1	Title:
2	Modeling of braided stents: Comparison of geometry reconstruction
3	and contact strategies
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28 Abstract (words: 244)

Braided stents are self-expandable devices widely used in many different clinical applications. In-29 silico methods could be a useful tool to improve the design stage and preoperative planning; however, 30 31 numerical modeling of braided structures is not trivial. The geometries are often challenging, and a parametric representation is not always easily achieved. Moreover, in the literature, different options 32 have been proposed to handle the contact among the wires, but an extensive comparison of these 33 modeling techniques is missing. In this work, both the geometry and contact issues are discussed. 34 Firstly, an effective strategy based on parametric equations to draw complex braided geometries is 35 36 illustrated and exploited to build three beam meshes resembling commercial devices. Secondly, three finite element simulations (bending, crimping and confined release) were carried out to compare 37 simplified contact techniques involving connector elements with the more realistic but 38 39 computationally expensive option based on the general contact algorithm, which has already been validated in the literature through comparisons with experimental results. Both local (stress 40 distribution) and global quantities (forces/displacements) were analyzed. The results obtained using 41 42 the connectors are significantly affected by wire interpenetrations and over-constraint. The percentage errors reached considerably high values, exceeding 100% in the confined release test and 43 50% in the remaining cases study. Moreover, the errors do not show uniform trends but vary 44 according to the stent geometry, boundary conditions, connector type and investigated entity, 45 suggesting that it is not possible to replace the use of the general contact algorithm with simplified 46 47 approaches.

49 Introduction

The introduction of stents significantly influenced vascular surgery by establishing a valuable 50 alternative to traditional surgery techniques. Despite the good results obtained so far, some problems 51 remain (McHugh et al., 2016). In-silico models can be a powerful tool to investigate the behavior of 52 endoprosthesis improving the design and optimization stages, and supporting the pre-operative 53 planning (Karanasiou et al., 2017; Morlacchi and Migliavacca, 2013). Numerical methods have been 54 55 extensively used in the literature to analyze the biomechanical behavior of stents. From a structural point of view, the crimping and expansion process assessment (Debusschere et al., 2015), the post-56 57 implantation evaluation and the structural or functional problems concerning the device or the native vessel (Auricchio et al., 2011; Derycke et al., 2019; Sturla et al., 2016), the long-term event like 58 degradation (Gastaldi et al., 2011) and fatigue fracture (Azaouzi et al., 2013; Petrini et al., 2016) have 59 60 been investigated. Fluid dynamic studies were also carried out to investigate the blood flow alterations (Cebral et al., 2011), the wall shear stresses (Chiastra et al., 2016; Gundert et al., 2012; Midulla et al., 61 2012) or the drug distribution in case of drug eluting stents (Balakrishnan et al., 2005). 62

Braided stents belong to the multitude of commercial devices available nowadays for endovascular treatment (Bishu and Armstrong, 2015; Ronchey et al., 2016). They are self-expandable consisting of interlaced wires, which provide great flexibility and kinking resistance. Both metallic and polymeric materials are adopted for their manufacturing. They are proposed for several applications (Han et al., 2006; Irani and Kozarek, 2010; Isotalo et al., 2006; Raju, 2013), including the treatment of stenotic peripheral arteries (Cremonesi et al., 2015), intracranial aneurysms (Briganti et al., 2015) and for the aortic valve replacement (Seigerman et al., 2019).

Analytical models, considering not-interacting helical wires, were proposed to predict the behavior of braided stents subjected to idealized boundary conditions (Jedwab and Clerc, 1993; Wang and Ravi-Chandar, 2004a, 2004b; Záhora et al., 2007). Numerical methods, particularly finite element methods (FEM), allow to analyze also more complex situations involving intricate geometries, nonlinearities, interactions, and dynamic conditions. However, the numerical studies available are
few, if compared to those related to laser-cut devices, and they are described below.

The main issues related to their numerical modeling are: the geometry reconstruction and thedescription of the high number of contacts among the wires.

For what concerns the geometry reconstruction, two solutions were proposed in the literature. Some research groups adopted the open-source software PyFormex developed at Ghent University (Verhegghe, 2013) which, following a sequence of mathematical transformations, generates the mesh of the stent (Conti, 2007; De Beule et al., 2009; Peirlinck et al., 2018; Shanahan et al., 2017a, 2017b). On the other hand, Kim et al. (Kim et al., 2008) and, more recently, Zhao et al. (Zhao et al., 2019) presented an analytical formula to build cylindrical open ends devices. However, a similar strategy has not yet been applied for more complex geometries.

Given the significantly lower computational cost respect to three-dimensional (3D) elements, beam 85 elements are usually chosen to model the wires (Auricchio et al., 2011; Conti, 2007; De Beule et al., 86 2009; Kim et al., 2008; Ma et al., 2012; Peirlinck et al., 2018; Shanahan et al., 2017a, 2017b; Záhora 87 88 et al., 2007; Zhao et al., 2012). Beam meshes offer different options to describe the interaction within the stent elements. The most realistic one consists of representing all the contacts and relative slips 89 90 among the wires (Kim et al., 2008; Ma et al., 2012; Zhao et al., 2012). However, this approach is computationally demanding. Accordingly, in the literature, simplified methods were proposed, where 91 92 the relative motions of two interacting wires are restricted, introducing connector elements in the 93 contact points where the wires are crossing. In particular, the connectors usually adopted are the join (Auricchio et al., 2011; Conti, 2007; De Beule et al., 2009) and the hinge (Shanahan et al., 2017b, 94 2017a). In particular, the connectors usually adopted are the join (Auricchio et al., 2011; Conti, 2007; 95 96 De Beule et al., 2009) and the hinge (Shanahan et al., 2017b, 2017a). The first option joins the relative position of two nodes (no relative displacements between the contact points), while a revolute 97 98 constraint is added in the latter case, permitting only relative rotations around the local radial direction

99 of the intersecting cross-sections. Notwithstanding the computational advantage, to the best of our 100 knowledge, an extensive comparison between these two approaches and the most realistic one, to 101 verify their level of accuracy, is lacking.

In this context, the present work aims to go further the literature results, both for what concerns the
geometry reconstruction and for the identification of the most suitable contact model. Accordingly,
the paper has two main objectives.

The first one is to propose an effective strategy to build complex braided geometries: the analytical approach is preferred due to the versatility of a mathematical description. The 3D parametric equations that allow replicating devices characterized by open or looped ends and cylindrical or variable section geometries (Fig. 1) are illustrated.

The second goal is to give indications about the opportunity of using simplified contact methods. A deep comparison is performed among the finite element strategies described above to model wire contacts: three different braided stents are considered and their performance under different working conditions (bending, crimping, and confined release) are compared, taking into account global (reaction force/moment, displacement) and local quantities (stress/strain).

114 Materials and methods

A code was developed using MATLAB (MathWorks, Natick, MA, USA) to build three stent models 115 resembling three commercial devices for peripheral artery stenting with different structural features: 116 Wallstent (Boston Scientific, Marlborough, MA, USA), Supera (Abbott Vascular, Santa Clara, CA, 117 USA), and Roadsaver (Terumo, Tokyo, Japan). The code returns to the user the nodes, elements, and 118 connectors lists (pair of nodes whose relative motions are constrained by connector elements). 119 Subsequently, the models were imported in the finite element code Abaqus 2018 (Dassault Systemes 120 Simulia, Providence, RI, USA), where the material parameters, connector sections (hinge/join) or 121 122 interaction property, and boundary conditions were defined.

123 Stents reconstruction

The wires were drawn using 3D parametric equations in which a sinusoidal component describes theintertwining. The meshes were obtained by sampling the θ parameter (Fig. 1).

The Wallstent is a cylindrical open ends braided stent. The repetitive unit of the counter-clockwise wire follows the set of equations (1), wherein R, r, n, α , L correspond respectively to the stent middle radius, the wire radius, the number of the clockwise wires, the pitch angle and the stent length (Fig. 1).

130
$$\begin{cases} x(\vartheta) = (R + r \cdot \cos(\vartheta \cdot n)) \cdot \cos(\vartheta) \\ y(\vartheta) = (R + r \cdot \cos(\vartheta \cdot n)) \cdot \sin(\vartheta) \\ z(\vartheta) = R \cdot \vartheta \cdot \tan(\alpha) \end{cases}$$

with
$$\vartheta \in \left[0, \frac{2\pi}{n}\right]$$
 (1)

The Supera stent, in contrast to the previous one, is a looped ends device. The central trait follows the same equations of the Wallstent model while the extreme portions need to be modified to join the clockwise wires with the counter-clockwise ones. Specifically, the oscillation amplitude was halved, and a quadratic term of the form $a \cdot (\vartheta - \vartheta_0)^2$ was subtracted on the longitudinal coordinate for $\vartheta \in$ 135 $\left[\vartheta_0, \frac{\pi}{n}\right]$. The parameter ϑ_0' , which determines the sharpness of the terminal loops, was set equal to 0. 136 Thus, the parameter a' was obtained by imposing the tangency on the extremities $\left(z'(\vartheta = \pi/n) = 0\right)$.

138
$$\begin{cases} x(\vartheta) = \left(R + \frac{r}{2} \cdot (1 + \cos(\vartheta \cdot n))\right) \cdot \cos(\vartheta) \\ y(\vartheta) = \left(R + \frac{r}{2} \cdot (1 + \cos(\vartheta \cdot n))\right) \cdot \sin(\vartheta) \\ z(\vartheta) = (\vartheta - \vartheta^2 \cdot n/(2\pi)) \cdot R \cdot \tan(\alpha) \end{cases}$$
$$with \ \vartheta \in \left[0, \frac{\pi}{n}\right]$$

139 The external mesh of the Roadsaver stent is characterized by a variable section diameter. To represent 140 the conical shape of the terminal traits, the radius and the length were expressed as linear functions 141 of ϑ and the oscillation term was split between the radial and the longitudinal coordinate.

142
$$\begin{cases} x(\vartheta) = \left(R + \Delta R \frac{\vartheta}{2\pi/n} + r \cdot \cos(\vartheta \cdot n) \cdot \cos\left(\operatorname{atan}\left(\frac{\Delta R}{\Delta Z}\right)\right)\right) \cdot \cos(\vartheta) \\ y(\vartheta) = \left(R + \Delta R \frac{\vartheta}{2\pi/n} + r \cdot \cos(\vartheta \cdot n) \cdot \cos\left(\operatorname{atan}\left(\frac{\Delta R}{\Delta Z}\right)\right)\right) \cdot \sin(\vartheta) \\ z(\vartheta) = \Delta Z \cdot \frac{\vartheta}{2\pi/n} - r \cdot \cos(\vartheta \cdot n) \cdot \sin\left(\operatorname{atan}\left(\frac{\Delta R}{\Delta Z}\right)\right) \end{cases}$$

with
$$\vartheta \in \left[0, \frac{2\pi}{n}\right]$$
 (3)

(2)

143 Where ΔR and ΔZ are the radius and length variation respectively related to the interval of the 144 parameter ϑ considered $(2\pi/n)$. Note that the illustrated equations may be extended to describe even 145 more complex geometry. The general form is:

146
$$\begin{cases} x(\vartheta) = \left(R + \Delta R(\vartheta) + r \cdot \cos(\vartheta \cdot n) \cdot \cos\left(\operatorname{atan}\left(\frac{dR}{dz}(\vartheta)\right)\right)\right) \cdot \cos(\vartheta) \\ y(\vartheta) = \left(R + \Delta R(\vartheta) + r \cdot \cos(\vartheta \cdot n) \cdot \cos\left(\operatorname{atan}\left(\frac{dR}{dz}(\vartheta)\right)\right)\right) \cdot \sin(\vartheta) \\ z(\vartheta) = \Delta Z(\vartheta) - r \cdot \cos(\vartheta \cdot n) \cdot \sin\left(\operatorname{atan}\left(\frac{dR}{dz}(\vartheta)\right)\right) \end{cases}$$

with
$$\vartheta \in \left[0, \frac{2\pi}{n}\right]$$
 (4)

Table 1 (top) reports the geometrical parameters of each model where Rext=R+2r and the number of beam elements (B31) chosen after a mesh sensitivity analysis (see Appendix A). Fig. 1 shows the final reconstructed geometries.

150 *Material and contact definition*

The Wallstent is made of Phynox, a cobalt-chromium alloy; the Supera and Roadsaver devices are made of Nitinol, a nickel-titanium alloy featuring super-elastic behavior above a specific temperature value (Af). Details about the mechanical models and material parameters used are reported in the Appendix B.

To describe the contact among the wires, three different strategies were analyzed: i) general contact 155 (GC) algorithm (hard contact in the normal direction and friction coefficient equal to 0.2 in the 156 tangential direction (Ma et al., 2012)), ii) hinge connectors (H) and iii) join connectors (J) (the stent 157 cylindrical coordinate system was used to define univocally the radial direction (Fig. 1)). The 158 correctness of the simplified models involving connector elements was evaluated considering the GC 159 strategy as the reference standard, given the greater accuracy of the contact description. For the H 160 and J strategies both the implicit and the explicit solvers can be used, while the GC model needs to 161 be solved in explicit due to the high nonlinearity introduced by the extremely large number of contacts 162 within the stent components. The simulations herein presented were conducted using the explicit 163 solver, once verified that, as regards connector models, quasi-static explicit simulations were 164 comparable with solutions provided by the implicit solver. 165

The GC model was previously validated replicating one of the localized compression tests performed
by Kim et al. (Kim et al., 2008) who provided both experimental and numerical curves. The details
and results of the validation process are reported in Appendix B.

169 *Simulations*

For each stent model three simulations were carried out (bending, crimping and confined release) 170 171 using the two types of connectors or general contact algorithm, for a total of 27 computational analyses. For the Supera and Roadsaver stents, the temperature was set constant and equal to 22°C 172 (>Af) in all the simulations. Since the aim of the study is purely comparative, the specific temperature 173 value chosen for the analyses does not affect the findings. Smooth step amplitudes, appropriate mass-174 scaling factor and linear bulk viscosity were set to optimize the computational time and to avoid 175 instability. In all the simulations, the kinetic energy and the viscous dissipations were kept lower than 176 the 5% compared to the internal energy throughout most of the process. 177

178 Bending

Two reference points (RP1 and RP2 in Fig. 2a) were introduced on the stent axis (Z-axis) and were associated with the end nodes through multiple-point constraints (MPC) using beam connections. A rotation of 1.5 radiant around the X-axis was imposed on the defined nodes, and all other degrees of freedom were locked apart for the Z translation of RP2. For each simulation, in addition to the deformed configurations and stress distribution, the following quantities were evaluated: reaction moment in RP1, Z-displacement of RP2 and Y-displacement of the middle section.

185 *Crimping*

For the crimping simulation, 12 rigid surfaces were introduced and radially moved to reduce the diameter of each stent to 1.85mm (Fig. 2b). To stabilize the model, the longitudinal displacements of two symmetrical points in the middle section of the stent were prevented. A frictionless interaction was defined between the stent and the rigid planes. The comparison between the different strategies for simulating the interaction within the stent elements was performed in terms of deformed configuration, stress distributions and significant quantities, namely: crimping force, length variation and diameter variation (evaluated both in the middle and side sections).

193 *Confined expansion*

Finally, the stent release in an idealized rigid stenotic vessel with a concentric plaque was simulated (Fig. 2c). From the crimped configuration, the rigid planes were moved back to their initial position and the interaction between the stent and the vessel internal wall was activated. Hard contact in the normal direction and a penalty factor of 0.2 were chosen (Dordoni et al., 2014). The internal contour of the stenosis was drawn following the Hicks-Henne function (Dordoni et al., 2014):

$$y = \frac{D_V}{2} \times (1 - RS) \times \sin\left(\pi \times \frac{x}{L_p}\right)^s \tag{1}$$

The values used for the healthy vessel inner diameter (D_v), residual stenosis (RS), plaque length (L_p) and sharpness of the peak (s) are reported in Table 1. The deformed configurations, stress distributions, contact pressure distributions, and forces acting on the confinement surfaces were considered in the comparison.

203 **Results**

Table 2 reports the percentage differences of the H and J model with respect to the general contact 204 205 option, in terms of reaction moments/forces, maximum von Mises stress and displacements/deformations entities. 206

207 **Bending**

Remarkable differences among the stress distribution are visible between the GC and H and J connector models, except when the J model is applied to the Supera geometry. Indeed, the deformed configurations of the Wallstent and Roadsaver significantly vary in accordance with the contact strategy (Fig. 3).

Fig. 4 compares the trend of the reaction moment in the fixed reference point RP1, the Z displacement of RP2 and the Y displacement of the central section, obtained as the mean between the displacements of two symmetrical points.

The H strategy overestimates the final reaction moment of the Wallstent, Supera and Roadsaver models by 14%, 58% and 69% respectively. The differences decrease if the J option is considered, especially for the Supera geometry where the error at the end of the test is lower than the 4%.

The difference on the Z displacement at the end of the test exceeds 15% and 30% for the H and J option respectively except for the Supera stent where the discrepancies are reduced to 1.30% and 5.25%. The maximum deviation of the Y displacement is visible in the Wallstent model, where it reaches the 3.71% for the H option and 6.17% for the J one.

222 <u>Crimping</u>

The deformed configurations with the Von Mises stress colored maps are reported in Fig. 5. Significant differences are visible on the extremities, where the connector elements are not able to describe relative slips among the wires and to prevent wires overlapping.

The crimping force, the diameter variations (evaluated both in the middle and in the side sections) and the length variation are reported in Fig. 6. To assess the radial stiffness, the sum of the reaction forces acting on the rigid planes was evaluated. The elongation and the diameter variation were determined as the mean of the distance variations between two pairs of opposite nodes.

When applied to the Wallstent geometry, the connector models report a quite similar trend of the reaction force with respect to the GC model throughout most of the process, while greater differences are visible for the looped ends structures.

Differences among the diameter variations in the middle section are visible only for the variable 233 section device, where the GC model predicts an initial increase of this entity before the contact 234 between the planes and the central trait of the stent occurs. Instead, when the side sections are 235 considered, the discrepancies are more evident. Especially for the Wallstent geometry where there is 236 237 a deviation of 19.44% and 10.45% for the H and J model, respectively. Note that in the open ends device, when the GC strategy is adopted, the side nodes can be subdivided into two subsets (internal 238 239 and external side nodes highlighted in Fig. 5) whose diameter variation differs by 12.8%. 240 Nevertheless, for clarity, only the mean value is reported in Fig. 6.

The length variations of the three contact strategies are superimposable for the cylindrical geometries, while, if the Roadsaver stent is considered, the connector models present a quite dissimilar trend compared to the GC option, although the final length differs less than 0.5%.

244 Expansion in an idealized vessel

The deformed configuration of the stent with the associated stress distribution and the contact pressure distribution on the stenotic rigid vessel are reported in Fig. 7. The J model shows similar results compared to the GC strategy for the Supera and Wallstent geometries, even if some variations in the contact pressures distribution are visible. On the other end, the H model overestimates the stress in the central trait for both the cylindrical devices and reports a significantly different configuration for the Wallstent geometry, in which only the central portion of the stent is in contact with the wall.Both the simplified models fail to catch the deformation of the variable section structure.

Fig. 8 shows the comparison among the reaction forces acting on the wall, evaluated both in the middle and in the lateral portions (as a sum of the distal and proximal part) of the vessel. The H model overestimates the force acting on the central trait and underestimates the lateral force, which is null for the Wallstent geometry. The J model shows better results, especially for looped ends geometry. Indeed, the difference on the total force lay below 15%, 7% and 1% for the Wallstent, Supera and Roadsaver, respectively.

Discussion and Conclusions

The building of braided stents is a quite challenging task due to the specific woven structure. Consider the correct distance from the wire centerlines in the overlapping zone and hence the correct local wire curvature is crucial to accurately model this kind of device. Indeed, in certain configurations, the intertwining has consequences from a kinematic as well as a geometric point of view (Appendix D).

In this paper, a simple method for geometry reconstruction, based on the definition of a set of 3D parametric equations, was proposed. The advantage of this approach is that the proposed equations may be easily modified to describe similar braided structures (Irani and Kozarek, 2010), not only stents, by just varying the defined geometrical parameters in a versatile way. Furthermore, it allows for obtaining the analytical description of the stent, the use of which is not limited to finite element analyses.

Three models resembling commercial braided stents were imported in a finite element code and used to compare the response of the different contact modeling techniques to different idealized boundary conditions. The general contact option was considered as the reference standard (Appendix B), and the accuracy of the simplified models, involving connector elements, was assessed. It is possible to notice that both the simplified approaches give different results which underestimate the general contact predictions, but it is difficult to find a general trend. Indeed, the differences are strongly dependent on the geometry and boundary conditions considered.

In general, H and J models are more rigid than the GC one: it means that the connectors prevent movements allowed by friction. However, this trend may be inverted if contacts among the wires, not detected by the connector models, occur when the general contact strategy is applied. This fact explains the final stiffening of the Wallstent and Roadsaver during the crimping simulations (Fig. 6) as well as of the Wallstent during the bending test (Fig. 4), and the underestimation of the final reaction force/moment (Table 2) by the connector models. In most of the studied cases, the join connector was found to be the best alternative giving the less restrictive constraint, showing smaller differences in terms of deformed shape, stress distributions and reaction forces/moments (Table 2). However, in the case of the bending test on the open ends and variable section devices, the J model allows excessive deformability resulting in significant differences partially smoothed in the H model.

With very few exceptions (such as the J model of the Supera geometry during the bending test (Table 2)), the results of the connector models are strongly influenced by wire interpenetrations and overconstraint. Thus, the general contact option remains the best choice.

One of the advantages of the simplified approach is the possibility to use the implicit solver. Unfortunately, the implicit approach can be exploited only when connectors are employed for running simplistic simulations (such as the tests carried out in this study). Otherwise, also for connectors, it is necessary to carry out explicit quasi-static simulations. Moreover, if all the models (GC, J, and H) are solved with the same setting, the differences in computational time are not relevant.

The limitations of this study include the type of connectors analyzed. In this work, the strategies mainly adopted in the literature were compared. However, more elaborated connector elements could be suggested, for example specifying spring-like behavior, which may be more appropriate than the ones proposed in the literature and analyzed in this study (McGee et al., 2019).

Moreover, only three device geometries were investigated. Also aware of the wide variety of the braided stents, the structures analyzed were assumed adequate to evaluate the impact of three features commonly present in this kind of devices, namely open ends, looped ends and variable sections. Nevertheless, only rotationally symmetrical structures were considered. Therefore, the present strategy does not involve bifurcated or angled stents (Han et al., 2006) that might be included in future developments. Note that, the present work does not pretend to describe mechanical behavior of the real devices. The simulations are only intended to compare different contact strategies. Thus, the geometries proposed, even if they do not match the commercial stents exactly, are considered meaningful for the stated purpose.

Finally, the proposed modeling strategy involving 3D parametric equations and accurate contact description seems to be a valid tool for deeply investigating the behavior of a large variety of braided stents.

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1 Figure legends

Fig. 1. Braided stents characterized by open or looped ends and cylindrical or variable section geometries on the longitudinal (ZY) and transversal (XY) planes (left). The geometrical parameters used in the 3D parametric equations are shown on the Wallstent views (top-left corner, top-center). Wallstent with the global coordinate system (XYZ) and a magnification of the mesh with a connector element, joining the nodes marked with the green triangle and square, and the relative local axis (r9z) (right).

Fig. 2. Schemes of the performed simulations. a) Bending: the extremities of the undeformed stent 8 9 (green) were connected through MPC to two reference nodes, RP1 and RP2. Referring to the global reference system, a rotation around the X-axis was applied to RP1 and RP2, while all other degrees 10 of freedom were locked apart for the Z translation of RP2. In blue the final configuration. $Z_{disp} = Z$ 11 translation of RP2, $Y_{disp} = Y$ translation in the middle section. b) Crimping: 12 planes were radially 12 moved (right) in order to reduce the stent diameter (left). ΔL = length variation between the stent 13 undeformed (green) and final (blue) configurations, ΔD_{middle} and ΔD_{side} = diameter reduction in 14 15 the middle and side sections. c) Confined release: the crimped stent (green) was self-expanded in an idealized stenotic rigid vessel. H_p = maximum thickness of the concentric plaque, D_V = healthy 16 17 vessel inner diameter.

18 Fig. 3. Bending test: deformed configurations with Von Mises stress colored map.

Fig. 4. Bending test: comparison among the GC, H and J models concerning reaction moment,
linear displacement of RP2 in the Z direction and linear displacement of the central section in the Y
direction with respect to the rotational displacement applied in RP2 and RP1.

Fig. 5. Crimping test: deformed configurations with Von Mises stress colored map. D_{ext} and D_{int}
 are the final diameters of the external and internal side nodes of the Wallstent respectively

Fig. 6 Crimping test: comparison among the GC, H and J models concerning crimping force,diameter variation (in the middle and in the side sections) and length variation.

Fig. 7. Confined release: deformed configurations with Von Mises stress colored map (left) and contact pressure distributions on the rigid vessel (right). The maximum contact pressure values are reached only in localized spot within the dotted red rectangles.

Fig. 8. Confined release: force acting on the rigid vessel, evaluated both in the middle (blue bar), in
the lateral portions (yellow bar) of the vessel and as a sum of all the contributions (red bar).









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1 Tables

Table 1. Geometrical parameters for the stent reconstruction and number of elements for the model
discretization (N_{el}) (top): wire radius (r), external stent radius (R_{ext}), stent length (L), pitch angle
(α) and the number of wires in the clockwise direction (n). Geometrical parameters of the stenotic
rigid vessel (Fig. 3c) for the confined release simulation (bottom): healthy vessel inner diameter

6 (D_V), maximum thickness of the concentric plaque (H_p), residual stenosis (RS = $(D_V - 2H_p)/D_V$),

Stonts	r	R _{ext}	L	α	n	N _{el}
Otento	[mm]	[mm]	[mm]	[°]		
Wallstent	0.065	4	20	30	12	3264
Supera	0.09 (Myint et al., 2016)	2.75	22	25	6	1728
Roadsaver	0.09 (Wissgott et al., 2015)	4	20.5	30	6	960
Vassals	D _V	H _p	RS L _P		Ъ	S
V655615	[mm]	[mm]	[-]	[n	nm]	[-]
Wallstent	6	1.5	0.5	4	10	5
Supera 5		1.25	0.5	2	10	5
Roadsaver	6	1.5	0.5	2	40	5

7 plaque length (L_P) and sharpness of the peak (s).

9 Table 2. Percent difference of the Hinge (H) and Join (J) model with respect to the general contact

10 option, in terms of: reaction moments/forces (RM, RF, RF_{center}, RF_{side}, RF_{total}), maximum Von

11	Mises stress (M	Aax. σ_{VM}), linear	displacements	(U_Z, U_Y)	() and deform	ations magnitude	$(\Delta D_{side}, \Delta L)$
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Percent difference	Walls	stent	Sup	oera	Road	saver
[%]	н	J	н	J	н	J
Bending						
RM	14,33	-16,57	57,95	-3,13	69,41	34,02
Max. σ_{VM}	0,32	-1,30	57,66	0,51	3,78	6,17
Uz	17,49	34,61	1,29	5,25	19,36	32,80
U _Y	3,71	-6,17	3,08	1,40	2,72	-4,60
Crimping						
RF	-29,93	-41,09	6,35	6,17	-49,44	-50,39
Max. σ_{VM}	-7,03	0,00	-7,78	60,44	-48,27	-28,17
ΔD_{side}	19,44	-10,45	-2,63	-6,14	6,80	3,01
ΔL	-0,15	1,05	0,15	0,15	0,30	0,23
Confined release						
RF _{center}	55,64	-7,21	126,04	-4,39	49,05	1,37
RF _{side}	-100,00	84,73	-44,76	10,46	-20,71	-8,29
RF _{total}	15,91	12,22	2,56	6,35	21,28	-0,70
Max. σ_{VM}	4,69	2,19	20,02	19,53	0,22	-2,67

Appendices

A. Mesh sensitivity

The mesh sensitivity was carried out on a single helical wire with length equal to 10mm. The same geometrical parameters adopted to replicate the Wallstent device were used. The lower extremity was fixed while the upper one was moved to stretch the helix of 10mm.

Both structured hexahedral meshes (C3D8I) and beam meshes (B31) were analyzed to ensure the convergence of the results (Table A.1). While the results obtained with the 3D meshes highlight a significant influence of the mesh refinement, no relevant differences were visible among the beam meshes considered.

Therefore, the differences between beam elements and 3D elements were assessed in terms of reaction force and maximum von Mises stress (Table A.2). Since the deviations from the finest hexahedral model are lower than 2.1% and 6.5% on the maximum reaction force and von Mises stress respectively, beam elements were considered suitable for the present work.

For the beam meshes, also contact thickness reductions were identified (Table A.2). Indeed, if the beam length is lower than a certain fraction of the beam section size, the contact thickness is reduced to avoid spurious self-contact, without affecting stiffness calculation. The coarsest beam mesh ensures the correct contact beam thickness is maintained (0.13mm) slightly increasing the error on the maximum von Mises stress. Instead, both the finest and the middle beam meshes feature a reduced contact section diameter (equal to 0.059mm and 0.117mm respectively).

Thus, all the meshes of the illustrated braided stents were generated using beams short enough to describe the wire curvature and long enough to prevent thickness reduction.

Table A.1. Beam section with three hexahedral meshes (left) and trait of a wire corresponding to $\vartheta \in \left[0, \frac{\pi}{n}\right]$ meshed with three different beam length (right). The approximate dimensions (size) and the total number of the elements (N_{el}) are reported.

Table A.2. On the left, the percent differences with respect to the finest 3D mesh (Mesh1) in terms of maximum force (F_{max}) and maximum von Mises stress (Max. σ_{VM}) are shown. On the right, the force-displacement plots for the different meshes are compared.

B. Material models and parameters

The Wallstent is made of Phynox, a cobalt-chromium alloy: for describing its mechanical behavior an elastic-plastic model with isotropic hardening was adopted. The material parameters were taken from the literature (De Beule et al., 2009; Auricchio et al., 2011) and their values are reported in Table B.1.

The Supera and Roadsaver stents are made of Nitinol, a nickel-titanium alloy. Above a specific temperature value (Af), Nitinol has a super-elastic behavior (Fig. B.1), due to the coexistence of two solid phases (austenite and martensite): it allows Ni-Ti structures to elastically recover their original shape even after large deformations are applied. For describing the mechanical behavior of Nitinol, the constitutive model available in Abaqus for super-elastic material was adopted. The material parameters were taken from the literature (Conti, 2007) and their values are reported in Table B.2.

Table B.1. Phynox material parameters: elastic modulus (E), yield strength (σ_{yield}), Poisson's ratio (v), density (ρ).

	Phynox mater	Phynox material parameters					
Е	σ_{yield}	ν	ρ				
[MPa]	[MPa]	[-]	[g/cm3]				
260000	2450	0.33	8				

Fig. B.1. Nitinol pseudo-elastic behavior: EA and EM are respectively the elastic moduli of the austenitic and martensitic phases; the stress values reported in the figure indicate the start/end-point of the load/unload transformation plateau in tension ($\sigma t_{L/U}^{S/E}$); ϵ^{L} is the strain value near the intersection between the martensitic branch and the strain axis.

Table B.2. Nitinol material parameters: austenite elastic modulus (E_A), martensite elastic modulus (E_M), start/end of transformation phase during loading/unloading (σt_L^S , σt_L^E , σt_U^S , σt_U^E), Poisson's ratio (v), transformation strain (ϵ_L), reference temperature (T₀), beta parameter ($\partial \sigma t/\partial T$) and density (ρ). See also Figure B.1 for the meaning of the parameters.

Nitinol material parameters										
EA	E _M	σt_L^S	$\sigma t_L^{\rm E}$	σt_{U}^{S}	σt^E_U	ν	$\epsilon_{\rm L}$	T ₀	<i>∂</i> σ/ <i>∂</i> T	ρ
[MPa]	[MPa]	[MPa]	[MPa]	[MPa]	[MPa]	[-]	[-]	[°C]	[MPa/°C]	[g/cm ³]
35877	24462	489	572	230	147	0.33	0.0555	22	6.7	6.7

C. Model validation

In the paper, the general contact was assumed as the most accurate contact model methodology. In order to verify this assumption, we referred to the work of Kim et al. (Kim et al., 2008) where experimental tests on braided stents in a complex configuration were performed: six cylindrical open ends stents (similar to the Wallstent) were compressed to half their original diameters between a plane and a circular rod with a diameter of 10mm (Fig. C.1a). This type of load condition is particularly interesting because it involves not axisymmetric deformations that allow to highlight differences between the three contact strategies: general contact algorithm, Hinge connectors, Join connectors. In particular, the A45 sample was reconstructed and the experimental test numerically replicated using the three different strategies. Abaqus explicit solver was used. The kinetic energy and the viscous dissipation were kept lower than the 5% of the internal energy throughout most of the process.

In Fig. C.1b the computational results are compared with the experimental curve and the numerical prediction obtained by Kim et al. (Kim et al., 2008), also using the Abaqus general contact algorithm.

While the models exploiting the general contact algorithm show a good agreement with the experimental data, substantial differences both concerning load values and hysteretic behavior are visible when the connector models are considered.

Fig. C.1. a) illustration of the compression test performed by Kim et al. (Kim et al., 2008). b) forcedisplacement plots obtained with the GC (general contact algorithm), H (Hinge connectors) and J (Join connectors) models compared with the experimental (EXP) and numerical (FEM) curves from the article of Kim et al. (Kim et al., 2008).

b)

D. Impact of local curvature

The geometry reconstruction of braided stents is complicated by the woven structure. However, this feature should not be neglected. Indeed, in some configurations, the local wire curvature may introduce kinematic restrictions, constraining the relative slip among the wires.

Note that, increasing the wires' diameter, all else being equal, the distance of the overlapping points increases and thus also the local wire curvature, reinforcing its impact. To better explicate this aspect, the Wallstent bending test was replicated (Fig. D.1), varying the wire diameter (from 0.13mm to 0.23mm).

The results obtained with the general contact and with the simplified models involving connector elements were compared in terms of deformed configuration (Fig. D.2), reaction moment, and linear displacements (Fig. D.3). The kinematic effects of the increased overall dimensions are observable only when the general contact is applied since, in the simplified models, the interaction among the wires was neglected. In the former option, this enhanced constraint restricts the displacement along the Z-axis (Fig. D.3 middle), leading to a different deformed configuration (Fig. D.2) and consequently to an intensified stiffening with respect to the one recorded in the simplified models (Fig. D.3 left). Similar conclusions can be extrapolated observing the percent differences of the models based on the hinge (H) and join (J) connectors with respect to the general contact option that are reported in Table D.1.

Finally, the intertwining is a critical feature of braided stents that should not be neglected in the modeling process. Indeed, the interaction among the wires may introduce kinematic constraints, whose impact depends on the geometrical parameters and is not observable in the simplified models.

Fig. D.1. Bending test: the extremities of the undeformed stent (green) were connected to two reference nodes, RP1 and RP2. Referring to the global reference system, a rotation around the X-axis was applied to RP1 and RP2, while all other degrees of freedom were locked apart for the Z translation of RP2. In blue the final configuration. UZ = Z translation of RP2, UY = Y translation in the middle section.

Fig. D.2. Bending test: deformed configurations with Von Mises stress colored map.

Fig. D.3. Bending test: comparison among the GC, H and J models concerning reaction moment, linear displacement of RP2 in the Z direction and linear displacement of the central section in the Y direction with respect to the rotational displacement applied in RP2 and RP1.

Table D.1. Percent difference of the Hinge (H) and Join (J) model with respect to the general contact option, in terms of reaction moments (RM) and linear displacements (UZ, UY).

	Dwire	0.23mm	Dwire	0.13mm
diff%	Н	J	Н	J
RM	14,33	-16,57	-15,77	-23,79
UZ	17,49	34,61	59,67	60,29
UY	3,71	-6,17	-7,21	-10,45

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