

Model vs. Data based Approaches Applied to Fault Diagnosis in Drinking Water Transport Networks

M.À. Cugueró-Escofet^{a,*}, J. Quevedo^a, C. Alippi^b, M. Roveri^b, V. Puig^a, D. García^a, F. Trovò^b

^a*Supervision, Safety and Automatic Control research group, Polytechnic University of Catalonia, Gaia Research Bldg., 22 Rambla Sant Nebridi, 08222 Terrassa (Barcelona), Spain.*

^b*Department of Electronics and Information, Politecnico di Milano, Piazza Leonardo da Vinci, 32 I-20133 Milano, Italy.*

Abstract

In this paper, the problem of fault diagnosis in drinking water transport networks (DWTNs) is addressed. Two different fault diagnosis approaches are proposed to deal with this problem. The first one is based on a model-based approach exploiting *a-priori* information regarding physical/temporal relations existing between the measured variables in the monitored system, providing fault detection and isolation capabilities by means of the residuals generated using these measured variables and their estimations. This *a-priori* information is provided by the topology and the physical relations between the elements constituting the system, which is used by design in order to derive fault diagnosis. Differently, the second approach does not require the physical *a-priori* information of the network to operate. It relies on a data-driven solution meant to exploit the spatial and temporal relationships present in the acquired data streams to detect and isolate faults. Relationships between data streams are modelled through sequences of linear dynamic time-invariant models whose estimated coefficients are used to feed a Hidden Markov Model (HMM). When the pattern of estimated coefficients cannot be explained by the trained HMM, a change is detected. Afterwards, a cognitive method based on a functional graph representation of the system isolates the fault. Finally, a performance comparison between these two approaches is carried out using a part of the Barcelona water transport network.

*Corresponding author

Email address: `miquel.angel.cuguer@upc.edu` (M.À. Cugueró-Escofet)

Keywords: Fault isolation, cognitive systems, model-based fault diagnosis, time series, hidden Markov models, critical infrastructure systems

1. Introduction

Water networks are complex large-scale systems needing highly sophisticated supervisory and control schemes to satisfy a certain degree of performance when unfavorable faulty conditions are occurring. To deal with this problem, the use of a Fault Detection and Isolation (FDI) system capable to detect and isolate these faults (or events) is highly desirable, aiming to help the operators to identify which is the actual event occurring in the water network. The FDI problem applied to water networks has been extensively studied from various perspectives and at different levels (see, e.g. Colombo and Karney, 2002; Misiunas et al., 2006; Lees, 2000). On the one hand, at the District Metering Area (DMA) level, many FDI approaches have addressed the problem of leak/burst detection and isolation (see, e.g. Wu et al., 2010; Perez et al., 2011; Bicik et al., 2011; Mounce et al., 2009; Mounce and Boxall, 2010; Mounce et al., 2011; Romano et al., 2013, 2014a,b; Palau et al., 2011), where different model-based approaches are applied. Sensor data validation and reconstruction when exploiting the temporal redundancy of the sensor measurements is also addressed in several works (see, e.g. Quevedo et al., 2010; Eliades and Polycarpou, 2012; Prescott and Ulanicki, 2001; Fillion et al., 2007; Farley et al., 2012). The problem of water quality monitoring concerning contamination event detection has also been extensively addressed (see, e.g. Eliades and Polycarpou, 2010). Moreover, regarding DMA monitoring (either for leaks or quality) there is a related problem considering optimal sensor placement in order to maximise the performance of the FDI algorithms applied. This problem has been studied separately both for leak detection and location (see, e.g. Casillas et al., 2014; Pérez et al., 2010; Krause et al., 2008; Wu, 2011; Ostfeld and Salomons, 2004) and quality monitoring (see, e.g. Eliades and Polycarpou, 2010). On the other hand, at the water transportation level (i.e. the network connecting the water potabilisation plants with the water distribution tanks) less research has been carried out (see, e.g., Ragot and Maquin, 2006; Quevedo et al., 2014). The water transportation networks,

28 also referred to as trunk main systems, are regional networks used to supply water to
29 the cities and villages of a certain region. This kind of networks can be analysed using
30 a flow-driven model, that is, using mass-balance linear relations, alternatively to wa-
31 ter distribution networks, which are generally modelled using pressure-driven models
32 implying non-linear non-explicit relations. The use of mass balance relations for mod-
33 elling regional water transport networks is appropriate because an actuator is typically
34 installed in each pipe, which establishes its flow. Of course, the energy balances could
35 also be formulated in this case, but this would add extra complexity which is actually
36 not needed since the goal is to establish analytical redundancy relations between flow
37 sensors. This is the case e.g. in Quevedo et al. (2014), where the problem of sensor
38 data validation and reconstruction (which is addressed for DMA networks in Quevedo
39 et al. (2010) exploiting the temporal redundancy of the sensor measurements) has been
40 extended to transport water networks, considering combined temporal/spatial redun-
41 dancy models. In Ragot and Maquin (2006), a model-based FDI approach is applied
42 to the Nancy water network, a city in the north-eastern French department of *Meurthe-*
43 *et-Moselle*, in order to detect faults in the sensors. The present paper also goes towards
44 the FDI application to a water transport network by proposing two different fault diag-
45 nosis approaches: a model-based approach using *a-priori* information of the system,
46 i.e. the physical relation between its elements, and a data-driven approach, which is
47 able to exploit *a-priori* information about the network topology to perform fault diag-
48 nosis but does not require any additional information about the physical models of the
49 water transport network. According to the literature, model-based approaches rely on
50 the concept of analytical redundancy (Blanke et al., 2006), which is based on the use
51 of software sensors i.e. models using available sensor historic records in order to esti-
52 mate the desired sensor measurement, as an alternative to hardware-based approaches,
53 which rely on the use of extra hardware sensors. Although hardware redundancy is
54 desirable in critical elements, the use of the latter in large-scale water networks may be
55 dramatically expensive because of the installation, calibration and maintenance actions
56 to be performed on the system when considering this approach.

57 The novelty in this paper is to address the fault diagnosis problem in drinking wa-
58 ter transport networks (DWTNs) by applying and comparing two well accepted gen-

59 eral purpose fault diagnosis methods (one model-based, the other data-based). The
60 Barcelona DWTN is used as the case study in this work. In ideal situations, the use
61 of a model obtained from the physical relations, as considered in the first approach,
62 should lead to the optimal solution. However, it may be noted that analytical models
63 may be affected by several system practical aspects, such as the potential uncertainty
64 on the model parameters (e.g. actual tank surface), the difficulty to have an on-line
65 well-calibrated model due to frequent network topology changes (caused by e.g., new
66 elements like tanks added or blocked pipes resulting from maintenance operations) and
67 common changes on the consumers demand behavior, which are hard to determine in
68 real-time operation. Hence, a data-based approach, as suggested in the second method,
69 is also a useful and effective alternative to the use of analytical models obtained from
70 physical/temporal relations existing in the network.

71 The structure of the paper is as follows: Section 2 shows the Barcelona DWTN.
72 Section 3.1 presents an FDI model-based method combining both spatial and time se-
73 ries models, whilst Section 3.2 presents the data based approach based on a Cognitive
74 Fault Diagnosis System (CFDS) method exploiting Hidden Markov Models (HMMs).
75 In Section 4, fault isolation results obtained by each methodology are presented, com-
76 pared and discussed. Finally, conclusions and on-going work are outlined in Section 5.

77 **2. Case study: Barcelona Drinking Water Transport Network**

78 The Barcelona DWTN (Figure 1), considered as a case study here, is distributed in
79 23 different districts covering 424 Km² area and providing water to about three million
80 end users. Water managed by this transport network is obtained from both surface and
81 underground sources, including Ter (surface source) and Llobregat (both surface and
82 underground source) as the most important ones in terms of usage and capacity. The
83 water supplied by these sources is distributed through a network of around 4645 Km of
84 pipes to 218 District Metered Areas or demand sectors (DMAs), including about 400
85 controlled/monitored points, 63 storage tanks, 84 pumps, 46 valves and 88 pressure
86 floors. Transport networks are constituted by multiple similar tank subsystems which
87 have alike behavior. In this work, the analysis of a single tank subsystem and a three-

88 tank subsystem is considered (*Orioles* and *Can Guey* in Figure 1 and Figures 6 and 7,
89 respectively). Similar results are also achieved when considering alternative tank sub-
90 systems in the same DWTN. Regarding data management, the Barcelona telecontrol
91 system receives real-time data mainly from the available flow meters, usually installed
92 in the DMAs supply points, so their reading closely fit the actual DMAs water demand.

93 **3. Fault Diagnosis Methodology**

94 In this work, two different well accepted general purpose fault diagnosis method-
95 ologies are used to address the FDI problem in DWTNs. The first approach is based
96 on checking the consistency between the observed and the nominal system behavior by
97 means of a set of Physical/Temporal Parity Relations (PTPR), which relates the mea-
98 sured system variables under normal (faultless) operation assumption of the monitored
99 system. The novelty of the PTPR approach presented here relies on the combined
100 usage of time series residuals with physical residuals, by means of a classical FDI
101 residual-based approach which generally considers only physical parity relations. An
102 inconsistency is detected when analytical redundancy relations derived from models do
103 not match the measurements, generating a non-null residual. Then, the fault diagnosis
104 mechanism is activated in order to isolate the possible fault by matching the residu-
105 als against the fault signature matrix (see, e.g. Puig et al. (2006)). The proposed FDI
106 scheme is shown in Figure 2, where $u_i(k)$ is the i -th measured system input, $x_i(k)$ is the
107 i -th measured system output, $\hat{x}_i(k)$ is the i -th predicted system output, $r_i(k)$ is the i -th
108 system residual of the complete set of n_r residuals and $\mathbf{s}(k)$ is the corresponding fault
109 signature at time instant k . Further details on this general fault diagnosis scheme are
110 given later in this section.

111 The second approach relies on the CFDS method presented in Alippi et al. (2013),
112 that is able to exploit spatial and temporal relationships among measured system vari-
113 ables. The considered CFDS, which does not require any *a-priori* information about
114 the physical model of the network, is based on a two-layer hierarchical architecture
115 to detect and isolate faults. In the first layer, a change-detection test (CDT) based on
116 HMMs (see, e.g. Alippi et al. (2012)) is able to detect a fault occurring in the system

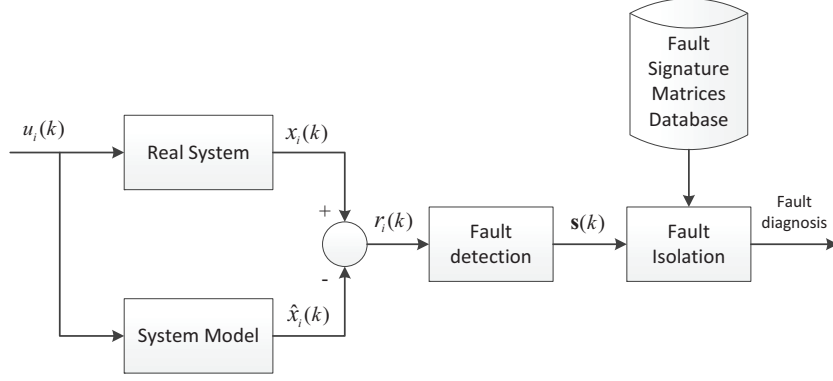


Figure 2: Fault Detection and Isolation (FDI) block diagram

117 by checking the variations in the relationship between couples of data streams, while,
 118 in the second layer, a cognitive method based on a functional graph representation of
 119 the system is able to isolate the fault occurring. Here, we are proposing a modified
 120 version of the original CFDS, specifically crafted for this application, where the avail-
 121 able topological information of the water network is integrated into the data-driven
 122 approach. For instance, Figure 3(a) represents all the relationships which may exists
 123 among data coming from the *Can Guey* subsystem (Figure 7) induced by the water
 124 flow physical phenomenon. This initial dependency graph in Figure 3(a) is reduced
 125 by taking into account the correlation analysis and the final outcome of the *Can Guey*
 126 subsystem (Figure 3(b)).

127 3.1. Method I: Fault diagnosis based on Physical/Temporal Parity Relations

128 3.1.1. Residual generation

129 The fault diagnosis method presented in this section evaluates the nominal residual
 130 $r_i(k)$ obtained from the difference between the system measurements and the model
 131 prediction, considering the model for the i -th subsystem expressed in input-output re-
 132 gressor form as follows

$$r_i(k) = x_i(k) - \hat{x}_i(k) = x_i(k) - \phi_i^T(k)\theta_i \quad (1)$$

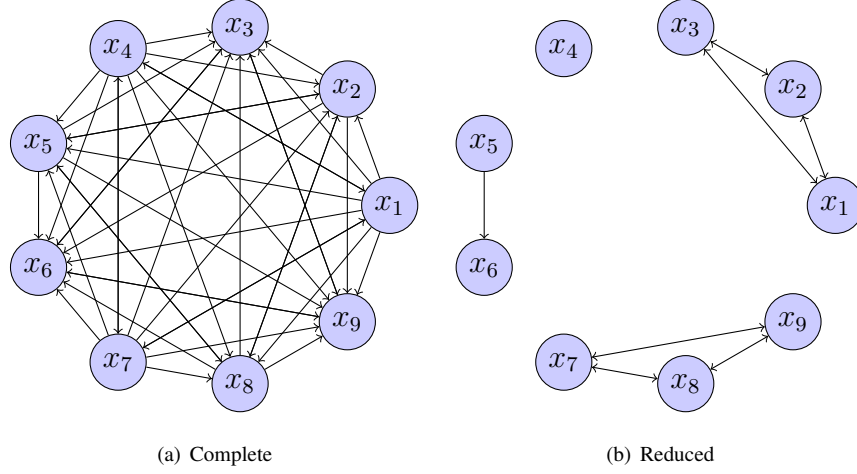


Figure 3: CFDS method dependency graphs of *Can Guey*

133 where θ_i are the nominal parameters obtained using a training dataset, $x_i(k)$, $i \in \{1, \dots, N\}$
 134 is the sensor measurement at time instant k , $N \in \mathbb{N}$ is the number of considered sensors,
 135 $\hat{x}_i(k)$ is the model prediction at time instant k and $\phi_i(k)$ is the regressor vector
 136 of dimensions $n_{\theta_i} \times 1$, including inputs $(u_i(k), u_i(k-1), u_i(k-2), \dots)$ and outputs
 137 $(y_i(k), y_i(k-1), y_i(k-2), \dots)$. Considering the uncertainty (e.g. modelling errors, noise)
 138 the detection test involves checking the condition

$$|r_i(k)| < \tau_i(\mu_i, \sigma_i) \quad (2)$$

139 where τ_i is the detection threshold, which is function of the mean value μ_i and the
 140 standard deviation σ_i of the i -th residual (i.e. $\tau_i = \mu_i + 3\sigma_i$, including the 99.7 % of
 141 the values of a normal distribution according to the *3-sigma* rule) which, according to
 142 the central limit theorem, is assumed to follow a Gaussian distribution. The threshold
 143 in (2) is designed to include the values of the whole residual distribution in the faultless
 144 situation and hence, it may be used for fault detection purposes. Test condition (2) can
 145 be equivalently expressed as follows:

$$x_i(k) \in [\hat{x}_i(k), \tilde{x}_i(k)] \quad (3)$$

146 where $\tilde{\hat{x}}_i(k) = \hat{x}_i(k) + \tau_i$ and $\underline{\hat{x}}_i(k) = \hat{x}_i(k) - \tau_i$, respectively.

147 *Spatial consistency residuals.* The PTPR method is based on establishing mass bal-
 148 ance equations for the water network constitutive elements. As an example, the mass
 149 balance expression for the i -th tank can be stated by means of the following discrete-
 150 time difference equation

$$y_i(k+1) = y_i(k) + \frac{\Delta t}{A_i} (q_{in_i}(k) - q_{out_i}(k)) \quad (4)$$

151 where $y_i(k)$ is the tank level, A_i is the cylindrical tank surface, $q_{in_i}(k)$ is the manipulated
 152 inflow and $q_{out_i}(k)$ is the outflow, which may include manipulated tank outflow and
 153 consumer demands, both given in m^3/s .

154 Similarly, in the water transport network nodes, the mass balance may be expressed
 155 as the static equation

$$\sum_i q_{in_i}(k) = \sum_i q_{out_i}(k) \quad (5)$$

156 where, similarly to Equation (4), $q_{in_i}(k)$ and $q_{out_i}(k)$ correspond to the inflow and out-
 157 flow of the i -th subnet node, also given in m^3/s .

158 *Time series residuals.* Additional residuals can be obtained considering that level in
 159 tanks and flow in demand sectors have a daily repetitive behavior which can be mod-
 160 elled using a Time Series (TS) model. TS models take advantage of the temporal
 161 redundancy of the measured variables. A wide used method for signal forecasting is
 162 the Holt Winters (HW) triple exponential smoothing approach (Winters, 1960; Makri-
 163 dakis et al., 1998). This method, which is of wide use because of its simplicity and
 164 performance, may be presented in several different versions e.g. additive or damped
 165 trend, additive or multiplicative seasonality, single or multiple seasonality. Here the
 166 additive single seasonality version is considered, which may be implemented as shown
 167 next for a forecasting horizon ℓ

$$\hat{x}_{ts}(k) = \hat{R}(k - \ell) + \ell \hat{G}(k - \ell) + \hat{S}(k - L) \quad (6)$$

168 where $\hat{x}_{ts}(k)$ is the TS model forecasted value, \hat{R} is the estimate of the deseasonalized
 169 level (i.e. removing the seasonal effect $\hat{S}(k - L - \ell)$), \hat{G} is the estimate of the trend
 170 and \hat{S} is the estimate of the seasonal component, which may be respectively stated as
 171 follows

$$\begin{aligned}\hat{R}(k - \ell) = & \alpha(x(k - \ell) - \hat{S}(k - \ell - L)) \\ & + (1 - \alpha)(\hat{R}(k - \ell - 1) \\ & + \hat{G}(k - \ell - 1)) \quad 0 < \alpha < 1\end{aligned}\quad (7)$$

$$\begin{aligned}\hat{G}(k - \ell) = & \beta(\hat{R}(k - \ell) - \hat{R}(k - \ell - 1)) \\ & + (1 - \beta)\hat{G}(k - \ell - 1) \quad 0 < \beta < 1\end{aligned}\quad (8)$$

$$\begin{aligned}\hat{S}(k - \ell) = & \gamma(x(k - \ell) - \hat{R}(k - \ell)) \\ & + (1 - \gamma)\hat{S}(k - \ell - L) \quad 0 < \gamma < 1\end{aligned}\quad (9)$$

172 where L is the season (i.e. daily here) periodicity, α , β and γ are the HW parameters
 173 (level, trend and season smoothing factors, respectively) and x is the measured value
 174 (i.e. y_m , q_{in_m} or q_{out_m} , depending on the TS model considered). Hence, analysing the
 175 historic records of the measured values in a certain sensor, a HW model is derived and
 176 used to validate the current data acquired by this device.

177 3.1.2. FDI scheme

178 The FDI methodology (Figure 2) is based on determining the *actual fault signature*
 179 $\mathbf{s}(k) = [s_1(k), s_2(k), \dots, s_{n_r}(k)]$ of the system for n_r different residuals, as a result of the
 180 fault detection phase (see Section 3.1.1) as follows

$$s_i(k) = \begin{cases} 0, & \text{if } |r_i(k)| < \tau_i \text{ (no fault)} \\ 1, & \text{if } |r_i(k)| \geq \tau_i \text{ (fault)} \end{cases}\quad (10)$$

181 where τ_i is the threshold associated to the i -th residual. The actual fault signature is
 182 compared against the *theoretical Fault Signature Matrix* (FSM) Σ that binary codifies
 183 the influence of each fault in the set of considered faults f_1, f_2, \dots, f_{n_f} on every residual
 184 in the set of considered residuals r_1, r_2, \dots, r_{n_r} . This matrix has as many rows as resid-
 185 uals and as many columns as considered faults. If $\Sigma_{ij} = 1$, the j -th fault appears in the
 186 expression of the i -th residual; otherwise $\Sigma_{ij} = 0$. Assuming classical FDI fault hy-
 187 potheseses, i.e, single faults and no-compensation (exoneration), fault isolation consists
 188 in looking for a column of Σ matching the actual fault signature $\mathbf{s}(k)$. More details
 189 about the algorithm implementation of this FDI scheme, including how to manage the
 190 temporal aspects of the binarized residuals, can be found in Meseguer et al. (2010)
 191 and Puig and Blesa (2013).

192 3.2. Method II: Fault Diagnosis System based on the Cognitive Approach

193 The considered CFDS method is based on the ability to characterize the functional
 194 dependencies among the streams of acquired data, where each functional dependency
 195 models the temporal and spatial relationships between couples of data streams. The
 196 main characteristics of the CFDS are the ability to work without any *a-priori* informa-
 197 tion about the physical models of the system and the possibility to isolate the potential
 198 faults by exploiting a functional graph representation of the system. Details about the
 199 considered CFDS can be found in Alippi et al. (2013). In this applicative scenario,
 200 we considered the possibility to include the *a-priori* information about the topology
 201 of the water transport network. In fact, the physical phenomenon of the water flow in-
 202 duces a causality among the respective acquired data streams, allowing to discard those
 203 relationships in which this causality principle does not hold.

204 The overall system architecture is presented in Figure 4. Each relationship is evalu-
 205 ated over time using a HMM-based CDT aiming to analyse the statistical behaviour of
 206 the estimated functional-relationship parameters over time. When a change in the esti-
 207 mated parameters is detected, the CFDS layer is activated to isolate the fault occurring
 208 in the system.

209 In more detail, let x_i be the i -th stream over the N sources of data within the con-
 210 sidered sensors network. Let $g_{(i,j)}, i, j \in \{1, \dots, N\}$ be the functional relationship (in

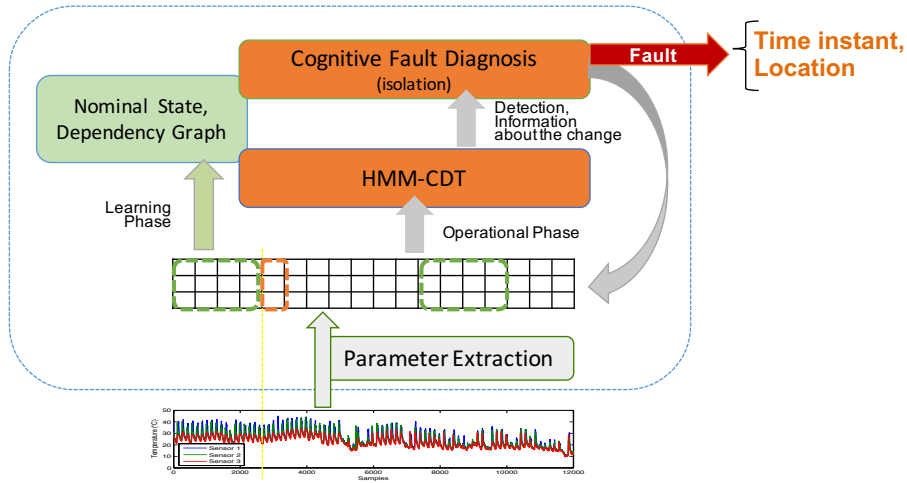


Figure 4: General architecture of the considered CFDS method

211 terms of transfer function) between the i -th and the j -th sensor. All the functional re-
 212 lationships present in the acquired data can be modelled as a *Dependency Graph* \mathcal{G} ,
 213 where the nodes of this graph represent the N sensors of the network, while the arcs
 214 between nodes represent the functional relationships. We emphasize that generally,
 215 in real-world situations, not all the relationships are meaningful, since there might be
 216 nonexistent or very weak relationships between two streams of data. To address this
 217 issue, we only consider those relationships not contradicting the causality provided
 218 by the physical phenomenon and, subsequently, we resort to the use of the analysis
 219 of the linear correlation between x_i and x_j to define a level of dependency associated
 220 with $g_{(i,j)}$. More specifically, to remove weakly correlated streams of data, those data
 221 streams with cross-correlation peak absolute value below a certain threshold ξ_{\min} , with
 222 $0 \leq \xi_{\min} \leq 1$, have been removed (e.g. ξ_{\min} can be set to 0.5 or larger, depending on
 223 the network complexity, to keep only highly correlated data streams). This led to the
 224 definition of a *reduced dependency graph* $G = \{V, E\}$, where V and E are the set of
 225 nodes representing the N network sensors and the set of arcs representing relationships
 226 characterized by higher correlation (i.e. cross-correlation above ξ_{\min}), respectively.
 227 Figures 3(b) and 5 show examples of the reduced dependency graph for Can Guey and

228 Orioles systems, respectively.

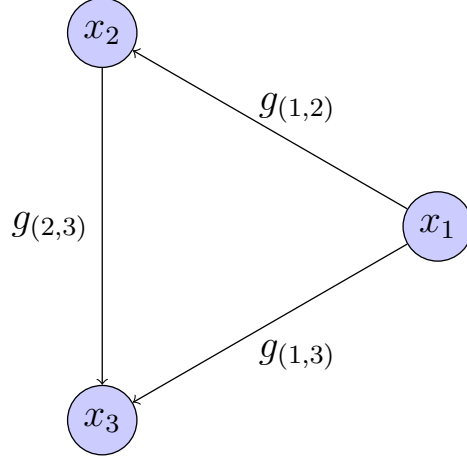


Figure 5: Example of a reduced dependency graph with three sensors (i.e., x_1 , x_2 and x_3) and three relationships (i.e., $g(1,2)$, $g(1,3)$ and $g(2,3)$).

229 Functional relationships $g_{(i,j)}$ in G are modelled either by a linear time-invariant
 230 (LTI) dynamic system or by a sequence of LTI dynamic systems following the HMM
 231 hypothesis (i.e., the Markov memoryless property of stochastic processes). Among the
 232 wide range of LTI dynamic systems, we focus on Single-Input Single-Output (SISO)
 233 models such as AutoRegressive with eXogenous input (ARX) models, AutoRegressive
 234 Moving Average with eXogenous inputs (ARMAX) models or Output Error (OE)
 235 models (Ljung, 1999) in their predictive form, i.e., $g_{(i,j)}^\theta$ parametrized in $\theta \in \mathbb{R}^p$. Here,
 236 θ represents parameter vector of the considered predictive models, while p represents
 237 the cardinality of θ .

238 Assuming that the data generating process satisfies the exponential stability for
 239 closed loop and following the hypotheses on $g_{(i,j)}^\theta$ stated in (Ljung, 1978), the theoretical
 240 results in (Ljung, 1978) grant that

$$\sqrt{N_T} P^{-\frac{1}{2}} (\hat{\theta} - \theta^*) \sim \mathcal{N}(0, I_p) \quad \text{when } N_T \rightarrow \infty, \quad (11)$$

241 where $P \in \mathbb{R}^{p \times p}$ is the covariance matrix of the estimated parameter $\hat{\theta}$ of the model, N_T
 242 is the length of the training set used to estimate $\hat{\theta}$ with the Least Square (LS) method,

243 θ^* is the optimal configuration of the parameters within the chosen model family and
 244 I_p is the identity matrix. From Eq. (11) it may be stated that, given N_T sufficiently
 245 large, the distribution of the estimates $\hat{\theta}$ s follows a multivariate Gaussian with mean
 246 vector θ^* and covariance matrix P . This theoretical result led us to consider HMMs
 247 ruled by a mixture of Gaussians (GMM) to model the statistical behaviour of estimated
 248 parameters $\hat{\theta}$ over time. In more detail, the HMM is defined as

$$\mathcal{H} = \{n, \mathcal{F}, A, \pi\}, \quad (12)$$

249 where n is the number of states, $\mathcal{F} = \{p_1, \dots, p_n\}$ is the set of Probability Density
 250 Functions (PDFs) associated with each state, $A \in [0, 1]^{n \times n}$ is the state transition prob-
 251 ability matrix and $\pi \in [0, 1]^n$ is the initial state distribution vector. It is worth noting
 252 that Eq. (11) allows us to model the PDF associated with the nominal state by using a
 253 GMM. Let

$$p_i(\hat{\theta}|\Phi_i) = \sum_{k=1}^{K_i} w_{k,i} \mathcal{N}(\hat{\theta}|\mu_{k,i}, \Sigma_{k,i}) \quad (13)$$

be the GMM associated with the i -th state, where K_i is the number of Gaussian mixtures
 for the i -th state, $w_{k,i}$ is the weight for state i and Gaussian mixture k ,

$$\Phi_i = [\mu_{1,i}, \dots, \mu_{K_i,i}, \Sigma_{1,i}, \dots, \Sigma_{K_i,i}] \quad (14)$$

254 with $\mu_{k,i}$ and $\Sigma_{k,i}$ the mean vector and the covariance matrix for state i and Gaussian
 255 mixture k , respectively.

256 The analysis of the evolution over time of estimated parameters $\hat{\theta}$ s by means of
 257 a HMM is the core mechanism of the HMM-based CDT. More specifically, for each
 258 $g_{(i,j)} \in V$, the sequence of $\hat{\theta}$ s are estimated by overlapping windows of N_T observations.
 259 The HMM $\mathcal{H}_{(i,j)}$, associated to relationship $g_{(i,j)}$, is trained on the estimated parame-
 260 ters computed from the first T_0 observations, i.e., the training dataset. Then, after the
 261 training phase, the HMM-based CDT keeps on estimating the parameter $\hat{\theta}$ by overlap-
 262 ping windows of data, and let $\hat{\theta}^s$ be the parameter estimated on the s -th window. The
 263 log-likelihood of the HMM is as follows

$$l_{(i,j)}(s) = P(\hat{\theta}^{s-\omega+1}, \dots, \hat{\theta}^s | \mathcal{H}_{(i,j)}) \quad (15)$$

264 where ω is the considered log-likelihood window length. This value indicates how
 265 likely the sequence of parameters $\hat{\theta}^{s-\omega+1}, \dots, \hat{\theta}^s$ has been generated by $\mathcal{H}_{(i,j)}$. When $l_{(i,j)}$
 266 decreases below an automatically defined threshold (i.e., the minimum value assumed
 267 by the log-likelihood in training or validation scaled by a user-defined coefficient fac-
 268 tor), a change in the relationship $g_{(i,j)}$ is detected. Details about the HMM-based CDT
 269 can be found in Algorithm 1 of Alippi et al. (2013) and in Alippi et al. (2012).

270 Once a change in one of the HMM-based CDTs is detected, the Cognitive Fault
 271 Diagnosis layer is activated to isolate the fault within the system. The basic idea of
 272 this cognitive isolation mechanisms is as follows: when a fault affects a sensor, all the
 273 relationships connected to that sensor should be affected by this change. Hence, by
 274 looking at the likelihood of all the relationships in V , we are able to identify the sensor
 275 of the system that has been affected by the fault, and thus to isolate it. Details about the
 276 cognitive level presented here can be also found in Algorithm 2 of Alippi et al. (2013).

277 4. Experimental Results

278 In this paper, the two fault diagnosis methods introduced in previous section are
 279 tested using a simulator of the Barcelona DWTN. This simulator is developed under
 280 MATLAB/SIMULINK platform, using a model calibrated and validated with real data
 281 which provides a good representation of the actual water network behavior. Without
 282 loss of generality, the results presented here are focused on two subsystems within the
 283 Barcelona water transport network (Figure 1), known as Orioles (Figure 6) and Can
 284 Guey (Figure 7), in order to illustrate the performance of the fault diagnosis method-
 285 ologies presented. This part of the network includes the following elements:

- 286 • **Tanks:** *d175LOR, d200CGY, d268CGY, d361CGY*
- 287 • **Actuators with flow sensors:** *iOrioles, iCanGuey1d2, iCanGuey2, iCanGuey3*
- 288 • **Demands with flow sensors:** *c175LOR, c200CGY, c268CGY, c361CGY*
- 289 • **Level sensors:** *xd175LOR, xd200CGY, xd268CGY, xd361CGY*

290 *4.1. Residual Definition*

291 In Figure 6 and Figure 7, q_{in} , q_{out} and y are the incoming tank flow, consumer
 292 demand and tank level, respectively, and q_{in_m} , q_{out_m} and y_m are the corresponding mea-
 293 sured values. The corresponding discrete-time model equations, including the consid-
 294 ered faults, are as follows

- 295 • Tank (level):

$$y(k+1) = y(k) + \frac{\Delta t}{A} [q_{in}(k) - q_{out}(k)] \quad (16)$$

- 296 • Pump (flow):

$$q_{in}(k) = \Gamma_p(k)q_p(k) + f_p(k) \quad (17)$$

- 297 • Tank level sensor:

$$y_m(k) = \Gamma_{y_m}(k)y(k) + f_{y_m}(k) \quad (18)$$

- 298 • Pump flow sensor:

$$q_{in_m}(k) = \Gamma_{q_{in_m}}(k)q_{in}(k) + f_{q_{in_m}}(k) \quad (19)$$

- 299 • Demand sector flow sensor:

$$q_{out_m}(k) = \Gamma_{q_{out_m}}(k)q_{out}(k) + f_{q_{out_m}}(k) \quad (20)$$

300 where $y(k)$ is the actual tank level, $y_m(k)$ is the measured tank level, $q_{out}(k)$ is the actual
 301 demand flow, $q_{out_m}(k)$ is the measured demand flow, $q_{in}(k)$ is the actual input tank flow,
 302 $q_p(k)$ is the set-point pump flow, $q_{in_m}(k)$ is the measured input flow, $\Gamma_c(k)$ is the multi-
 303 plicative fault signal component related to element c , $f_c(k) = \beta_c(k)\chi_c(k)$ is the additive
 304 fault signal component related to element c , with $\beta(k)$ time profile and $\chi(k)$ behavior,
 305 Δt is the sampling time and A is the cylindrical tank surface.

306 Spatial consistency residuals can be obtained using the mass flow model (16) and
 307 the sensor measurements (17)-(20) in a non-faulty situation. In particular, the following

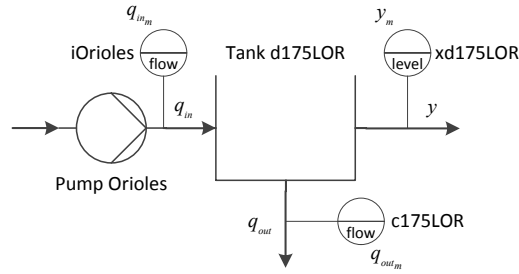


Figure 6: Orioles subsystem

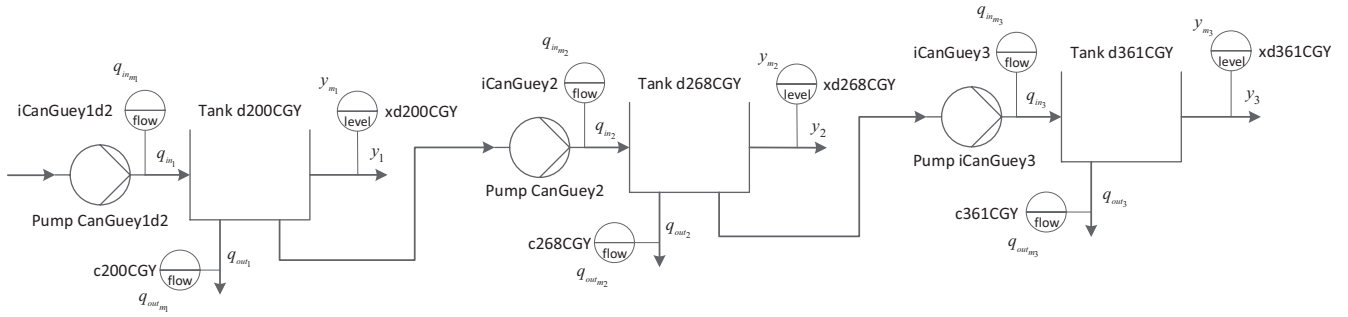


Figure 7: Can Guey subsystem

308 residual $r_{i,1}$ may be obtained using the tank model (16) for the i -th tank subsystem using
 309 measured variables

$$r_{i,1}(k) = y_{m_i}(k) - \hat{y}_{sc_i}(k) \quad (21)$$

310 with

$$\hat{y}_{sc_i}(k) = y_{m_i}(k-1) + \frac{\Delta t}{A_i} [q_{in_{m_i}}(k-1) - q_{out_{m_i}}(k-1)] \quad (22)$$

311 where \hat{y}_{sc_i} is the tank level spatial consistency estimation, A_i is the cylindrical tank
 312 surface, $q_{in_{m_i}}$ is the manipulated measured inflow and $q_{out_{m_i}}$ is the measured outflow,
 313 both given in m^3/s .

314 Furthermore, for each input and output with periodic behaviour of the i -th tank
 315 subsystem, a TS HW model can be derived and the following Analytical Redundancy

316 Relations (ARRs) may be obtained:

- 317 • Tank (level) TS:

$$\hat{y}_{ts_i}(k) = g(y_{m_i}(k-1), \dots, y_{m_i}(k-L)) \quad (23)$$

- 318 • Demand sector flow TS:

$$\hat{q}_{out_{ts_i}}(k) = h(q_{out_{m_i}}(k-1), \dots, q_{out_{m_i}}(k-L)) \quad (24)$$

- 319 • Pump flow TS:

$$\hat{q}_{in_{ts_i}}(k) = l(q_{in_{m_i}}(k-1), \dots, q_{in_{m_i}}(k-L)) \quad (25)$$

320 where g , h and l are the HW TS expressions (6)-(9) for the tank level sensor, sector
321 demand sensor and pump flow sensor respectively, for data exhibiting a periodicity of
322 L samples.

323 Using the TS models (23)-(25), the following residuals are obtained

$$r_{i,2}(k) = y_{m_i}(k) - \hat{y}_{ts_i}(k) \quad (26)$$

$$r_{i,3}(k) = q_{out_{m_i}}(k) - \hat{q}_{out_{ts_i}}(k) \quad (27)$$

$$r_{i,4}(k) = q_{in_{m_i}}(k) - \hat{q}_{in_{ts_i}}(k) \quad (28)$$

324 It may be noted that TS residuals in Equations (26)-(28) can only be applied for
325 those sensors presenting periodic behavior. This is applicable to all the faulty elements
326 considered in this work and also to the major part of the elements of the network,
327 but still there are some which are not expected to evolve periodically (e.g. pump sta-
328 tions not directly serving water to a demand sector). Hence, in order to apply PTPR
329 fault isolation methodology using TS residuals, elements involved should be previously
330 checked for periodic behavior. As a counterpart, TS residuals may be computed with
331 information provided by a single sensor, which may be advantageous in certain appli-
332 cations with non-obvious/non-existent model relation among sensors, e.g. intelligent
333 sensors with embedded diagnosis unit (Alippi et al. (2012)).

Table 1: Faults signatures

	f_{ym}	f_{qout_m}	f_{qin_m}	f_p	f_{ym1}	$f_{qout_{m1}}$	$f_{qin_{m1}}$	f_{p1}	f_{ym2}	$f_{qout_{m2}}$	$f_{qin_{m2}}$	f_{p2}	f_{ym3}	$f_{qout_{m3}}$	$f_{qin_{m3}}$	f_{p3}
$r_{1,1}$	1	1	1	1	0	0	0	0	0	0	0	0	0	0	0	0
$r_{1,2}$	1	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0
$r_{1,3}$	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0
$r_{1,4}$	0	0	1	1	0	0	0	0	0	0	0	0	0	0	0	0
$r_{2,1}$	0	0	0	0	1	1	1	1	0	0	0	0	0	0	0	0
$r_{2,2}$	0	0	0	0	1	0	0	1	0	0	0	0	0	0	0	0
$r_{2,3}$	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0
$r_{2,4}$	0	0	0	0	0	0	1	1	0	0	0	0	0	0	0	0
$r_{3,1}$	0	0	0	0	0	0	0	0	1	1	1	1	0	0	0	0
$r_{3,2}$	0	0	0	0	0	0	0	0	1	0	0	1	0	0	0	0
$r_{3,3}$	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0
$r_{3,4}$	0	0	0	0	0	0	0	0	0	0	1	1	0	0	0	0
$r_{4,1}$	0	0	0	0	0	0	0	0	0	0	0	0	1	1	1	1
$r_{4,2}$	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0	1
$r_{4,3}$	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0
$r_{4,4}$	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	1

334 From residuals (21), (26) to (28) and equations (17) to (20) the theoretical FSM
335 for the subsystems considered (Figure 6 and Figure 7) is presented in Table 1. In the
336 latter, the sensitivity of each residual to each fault is detailed by means of a 0 (i.e. non-
337 sensitive) or a 1 (i.e. sensitive) in the corresponding element of the matrix, obtaining a
338 fault signature from each of its columns. Also, ordinal index i is assigned for each tank
339 subsystem as follows: $i = 1$ for d175LOR, $i = 2$ for d200CGY, $i = 3$ for d268CGY and
340 $i = 4$ for d361CGY tank subsystem. Moreover, it may be also observed how spatial
341 consistency residuals are used for fault detection here, since $r_{i,1}$ is sensitive to all the
342 considered faults within each i single tank subsystem, whilst TS residuals are employed
343 for fault isolation purposes.

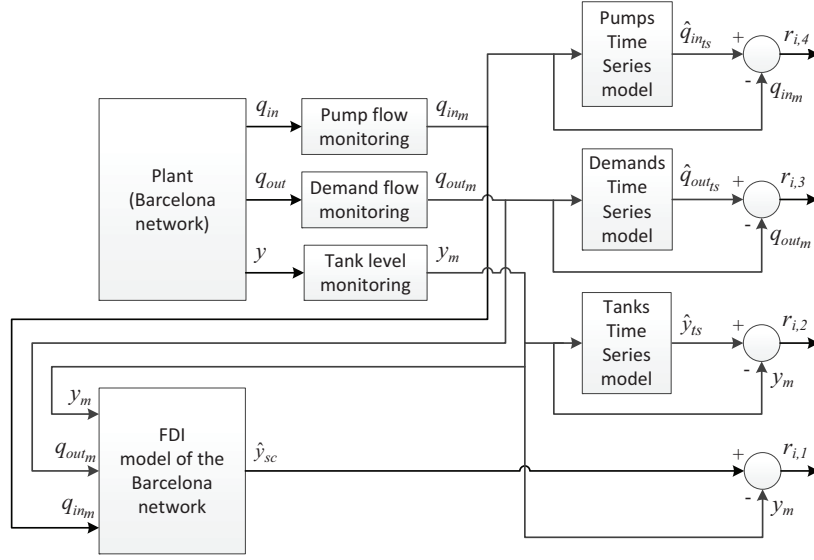


Figure 8: FDI Scheme for Barcelona DWTN

344 The resulting PTPR fault diagnosis scheme implemented in the Barcelona DWTN
 345 system, involving the different elements detailed in this section, is shown in Figure 8.

346 4.2. Fault scenarios

347 The Barcelona DWTN simulator allows the introduction of faults of different kinds
 348 in distinct elements of this water network. Here, faults of freezing, offset and drift
 349 nature are considered

- 350 • **Freezing:** $\Gamma(k) = 0$ and $\chi(k) = \kappa$ for $k \geq k_f$
- 351 • **Offset:** $\Gamma(k) = 1$ and $\chi(k) = \eta$ for $k \geq k_f$
- 352 • **Drift:** $\Gamma(k) = 1$ and $\chi(k) = R(k - k_f)$ for $k \geq k_f$

353 where κ and η are constants, R denotes the ramp function of a certain slope and k_f is
 354 the time instant when the fault is occurring.

355 Moreover, the faults considered are either of abrupt or incipient nature, as defined
 356 by their time profile $\beta(k)$ as follows

357 • **Abrupt:**

$$\beta(t) = \begin{cases} 0, & k < k_f \\ 1, & k \geq k_f \end{cases}$$

358 • **Incipient:**

$$\beta(t) = \begin{cases} 0, & k < k_f \\ 1 - e^{-\rho(k-k_f)}, & k \geq k_f \end{cases}$$

359 where $\rho > 0$ is the constant characterizing the evolution of the corresponding fault and
360 k_f is the time instant when the fault occurs.

361 Different fault scenarios are defined in order to test and compare the methods pre-
362 sented here, all including random normally distributed measurement noise of ± 1 %
363 full scale. The dataset considered to implement these fault scenarios lasts for seven
364 months, with a sampling period $T = 1$ hour and a fault appearing at $t_f = 744 \cdot T$ in
365 different elements of the Barcelona DWTN subsystems considered (Figures 6 and 7,
366 respectively):

- 367 • iOrioles pump sensor ($f_{q_{inm}}$) in Orioles subsystem
- 368 • c175LOR demand sensor ($f_{q_{outm}}$) in Orioles subsystem
- 369 • iCanGuey1d2 pump sensor ($f_{q_{inm_1}}$) in Can Guey subsystem
- 370 • iCanGuey2 pump sensor ($f_{q_{inm_2}}$) in Can Guey subsystem
- 371 • iCanGuey3 pump sensor ($f_{q_{inm_3}}$) in Can Guey subsystem
- 372 • c361CGY demand sensor ($f_{q_{outm_2}}$) in Can Guey subsystem
- 373 • c268CGY demand sensor ($f_{q_{outm_3}}$) in Can Guey subsystem

374 These fault scenarios are part of a fault benchmark used in the framework of the
375 Seventh Framework Program European project iSense (ref. FP7-ICT-2009-6) as a col-
376 laborative dataset provided by the Polytechnic University of Catalonia to be used by
377 all the partners involved. The parametrization of the faults involved in this benchmark
378 is depicted in Table 2.

379 4.3. Methods Setting

380 The HMM-based CDT uses ARX linear models for the extraction of the param-
381 eters θ . In the case of Orioles subsystem (Figure 6), the relationship pattern among
382 the measured tank level, the input flow and the measured demands are modelled. The
383 dependency graph is learned by considering all the binary relationships with autocor-
384 relation greater or equal to $\xi_{\min} = 0.5$. The result is the graph presented in Figure 5
385 with $(x_1, x_2, x_3) = (y_m, q_{in_m}, q_{out_m})$. In the case of Can Guey subsystem (Figure 7), we
386 only considered those relationships compatible with the causality given by the water
387 flow phenomenon (i.e. those in Figure 3(a)) and selected those having autocorrela-
388 tion greater or equal to $\xi_{\min} = 0.8$, where the higher threshold is due to the increased
389 complexity of the network. Under faulty conditions, the considered relationships will
390 exhibit changes that will depend on the kind and magnitude of the fault introduced,
391 thus its monitoring is useful for fault isolation purposes.

392 Regarding the PTPR initialisation, the first 13 days of data are used as training
393 dataset to identify the model parameters, the next 13 days are used as validation dataset
394 to obtain the corresponding fault detection threshold and the rest of the data is used as
395 test dataset. Regarding the HMMs, also a total of 26 days are used for training and
396 validation purposes: 23 and 25 days were used for training the Orioles and the Can
397 Guey cases, respectively, while the remaining days have been used to compute the
398 threshold for detection and validation (Alippi et al., 2013). The orders of ARX models
399 have been chosen by means of a validation procedure. The log-likelihood window
400 length has been set to $\omega = 10$ and the batch size has been set to $N_T = 96$ and $N_T = 100$
401 for the Orioles and Can Guey subsystems, respectively.

402 4.4. Figures of Merit

403 The numerical results are presented by means of different figures of merit. First
404 stage in fault diagnosis deals with faultless vs. faulty situation discrimination. The
405 performance achieved in this fault detection stage is measured by the next indices:

- 406 • **Detection delay:** Number of samples needed by the fault diagnosis method to
407 detect a certain fault.

408 • **False Positives (FP):** Percentage of test dataset faultless samples (i.e. non-
409 affected by a certain fault) that are determined as faulty by the fault detection
410 method.

411 • **False Negatives (FN):** Percentage of test dataset faulty samples (i.e. affected
412 by a certain fault) that are determined as faultless by the fault detection method
413 within the 72 samples (i.e. 3 days) after a fault is produced.

414 Moreover, the second stage in fault diagnosis involves fault isolation and classifica-
415 tion abilities of the FDI method. These may be quantified by different figures of merit,
416 which are defined as follows:

417 • **Isolation delay:** Number of samples needed by the fault diagnosis method to
418 isolate a certain fault.

419 • **Isolation index:** Percentage of test dataset faulty samples (i.e. affected by a
420 certain fault) that are properly isolated within the 72 samples (i.e. 3 days) after a
421 fault is produced, considering a certain fault scenario.

422 4.5. Results

423 In Table 2, fault diagnosis results achieved by both FDI methods are detailed. In
424 Figures 9 and 10, isolation results obtained by PTPR method for faults Id. 2 and Id. 14
425 in Table 2 are also depicted. As may be seen in the latter figures, residuals evolution
426 fit the fault signatures corresponding to the respective faults occurring in the system
427 when these results are attained, i.e. iOrioles actuator sensor fault ($f_{q_{im}}$ in Table 1) and
428 c175LOR demand sensor fault ($f_{q_{out}}$ in Table 1). Similar isolation results have been
429 obtained for faults included in Table 2 affecting similar network elements.

430 On the one hand, Table 2 shows generally better detection and isolation delay re-
431 sults achieved by PTPR method than by CFDS method, for the pump sensors of iOri-
432 oles (e.g. fault Id. 3, 4), iCanGuey1d2 (e.g. fault Id. 21, 22, 26), iCanGuey3 (e.g. fault
433 Id. 37, 38) and the demand sensor c175LOR (e.g. fault Id. 11, 12, 13, 15, 19), with
434 the exceptions of some faults with similar or better performance achieved by CFDS
435 affecting iOrioles pump sensor (e.g. fault Id. 1, 2, 5, 6, 8), c175LOR (e.g. fault Id. 10),

Table 2: Faults parametrization and diagnosis results (MFD stands for maximum flow/demand)

Id.	Type of fault	Magnitude	PTPR method					CFDS method				
			Delay [# of samples]		FP [%]	FN [%]	Iso. [%]	Delay [# of samples]		FP [%]	FN [%]	Iso. [%]
			detection	isolation				detection	isolation			
1	Offset abr. iOrioles	10 % MFD	2	4	0	7.34	22.22	4	4	7.44	94.52	5.48
2	Offset abr. iOrioles	25 % MFD	2	2	0	2.37	79.16	3	3	11.57	4.11	95.89
3	Offset inc. iOrioles	10 % MFD	12	23	0	3.04	4.16	35	35	12.40	82.19	17.81
4	Offset inc. iOrioles	25 % MFD	9	13	0	4.53	52.77	16	16	0.00	27.40	72.60
5	Drift abr. iOrioles	1 % MFD	9	13	0	2.71	73.61	8	8	13.22	10.96	89.04
6	Drift abr. iOrioles	10 % MFD	3	3	0	2.78	84.72	4	4	1.65	5.48	94.52
7	Drift inc. iOrioles	1 % MFD	12	23	0	3.54	59.72	18	18	9.92	24.66	75.34
8	Drift inc. iOrioles	10 % MFD	7	7	0	4.09	77.77	4	4	8.26	8.22	91.78
9	Offset abr. c175LOR	10 % MFD	1	3	0	0.02	65.27	3	3	0.00	4.11	95.89
10	Offset abr. c175LOR	25 % MFD	1	3	0	0.02	65.27	1	1	0.00	1.37	98.63
11	Offset inc. c175LOR	10 % MFD	10	21	0	0.29	34.72	47	47	0.00	64.38	35.62
12	Offset inc. c175LOR	25 % MFD	7	11	0	0.13	58.33	65	65	0.00	89.04	10.96
13	Drift abr. c175LOR	1 % MFD	7	7	0	0.11	59.72	33	33	0.00	45.21	54.79
14	Drift abr. c175LOR	10 % MFD	2	4	0	0.04	63.88	4	4	0.00	5.48	94.52
15	Drift inc. c175LOR	1 % MFD	10	15	0	0.25	52.77	39	39	0.00	53.42	46.58
16	Drift inc. c175LOR	10 % MFD	5	7	0	0.11	59.72	8	8	38.02	10.96	89.04
17	Freezing abr. iOrioles	-	7	12	0	7.22	8.33	17	17	10.74	68.49	31.51
18	Freezing inc. iOrioles	-	19	36	0	7.52	5.55	3	3	22.31	73.97	26.03
19	Freezing abr. c175LOR	-	11	14	0	16.79	6.94	33	33	0.00	45.21	54.79
20	Freezing inc. c175LOR	-	59	-	0	92.84	0	58	58	4.13	79.45	20.55
21	Offset abr. iCanGuey1d2	15 % MFD	2	4	0	1.37	39.73	21	22	0	30.56	69.44
22	Offset inc. iCanGuey1d2	15 % MFD	9	26	0	12.33	8.22	32	50	0	69.44	30.56
23	Drift abr. iCanGuey1d2	15 % MFD	3	4	0	2.74	93.15	5	11	0	15.28	84.72
24	Freezing abr. iCanGuey1d2	-	3	8	0	9.59	71.23	12	21	0	29.17	70.83
25	Offset abr. iCanGuey2	15 % MFD	2	-	0	1.37	-	14	29	0	40.28	59.72
26	Offset inc. iCanGuey2	15 % MFD	8	26	0	12.33	2.74	32	53	0	73.61	26.39
27	Drift abr. iCanGuey2	15 % MFD	3	4	0	2.74	93.15	7	9	0	12.50	87.50
28	Freezing abr. iCanGuey2	-	3	4	0	5.48	67.12	11	12	0	16.67	83.33
29	Offset abr. c361CGY	15 % MFD	2	4	0	1.37	93.15	3	3	0	4.17	95.83
30	Offset inc. c361CGY	15 % MFD	9	11	0	10.96	82.19	10	12	0	16.67	83.33
31	Drift abr. c361CGY	15 % MFD	3	4	0	2.74	93.15	3	3	0	4.17	95.83
32	Freezing abr. c361CGY	-	10	12	0	34.25	10.96	9	11	0	15.28	84.72
33	Offset abr. c268CGY	15 % MFD	2	4	0	1.37	93.15	1	1	0	1.39	98.61
34	Offset inc. c268CGY	15 % MFD	8	11	0	9.59	80.82	3	9	0	12.50	87.50
35	Drift abr. c268CGY	15 % MFD	3	4	0	2.74	93.15	2	2	0	2.78	97.22
36	Freezing abr. c268CGY	-	10	12	0	56.16	6.85	3	11	0	15.28	84.72
37	Offset abr. iCanGuey3	15 % MFD	2	4	0	1.37	63.01	5	7	0	9.72	90.28
38	Offset inc. iCanGuey3	15 % MFD	8	28	0	28.77	12.33	28	29	0	40.28	59.72
39	Drift abr. iCanGuey3	15 % MFD	3	4	0	2.74	93.15	4	4	0	5.56	94.44
40	Freezing abr. iCanGuey3	-	3	10	0	26.03	64.38	9	13	0	18.06	81.94

436 c268CGY and c361CGY demand sensors (e.g. fault Id. 29 to 36), freezing incipient
437 faults affecting Orioles system (e.g. faults Id. 18, 20) or iCanGuey pump sensor (fault
438 Id. 25) for isolation delay. Also, generally better FP and FN rates are achieved by the
439 PTPR method, with some exceptions regarding freezing nature faults (i.e. faults Id. 20,
440 32, 36, 40) for FN rates. This overall detection and isolation behavior leads to a gener-
441 ally quicker and more reliable diagnosis of the faulty component under study achieved
442 by the PTPR method. On the other hand, CFDS method grants better isolation rates in
443 general (with the exception of faults Id. 1, 12, 13, 15, 23, 24, 27 where PTPR method
444 provides similar or better results, depending on the scenario considered) which makes
445 it useful to confirm the isolated fault occurring in the system. It is worth noting that
446 the CFDS method provides the performance in Table 2 without assuming any *a-priori*
447 information about the physical model of the system. In the case of faults with an in-
448 creasing profile, the detection delays of the CFDS are worse than those obtained with
449 the PTPR method. This is due to the fact that the HMM-based CDT is more sensitive to
450 abrupt changes in the parameter distribution. Also, CFDS is generally characterized by
451 higher FP index values. The reason of this behaviour is twofold: nominal state approx-
452 imation and process time invariance. First, the nominal model is estimated during an
453 initial training phase that, in principle, could led to inaccurate models, i.e., model bias
454 due to e.g. an incorrect selection of the family of models, the lack of enough data for
455 training or the fact that training data do not excite the whole dynamics of the process.
456 This undesired model bias tends to induce FP detections in the testing phase. Second,
457 the process under monitoring could be intrinsically time-varying and does not follow
458 the Markov assumption. This leads to FP detection induced by an estimated model
459 which is not able to fully describe the process.

460 4.6. Discussion

461 From the light of the results in Section 4.5, both FDI methods introduced present
462 satisfactory performance for the fault scenarios considered, also showing some com-
463 plementarity features which suggest possible integration in order to improve the overall
464 fault diagnosis. Specifically, the PTPR method obtains generally lower detection and
465 isolation delays, as well as better FP and FN rates. Hence, it is a good choice for early

466 reliable isolation of the faults appearing in the system, whilst the CFDS obtains generally better isolation rates, which allows to reliably confirm the fault being detected
 467 and isolated. Regarding the benefits of each method, on the one hand PTPR is based
 468 and isolated. Regarding the benefits of each method, on the one hand PTPR is based
 469 on physical models describing the normal behavior and does not require to have data
 470 from all the possible fault scenarios to perform the fault diagnosis, in contrast to the
 471 CFDS method. On the other hand, the main drawback of the PTPR approach is the
 472 deep knowledge of the model structure and parameters required to successfully apply
 473 this methodology, which is not needed by the CFDS since it is a data-based approach.
 474 These facts further motivate the integration of both methods for FDI, taking advantage
 475 of the highlights which characterize each one separately.

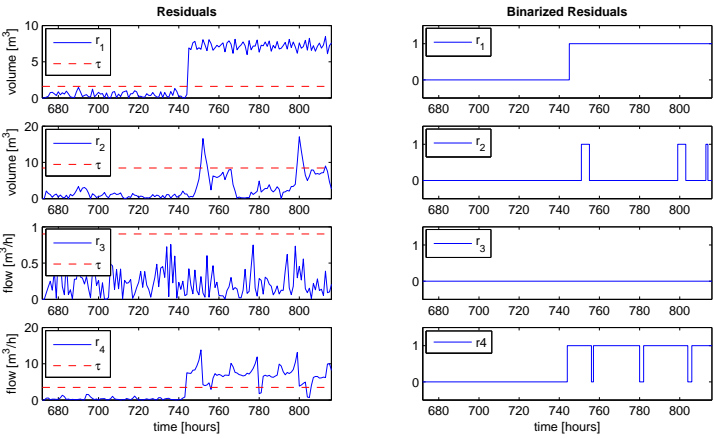


Figure 9: Fault Id.2 residuals, PTPR method

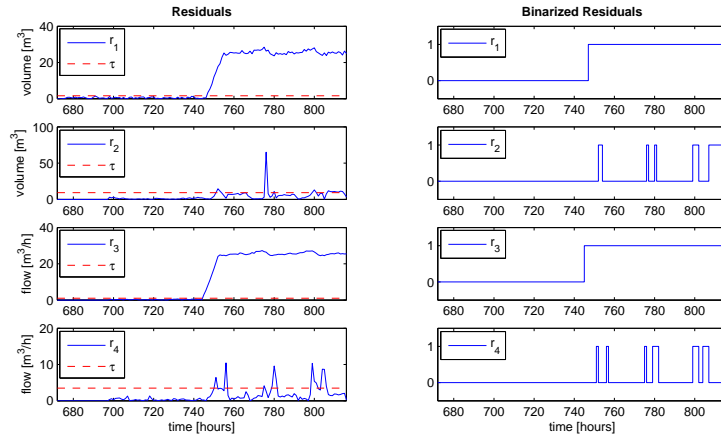


Figure 10: Fault Id.14 residuals, PTPR method

476 5. Conclusions

477 In this work, the application and comparison of two well accepted general purpose
 478 fault diagnosis methods (one model-based, the other data-based) applied to a real
 479 DWTN located in the Barcelona area, is developed. Most of the works in the literature
 480 addressing fault diagnosis in water networks have treated the problem at the
 481 distribution level, but not at the transport level. However, water transport networks
 482 have characteristics which allow the application of techniques that cannot be applied to
 483 distribution networks. The first method is built upon a model-based approach exploiting
 484 *a-priori* information regarding physical/temporal relations which exist between the
 485 measured variables within the monitored system, whilst the second aims at characterizing
 486 and detecting changes in the probabilistic pattern sequence of the data coming from
 487 this system. Some enhancements of the two approaches considered are introduced, as
 488 the use of time series residuals, not generally considered in classical residual-based
 489 fault diagnosis schemes, which traditionally use physical residuals. Successful results
 490 have been achieved by both methods, showing good complementary conditions which
 491 may suggest the integrated usage in order to improve the results achieved by each one
 492 separately. These results have been tested using heterogeneous types of faults in repre-

493 tentative subsystems within the network under study. Future work including additional
494 analysis of the fault diagnosis results achieved, considering uncertainty such noise and
495 modelling/measurement errors derived by the examination of the system under study,
496 is to be done on the ongoing works involving the Barcelona DWTN.

497 **Acknowledgement**

498 This work has been partially funded by the Spanish Ministry of Science and Tech-
499 nology through the Project WATMAN (Ref. DPI-2009-13744), Project SHERECS
500 (Ref. DPI-2011-26243), Project ECOCIS (Ref. DPI2013-48243-C2-1-R), Project
501 HARCRICS (Ref. DPI2014-58104-R), and by i-Sense grant FP7-ICT-2009-6-270428
502 and EFFINET grant FP7-ICT-2012-318556 of the European Commission.

503 **References**

- 504 Alippi C, Ntalampiras S, Roveri M. An HMM-based change detection method for
505 intelligent embedded sensors. In: Neural Networks (IJCNN), The 2012 International
506 Joint Conference on. 2012. p. 1 –7. doi:10.1109/IJCNN.2012.6252610.
- 507 Alippi C, Ntalampiras S, Roveri M. A cognitive fault diagnosis system for distributed
508 sensor networks. IEEE Transactions on Neural Networks and Learning Systems
509 2013;24(8):1213 –26.
- 510 Bicik J, Kapelan Z, Makropoulos C, Savić Da. Pipe burst diagnostics using evi-
511 dence theory. Journal of Hydroinformatics 2011;13(4):596. URL: <http://www.iwaponline.com/jh/013/jh0130596.htm>. doi:10.2166/hydro.2010.201.
- 513 Blanke M, Kinnaert M, Lunze J, Staroswiecki M, Schröder J. Diagnosis and Fault-
514 Tolerant Control. Secaucus, NJ, USA: Springer-Verlag New York, Inc., 2006.
- 515 Casillas MV, Garza LE, Puig V. Model-based leak detection and location in water
516 distribution networks considering an extended-horizon analysis of pressure sensitivi-
517 ties. Journal of Hydroinformatics 2014;In Press. URL: <http://www.iwaponline.com/jh/up/jh2013019.htm>. doi:10.2166/hydro.2013.019.

519 Colombo A, Karney B. Energy and costs of leaky pipes: Toward compre-
520 hensive picture. *J Water Resour Plann Manage* 2002;128(6):441–50. URL:
521 [http://dx.doi.org/10.1061/\(ASCE\)0733-9496\(2002\)128:6\(441\)](http://dx.doi.org/10.1061/(ASCE)0733-9496(2002)128:6(441)).
522 doi:10.1061/(ASCE)0733-9496(2002)128:6(441).

523 Eliades D, Polycarpou M. A fault diagnosis and security framework for water systems.
524 *IEEE Transactions on Control Systems Technology* 2010;18(6):1254–65.

525 Eliades D, Polycarpou M. Leakage fault detection in district metered areas of water
526 distribution systems. *Journal of Hydroinformatics* 2012;In Press. doi:10.2166/
527 hydro.2012.109.

528 Farley B, Mounce S, Boxall J. Development and field validation of a burst lo-
529 calization methodology. *J Water Resour Plann Manage* 2012;139(6):604–13.
530 URL: [http://dx.doi.org/10.1061/\(ASCE\)WR.1943-5452.0000290](http://dx.doi.org/10.1061/(ASCE)WR.1943-5452.0000290). doi:10.
531 1061/(ASCE)WR.1943-5452.0000290.

532 Filion Y, Li Z, Buchberger S. Temporal and spatial scaling of instantaneous residential
533 water demand for network analysis. In: *World Environmental and Water Resources*
534 *Congress 2007*. American Society of Civil Engineers; 2007. p. 1–10. URL: [http://dx.doi.org/10.1061/40927\(243\)512](http://dx.doi.org/10.1061/40927(243)512). doi:10.1061/40927(243)512.

536 Krause A, Leskovec J, Guestrin C, VanBriesen J, Faloutsos C. Efficient
537 sensor placement optimization for securing large water distribution net-
538 works. *J Water Resour Plann Manage* 2008;134(6):516–26. URL:
539 [http://dx.doi.org/10.1061/\(ASCE\)0733-9496\(2008\)134:6\(516\)](http://dx.doi.org/10.1061/(ASCE)0733-9496(2008)134:6(516)).
540 doi:10.1061/(ASCE)0733-9496(2008)134:6(516).

541 Lees M. Data-based mechanistic modelling and forecasting of hydrological systems.
542 *Journal of Hydroinformatics* 2000;:15–34URL: [http://www.iwaponline.com/
543 jh/002/jh0020015.htm](http://www.iwaponline.com/jh/002/jh0020015.htm).

544 Ljung L. Convergence analysis of parametric identification methods. *Automatic Con-*
545 *trol*, *IEEE Transactions on* 1978;23(5):770–83.

546 Ljung L. System identification. Wiley Online Library, 1999.

547 Makridakis S, Wheelwright S, Hyndman R. Forecasting methods and applications.
548 John Wiley & Sons, 1998.

549 Meseguer J, Puig V, Escobet T. Fault diagnosis using a timed discrete-event approach
550 based on interval observers: application to sewer networks. IEEE Transactions on
551 Systems Man and Cybernetics Part A: Systems and Humans 2010;40(5):900–16.

552 Misiunas D, Vítkovský J, Olsson G, Lambert M, Simpson a. Failure monitoring in
553 water distribution networks. Water science and technology : a journal of the In-
554 ternational Association on Water Pollution Research 2006;53(4-5):503–11. URL:
555 <http://www.ncbi.nlm.nih.gov/pubmed/16722103>.

556 Mounce S, Boxall J, Machell J. Development and verification of an on-
557 line artificial intelligence system for detection of bursts and other abnormal
558 flows. J Water Resour Plann Manage 2009;136(3):309–18. URL: [http://dx.doi.org/10.1061/\(ASCE\)WR.1943-5452.0000030](http://dx.doi.org/10.1061/(ASCE)WR.1943-5452.0000030). doi:10.1061/(ASCE)WR.
559 1943-5452.0000030.

560

561 Mounce SR, Boxall JB. Implementation of an on-line artificial intelligence district
562 meter area flow meter data analysis system for abnormality detection: a case study.
563 Water Science & Technology: Water Supply 2010;10:437–44.

564 Mounce SR, Mounce RB, Boxall JB. Novelty detection for time series data analy-
565 sis in water distribution systems using support vector machines. Journal of Hy-
566 droinformatics 2011;13(4):672. URL: [http://www.iwaponline.com/jh/013/](http://www.iwaponline.com/jh/013/jh0130672.htm)
567 [jh0130672.htm](http://www.iwaponline.com/jh/013/jh0130672.htm). doi:10.2166/hydro.2010.144.

568 Ostfeld A, Salomons E. Optimal layout of early warning detection stations for wa-
569 ter distribution systems security. J Water Resour Plann Manage 2004;130(5):377–
570 85. URL: [http://dx.doi.org/10.1061/\(ASCE\)0733-9496\(2004\)130:](http://dx.doi.org/10.1061/(ASCE)0733-9496(2004)130:5(377))
571 [5\(377\)](http://dx.doi.org/10.1061/(ASCE)0733-9496(2004)130:5(377)). doi:10.1061/(ASCE)0733-9496(2004)130:5(377).

572 Palau C, Arregui F, Carlos M. Burst detection in water networks using prin-
573 cipal component analysis. J Water Resour Plann Manage 2011;138(1):47–54.

574 URL: [http://dx.doi.org/10.1061/\(ASCE\)WR.1943-5452.0000147](http://dx.doi.org/10.1061/(ASCE)WR.1943-5452.0000147). doi:10.
575 1061/(ASCE)WR.1943-5452.0000147.

576 Perez R, Puig V, Pascual J, Quevedo J, Landeros E, Peralta A. Methodology for leakage
577 isolation using pressure sensitivity analysis in water distribution networks. *Control*
578 *Engineering Practice* 2011;19(10):1157-67. URL: <http://www.sciencedirect.com/science/article/pii/S0967066111001201>.
579

580 Prescott SL, Ulanicki B. Time series analysis of leakage in water distribution networks.
581 *Water software systems - Theory and applications* 2001;2:17-28.

582 Pérez R, Puig V, Pascual J, Quevedo J, Landeros E, Peralta A. Leakage isolation
583 using pressure sensitivity analysis in water distribution networks: Application to the
584 Barcelona case study. In: *12th IFAC Symposium on Large-Scale Systems: Theory*
585 *and Applications*. volume 9; 2010. p. 578-84.

586 Puig V, Blesa J. Limnimeter and rain gauge FDI in sewer networks using an inter-
587 val parity equations based detection approach and an enhanced isolation scheme.
588 *Control Engineering Practice* 2013;21(2):146-70.

589 Puig V, Stancu A, Escobet T, Nejari F, Quevedo J, Patton R. Passive robust
590 fault detection using interval observers: Application to the damadics benchmark
591 problem. *Control Engineering Practice* 2006;14(6):621-33. URL: <http://www.sciencedirect.com/science/article/pii/S0967066105001048>.
592

593 Quevedo J, Chen H, Cugueró MA, Tino P, Puig V, García D, Sarrate R, Yao X. Com-
594 bining learning in model space fault diagnosis with data validation/reconstruction:
595 Application to the barcelona water network. *Engineering Applications of Arti-*
596 *ficial Intelligence* 2014;30(0):18-29. URL: <http://www.sciencedirect.com/science/article/pii/S0952197614000153>.
597

598 Quevedo J, Puig V, Cembrano G, Blanch J, Aguilar J, Saporta D, Benito
599 G, Hedó M, Molina A. Validation and reconstruction of flow meter data
600 in the Barcelona water distribution network. *Control Engineering Practice*

601 2010;18(6):640–51. URL: [http://linkinghub.elsevier.com/retrieve/](http://linkinghub.elsevier.com/retrieve/pii/S0967066110000791)
602 [pii/S0967066110000791](http://linkinghub.elsevier.com/retrieve/pii/S0967066110000791). doi:10.1016/j.conengprac.2010.03.003.

603 Ragot J, Maquin D. Fault measurement detection in an urban water supply
604 network. *Journal of Process Control* 2006;16(9):887–902. URL: <http://www.sciencedirect.com/science/article/pii/S0959152406000655>.
605 [doi:10.1016/j.jprocont.2006.06.005](http://www.sciencedirect.com/science/article/pii/S0959152406000655).

607 Romano M, Kapelan Z, Savic D. Geostatistical techniques for approximate location
608 of pipe burst events in water distribution systems. *Journal of Hydroinformatics*
609 2013;15(3):634–51.

610 Romano M, Kapelan Z, Savic D. Automated detection of pipe bursts and other events
611 in water distribution systems. *J Water Resour Plann Manage* 2014a;140(4):457–67.
612 URL: [http://dx.doi.org/10.1061/\(ASCE\)WR.1943-5452.0000339](http://dx.doi.org/10.1061/(ASCE)WR.1943-5452.0000339). doi:10.
613 [1061/\(ASCE\)WR.1943-5452.0000339](http://dx.doi.org/10.1061/(ASCE)WR.1943-5452.0000339).

614 Romano M, Kapelan Z, Savic D. Evolutionary algorithm and expectation maxi-
615 mization strategies for improved detection of pipe bursts and other events in wa-
616 ter distribution systems. *J Water Resour Plann Manage* 2014b;140(5):572–84.
617 URL: [http://dx.doi.org/10.1061/\(ASCE\)WR.1943-5452.0000347](http://dx.doi.org/10.1061/(ASCE)WR.1943-5452.0000347). doi:10.
618 [1061/\(ASCE\)WR.1943-5452.0000347](http://dx.doi.org/10.1061/(ASCE)WR.1943-5452.0000347).

619 Winters PR. Forecasting sales by exponentially weighted moving averages. *Manage-*
620 *ment Science* 1960;6(52):324–42. URL: [http://www.jstor.org/stable/10.](http://www.jstor.org/stable/10.2307/2627346)
621 [2307/2627346](http://www.jstor.org/stable/10.2307/2627346).

622 Wu Z. Online monitoring and detection; Exton: Bentley Systems. p. 168–89.

623 Wu Z, Sage P, Turtle D. Pressure-dependent leak detection model and its
624 application to a district water system. *Journal of Water Resources Plan-*
625 *ning and Management* 2010;136(1):116–28. URL: [http://ascelibrary.](http://ascelibrary.org/doi/abs/10.1061/(ASCE)0733-9496(2010)136:1(116))
626 [org/doi/abs/10.1061/\(ASCE\)0733-9496\(2010\)136:1\(116\)](http://ascelibrary.org/doi/abs/10.1061/(ASCE)0733-9496(2010)136:1(116)). doi:10.1061/
627 [\(ASCE\)0733-9496\(2010\)136:1\(116\)](http://ascelibrary.org/doi/abs/10.1061/(ASCE)0733-9496(2010)136:1(116)).