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*Determination of the fracture resistance of ductile polymers: the ESIS TC4  
recent experience*

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**Round-robin (RR) tests carried out under the direction of the Technical Committee 4, “Polymers, Polymer Composites and Adhesives”, of the European Structural Integrity Society (ESIS TC4) showed that the multi-specimen methodology employed for the construction of the crack growth resistance curve (J vs crack extension,  $\Delta a$ ) of polymers often does not provide reliable data, because of the uncertainties associated with the measurement of  $\Delta a$ . With this in mind, the ESIS TC4 attention has been more recently focused on the analysis of a testing scheme based on the load separation criterion, which does not require the measurement of  $\Delta a$ . With the aim to employ this new approach into a standardized procedure, the degree of reproducibility of the results obtainable with the application of this testing scheme to ductile polymers has been assessed by means of multi-laboratory RR testing exercises, started in 2011. An ESIS TC4 reference draft protocol was prepared and ten laboratories participated in the RR activities. The present work describes the load separation criterion-based testing procedure recently examined by ESIS TC4, and gives a summary of the results obtained in the RR activities, which appear encouraging.**

## INTRODUCTION

For determining the low-rate fracture resistance of ductile polymers, for which the standard linear elastic fracture mechanics tests fail, the material crack growth resistance ( $J_R$ ) curve ( $J$  vs crack extension,  $\Delta a$ ) is generally employed. This is usually constructed by means of a multi-specimen approach (procedure [1] developed by ESIS TC4, that is the Technical Committee 4, “Polymers, Polymer Composites and Adhesives”, of the European Structural Integrity Society [2], and ASTM D6068 [3]). Specific ESIS TC4 round-robin, RR, tests showed that the uncertainties associated with the measurement of  $\Delta a$  often make this approach unreliable. Further, in many cases, an initiation fracture resistance parameter,  $J_{Ic}$ , cannot be obtained. With this in mind, the attention of ESIS TC4 has been recently paid to the analysis of a single-specimen testing scheme based on the load separation criterion (LSC), which does not require the measurement of  $\Delta a$  [4]. This approach would allow to: i) determine a material initiation fracture resistance parameter,  $J_{I,lim}$ ; ii) provide a rough measure of  $\Delta a$  produced during the fracture test, in the plastic region. In order to assess the degree of reproducibility of the results obtainable with the application of this method, in view of its possible employment in a standardized procedure, a multi-laboratory activity has started in September 2011 under the direction of ESIS TC4, with Università degli Studi di Brescia (I) as the coordinating laboratory. Ten laboratories (indicated in the authors’ list) have participated in this activity, organized on three consecutive RR testing exercises (RR1 to RR3). RR1 consisted in a preliminary work aimed at setting the key-points for the preparation of the reference draft testing protocol [5]. In RR2 and RR3, this protocol was applied to the fracture characterization of polymeric materials with different degrees of ductility, and the outcomes used to enhance the robustness of the method and to improve the protocol itself. The examined materials are: an acrylonitrile-butadiene-styrene (ABS) resin and a high-impact polystyrene (HIPS), in RR2; a rubber-toughened polybutylene terephthalate (RT-PBT) and a linear low-density polyethylene (LLDPE), both exhibiting a very high degree of ductility, in RR3. The present work describes the LSC-based testing procedure examined by ESIS TC4, and gives a summary of the results obtained during the RR activities.

## TEST METHOD – EXPERIMENTAL

The method described in the RR protocol, founded on the LSC proposed by Ernst [6], derives from Sharobeam and Landes' works published in the early 90's on metals [7,8]. The applicability of the LSC to polymeric materials, during both blunting and crack propagation phase, has been demonstrated (see [9] and referenced papers). The RR procedure is based on the construction of a “load separation parameter curve”,  $S_{sb}$  curve, which requires the execution of two tests, on a sharp-notched specimen (sN, crack growth allowed) and on a blunt-notched specimen (bN, crack growth hindered). Single edge notched in bending, SE(B), configuration is adopted. From the load,  $P$ , vs displacement,  $u$ , curves obtained from quasi-static tests on a sN and a bN specimen, the separation parameter,  $S_{sb}$ , is determined as:

$$S_{sb}(u_{pl}) = \frac{P_s}{P_b} \Big|_{u_{pl}} \quad (1)$$

where  $P_s$  and  $P_b$  are load values read on  $P$  vs  $u_{pl}$  curves of sN and bN specimen, respectively, at a given value of (nominal) plastic displacement,  $u_{pl}$ , which is determined for each specimen as:

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$$u_{pl} = u - P \cdot C_0 \quad (2)$$

$C_0$  being the initial elastic compliance of the specimen. It is expected that  $S_{sb}$  curve, that is  $S_{sb}$  plotted against  $u_{pl}$ , shows a “plateau” region, where  $S_{sb}$  maintains an almost constant value ( $S_{sb,plateau}$ ), followed by a decreasing  $S_{sb}$  region. The former region corresponds to the crack blunting phase and the latter to the crack propagation phase, in the fracture process of the sN specimen. The point between these two regions (limit point), at  $u_{pl} = u_{pl,lim}$ , corresponds to fracture initiation (or pseudo-initiation, by considering that for ductile polymers fracture initiation can be a complex progressive process [10]). J-integral value at  $u_{pl,lim}$ , that is  $J_{I,lim}$ , which can be taken as a material pseudo-initiation fracture resistance parameter in place of the more conventional  $J_{0.2}$  computed by the  $J_R$  curve (see [1]), is evaluated as:

$$J_{I,lim} = \frac{2 \cdot U_{lim,c}}{B \cdot (W - a_0)} \quad (3)$$

where  $U_{lim,c}$  is the energy up to the limit point, corrected for indentation (see [1]), and  $B$ ,  $W$  and  $a_0$ , the thickness, width and initial crack length of the sN specimen, respectively. Further, the normalized separation parameter curve, i.e.  $R_S$  vs  $u_{pl}$ , is traced ( $R_S$  is obtained as the ratio of  $S_{sb}$  over  $S_{sb,plateau}$ ) and the parameter  $m_S$  determined in the region of fracture propagation as (see also Figure 1):

$$m_S = - \left. \frac{dR_S}{du_{pl}} \right|_{u_{pl} > u_{pl,lim}} \quad (4)$$

Parameter  $m_S$ , which is a specimen characteristic (i.e. dependent on both specimen geometry and material), provides an indication of the crack advancement produced per unit of  $u_{pl}$  and could be used, as a “ductility index”, to classify the fracture propagation processes by the amount of crack growth occurring within the plastic region (if  $m_S = 0$  the process is governed by crack blunting). For further details concerning this methodology, ref. to [4,5,10].

Materials ABS, HIPS and LLDPE were provided by Versalis SpA (Mantova, I), whereas RT-PBT by Radici Novacips SpA (Villa d’Ogna, Bergamo, I). Table 1 reports the as-supplied form of the materials, their basic mechanical properties, the nominal dimensions of the SE(B) specimens used in the RR fracture tests, and the fracture resistance  $J_{0.2}$  data (from the  $J_R$  curve constructed by the application of the ESIS TC4 multi-specimen approach [1] on specimens having same geometry and dimensions of the RR tests). Each laboratory prepared and tested at least three sN and one bN specimens for each of the materials considered. The notching techniques were freely chosen by the laboratory. For LLDPE, two sets of specimens (#a and #b), differing in size, were examined. The experiments were performed by means of universal testing machines, at  $\approx 23^\circ\text{C}$  and with a crosshead rate of 1 mm/min. The data were processed according to the RR protocol [5], and the results (consisting in  $S_{sb}$  curve and data of  $J_{I,lim}$  and  $m_S$ , for each sN specimen tested) sent to the laboratory of Brescia for the comparative analysis.

## RESULTS AND DISCUSSION

Table 2 reports  $J_{I,lim}$  and  $m_S$  results for the various materials examined. Each datum is the mean value obtained by averaging all the data from the various laboratories. The datum considered for

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**Table 1** – Supply-form of the materials examined and their basic mechanical properties (Young’s modulus,  $E$ , and tensile yield stress,  $\sigma_y$ ), nominal dimensions of SE(B) specimens,  $J_{0.2}$  data.

Material (RR)	As-supplied form	Basic mechanical properties <sup>a</sup>		SE(B) specimen dimensions <sup>b</sup>			$J_{0.2}$ [kJ/m <sup>2</sup> ]
		$E$ [MPa]	$\sigma_y$ [MPa]	$B$ [mm]	$W$ [mm]	$a_0/W$	
HIPS (RR2)	inject. moulded dumb-bells <sup>c</sup>	1760	18	4	10	0.6	2.84
ABS (RR2)	6 mm thick compression moulded plates	2500	44	6	12	0.6	5.71
RT-PBT (RR3)	inject. moulded dumb-bells <sup>c</sup>	1450	31	4	10	0.6	6.58
LLDPE <sup>d</sup> (RR3)	10 mm thick inject. moulded plates	250	- <sup>e</sup>	10	10 (#a)	0.6	- <sup>e</sup>
					20 (#b)		

<sup>a</sup> from quasi-static tests at room temperature.

<sup>b</sup>  $B$ , thickness;  $W$ , width;  $a_0$ , initial crack length (in bN specimen, notch tip radius of 1 mm); span used in fracture tests,  $S = 4W$ .

<sup>c</sup> acc. to ISO 3167; central narrow portion (with dimensions 80x10x4 mm<sup>3</sup>) used for SE(B) specimen preparation.

<sup>d</sup> two sets of SE(B) specimens (#a and #b) used.

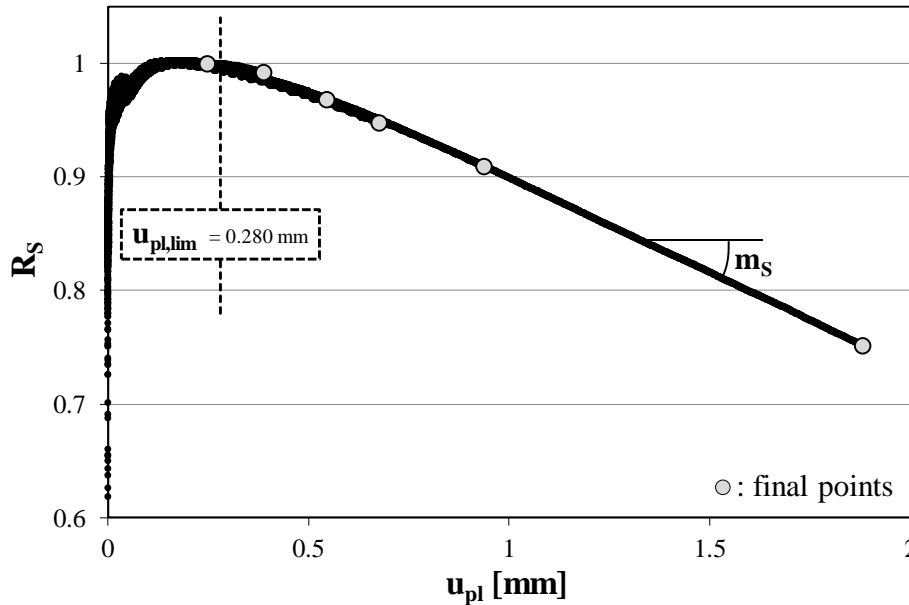
<sup>e</sup> not measured ( $J_R$  curve not constructed).

**Table 2** – Mean values ( $\pm$  standard deviation,  $\delta$ ) of  $J_{I,lim}$  and  $m_S$  obtained by averaging all the (mean) data from the different laboratories. Values between {} indicate  $\delta$  expressed as percentage of the corresponding mean value.

Material	$J_{I,lim}$ [kJ/m <sup>2</sup> ]	$m_S$ [mm <sup>-1</sup> ]
HIPS	1.53 $\pm$ 0.251 {16%}	0.325 $\pm$ 0.0077 {2%}
ABS	4.09 $\pm$ 0.630 {15%}	0.244 $\pm$ 0.0132 {5%}
RT-PBT	4.6 $\pm$ 1.03 {22%}	0.163 $\pm$ 0.0045 {3%}
LLDPE #a	- <sup>a</sup>	0.025 $\pm$ 0.0096 {38%}
LLDPE #b	- <sup>a</sup>	0.010 $\pm$ 0.0052 {52%}

<sup>a</sup> reliable data not obtained.

each laboratory is the average of the data obtained from the various sN specimens tested. The degree of repeatability of the results within the same laboratory (index of repeatability not shown here) was generally higher than that of reproducibility (represented by the data of standard deviation in Table 2). Results with a very high degree of repeatability could be obtained. As an example, Figure 1 shows the  $R_S$  curves obtained by the same laboratory (Brescia) from six nominally identical sN specimens of RT-PBT, tested up to different levels of displacement. The curves overlap well, and they practically draw one single curve in which the plateau region that extends up to  $u_{pl,lim}$  is clearly visible.



**Figure 1** –  $R_S$  curves obtained at Brescia laboratory from six nominally identical sN specimens of RT-PBT, tested up to different levels of displacement (final points).  $u_{pl,lim}$  is indicated by the vertical dashed line.  $m_s$  is also represented.

For HIPS, ABS and RT-PBT, the degree of reproducibility obtained for the  $m_s$  data is higher than that of  $J_{I,lim}$  data. This suggests that, with respect to the fracture propagation phase, to which  $m_s$  parameter refers to, fracture initiation/early-stages of crack growth are less reproducible (at a macroscopic scale). Analysis of the data collected from the various laboratories seem to indicate that the scattering observed for  $J_{I,lim}$  data is related to a combination of testing and data analysis aspects. In relation to testing, the quality of the notch, both sharp and blunt, seems to play an important role. With regard to data analysis, a crucial role is played by the determination of the initial specimen compliance,  $C_0$ ; in addition, the procedure proposed for the identification of the limit point on the  $S_{sb}$  curve can be further improved. Within ESIS TC4, new activities aimed at examining carefully these aspects are in progress. It is worth noting, however, that the degree of scattering observed for  $J_{I,lim}$  data could be acceptable within the field of fracture mechanics tests. Interestingly, for HIPS, ABS and RT-PBT,  $J_{I,lim}$  value is lower than the technological  $J_{0.2}$  parameter read on the  $J_R$  curve (see Table 1 and 2).

Among the various materials, LLDPE (irrespective of specimen size, either #a or #b) was largely the most hard-to-characterize material. A reliable plateau region could not be identified in the  $S_{sb}$  curves, indicating that crack blunting phase cannot be distinguished from crack propagation. The low values of  $m_s$  obtained (see Table 2) clearly suggest that fracture process is governed by blunting (irrespective of the specimen size considered, crack growth produced per unit of  $u_{pl}$  is very small). LLDPE shows a high degree of scattering for  $m_s$  data, and this suggests that its fracture process is not easily reproducible, contrary to what observed for the other materials for which standard deviations of  $m_s$  are quite small. This is one of the reason why a reliable  $J_R$  curve could not be constructed for this material (see Table 1), for which, furthermore, valid data of  $\Delta a$  could not be obtained by the inspection of the fracture surface produced. Even if valid fracture resistance data ( $J_{I,lim}$ ) have not been determined for LLDPE, the testing procedure here examined was able to

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highlight, through  $m_s$  determination, that a testing scheme based on the propagation of a crack cannot be successfully applied to this material, working on SE(B) specimens with dimensions as in Table 1. It would be necessary to use a different testing geometry, or to resort to another testing approach, such as cutting [11].

### CONCLUSIONS

The results obtained in the ESIS TC4 RR activity on the use of LSC in J-testing of ductile polymers are encouraging. The method examined has been successfully applied to polymers with different degrees of ductility. It allows determining a material pseudo-initiation fracture resistance parameter ( $J_{I,lim}$ ), as well as a parameter ( $m_s$ ) that can have a key-role in a criterion to check *a priori* if the multi-specimen approach for J-testing [1,3] applied to a ductile polymer (with given specimen geometry and dimensions) is likely to fail. The RR activity is still in progress, and special attention is given to this latter outcome.

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