct the representative data sequence of each cluster, $x_j^{rec} = f_{inv}(\mu_j)$. Where x_j^{rec} is the reconstructed data sequence (600 dimensions) for the feature vector μ_j (*j*th cluster center with the dimension *p*). These reconstructed data sequences are used as the representative data patterns for the individual clusters.

(e) Visualization of principal and clustered features by t-SNE

To visualize the principal feature vectors (h_i^{pD}) (non-clustered) from *H m*×*p* and the clustered principal vectors (clustered *hi*), a t-SNE method [[50](#page-11-38)] is used. T-SNE is another embedding method for converting high-D Gaussian distributed feature points into low-D (two/three) points in a t-student distribution. First, the similarity between two feature vectors, *i* and *j* belong to spaces nonclustered/clustered h_i are modeled by p_{ii} and q_{ii} in the input and

output of t-SNE, respectively. The mapping is then obtained by minimizing the KL divergence between those two distributions:

$$
KL(P \parallel Q) = \sum_{i \neq j} p_{ij} \log \frac{p_{ij}}{q_{ij}}
$$
\n(8)

In our case, using t-SNE is only for 2D visualization of feature vectors, principal and clustered principal to see how the proposed unsupervised methodology extracts *K* different patterns.

4. Measurement dataset

Time series of the 1-s rms voltage were obtained from recorded measurements of a location, which was an apartment in a city in southern Sweden. The apartment is part of a 12-story apartment building with two elevators. During a non-continuous eightmonth period between 2017 and 2018, all measurements were performed at a wall outlet, 230-V, 50-Hz. A Metrum PQsmart portable monitor was used for the measurements. All measurements were following IEC 61000-4-30 Class A. 44 different periods of measurement, each period about 168 10-min windows, corresponded a total dataset consisting of 7380 10-min windows. By pre-processing the dataset and considering each window as an input sample, $m = 7356$ input feature vectors x_i (10-min sequences, containing 600 1-s samples each) is obtained and concludes matrix $X^{7356\times600}$ (removing only 7380-7356 = 24 windows, i.e., 0.32% of all windows). Four different examples of the variations in rms voltage within a 10-min window from the input dataset, samples 9, 530, 2515, and 3030, are shown in [Fig.](#page-3-4) [2.](#page-3-4) The variations can belong to a similar pattern or into some different patterns. Therefore, it is worth discovering underlying patterns from the dataset, where one may further find good interpretations coupled with physical reality. Moreover, this can obtain a picture of voltage magnitude variations at the time scales below ten minutes.

5. Results and analysis

5.1. Analysis of discussed single-window indices on the whole dataset

The probability distribution functions of the fourteen indices ([Table](#page-1-0) [1](#page-1-0)), obtained over all 10-min windows of the whole dataset,

Fig. 3. A probability distribution for single-window indices over the whole dataset. (a) Indices quantifying the range in value (b) Overdeviation indices (c) Underdeviation indices (d) 10-min VSVs and standard deviations.

are shown in [Fig.](#page-4-0) [3](#page-4-0) to see how the general situation of the dataset looks like in the statistical view. The average value of the indices within the windows is almost equal to the values corresponding to the median. From [Fig.](#page-4-0) [3](#page-4-0)a, voltage typically has varied by 0.5 V–3 V within a 10-min window. A range exceeding 1–2 V is common. The differences between higher-order and lower-order statistics for the R100, R98, R90, and R80 indices are higher and show a kind of variations within a 10-min window. For example, for the 80th percentile, the difference between R80 and R100 is 1.23 V and, for the median (50th percentile), the difference is 1 V. The distribution functions for [Fig.](#page-4-0) [3a](#page-4-0) and b have a similar pattern (only a factor of two is the difference). For the 80th percentile, there is a difference of 0.56 V between P90 and P100 for overdeviation indices, but there is a 0.42 V difference for the median. The difference for the median between P0 and P10 (for underdeviations) is 0.5 V, as seen in [Fig.](#page-4-0) [3](#page-4-0)c, which is higher than the value for overdeviations. As shown in [Fig.](#page-4-0) [3](#page-4-0)d, VSV is slightly higher than Std., and there is only a 0.12 V difference for the median.

[Fig.](#page-4-1) [4](#page-4-1) shows a correlation matrix between all the fourteen indices mentioned above. A high value of the coefficients between two indices shows a strong correlation, and they vary together. The pairs R98-R100, P99-P100, and R80-Std. have the highest correlations (99%). By taking an average over the correlation between each index and other ones, the most suitable indices (strongest correlation) are calculated as R90 (from the range indices), P95 (from the overdevition indices), and P5 (from the underdeviation indices).

The authors of this paper tried to consider a feature engineering and inputted all the 14 statistical indices besides the 10-min windows as input features to the proposed unsupervised learning schema. However, the high correlation between some indices did not positively affect the clustering results. As a conclusion from Section [5.1,](#page-3-5) the most suitable indices along with Std. (which is somehow similar to VSV) are used, in the next section, for the

Fig. 4. Correlation coefficients between various single-window indices.

windows belonging to each cluster to show how the concluded patterns are proper and to confirm almost similar 1-s rms voltage variations within the windows belonging to each cluster.

5.2. Results of proposed unsupervised learning schema

After many runs of the function of *KernelPCA by ''cosine''* kernel on the input dataset, the singular values corresponding to each singular mode index, related to every one of the first 50 principal components, are shown in [Fig.](#page-5-0) [5](#page-5-0). The singular values are equal to the 2-norms of the variables of principal components in the lower-dimensional space. In this study, we have considered only

Fig. 5. Singular values corresponding to each singular mode index for KPCA.

Fig. 6. The inertia of k-means vs. a different number of clusters.

the first $p = 10$ principal components (saving 82.38% information) during the training process of KPCA since almost the same results were obtained in comparison to 50 components, which could save 94.8% information.

[Fig.](#page-5-1) [6](#page-5-1) shows different inertia (within-cluster sum of squares criterion, a measure of how internally coherent clusters are, low values are better) versus a different number of clusters. The interval to choose the optimal number of clusters is marked by a rectangular, which is a number from 8 to 13 selected according to the knee of the curve. After checking the results of all the six numbers of *K*, $K = 10$ was chosen as the elbow point [[51\]](#page-11-39). In this way, some good interpretations coupled with physical reality were found.

A function 2D t-SNE was used to visualize the principal feature vectors (10 dimensions) and the clustered principal features (10 dimensional), as shown in [Figs.](#page-6-0) [7a](#page-6-0) and [7](#page-6-0)b, respectively. The parameters of the t-SNE (input:10D, output:2D) were set as Barnes–Hut algorithm, Euclidean distance metrics, perplexity = 30. The best 2D embedding space for visualization was selected by selecting the minimum loss values from running t-SNE 100 times. Ten clusters, colored in [Fig.](#page-6-0) [7b](#page-6-0), show 10 different possible patterns, whose overlap between some clusters shows a need for more dimensions (principal components more than three) to be plotted. However, each time series belongs to only one cluster (hard clustering). Later on, [Fig.](#page-7-1) [9](#page-7-1) will show a better visualization of the clusters.

The ten centroids (cluster centers), which are 10D time series of rms voltages, are an average of all the 10D time series belonging to each of 10 clusters. All ten centroids are reconstructed as 600D time series using an inverse function of KPCA. The reconstructed data sequences indicate representative patterns for the ten individual clusters, as shown in [Fig.](#page-6-1) [8.](#page-6-1) Cluster 5 [\(Fig.](#page-6-1) [8](#page-6-1)e) includes 3287 samples, the maximum number of 10-min time series belonging to clusters (the dark yellow circles in [Fig.](#page-6-0) [7b](#page-6-0)).

Cluster 8 ([Fig.](#page-6-1) [8f](#page-6-1)) consists of only one sample. In order to check the behavior of this cluster, a plot of the two first principal components of KPCA has shown in [Fig.](#page-7-1) [9](#page-7-1). As seen in this figure, this type of plot shows a clearer visualization of clusters than t-SNE ([Fig.](#page-6-0) [7b](#page-6-0)) and that cluster 8 is different from other clusters and may be considered an outlier. Hence, one may consider the number of obtained clusters as 9 and not 10. The observed different behavior for cluster 8 is related to two things: first, the cluster has a minimum 1-s value of rms voltage from 0 min–8 min between all input 10-min time series and the latter is regarding a different variation pattern. As seen in [Fig.](#page-6-1) [8](#page-6-1), the differences between the patterns are in the range of rms voltage (value/magnitude), the shape of variations (profile/growth pattern), and variations times. Cluster 4 (regardless of cluster 8) has a maximum range of variations. Clusters 6 and 9 seem to be similar, but the vertical axis range is different, and looking at [Fig.](#page-6-0) [7](#page-6-0)b shows a separation of those clusters.

Moreover, the patterns realized in [Fig.](#page-6-1) [8](#page-6-1) are smoother than the real samples [\(Fig.](#page-3-4) [2\)](#page-3-4) because there is an intrinsic characteristic of averaging in k-means clustering. In order to show that the patterns are a good representation of all samples, four normalized samples that belong to each of clusters 2, 4, 6, 7, 9, and 10 are shown in [Fig.](#page-8-0) [10](#page-8-0). The sample numbers are according to the row numbers of the input dataset. As seen in [Fig.](#page-8-0) [10](#page-8-0), the samples in each cluster can show some differences depending on the intraclass variance (associated with within-class spread). However, the overall patterns of the samples would remain largely the same.

5.3. Analysis of the reconstructed cluster centers and cluster samples

An analysis of the ten reconstructed cluster centers (patterns) and clusters' samples is explained in this section to show: (1) Well separation of the ten clusters; (2) The necessity of obtained patterns beside statistical indices over a sub-10-min time scale.

5.3.1. The similarity between the ten-reconstructed cluster centers

In order to show similarity/dissimilarity between the tenreconstructed cluster centers, a correlation matrix is calculated and shown in [Fig.](#page-8-1) [11.](#page-8-1) This similarity measure estimates the cosine of the angle between two centered (adjusted) cluster centers, therefore only checking the growth patterns and not magnitude differences. Actually, we used a Cosine similarity measure, unlike the Euclidian distance used in k-means. As marked in this figure, the maximum positive correlation is between cluster centers 3 and 4 because they have an almost similar growth pattern. However, [Fig.](#page-6-1) [8](#page-6-1)c (cluster 3) and [Fig.](#page-6-1) [8d](#page-6-1) (cluster 4) show a clear difference in the voltage ranges.

The Euclidian distance between them (real values, not normalized) is 61.82, and cluster 4 is totally below cluster 3 in terms of voltage magnitude. Another seen difference is the variation shape after $t = 7$ min. Moreover, t-SNE in [Fig.](#page-6-0) [7b](#page-6-0) and 9 also show the separation of the two clusters. A maximum negative correlation is obtained for clusters 4 and 9. As seen in [Fig.](#page-6-1) [8](#page-6-1)d, there is a very inverse behavior, which can also be seen in [Fig.](#page-8-1) [11](#page-8-1) since clusters 4 and 9 are placed in the opposite directions of principal component 1 in the t-SNE plot. The other correlation coefficients confirm distinguishing between the obtained cluster centers from the proposed schema.

5.3.2. Selected single-window indices for the clusters' samples

In order to show how well the 10-min time series are grouped into ten clusters and to display a homogeneity between the time series placed in each cluster, a statistical analysis is done. In this regard, the selected indices of R90, P95, P5, and Std. are employed (Section 4.1), and a probability distribution for

Fig. 7. Visualization of feature vectors (10D) by 2D t-SNE. (a) Principal (before k-means); (b) Clustered principal (after k-means), cluster 8 includes only one sample.. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

Fig. 8. Reconstructed patterns (cluster centers) including the number of samples belonging to each cluster (a) Cluster 1 and 7; (b) Cluster 2; (c) Cluster 3 and 6; (d) Cluster 4, 9 and 10; (e) Cluster 5; (f) Cluster 8.

each cluster, including their samples, is shown in [Figs.](#page-8-2) [12](#page-8-2)[–15,](#page-9-0) respectively.

It is seen from all four indices that the probability distribution function for clusters 5 and 3 shows a softer curve, which is because the clusters are the most dominant ones with the highest number of samples. There is also a clear separation of the values for the indices between different clusters in terms of the probability distribution. This is a result of the well separation of the samples as grouped into ten clusters and displaying a homogeneity between the samples within each cluster. The indices, which show an almost similar result between a pair cluster, are explained here:

- R90: Clusters $\{1,7\}$ (marked in [Fig.](#page-8-2) [12\)](#page-8-2)
- P95 and Std.: Clusters {1,7} and clusters {3,6} (marked in [Figs.](#page-8-3) [13](#page-8-3) and [15](#page-9-0))
- P5: Clusters $\{1,7\}$ and clusters $\{2,6\}$ (marked in [Fig.](#page-8-4) [14\)](#page-8-4)

However, for cluster centers {1,7}, the shape of variations of rms voltage is completely different ([Fig.](#page-6-1) [8](#page-6-1)a), and there is only a −30% correlation between those cluster centers [\(Fig.](#page-8-1) [11\)](#page-8-1). Also, the shape of variations for cluster centers {3,6} is totally dissimilar ([Fig.](#page-6-1) [8c](#page-6-1)), and a −67% correlation is seen in [Fig.](#page-8-1) [11](#page-8-1). Regarding cluster centers {2,6}, the shape and range of variations are different ([Fig.](#page-6-1) [8](#page-6-1)b and c), and a small +29% correlation is obtained between them ([Fig.](#page-8-1) [11](#page-8-1)).

5.3.3. Selected single-window indices for the ten-reconstructed cluster centers

In the following, the selected indices are applied to the reconstructed cluster centers, and the results in terms of range and a percentage of nominal voltage are given in [Table](#page-7-2) [2](#page-7-2). The indices showing an almost similar result between a pair of clusters are as follows:

Table 2

 V_n : Nominal voltage; Colored highlights show close values of indices for different cluster centers.

Fig. 9. Visualization of clustered principal feature vectors (10D) by only the first two principal components of KPCA. Note the place of cluster 8.

- R90, P95, and Std.: Clusters $\{1,7\}$ and clusters $\{3,6\}$
- P5: Clusters $\{1,7,9\}$ and clusters $\{2,6\}$

Concerning clusters {1,9}, there is a different range and vari-ation shape [\(Fig.](#page-7-1) [9](#page-7-1)a and d) with a -82% correlation. For clusters {7,9}, the range and time of variations are dissimilar ([Fig.](#page-8-0) [10a](#page-8-0) and d) even with a +75% correlation.

It is concluded from Section 4.3 that the patterns obtained from the proposed unsupervised schema are correctly separated, and their related time series have mostly similar behavior. Moreover, the statistics, the single-window indices, applied on cluster centers or their samples may wrongly consider some clusters in the same category and cannot distinguish between clusters. The correlation coefficients between cluster centers are a good measure to show the separation of the clusters. However, in this paper, clusters {3,4} are considered separately even if there is a high similarity in the variation shape between them, and that cluster 3 consists of only 164 samples compared with 1027 ones placed in cluster 4. This is because the range of variations of cluster 4 is totally below cluster 3.

As an overall conclusion, firstly, the variations in rms voltage at a time scale between 1-s and 10-min should not be neglected. Secondly, the statistical single-window indices may not be enough to show a full picture of the sub-10 min real variations. Hence, besides the statistics, extracting 10-min window patterns from a proper unsupervised framework (proposed schema in this paper) is essential.

6. Discussion and future works

6.1. Application of the unsupervised learning schema

The work presented in this paper uses time series of 1-s rms voltages over a 10-min window. According to the results of this paper and literature [\[16\]](#page-11-31), oscillations are happening in the sub-10 min period. As one way to show the oscillations, this work seeks the sub-10 min patterns of rms voltage using a proposed unsupervised method. In that way, some important patterns in the large data of low voltage variational measurements were found. Compressing a huge amount of data from power-quality monitoring is also done in this study since the input data size is reduced from 600 to 10 by a factor of 60. The proposed schema, besides the statistics, is the first step before studying the potential impacts of the sub-10-min variations on equipment and quantifying the grid's hosting capacity for different types of new equipment connected to the grid. The proposed schema is scalable and computationally cheap, which makes it appropriate for extracting typical patterns in the big data domain.

Compared with some literature [[52](#page-11-40)–[56\]](#page-11-41) that uses pre-defined scalar features in a labeled dataset to locate the source of voltage dips, one important application of our proposed schema can be solving that two-classes problem in an unsupervised intelligent schema. In this way, the input of KPCA is the rms waveforms of voltages and currents (merged as one signal or into two separate signals) with a high time resolution over a selected window, including pre and after dip cycles. The output of k-means will show two groups, with which one expert can label the group members as downstream and upstream as the source location of voltage dips.

6.2. The number of clusters

The k-means clustering method requires the user to select the number of clusters in advance. In our study, the interval to select an optimum number of *K* is a number between 8–13 ([Fig.](#page-5-1) [6\)](#page-5-1), and through multiple tries, $K = 10$ is chosen so that some good interpretations coupled with physical reality are found. [Table](#page-9-1) [3](#page-9-1) compares two numbers of *K*, 10, and 13 and their samples. As seen in this table, there is not much difference between the

Fig. 10. Several reconstructed normalized samples in 6 clusters. (a) Cluster 2; (b) Cluster 4; (c) Cluster 6; (d) Cluster 7; (e) Cluster 9; (f) Cluster 10.

Fig. 11. The similarity between centered cluster centers.

Fig. 12. Probability distribution of R90 for the time series of each cluster.

results, and by choosing $K = 13$, we might just be splitting the clusters for no good reason. Also, for both numbers of *K*, the cluster with 1 sample is seen as an outlier. One may consider only 4 clusters; however, choosing $K = 10$ (from [Fig.](#page-5-1) [6](#page-5-1)), the possible sub-patterns showing different values and variation shapes under some clusters are extracted, where feature vectors can display large within-cluster variance.

Fig. 13. Probability distribution of P95 for the time series of each cluster.

Fig. 14. Probability distribution of P5 for the time series of each cluster.

A future implementation of the scheme could allow the user to select the number of clusters so that an interpretation of the results is possible.

6.3. Sub-10-min variations from the view of the unsupervised learning schema

The samples (10-min windows) within the clusters differ depending on the intra-class variance. However, the overall pattern of samples remains largely the same. Since each pattern is an average of its own samples, the fewer the number of samples

Table 3

Number of samples and a percentage of the total number of samples for two different numbers of *K*.

\bf{v}		Cluster no.												
		1 a									10			
10	No. of samples	3287	1027	914	627	503	430	209	194	164				
	(% of total samples)	44.68	3.96	12.43	8.52	6.84	5.85	2.84	2.64	2.23	0.01			
13	No. of samples	2760	174	905	519	386	379	364	356	248	127	74	63	
	(% of total samples)	37.52	15.96	12.30	7.06	5.25	5.15	4.95	4.84	3.37	1.73	1.01	0.86	0.01

^aThe number of samples/clusters is sorted to show a better comparison between two numbers of *K*.

Fig. 15. Probability distribution of Std. for the time series of each cluster.

within a cluster, the more similar those samples are to the reconstructed cluster center (pattern). Hence, all clusters except 3, 5, and 6 look very similar to their own samples. Pattern 5 is very common (small random variations in rms voltage), and patterns 3 and 6 are less common (a negative/positive ramp or a single curvy step superimposed on a very small random variation).

Each of the ten patterns is a representative of a number of 10-min windows. According to the actual recordings, they can be considered ''ten typical patterns''. However, to say this with more confidence, there is still a need for more 10-min windows over months, seasons, or one year. Moreover, the number of clusters should also be selected carefully. From the output of the unsupervised schema, the samples 9, 530, 2515, and 3030 shown in [Fig.](#page-3-4) [2](#page-3-4) belong to the patterns 3, 3, 6, and 1, respectively. The real samples are somehow following the related patterns. Nevertheless, although the samples' overall patterns within clusters 3, 6, and 1 are similar, the averaging of many samples within the clusters generates smooth cluster centers, making some differences in oscillation values between the patterns and real samples.

6.4. Other feature-size reduction tools, distance measurement, and clustering methods

The KPCA with ''Cosine'' kernel, as a simple tool, was employed in the proposed unsupervised schema to reduce the feature size from 600 to 10. Meantime, other tools like linear PCA and sparse PCA were also investigated. Nevertheless, they were not successful in separating and unfolding input data as a tool to help k-means clustering. Moreover, the results without using KPCA and only k-means were checked. [Fig.](#page-9-3) [16](#page-9-3) shows a 2D visualization of input data for 10 clusters. As seen in this figure, there is no good separation between clusters compared to [Fig.](#page-6-0) [7b](#page-6-0) (KPCA+kmeans). A selection of 2 clusters would be effective for [Fig.](#page-9-3) [16](#page-9-3) (only k-means), which cannot show the real patterns of our dataset with 7356 input samples.

Other feature size reduction tools like a deep autoencoder (DAE) can be considered in future works instead of the KPCA to see how the clustering results would be for high-resolution

Fig. 16. Visualization of feature vectors (600D) by 2D t-SNE without using KPCA.

time series. However, using a DAE is not as simple as the used KPCA. [Table](#page-10-12) [4](#page-10-12) shows a structured-based comparison between our proposed schema (KPCA+k-means) and (DAE+k-means) [\[42](#page-11-29)]. As shown in this table, the proposed schema/ref. [\[42](#page-11-29)] reached 10/2 clusters/patterns while having a higher/fewer number of input samples, longer/shorter window length, higher/lower time resolution, less/more principal components, and somehow a slower/ faster workstation. The findings from [Table](#page-10-12) [4](#page-10-12) confirm the much simpler schema of the proposed method.

Although the proposed method is intended for off-line use and aimed initially at obtaining general knowledge about a new phenomenon, [Table](#page-10-13) [5](#page-10-13) shows the detailed time required for running the proposed schema and the method in [[42\]](#page-11-29). The total running time of the proposed schema is about 20% of the total running of the [[42](#page-11-29)].

On the other hand, replacing the Euclidian distance used in kmeans clustering by DTW [\[38\]](#page-11-25) can be another future work. Using the k-medoid method [[57](#page-11-42)] instead of k-mean can be another way to obtain patterns. In this way, the most center of each cluster is selected as the cluster pattern.

6.5. Other variations

The proposed unsupervised learning schema was illustrated by applying it to rms voltage variations over a 10-min period. Since the schema is structured in such a way that its application is possible for any kind of signal, voltage, and current, future studies can seek the patterns for variations in harmonic voltage/current in a sub-10 min period.

6.6. Supplementary works

The measurements used in this study were related to 44 different periods in one location. In order to find more actual patterns, measurements from a number of locations around the

Table 4

A comparison of our proposed schema and ref. [\[42\]](#page-11-29).

 \mathbf{N}_2 , V_3 , V_4 ,

Table 5

world are recommended, which is an ongoing work of the authors of this paper. Using the four selected statistical indices in this paper as input features added to each 10-min window may make more complete patterns, while adding all the fourteen indices could not help in clustering results. Quantifying the variations by installing the PQsmart monitor close to solar power, electric vehicle charging, wind power, electric heat pumps, etc., which can easily change the variation patterns, is needed for future work. Measurements at higher voltage levels like the medium voltage at industrial installations and the impact of variations on the connected equipment are also needed for extra investigations. A possible future direction is to link actual events in the grid or at the load side with characteristics of the sub-10-min variations. However, this will require a bigger data collection.

7. Conclusion

This paper presented an unsupervised learning schema to find patterns in rms voltage variations at the time scale between 1 s and 10 min. First, an analysis of fourteen statistical single-window indices was made on 44 different periods of rms voltage measurements obtained from a location south of Sweden. It was shown that the voltage typically varies between (0.5–3) V over a 10-min window, in which a range exceeding 2 V is common. Calculated correlation coefficients between the fourteen indices showed a high correlation, indicating high similarity. Also, the most suitable ones were obtained: R90, P95, P5, and very short variation or standard deviation. Later, in order to show a full picture of sub-10-min variations, an unsupervised learning method was proposed to seek the sub-10-min patterns. The method consisted of a kernel principal component analysis, followed by principal feature clustering using a k-means algorithm. Ten typical patterns were obtained by reconstructing the 10-min time series from each clustering center. The results showed that the proposed scalable schema effectively extracted patterns, and a correlation matrix between the reconstructed cluster centers confirmed a good separation between them. It is worth mentioning that the unsupervised schema can be applied to any kind of signal.

Applying the most suitable statistics separately to the obtained cluster centers and their belonging samples showed that the existing statistical indices cannot be enough to show a full picture of the sub-10 min actual variations. Henceforth, besides the statistics, extracting 10-min window patterns from our proposed schema would be vital. According to the actual recordings, the patterns can be considered ''ten typical patterns''. However, a trade-off between the number of clusters and the number of 10-min windows in a big dataset would be a vital task for future works. Future work must study potential impacts on the equipment after quantifying the variations, levels, and patterns.

CRediT authorship contribution statement

Younes Mohammadi: Conceptualization, Methodology, Software, Investigation, Writing – original draft, Writing – review & editing. **Seyed Mahdi Miraftabzadeh:** Methodology, Software, Investigation. **Math H.J. Bollen:** Conceptualization, Investigation, Writing – review & editing. **Michela Longo:** Investigation, Writing – review & editing.

Declaration of competing interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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The authors regret <to inform you that the current status of 1st (Younes Mohammadi) and 2nd (Seyed Mahdi Miraftabzadeh) author as ''Postdoctoral researcher'' has been wrongly added to their names during the proofreading stage; Hence the updated list of authors are as below:

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Moreover, the following corrections, are made to the main version of the paper to make the text clearer and simpler for the readers and show the originality of the text purer. The corrections modify some sentences, cite some missing references from the already existing references, and do not affect the main parts of the paper; idea, contribution, and results. Abbreviations used are as: Page (P), Column (C), Section (S), and Line (L). References refer to the initial version of the paper.

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