Identification of the hygro-thermo-chemical-mechanical model parameters of concrete through inverse analysis Massimiliano Bocciarelli¹*, Gianluca Ranzi² ¹ Architecture, Built environment and Construction engineering Department, Politecnico di Milano (Technical University), Italy ² School of Civil Engineering, The University of Sydney, Australia * Corresponding Author. E-mail: massimiliano.bocciarelli@polimi.it

8 Abstract

9 A wide range of parameters is required in input when applying hygro-thermo-chemical-10 mechanical models to concrete components with the aim of determining the variations over time 11 of temperature, relative humidity and shrinkage induced deformations. While a sub-set of these 12 material parameters can be evaluated on the basis of the concrete mix specifications or from literature data, this paper presents a robust inverse analysis procedure for the identification of 13 14 the remaining sub-set of parameters that are characterised by a large variability and, in some 15 cases, do not have a precise physical meaning and are not amenable to a direct measurement. 16 The particularity of this paper is to propose different strategies for the characterisation of these 17 material parameters that account for the presence of different exposure conditions, as these affect 18 the outcomes and requirements of the parameter identification procedure. After introducing the 19 adopted hygro-thermo-chemical-mechanical model, representative results of an extensive 20 sensitivity analysis are presented in the first part of the paper to give insight into most effective 21 number, location and duration of measurements to be used in input of the inverse analysis. The 22 inverse analysis procedure is then presented and applied to a number of selected scenarios to 23 highlight its robustness considering different boundary conditions in terms of external 24 temperature and relative humidity surrounding the concrete. The ability to characterise these 25 parameters will support a wider use of these hygro-thermo-chemical-mechanical models, especially for those applications in which humidity and temperature profiles significantly 26 27 influence the structural response, for example when predicting curling in industrial pavements 28 and non-uniform shrinkage profiles in composite steel-concrete slabs.

29 Keywords

30 Concrete; inverse analysis; long-term behaviour; moisture diffusion; sensitivity analysis;
31 shrinkage.

32 **1. Introduction**

33 Concrete structures are significantly influenced by the time-dependent behaviour of the concrete 34 that affects their serviceability and durability. An inaccurate evaluation of this service response 35 can lead to undesired excessive deformations and occurrence of cracking. Concrete time effects 36 are significantly dependent on the moisture transport and heat transfer mechanisms that take 37 place in the concrete and that control, for example, the hardening process, water release, cement 38 hydration, and volume changes. Different numerical and experimental studies are available in 39 the literature that deal with the concrete behaviour, especially considering its early age. Bažant 40 and Najjar [1] presented a material model capable of describing the nonlinear moisture transport 41 that takes place in concrete. Several researchers extended this approach in following years, for 42 example, by incorporating a thermodynamics based approach for the cement hydration [2] or by 43 establishing a thermo-chemo-mechanical model to account for the aging effect on strength 44 development and the micro-scale description of the material [3-5]. Other recent contributions 45 considered the influence of cracking on the permeability [6] or included a sink term into the 46 diffusive moisture equation to capture the internal water consumption occurring during cement 47 hydration [7,8]. The use of an enhanced cement hydration model was presented in [9] while the 48 influence of the meso-structure was investigated in [10-12]. A hygro-thermo-chemical model 49 that accounted for the effect of cement hydration on both moisture and temperature calculations was considered in [13,14]. The mechanical coupling is usually based on a linear relationship 50 51 between the variations over time of the relative humidity and the consequent free shrinkage 52 deformations (see, e.g. [13,14,15,16]).

The use of these models is particularly relevant in applications where the effect of shrinkage induced deformations are important, such as curling in industrial pavements [17,18] and shrinkage gradients in composite floor systems [19-22] (where the presence of different exposure conditions, due to the presence of subgrade/waterproofing membrane and profiled steel sheeting, respectively, influence the mechanical response). In the latter case, the occurrence of the non58 uniform shrinkage profiles has been only recently identified [19] and the ability to couple the hygro-thermo-chemical behaviour to its mechanical response will enable more accurate 59 structural predictions associated to the serviceability limit state requirements of building floors. 60 61 For these applications, the wider use of hygro-thermo-chemical-mechanical models for service 62 design and modelling needs to be supported by techniques capable of adequately identifying the 63 required material parameters, especially in applications where they can give useful insight into 64 the structural problem. Not all material parameters to be specified in input in these hygro-thermo-65 chemical-mechanical models can be easily determined and, to better highlight this aspect, the 66 model material parameters are subdivided into the following two sets: (i) one set of parameters 67 that can be evaluated based on the concrete mix specifications or from data reported in the 68 literature; and (ii) a second set of parameters characterised by a large variability (based on data 69 available in the literature) and, among these, many parameters do not possess a precise physical 70 meaning and, for this reason, are not amenable to a direct measurement.

In this context, the main contribution of this paper relies on the development of a robust inverse analysis procedure for the identification of the second set of material parameters (i.e. listed at point (ii) above) that are required in input for the use of the hygro-thermo-chemical-mechanical models. This paper contributes to this effort by proposing different strategies for the characterisation of the material parameters considering different exposure conditions.

76 In this work, the robustness of the proposed inverse analysis procedure is determined based on 77 the use of pseudo-experimental results as input data (e.g. [23-25]) that includes measurements 78 of temperature, relative humidity and total deformations. This data has been generated 79 considering the same exposure conditions of commonly available reinforced or prestressed 80 concrete slabs, i.e. exposed on both its surfaces, and of slabs exposed only from one side because 81 sealed on its opposite side (e.g. composite slabs and industrial pavements). The proposed 82 methodology is developed with the idea of minimising the number and the duration of the 83 measurements to be carried out and of investigating how these are influenced by different

84 exposure conditions. After introducing the key features of the hygro-thermo-chemicalmechanical model considered in this study, the main outcomes and representative results 85 86 obtained from an extensive sensitivity analysis are presented because providing insight into the 87 most effective number, location and duration of the measurements to be used as input of the inverse analysis procedure. The basis of the inverse analysis procedure is then presented and its 88 89 robustness is tested against selected scenarios constructed using pseudo-experimental data subjected to different degrees of noise and for different external temperatures and relative 90 humidities surrounding the concrete. Representative results are reported in the paper to give 91 insight into the use and effectiveness of the proposed methodology. These results are also 92 93 expected to support the effective planning of the instrumentation setup to be used in experimental tests on service conditions performed in controlled laboratory environments and for the 94 95 arrangement of in-situ monitoring and investigations, for example during construction or during day-to-day service operations, associated to applications whose service response is influenced 96 97 by shrinkage.

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2. Hygro-thermo-chemical-mechanical model

99 The hygro-thermo-chemical-mechanical model considered in this paper is able to predict the 100 variations of the relative humidity *h*, temperature *T* and deformation ε that take place over time 101 within the spatial domain Ω of a concrete component taking into account its environmental 102 conditions. The model here presented has been proposed in [13] and applied to a concrete mix 103 without the presence of silica fume. The main features of the model and its numerical 104 implementation are described in the following.

105 The principal chemical reaction occurring during hardening of a concrete mix is cement 106 hydration, whose extent is here expressed through a scalar variable α_c , computed as the ratio 107 between the actual level of hydration X_c and its theoretical asymptotic value $X_c^{\infty,th}$ achievable 108 under ideal hygro-thermal conditions. The maximum level of the reaction degree 109 $\alpha_c^{\infty} = X_c^{\infty}/X_c^{\infty,th}$ is usually smaller than one, i.e. $\alpha_c^{\infty} < 1$. According to [26], we may assume 110 $\alpha_c^{\infty} = (1.032 \, w/c)/(0.194 + w/c)$, in which w/c depicts the water-to-cement ratio. The variation 111 over time \mathcal{R}_c increases with relative humidity content and reduces while approaching its 112 asymptotic value α_c^{∞} as expressed by the following Arrhenius type equation:

$$\boldsymbol{a}_{c}^{\boldsymbol{k}} = \frac{A_{c1} \left(A_{c2} / \alpha_{c}^{\infty} + \alpha_{c} \right) \left(\alpha_{c}^{\infty} - \alpha_{c} \right) e^{\left(-\eta_{c} \alpha_{c} / \alpha_{c}^{\infty} \right)}}{\left[1 + \left(a - ah \right)^{b} \right]} \cdot e^{\left(-\gamma_{c} / T \right)}$$
(1)

113 where $\gamma_c = E_{ac}/R$, E_{ac} is the hydration activation energy and *R* represents the universal gas 114 constant. Parameters A_{c1} , A_{c2} and η_c have no precise physical meaning and govern the so-called 115 normalized chemical affinity. The function $b_h(h) = \left[1 + (a - ah)^b\right]^{-1}$ takes into account the 116 slowing of the hydration process when relative humidity decreases below a certain value (around 117 80%). Parameters *a* and *b* are usually taken equal to 7.5 and 4.0, respectively, (see [1]).

118 The total water content *w*, present in the concrete mix, is expressed as the sum of the evaporable 119 water w_e and the non-evaporable water w_n , the latter being the water chemically bonded by 120 cement hydration and expressed as $w_n(\alpha_c) = k_c \alpha_c c$, with *c* being the cement ratio content and 121 k_c a material parameter that, according to [13] and references herein, can be assumed equal to 122 0.253. The evaporable water is expressed as a function of the relative humidity (sorption 123 isotherm curve) and of the degree of cement hydration α_c as follows:

$$w_e(h,\alpha_c) = \kappa_{vg}^c \alpha_c c \left(1 - 1/\overline{e_2}\right) + \left[w_0 - 0.188\alpha_c c - \kappa_{vg}^c \alpha_c c \left(1 - 1/\overline{e_1}\right)\right] \cdot \frac{\overline{e_2} - 1}{\overline{e_1} - 1}$$
(2)

124 in which $w_0 (= (w/c)c)$ is the initial water content and it is assumed that $\overline{e}_2 = e^{10(g_1\alpha_c^{\infty} - \alpha_c)h}$

125 and $\overline{e}_1 = e^{10(g_1 \alpha_c^{\infty} - \alpha_c)}$. Equation (2) also depends on material parameters κ_{vg}^c and g_1 that 126 govern the amount of water contained in the cement gel pores and the shape of the sorption curve, 127 respectively.

Starting from the consideration that $w = w_e(h, \alpha_c) + w_n(\alpha_c)$, the variation of the humidity field over time and space is described by the combination of the Fick's law, expressing the flux of water mass **j** as proportional to the gradient of the relative humidity *h* (i.e. $\mathbf{j} = -D_h \nabla h$) and the water mass balance equation, e.g. [1,13]:

$$\frac{\partial w_e}{\partial h} \frac{\partial h}{\partial t} = \nabla \cdot \left[D_h \nabla h \right] - \left(\frac{\partial w_e}{\partial \alpha_c} + \frac{\partial w_n}{\partial \alpha_c} \right) \partial_c \delta_c \qquad \text{in } \Omega$$
(3)

132 In the above equation, the moisture permeability D_h depends on the relative humidity *h* and 133 temperature *T* as per the following expression [13,27]:

$$D_{h}(h,T) = \frac{D_{1}}{\left[1 + (D_{1}/D_{0} - 1)(1 - h)^{n}\right]} \cdot e^{\left(E_{ad}/RT_{0} - E_{ad}/RT\right)}$$
(4)

134 in which T_0 is the reference room temperature (assumed equal to 296°*K*), $E_{ad}/R = 4700K$ (see 135 e.g. [1]), and parameters D_0 , D_1 and *n* depend on the specific concrete mix.

136 The temperature field is described by the combination of the Fourier's law, expressing the heat 137 flux **q** as a function of the temperature spatial gradient ($\mathbf{q} = \lambda \nabla T$), and the enthalpy balance 138 equation as follows:

$$\rho c_t \frac{\partial T}{\partial t} = \nabla \cdot \left[\lambda \nabla T \right] + \mathcal{Q}_c \qquad \text{in } \Omega \tag{5}$$

139 where *T* is the absolute temperature, λ is the heat conductivity assumed constant in the present 140 study, ρ and c_t depict the concrete mass density and the specific heat, respectively, and \mathcal{G}_c 141 represents the rate of heat generated by cement hydration, calculated as $\mathcal{G}_c = \mathcal{G}_c \mathcal{O}_c^{\prime \prime}$, with $\mathcal{O}_c^{\prime \prime}$ 142 being the total heat content per unit cement mass.

Equations (3) and (5) are coupled by their dependency on the degree of cement hydration α_c as well as by the moisture diffusion coefficient D_h that depends on both temperature and relative humidity.

146 The relative humidity obtained with the hygro-thermo-chemical model is then associated to a147 free shrinkage hydrostatic strain tensor by means of the following expression:

$$\mathbf{\mathcal{S}}_{sh} = k_{sh} \mathbf{\mathcal{P}}$$
(6)

which defines a linear relationship between the rate of change over time of the free shrinkage 148 deformation \mathcal{B}_{sh} and the corresponding rate of change of the relative humidity \mathcal{B} by means of 149 the coefficient k_{sh} . The value for k_{sh} is usually considered to remain constant for practical 150 applications (e.g. [6,15,28,29]) even if, in reality, it has been shown that its value varies with the 151 152 relative humidity, e.g. [16,30]. Values reported in literature for k_{sh} exhibit a large scatter, ranging between 5×10^{-4} and 3.5×10^{-3} (e.g. [29,31]) and, because of this, the value for k_{sh} needs 153 154 to be calibrated for different concrete mixes. By performing a time integration of Equation (6), 155 the free shrinkage deformation can be expressed as:

$$\varepsilon_{sh}(t) = k_{sh}(h(t) - h(0)) \tag{7}$$

The hygro-thermo-chemical-mechanical relationships introduced in Equations (1-7) depend on many parameters. Some of them, listed in the upper part of Table 1, can be evaluated based on the concrete mix specifications or from well-known data reported in the literature. Other parameters are affected by a large variability and, among these, some do not possess a precise

- physical meaning. This set of parameters is reported in the lower part of Table 1 and their rangeof variation (obtained and derived from [13,14,31,32]) is collected in Table 2.
- 162 The numerical solution of the proposed hygro-thermo-chemical model is achieved with the finite163 element method by solving the following discretized equations:

$$\begin{cases} \mathbf{W}\mathbf{P} + \mathbf{D}\mathbf{H} = \mathbf{F} \\ \mathbf{C}\mathbf{P} + \mathbf{A}\mathbf{T} = \mathbf{Q} \end{cases}$$
(8)

164 where **H** and **T** depict unknown vectors that collect all nodal values (of the finite element 165 discretization) of the relative humidity and temperature fields at each instant, while the system 166 matrices are defined in Appendix A. The Dirichlet's boundary conditions (on *h* and *T*) are 167 directly enforced on the vectors **H** and **T**, while Cauchy's boundary conditions enter into the 168 right end side of the equation, see [33]. The system described in Equation (8) is solved by 169 applying an explicit algorithm based on the θ -method [33,34].

The mechanical analysis of the problem is then carried out using standard structural analysis procedures. In particular, for the purpose of the simulations presented in this paper a timedependent cross-sectional analysis is performed to account for the shrinkage effects evaluated with Equation (7) based on method of analysis widely accepted in the literature, e.g. [35].

The use of the proposed numerical model is illustrated in the following considering an unreinforced and unloaded concrete component with the following boundary conditions: (i) heat exchange can take place from its opposite surfaces; and (ii) two different sets of boundary conditions are considered for the relative humidity, i.e. one with both concrete surfaces exposed for drying (Figure 1a) and a second with only one surface exposed to dry and opposite surface sealed (Figure 1b). For ease of reference, these boundary conditions have been referred to as EE and ES, respectively, in Figure 1.

181 Representative results related to the humidity profiles are provided in Figures 2 and 3 at different 182 time increments for a period of 10 years and considering two concrete thicknesses, namely 183 100 mm and 250 mm. The adopted concrete mix is typical of a normal-strength concrete and its 184 specifications are presented in Table 3. The simulations have been performed considering two 185 boundary conditions, i.e. exposed-exposed (Figure 1a) in Figures 2a and 3a as well as exposed-186 sealed (Figure 1b) in Figures 2b and 3b, and the model parameters are based on the mean values 187 of the ranges included in Table 2 and on the values specified in Table 3. Results presented in 188 Figures 2 and 3 have been calculated assuming a wet curing period of 10 days.

189 The results of Figures 2 and 3 highlight the ability of this model to simulate the highly nonlinear 190 humidity profiles that can develop through the concrete thickness and how these can be 191 influenced by the drying mechanism activated by the different external environmental 192 conditions. In particular, the nonlinear variations of relative humidity illustrated in Figure 2 show 193 that, when exposed to a dry environment (i.e. environmental relative humidity of 40%), the thin 194 concrete component cannot approach an equilibrium condition through its entire thickness with 195 the ambient conditions even after nearly 10 years from casting. In the case of the concrete 196 component subjected to exposed-sealed environmental conditions, non-symmetric humidity 197 distributions develop due to the inability of the concrete to dry from its sealed surface as shown 198 in Figures 2b and 3b. For a thicker concrete component the moisture transport process is slower 199 and requires more time than a thinner one in achieving a stationary solution. For example, after 200 ten years of simulation the variation of relative humidity measured at mid height is smaller 201 (Figure 3) than that occurring in the thinner specimen (Figure 2).

The corresponding free shrinkage profiles are determined by inserting the relative humidity distributions of Figures 2 and 3 into Equation (7) as shown in Figures 4 and 5 for thicknesses of 100 mm and 250 mm, respectively. The consequent total deformations are then evaluated from a time-dependent cross-sectional analysis based on the calculated free shrinkage profiles (dot lines in Figures 4 and 5), widely used in the literature for the evaluation of the service response of concrete structures (e.g. [35]) and their variations (i.e. of calculated total deformations) are 208 also plotted in Figures 4 and 5 at different instants in time (see continuous lines). From a 209 qualitative viewpoint, the total deformations induced in an exposed-exposed unreinforced 210 concrete component by the nonlinear shrinkage are constant through its thickness and well reflect 211 the simplifying assumption adopted in international concrete codes (e.g. [36,37]) that specify the 212 use of a constant shrinkage distribution for design purposes. In the case of an exposed-sealed 213 concrete component, the total deformations produced by the calculated humidity profile lead to 214 the development of a non-uniform shrinkage distribution. This behaviour is typical of industrial 215 pavements that can dry predominantly from their exposed upper surface (see e.g. [17,18]) and, 216 as recently reported in the literature, of composite floor systems in which concrete slabs are cast 217 on profiled steel sheeting and can only dry from the exposed surface (see e.g. [19,20,21,22]). As 218 expected, free shrinkage and total deformations are larger when considering thinner components, 219 as noted comparing Figures 4 and 5.

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3. Sensitivity analysis

The sensitivity analysis is intended to compute the influence of each sought parameter on the measurable quantities and to support the design of the experiments for inverse analysis purposes. In particular, the sensitivity analysis is applied to gain a better understanding on how the sought material parameters, i.e. those listed in the lower part of Table 1, influence the variations of the total deformations over time in order to assist the selection of the most effective time duration and spatial positions to be considered for the proposed inverse analysis (see e.g., [25], [38]).

A preliminary sensitivity study was carried out considering the hygro-thermo-chemical model applied to an exposed-exposed concrete component that highlighted the presence of two regions where the humidity measurements presented the highest sensitivities, i.e. at the concrete midheight and a position close to the concrete surface (i.e. at about 10 mm from the external surface), for the first few months from casting, while the highest sensitivity for the temperature distributions are noted at the mid-height of the concrete component in the first 6 hours fromcasting.

The sensitivity index is computed as partial derivative of the measured quantities, e.g. total deformation ε , with respect to the model parameters p_i at a certain time instant *t* and in a certain position *z* along the thickness of the concrete component as follows:

$$S_{\varepsilon,p_i}(z,t,\mathbf{p}) = \frac{\partial \varepsilon(\mathbf{p},z,t)}{\partial p_i} \frac{p_i}{\varepsilon(\mathbf{p},z,t)}$$
(9)

This index is normalised, for comparison purposes, with respect to both the parameter and the measured quantity value. In the numerical computations, the derivatives have been approximated by forward finite-differences with 0.1% increment, and have been evaluated at the top and bottom surfaces of the concrete component and for a certain number of time instants.

Figure 6 shows the sensitivity index, continuously varying in time and space, computed according to Equation (9), of the deformation profiles measured at the top and bottom surfaces of both exposed-exposed and exposed-sealed concrete components. In particular, the sensitivity index computed for the exposed-sealed (ES) concrete component appear to be generally higher than those determined for the exposed-exposed (EE) case. Under the ES boundary condition, the deformations measured at the sealed (bottom) surface generally show a higher sensitivity to the model parameters than that of the deformation measured at the exposed (top) surface.

All parameters governing cement hydration, namely A_{c2} , η_c and γ_c , reach their highest sensitivity on the measured deformation profiles after a few days from casting, when this chemical reaction is more active, and the maximum value among these occurs for parameter γ_c related to the hydration activation energy while sensitivity with respect to A_{c2} is almost negligible. It is also interesting to observe that the sensitivity of the deformation profile, measured at the sealed surface, with respect to the model parameters other than those governing cement hydration, reaches always its highest value in the first few months after casting, therefore highlighting how, during this period, the experimental information collected are mostly boundto enhance the identifiability of the sought parameters.

Among the parameters governing moisture permeability, the one which most affects the deformation profiles is the exponent *n*, characterized by a sensitivity index greater than the ones computed for parameters D_0 and D_1 . Sensitivity with respect to \mathcal{D}_c^{*} is almost negligible since this parameter is expected to influence primarily the variation of the temperature field.

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Figure 7 illustrates some representative sensitivity results obtained with respect to selected model parameters over a period of one year for concrete thicknesses of 100 mm and 250 mm. In particular, the thinner component exhibits an extremely high sensitivity for the deformation measured at its sealed (bottom) surface for about 30 days from casting, and the differences in sensitivity exhibited between the strains measured at the sealed (bottom) and exposed (top) sides of the thinner component are more pronounced than those calculated for the thicker component.

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4. Inverse analysis

The inverse problem is usually formulated as the minimization of the discrepancy between the experimental results and same quantities numerically computed as a function of the sought parameters.

The identifiability of the parameters contained in the hygro-thermo-chemical-mechanical model presented in Section 2 has been investigated following a numerical procedure already adopted in other studies (see e.g. [39,40,41]), which consists of the implementation of different inverse analysis exercises starting from the so-called pseudo-experimental results, i.e. results numerically generated from a given set of model parameters, supplied in input to the inverse problem, which, if well-posed, should provide in output the values of the parameters adopted to generate the pseudo-experimental data.

The input data consist of humidity and temperature profiles taken at different locations throughthe concrete thickness and at different time instants as well as the total deformations measured

281 at both sides of the concrete component after completion of the curing period. In particular, the relative humidity $h_{e,ts}$ is measured through the concrete component thickness in a discretised 282 number of locations s = 1K N_{hz} and for a certain number of time instants $\tau = 1$ K N_{ht} . Similarly, 283 at each instant $\tau = 1 \text{K} N_{T_t}$, the temperature distribution T_{e,τ_s} is measured through the thickness 284 of the component in a discretised number of points $s = 1 \text{K} N_{T_z}$; and at each instant $\tau = 1 \text{K} N_{\varepsilon t}$, 285 total deformation $\varepsilon_{e,ts}$ is measured at the two sides (i.e. top and bottom) of the concrete 286 287 component. The choice of the discretization points adopted for both the space and time domains 288 is based on the outcomes of the sensitivity analysis.

In the present study all experimental information are processed together and uncertainties of both experimental measurements and system modelling are not considered within a stochastic framework, but the effect of random noise, applied to the inverse problem input data, is accounted for to investigate the robustness of the proposed identification procedure.

Collecting the model parameters to be estimated (i.e. those listed in the lower part of Table 1) in vector p, and denoting experimental and computed quantities by subscripts "e" and "c", respectively, the discrepancy norm between measured and computed quantities can be expressed as follows:

$$w(\mathbf{p}) = \phi_h \sum_{\tau}^{N_{h\tau}} \sum_{s}^{N_{h\tau}} \left[\frac{\left(h_{n,\tau s} - h_{e,\tau s}\right)^2}{h_{e,\tau s}^2} \right] + \phi_T \sum_{\tau}^{N_{T\tau}} \sum_{s}^{N_{T\tau}} \left[\frac{\left(T_{n,\tau s} - T_{e,\tau s}\right)^2}{T_{e,\tau s}^2} \right] + \phi_\varepsilon \sum_{\tau}^{N_{e\tau}} \sum_{s}^2 \left[\frac{\left(\varepsilon_{n,\tau s} - \varepsilon_{e,\tau s}\right)^2}{\varepsilon_{e,\tau s}^2} \right]$$
(10)

297 where $\phi_h = 1/(N_{ht}N_{hz})$, $\phi_T = 1/(N_{Tt}N_{Tz})$ and $\phi_{\varepsilon} = 1/(2N_{\varepsilon t})$ are weight factors defined in order 298 to ensure an equivalent contribution of the three terms defining the objective function.

The minimization of the objective function in Equation (10) is performed by the Trust Region (TR) algorithm (see, e.g. [42,43]). Starting from an assigned initialization vector, this is automatically updated by means of an iterative procedure based on the minimization of a quadratic approximation of the objective $w(\mathbf{p})$ within a "trust" region, whose dimensions are 303 updated step by step based on the results of the previous iteration. The process is stopped by the 304 fulfilment of a priori tolerances on either the variation of the objective function or the Euclidean 305 norm of the normalized optimization variables.

For each adopted set \mathbf{p}^{ad} of the parameters model, pseudo-experimental data are generated and 306 perturbated by different noise extractions $(n = 1...N_{NOISE})$, generated with uniform probability 307 density over an interval centred on the exact value. For each noise extraction, the inverse problem 308 is solved several times $(i = 1...N_{INIT})$ starting from different initialization vectors, to check the 309 occurrence of local minima that might exist in view of the nonlinear and non-convex nature of 310 the objective function. For a given noise extraction the identified value \mathbf{p}_n^{id} is computed as 311 average of all values \mathbf{p}_{ni}^{id} identified in relation to the different initializations, weighted with 312 313 respect to the inverse of the objective function in solution, as:

$$\mathbf{p}_{n}^{id} = \sum_{i}^{N_{INT}} \mathbf{p}_{ni}^{id} \chi_{i} / \sum_{i}^{N_{INT}} \chi_{i}, \quad \chi_{i} = 1 / w \left(\mathbf{p}_{ni}^{id} \right)$$
(11)

314 The identification error for each model parameter *k* is then computed as:

$$err_{n,k}^{id} = 100 \cdot \left| \frac{p_{n,k}^{id} - p_k^{ad}}{p_k^{ad}} \right|$$
 (12)

A final measure of the identifiability error of each sought parameter is defined in terms of averageof all the single errors, computed for each noise extraction:

$$err_{k}^{id} = \frac{1}{N_{NOISE}} \sum_{n}^{N_{NOISE}} err_{n,k}^{id}$$
(13)

with $err_{n,k}^{id}$ being defined as absolute value, see equation (12), to avoid compensations between errors of opposite signs when a large number of random noise extractions is adopted.

319 **4.1 Results**

Different inverse analysis exercises have been solved in the following to investigate the optimal
 formulation of the inverse problem for the full identification of the parameters listed in the lower

322 part of Table 1, i.e. those characterised by a large variability or not amenable to direct 323 measurement for the lack of a precise physical meaning. As input data to the inverse problem, 324 humidity, temperature and deformation profiles' measurements have been considered. In the 325 following, only representative results are presented to outline and support the key findings of 326 this work.

The concrete properties included in the simulations correspond to the mean values reported in Table 2 and those specified in Table 3. The external temperature has been assumed constant and equal to 20°C. In all simulations, a random noise of 10% has been applied to the numerically generated pseudo-experimental data used in input.

331 The first inverse analysis simulations highlighted how the inverse problem is not well posed for the concurrent identification of parameters A_{c1} and γ_c . This lack of identifiability is attributed 332 333 to the form in which these parameters appear in Equation (1) for the evaluation of the rate of 334 cement hydration reaction &. In this equation, both parameters have an equivalent effect on \mathcal{A}_{c} , i.e. an increase in A_{c1} leads to an increase of \mathcal{A}_{c} that could be similarly produced by a 335 decrease of γ_c . Because of this, the inverse analysis procedure cannot distinguish between these 336 two parameters and, in view of a much higher sensitivity of γ_c , the following inverse analysis 337 exercises will be carried out assuming A_{c1} known a priori while still identifying γ_c . The validity 338 339 of this assumption is later confirmed by the results outlining how the adoption of different a priori values for A_{c1} does not jeopardize the identifiability of the sought parameters. 340

Table 4 reports the results obtained considering a 100 mm thick concrete component wet cured for 1 day from casting, exposed to an ambient relative humidity equal to 40% and assuming different boundary conditions. The number of discrete humidity measurements through the thickness of the concrete component have been varied and the inclusion of a temperature measurement has been considered. The measurements are performed for a period of 30 days (with a frequency of one measurement per hour). Columns A, B, C and D in Table 4 provide the 347 results obtained under exposed-exposed (denoted as EE) conditions (Figure 1a) and highlight the 348 need to use two relative humidity measurements (column D) to ensure the identifiability of all 349 parameters (with identified errors' magnitude within the noise level introduced in the pseudo-350 experimental data). By using one relative humidity measurement, for example located at 50 mm 351 (Column B) or 10 mm (Column C) from the external concrete surface, or without monitoring 352 relative humidity (Column A), the information provided as input of the inverse problem is not 353 sufficient for the identification of all sought parameters, because the estimation of D_0 or D_1 354 produces an error (at its maximum of 36.5%) that is larger than the magnitude of the added noise. 355 For an exposed-sealed (referred to as ES) concrete component, column E shows that the 356 experimental information consisting of one temperature and both surface deformation measurements are sufficient to guarantee the identifiability of all parameters. The inclusion of 357 358 one relative humidity measurement for the ES conditions, for example located at the component 359 mid-height, does not improve significantly the results as depicted by the values reported in 360 column F of Table 4. Columns G and H highlight that, without the inclusion of a temperature measurement, the identification procedure does not lead to a successful characterisation of $\partial_{\alpha}^{\prime}$ 361 and A_{c2} when considering both EE and ES exposure conditions. These observations highlight 362 363 how the use of a temperature measurement as experimental information is crucial for the 364 identification of the model parameters governing cement hydration that cannot be identified if 365 information on deformation or relative humidity only are considered.

The results discussed above have been obtained for a relatively thin concrete component with a thickness of 100 mm. In the case of a 250 mm thick component, representative errors are presented in Table 5. In this case, a longer period of measurements, of at least 60 days, is needed for the exposed-exposed case (as depicted in Columns B and C) to collect the amount of experimental information needed for the calibration of the model parameters, especially of those governing the moisture permeability. Shorter monitored periods (reported in column A for 372 30 days) do not provide sufficient experimental information for the identification. For an exposed-sealed concrete component, differently from the 100 mm thickness, temperature and 373 374 deformation profiles are not sufficient for the present identification purposes (see columns D and 375 E), and one humidity measurement taken at mid-height is necessary to make the inverse problem 376 well posed (see columns F and G). This is here attributed to the fact that, as shown in Figure 7, 377 the sensitivity of the deformation measurements at the sealed concrete surface of a thicker 378 component is much lower than the corresponding value obtained for a thinner component. As a 379 consequence, the experimental information obtained from a thicker component is not sufficient 380 for the definition of a well-posed inverse problem without the use of humidity measurements. 381 This consideration is confirmed by the results reported in Table 6, where it is shown that for an 382 increasing concrete component thickness (varying from 100 mm to 400 mm in columns A to D), the parameter $\kappa_{v_{e}}^{c}$ is identified with an increasing error. For the thicknesses considered in 383 384 columns B-D, it is necessary to include at least one relative humidity measurement, for example 385 placed at the concrete mid-height, to ensure the identifiability of all model parameters as depicted in columns F-H. 386

At the beginning of this section, it has been discussed that the parameters A_{c1} and γ_c could not 387 388 be uniquely identified. For this reason, the inverse methodology followed in this study consisted in assigning an a priori value to A_{c1} equal to its mean value reported in the literature (=29450 s⁻¹ 389 390 based on the range provided in Table 2), i.e. the same value adopted in generating the pseudo-391 experimental data. Table 7 reports the results of some inverse analysis exercises when an 392 incorrect value for A_{c1} (i.e. different from the one used for the generation of the pseudo-393 experimental data) is specified in input of the inverse analysis. In particular, the upper and lower limits of A_{c1} (as specified in Table 2) are used for the results reported in columns B and C 394 considering the EE conditions and in columns E and F for the ES conditions, while columns A 395 396 and D depict the errors determined using the exact value for A_{c1} (i.e. the value adopted to 397 generate pseudo-experimental data). These results confirm that the identifiability of all 398 parameters is not affected by an incorrect assumption of A_{c1} , except for the "companion" 399 parameter γ_c , whose identification error increases, especially when the lower limit is assumed 400 (however always within the order of magnitude of the added noise for the cases considered).

401 The inverse analysis cases proposed for the exposed-exposed and exposed-sealed conditions are 402 revisited in the following assuming sinusoidal time-varying boundary conditions expressed in 403 terms of external temperature and relative humidity applied to the concrete surfaces. Only 404 selected case studies (taken from Tables 4 and 5) are considered in the following with the 405 sinusoidal boundary conditions. In particular, columns A and C in Table 8 correspond to columns 406 E and D in Table 4, respectively; while columns D and E correspond to columns B and F in 407 Table 5, respectively. Based on these results, the optimal (in terms of minimum measurements 408 to be taken) experimental setups studied for the 250 mm thick concrete component under external 409 constant boundary conditions (Table 5) are still effective for the identification of the sought 410 material parameters in the case of sinusoidally-varying boundary conditions, see columns D and 411 E in Table 8. For the thinner specimen, some problems arise (with the varying boundary 412 conditions) in relation to the identification of the parameter Ac2. In particular, column A in Table 413 8 shows that for the case of the exposed-sealed specimen the error increases (when compared to 414 the case with constant boundary conditions) but it remains of the same order and magnitude of 415 the added noise. It has been observed that this error can be further reduced by adding a 416 temperature measurement close to the external surface (see column B in Table 8). The 417 combination of the small thickness and of the exposed-exposed boundary conditions maximizes 418 the influence of the time-varying boundary conditions on the measurements taken inside the 419 specimen and induces the largest identification error of the parameter A_{c2}, as reported in column 420 C (Table 8), however, without jeopardizing the identification of the other parameters.

421 **5.** Conclusions

422 This paper has focussed on the identifiability of the parameters required for a hygro-thermo-423 chemical-mechanical model that predicts variations of temperature, relative humidity and 424 shrinkage induced deformations in concrete components. In particular, the model parameters 425 have been subdivided into two main sets: (i) one set of parameters that can be evaluated on the 426 basis of the concrete mix specifications or from literature data; and (ii) a second set of parameters 427 that are characterised by a large variability and, in some cases, without a precise physical 428 meaning, are not amenable to a direct measurement. This paper has proposed an inverse analysis 429 procedure for the identification of the model parameters contained in this second set by 430 considering different concrete exposure conditions and by using following variables as input 431 data: total deformations at the concrete surfaces, temperature and relative humidity profiles in 432 some positions inside the concrete component. These results may find applications in enhancing 433 the design of in-situ investigations and of experimental tests, and in minimising the necessary 434 collected experimental information (in terms of monitored period and number of discrete 435 temperature and relative humidity measurements). The outcomes of the different inverse 436 analyses' exercises have been considered successful when all parameters have been identified 437 with an error smaller than the noise added to the pseudo-experimental data in input to the inverse 438 problem. The boundary conditions included in this study are described as follows: (i) heat 439 transfer has been assumed to take place through both concrete surfaces; and (ii) two exposure 440 conditions have been considered for the relative humidity, i.e. one assuming both concrete 441 surfaces to be exposed for drying (referred to as EE) and one where only one surface has been 442 exposed with the remaining one being sealed (denoted as ES). The identification process has 443 been applied considering different environments of external temperature and relative humidity 444 surrounding the concrete.

445 Based on the results and case studies considered in this paper, it is possible to draw the 446 conclusions listed below.

For concrete components, subjected to constant boundary conditions (i.e. constant
 external temperature and relative humidity) and exposed on both sides (EE conditions),
 the minimum measurements required for the identification of all model parameters
 consist of relative humidities taken at two locations within the concrete thickness (e.g.
 one at the mid-height and one close to the surface), one temperature reading at mid-height
 and total deformation at the concrete surface.

Concrete components, exposed to constant environmental conditions, sealed on one side
 and allowed to dry on the opposite one (ES conditions) require varying strategies
 depending on their thickness. For thinner components (here taken as 100 mm thick), all
 model parameters are identifiable by monitoring the total deformations at both the
 concrete surfaces and temperature at mid-height. For larger components, additional
 measurements related to relative humidity need to be included in the input data of the
 inverse analysis procedure.

460 For concrete components exposed to sinusoidally-varying environmental conditions (i.e. 461 varying external temperature and relative humidity), the inverse analysis requires the use 462 of the measured external temperature and relative humidity variations as input data of the 463 direct operator. It has been observed that for relatively large concrete thicknesses (here 464 taken as 250 mm), the same minimum experimental information required for a concrete 465 specimen exposed to constant boundary conditions is sufficient for the identification of 466 the sought material parameters, while for thinner concrete components (here taken as 467 100 mm) the use of the same approach leads to larger error for only one parameter 468 (associated with the variation of the degree of cement hydration over time) without ieopardizing the identification of the remaining parameters. 469

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473 Appendix A

474 Matrices and vectors of the system in equation (8) are defined as follows:

$$\mathbf{W} = \bigcup_{e} \prod_{\Omega_e} \mathbf{N}_e^T \frac{\partial w_e}{\partial h} \mathbf{N}_e \mathrm{d}\Omega$$
(A1)

$$\mathbf{D} = \bigcup_{e} \iint_{\Omega_{e}} \mathbf{B}_{e}^{T} D_{h} \mathbf{B}_{e} \mathrm{d}\Omega$$
(A2)

$$\mathbf{F} = -\bigcup_{e} \iint_{\Gamma_{e}} \mathbf{N}_{e}^{T} \mathbf{n}^{T} \mathbf{j} d\Gamma - \bigcup_{e} \iint_{\Omega_{e}} \mathbf{N}_{e}^{T} \left(\frac{\partial w_{e}}{\partial \alpha_{c}} + \frac{\partial w_{n}}{\partial \alpha_{c}} \right) \partial_{\mathbf{k}}^{\mathbf{k}} d\Omega$$
(A3)

$$\mathbf{C} = \bigcup_{e} \iint_{\Omega_{e}} \mathbf{N}_{e}^{T} \rho c_{t} \mathbf{N}_{e} \mathrm{d}\Omega$$
(A4)

$$\mathbf{\Lambda} = \bigcup_{e} \int_{\Omega_{e}} \mathbf{B}_{e}^{T} \lambda \mathbf{B}_{e} \mathrm{d}\Omega$$
(A5)

$$\mathbf{Q} = -\bigcup_{e} \iint_{\Gamma_{e}} \mathbf{N}_{e}^{T} \mathbf{n}^{T} \mathbf{q} \, \mathrm{d}\Gamma + \bigcup_{e} \iint_{\Omega_{e}} \mathbf{N}_{e}^{T} \mathcal{O}_{c}^{*} \mathrm{d}\Omega$$
(A6)

475 where symbol \bigcup_{e} refers to the assembly operation typical of the finite element approach, and 476 matrices \mathbf{N}_{e} and \mathbf{B}_{e} collect shape functions and their spatial derivatives, respectively.

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Table 1. Material parameters required in input	
of the hygro-thermo-chemical-mechanical model	١.

	Parameter	Description				
	c cement content					
	w/c	water-to-cement ratio				
Parameters calculated based on concrete mix	a,b	parameters associated with the variation of the degree of cement hydration over time and taken as $a = 7.5$ and $b = 4.0$ [1]				
specifications or assigned	λ	heat conductivity				
known values well	ρ	concrete mass density				
accepted in the interature	C_t	concrete specific heat				
	k_{c}	parameter associated with non-evaporable water and taken as 0.253 (as suggested in [13])				
	A_{c1},A_{c2},η_c	parameters with no precise physical meaning associated with the variation of the degree of cement hydration over time				
Parameters characterised	γc	parameter calculated as the ratio of the hydration activation energy over the universal gas constant				
by a large variability (see Table 2) – some of which	∂_c^{κ}	total heat content per unit cement mass due to cement hydration				
do not possess a precise physical meaning	κ^c_{vg}	parameter that governs the amount of water contained in the cement gel pores				
(to be identified with the inverse analysis	g_1	parameter that governs the shape of the sorption curve				
presented in Section 4)	D_0, D_1, n	parameters that control the moisture permeability and depend on the specific concrete mix				
	k _{sh}	parameter that relates the change over time of the free shrinkage deformation to the rate of the relative humidity				

Parameter	Range of variation	Mean value
A_{c1}	3900 - 55000 [s ⁻¹]	29450
A_{c2}	$10^{-6} - 5 \cdot 10^{-2}$	$2.5 \cdot 10^{-2}$
η_{c}	5.5 - 8.0	6.75
γ_c	3000 – 8000 [K]	5500
$\partial_c^{\prime 6}$	400 – 550 [kJ/kg]	475000
κ_{vg}^{c}	0.10 - 0.26	0.18
g_1	1.20 - 2.20	1.70
D_0/c	$0.2 \cdot 10^{-14} - 7.5 \cdot 10^{-14} \text{ [m}^2\text{/s]}$	3.85.10-14
D_1/c	$4.8 \cdot 10^{-10} - 12 \cdot 10^{-10} \text{ [m}^2\text{/s]}$	$8.4 \cdot 10^{-10}$
n	3.0 - 4.5	3.75
k_{sh}	5×10 ⁻⁴ - 3.5×10 ⁻³	2.0×10 ⁻³

Table 2. Range of variation for the parameters listed in the lower part of Table 1.

Table 3. Specifications of the concrete mix and some parameters used in the numerical simulations

SIII	ulations.
Parameter	Assumed value
С	312 kg/m^3
w/c	0.57
λ	2.3 W/m°C
ρ	2400 kg/m ³
C _t	1100 J/kg°C
k _c	0.253

597	tem	peratu	re T.				5		
	D	1()0 mm						
	RH	40)%						
	Period of wet curing 1 day								
	Period monitored	30) days						
	Added noise	10)%						
	Boundary conditions		I	EΕ		E	S	EE	ES
	Location of discrete measurements ¹ for <i>h</i> [mm]	/	50	10	50/10	/	50	50/10	50/10
	Location of discrete measurements ¹ for <i>T</i> [mm]		4	50		5	0	/	/
	Column	Α	В	С	D	Е	F	G	Н
	D_0	8.5	36.5	10.6	8.7	4.1	2.3	2.7	2.0
	D_1	13.7	5.9	4.8	6.4	1.9	1.3	2.1	0.8
	n	2.8	4.4	0.9	0.7	0.4	0.5	0.4	0.3
	$\kappa^c_{_{vg}}$	8.0	8.8	6.8	9.6	3.1	3.9	4.6	3.7
	g_1	7.2	5.0	5.2	8.2	1.4	0.6	3.0	1.1
	γc	0.1	0.1	0.1	0.1	0.2	0.2	0.2	0.6
	∂_c^{c}	6.1	3.7	3.7	4.2	1.9	1.2	13.3	6.8
	A_{c2}	8.2	5.3	6.2	8.1	3.8	2.8	4.9	12.2
	η_{c}	8.9	5.2	5.1	6.1	2.6	1.6	2.4	0.9
	k _{SH}	8.0	2.2	0.6	0.6	1.3	0.3	0.3	1.2
598	NOTE: ¹ Locations measured from ex	ternal	surface	s of co	ncrete c	ompo	nent [mm].	
599									
600									
601									
602									
603									

595Table 4. Results of the inverse analysis exercises in terms of err_k^{id} [%] by varying: boundary596conditions and location of discrete measurements for the relative humidity h and the

D	250 n	nm						
Location of discrete measurements for T	125 n	nm						
RH	40%							
Period of wet curing	1 day	,						
Added noise	10%							
Boundary conditions		EE			ES			
Location of discrete measurements for h [mm]	1	25/10)	,	/	12	125	
Period monitored [days]	30	60	90	60	90	60	90	
Column	А	В	С	D	Е	F	G	
D_0	14.5	6.1	2.3	5.3	8.1	6.8	4.8	
D_1	3.0	1.8	2.4	2.4	3.5	3.2	3.1	
n	2.2	1.0	0.4	0.9	1.2	1.1	0.8	
κ^c_{vg}	10.3	6.0	6.2	11.8	19.0	8.2	7.1	
g_1	3.5	1.8	2.3	2.6	5.3	2.3	1.9	
$\gamma_{\rm c}$	0.1	0.1	0.1	0.2	0.2	0.1	0.2	
$\partial_c^{\prime 6}$	1.4	1.0	1.2	0.7	1.7	0.8	1.1	
A_{c2}	2.8	3.3	4.5	6.2	4.6	4.7	4.8	
η_{c}	1.7	1.0	1.0	1.7	2.0	1.5	0.8	
k _{SH}	0.5	0.2	0.2	1.3	2.2	0.2	0.2	
NOTE: ¹ Locations measured from external s	surface	s of c	oncre	te com	ponent	[mm]		

Table 5. Results of the inverse analysis exercises in terms of err_k^{id} [%] by varying: boundary

605 conditions, location of discrete measurements for the relative humidity *h* and period monitored.

610 Table 6. Results of the inverse analysis exercises in terms of err_k^{id} [%] for an exposed-sealed

specimen by varying: location of discrete component	measu	remen	ts for	the rel	ative	humic	lity h	and	
Location of discrete measurements for T	$0.5 \times$	D							
RH	40%								
Period of wet curing	1 day	y							
Period monitored	90 da	ays							
Added noise	10%	•							
Boundary conditions		E	ES			E	,S		
Location of discrete measurements for <i>h</i> [mm]			/			0.5	0.5×D		
D [mm]	100	200	300	400	100	200	300	400	
Column	Α	В	С	D	Е	F	G	Η	
D_0	3.2	5.8	7.2	8.4	4.9	3.0	6.6	6.8	
D_1	1.7	1.9	2.9	6.4	1.6	2.1	3.5	5.2	
n	0.4	0.7	1.0	1.4	0.3	0.5	1.0	1.1	
κ^{c}_{vg}	5.3	14.3	18.6	20.5	5.1	6.0	7.5	9.4	
<i>g</i> 1	1.2	3.5	5.3	5.9	1.6	1.5	2.0	2.7	
γ_{c}	0.1	0.2	0.2	0.2	0.1	0.2	0.2	0.2	
$\partial_c^{\prime \circ}$	1.0	1.5	1.5	1.4	0.9	1.1	1.1	1.1	
A_{c2}	2.5	4.2	5.5	5.8	2.9	4.1	5.3	5.8	
η _c	1.6	1.6	1.5	1.5	1.3	0.8	0.8	0.8	
ksH	0.7	1.7	2.2	1.8	0.2	0.2	0.2	0.3	

NOTE: ¹Locations measured from external surfaces of concrete component [mm].

616 Table 7. Results of the inverse analysis exercises in terms of err_k^{id} [%] by varying: boundary

617 conditions, location of discrete measurements for the relative humidity *h* and assuming

different a-priori values for the parameter A_{c1} .								
D	100 mn	1						
Location of discrete measurements for T	50 mm							
RH	40%							
Period of wet curing	1 day							
Period monitored	30 days							
Added noise	10%							
Boundary conditions		EE			ES			
Location of discrete measurements ¹ for h [mm]		50/10			50			
Parameter $A_{c1}[s^{-1}]$	29450	3900	55000	29450	3900	55000		
Column	А	В	С	D	Е	F		
D_0	8.7	9.0	9.0	2.3	3.4	2.4		
D_1	6.4	5.6	5.5	1.3	0.8	1.3		
n	0.7	0.6	0.6	0.5	0.3	0.6		
$\kappa^c_{_{vg}}$	9.6	6.1	6.1	3.9	2.8	4.1		
<i>g</i> 1	8.2	7.1	7.0	0.6	0.9	0.6		
$\gamma_{\rm c}$	0.1	10.8	3.3	0.2	10.5	3.4		
$\partial_c^{\prime 6}$	4.2	4.5	4.4	1.2	0.8	1.1		
A_{c2}	8.1	7.2	7.0	2.8	1.5	3.2		
η _c	6.1	6.8	6.7	1.6	1.2	1.6		
k _{SH}	0.6	0.3	0.3	0.3	0.4	0.5		
NOTE: ¹ Locations measured from extern	nal surfac	es of co	oncrete co	omponen	t [mm].			

Table 8. Results of the inverse analysis exercises in terms of err_k^{id} [%] by considering sinusoidal time-varying boundary conditions, in terms of external temperature and relative

humidity.				-	
RH	40%±	-10%			
Temperature	20°±4	5°			
Period of wet curing	1 day				
Added noise	10%				
Concrete thickness D [mm]		100		250)
Period monitored [days]		30		60	
Boundary conditions	ES	ES	EE	EE	ES
Location of discrete measurements for h [mm]	/	/	50/10	125/10	125
Location of discrete measurements for T [mm]	50	50/5	50	125	125
Column	Α	В	С	D	Е
D_0	1.8	2.7	1.6	5.6	3.5
D_1	1.2	1.3	5.4	2.4	2.7
n	0.8	0.7	0.6	1.0	0.4
κ^c_{vg}	1.9	1.2	7.2	4.0	3.5
81	0.9	0.6	5.4	1.5	0.8
γ _c	1.2	1.5	1.3	0.3	0.2
$\partial_c^{\prime 6}$	4.6	4.0	7.0	0.9	1.0
$A_{ m c2}$	11.5	9.3	23.1	9.5	9.7
η _c	1.6	1.9	2.7	0.9	1.2
k_{SH}	2.2	2.3	0.4	0.5	0.4







Figure 2. Relative humidity (RH) profiles for 10 years of simulation under different exposure conditions for a 100 mm thick concrete component exposed to environmental RH of 40%.



Figure 3. Relative humidity (RH) profiles for 10 years of simulation under different exposure
 conditions for a 250 mm thick concrete component exposed to environmental RH of 40%.



- Figure 4. Total deformations (continuous lines) and free shrinkage deformations (dotted lines)
 for 10 years of simulation (at same instants in time of Figure 2) under different exposure
 conditions over a 100 mm concrete thickness exposed to environmental RH of 40%.



- Figure 5. Total deformations (continuous lines) and free shrinkage deformations (dotted lines)
 for 10 years of simulation (at same instants in time of Figure 3) under different exposure
 conditions over a 250 mm concrete thickness exposed to environmental RH of 40%.





Figure 6. Sensitivity of deformation measurements with respect to the model parameters for a
 250 mm thick concrete component and an external humidity of 40 %.





Figure 7. Sensitivity of deformation measurements with respect to selected model parameters
 for thicknesses of 100 mm and 250 mm, and external humidity of 40%.