

Title page

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Cracking behavior of CA-UHPC overlay in steel-CA-UHPC composite bridge deck: Flexural tension test and restrained shrinkage effect

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ABSTRACT

Coarse Aggregate Ultra-High Performance Concrete (CA-UHPC) has emerged as a promising alternative UHPC material for steel-UHPC composite decks due to its reduced autogenous shrinkage. The cracking performance of CA-UHPC overlay is of interest to ensure the composite deck stiffness. To this end, flexural-tension tests on the composite decks were conducted to explore the effects of reinforcement ratios, concrete covers, concrete types (CA-UHPC vs. normal concrete), and loading nature (monotonic vs. cyclic). Test observations indicate that the restrained shrinkage effect leads to premature cracking of the CA-UHPC overlay under external loads. Increasing reinforcement ratios or reducing concrete covers helps to control maximum crack widths. When reinforcement ratios exceed 2.1%, maximum crack widths of CA-UHPC overlay remain below 0.2 mm. Unlike normal concrete, steel rebars embedded in CA-UHPC overlays do not yield. Limited cyclic tension has a negligible impact on the cracking response. Moreover, a theoretical analysis based on the Trost-Bazant-algebraic-equations was conducted to understand the restrained shrinkage-induced internal force redistribution. Finally, an empirical model between the proposed restrained degree and steel-CA-UHPC bending stiffness ratio was developed to predict the restrained tensile stresses and the initial cracking loads. This study provides deeper insights into the cracking behavior of CA-UHPC overlay under various conditions, contributing to the optimization of such composite decks.

Keywords: CA-UHPC, steel-UHPC composite deck, crack pattern, restrained shrinkage effect, restrained tensile stress.

1. Introduction

Orthotropic steel deck (OSD) systems, as plotted in Fig.1(a), consisting of a OSD (including steel deck plate, closed longitudinal ribs, and crossbeams) and asphalt wearing course, have been widely used in large-span bridges throughout the world, owing to the higher load-bearing capacity, lighter self-weight, and easier installation [1]. Due to the complicated welded connections and insufficient local deck stiffness [2,3], fatigue cracking at the welds [4,5] and wearing of asphalt surfacing [2,6] have become interest of concern

38 worldwide since the 1970s. To tackle these challenges, a thin rebar-reinforced ultra-high
39 performance concrete (UHPC) overlay (35~80 mm) has been introduced into the OSD in
40 order to stiffen the deck system. The UHPC overlay is connected to the steel deck plate by
41 using epoxy-based adhesive [7–9] or welded studs [10–12], and the deck system is usually
42 named steel-UHPC composite bridge deck, as shown in Fig.1(b).

43 UHPC, as a nowadays “state-of-art” category of fiber-reinforced cementitious
44 composites, is typically characterized by [13]: (1) compressive strength higher than 120 MPa;
45 (2) elastic modulus greater than 40 GPa; (3) sustained post-cracking tensile strength larger
46 than 5 MPa; and (4) a disconnected pore structure that significantly reduces permeability and
47 thus enhances durability. However, an extremely low water/binder ratio (less than 0.2) and a
48 high amount of fine reactive admixtures lead to a significantly high early-age autogenous
49 shrinkage for UHPC [14–16]. This will induce restrained tensile stress and even tensile
50 cracking of UHPC overlay in the composite deck system at early ages, resulting in a
51 decreased stiffening effect on the OSD. Therefore, reducing the early-age shrinkage of UHPC
52 has become a major concern when used in the composite deck.

53 So far, the steam-curing strategy [16,17] and the use of shrinkage-reducing admixture
54 [14,18,19] have been investigated to identify the shrinkage-reducing effect. Another
55 alternative solution is to add coarse aggregates to mitigate the cement paste shrinkage [20–22].
56 The UHPC containing coarse aggregates is denoted as CA-UHPC to distinguish it from the
57 conventional UHPC. Moreover, compared with UHPC without coarse aggregates, CA-UHPC
58 has demonstrated enhanced compressive strength and elastic modulus, anyway accompanied
59 by a reduced tensile performance [22–25], especially in terms of tensile ductility and ultimate
60 strain capacity as well as in the ability to achieve tensile strain-hardening behavior.

61 When CA-UHPC is used as the overlay material in the composite deck system, cracking
62 concerns are of the utmost importance. On one hand, as shown in Fig.1(b), under repeated
63 vehicle wheel loads, the concrete overlay above the crossbeams is inevitably subjected to
64 tension, leading to a significant external load-induced cracking potential. On the other hand,
65 though characterized by reduced autogenous shrinkage, the free shrinkage of the CA-UHPC
66 overlay will be restrained by the steel rebars and by the OSD as a whole, resulting in internal
67 tensile stresses and cracking risks. However, the application of CA-UHPC in the composite
68 deck is still in the preliminary stage [26]. To the best of the authors' knowledge, insights into
69 both the cracking performance and cracking potential of the CA-UHPC overlay have not been
70 investigated and reported. This has created a knowledge gap in the engineering practice worth
71 further investigation at both the material and macro-structural scale.

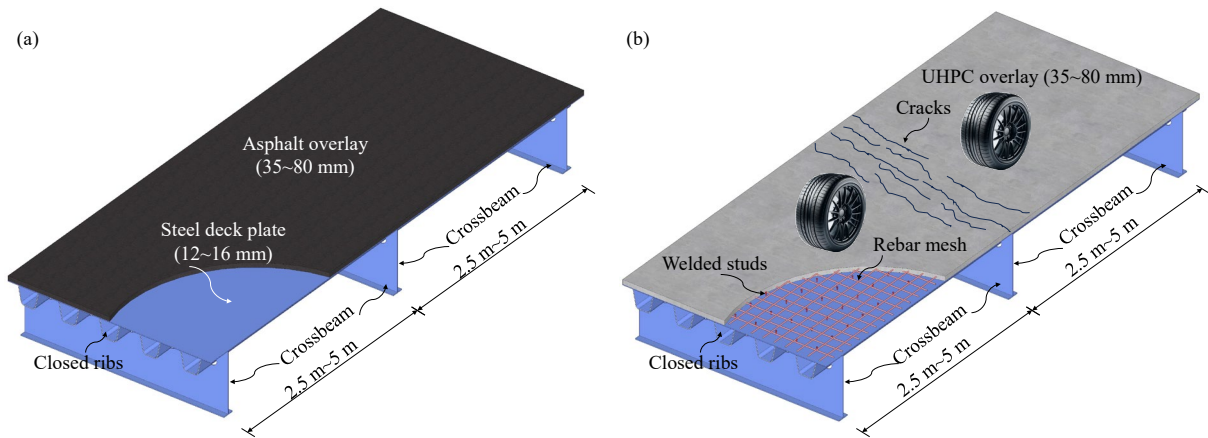


Fig.1. Bridge deck system: (a) OSD; and (b) steel-UHPC composite deck.

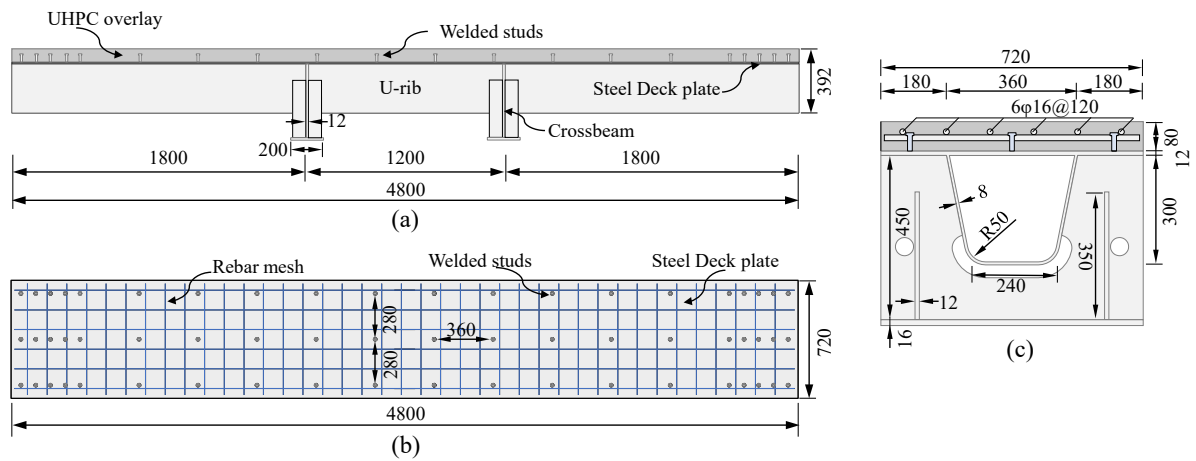
Therefore, in the framework described above, this study aims to clarify the cracking performance and restrained shrinkage-induced cracking potential of the CA-UHPC overlay in the composite deck. Full-scale flexural tension tests were conducted to identify the influence of reinforcement ratios, concrete covers, concrete types, and load nature (monotonic vs cyclic) on the crack patterns and crack widths of the CA-UHPC overlay. A theoretical analysis based on the Trost-Bazant-algebraic-equations was performed to clarify the restrained shrinkage effects and validated with experimental measurements. Finally, a restrained degree parameter was proposed to quantify the restrained shrinkage effect and a restrained shrinkage model was developed to predict the restrained tensile stresses and the initial cracking loads of the composite deck.

2. Experimental program

2.1 Test design and conduction

2.1.1 Specimen design

Eight steel-concrete composite deck specimens with a single rib were designed and fabricated. Fig.2 shows the structural details of the benchmark specimen. All specimens had a total length of 4800 mm, a width of 720 mm, and a depth of 392 mm, consisting of an 80-mm thick reinforced concrete/CA-UHPC overlay and single-rib-stiffened steel plate. The steel plate and the concrete overlay were connected by short welded studs (diameter of 13 mm and a post-weld height of 45 mm). The longitudinal and transverse spacings of the welded studs were 360 mm and 280 mm, respectively. In the concrete overlay, 16-mm diameter HRB400 steel rebars were arranged in a mesh, arranged with longitudinal rebars on the top and transverse rebars at the bottom, with a longitudinal spacing of 120 mm.



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Fig.2. Specimen details (unit: mm): (a) basic sizes; (b) welded studs and steel rebar arrangements; and (c) cross-section at the crossbeam location.

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Table 1 lists the basic information of the designed specimens, where specimen SN-3 served as the benchmark. The studied parameters are as follows:

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(1) Reinforcement ratios ρ_s : 0 to 3.1%. This value was calculated as the ratio of the longitudinal steel rebar area to the gross cross-sectional area of the concrete overlay. For specimen SN-1 with a reinforcement ratio of 0, no transverse rebars were provided. The transverse rebar arrangement for the remaining specimens was the same with a spacing of 120 mm.

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(2) Concrete covers c : 10 mm, 20 mm, and 30 mm, which was defined as the clear distance from the longitudinal steel rebar to the concrete top surface.

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(3) Concrete types, comparing the cracking behavior between CA-UHPC and normal concrete (NC).

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(4) Load nature, identifying the influence of monotonic vs. cyclic loadings on the cracking response of CA-UHPC overlay.

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Table 1. Specimen design.

| No. | Parameters | Rebar quantity | ρ_s | c [mm] | Loading methods | Concrete types | |
|------|-------------------------------|----------------|----------|----------|-----------------|----------------|---------|
| SN-1 | reinforcement ratios ρ_s | 0 | 0 | — | monotonic | CA-UHPC | |
| SN-2 | | 3 | 1.1% | 20 | | CA-UHPC | |
| SN-3 | | 6 | 2.1% | 20 | | CA-UHPC | |
| SN-4 | | 9 | 3.1% | 20 | | CA-UHPC | |
| SN-5 | concrete covers c | 6 | 2.1% | 10 | | CA-UHPC | |
| SN-6 | | 6 | 2.1% | 30 | | CA-UHPC | |
| SN-7 | concrete types | 6 | 2.1% | 20 | | | NC |
| SN-8 | loading methods | 6 | 2.1% | 20 | | cyclic | CA-UHPC |

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2.1.2 Specimen preparation and curing

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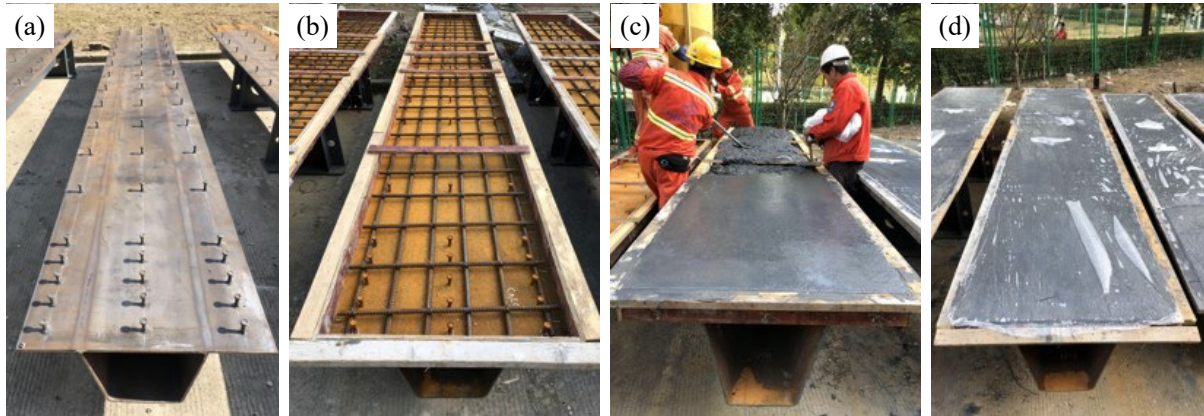
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Fig.3 shows the four main fabricating procedures for the specimens. To minimize water evaporation and prevent early-age cracking in the concrete overlay, the concrete overlay was covered with film as soon as after leveling it. Then, the specimens were cured for 37 days in

118 an outdoor environment with an average temperature of 12~18°C and an average relative
119 humidity of 72% (mid-November in Shanghai, China).

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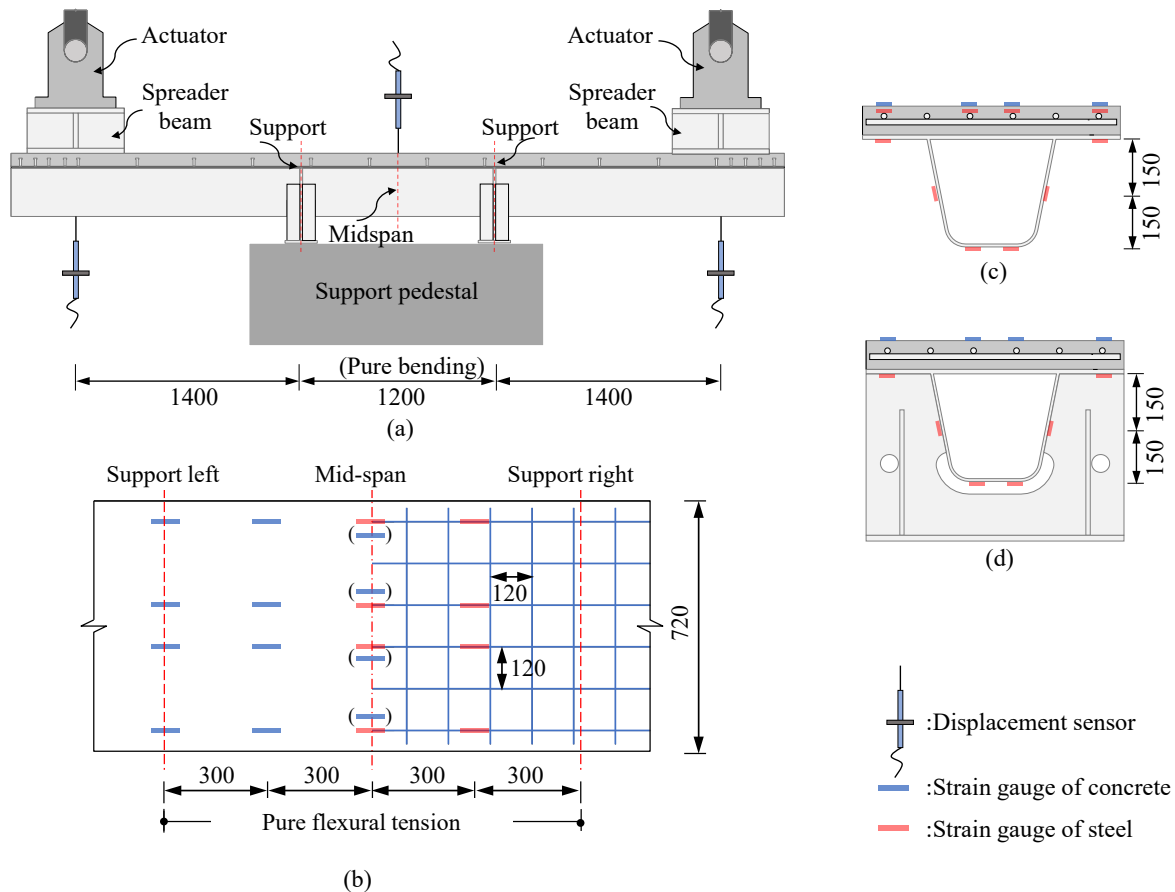
122 **Fig.3.** Specimen fabrication: (a) making of OSD and welded studs; (b) rebar tying and
123 formwork erection; (c) concrete casting; and (d) concrete curing.

124 2.1.3 Test setup and loading protocols

125 The crack initiation and propagation of the CA-UHPC overlay are the major concerns of
126 this study. To facilitate the crack observation, the specimens were designed into a 4-point
127 bending form, which consisted of a 1200-mm long central pure bending zone (for crack
128 monitoring) and two 1800-mm long cantilever zones (for test loading).

129 **Fig.4(a)** shows the 4-point bending test setup. The specimens were placed on a support
130 pedestal. Vertical loads were applied to the specimens using an MTS electro-hydraulic servo
131 loading system, which was able to enforce the force to two loading points simultaneously.

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Fig.4. Test setup and measuring points arrangement (unit: mm): (a) test setup and displacement sensor arrangement; (b) measuring points for concrete overlay and longitudinal rebars; (c) measuring points at mid-span cross-section; (d) measuring points at the support cross-section.

The measuring points are illustrated in Fig.4(a) to (d). The deflection at the loading-point cross-section was monitored through displacement sensors placed at the U-rib bottom. Longitudinal strain developments were measured using strain gauges placed on the surfaces of the concrete overlay, steel rebars, steel deck plate, U-rib web, and U-rib bottom at the mid-span cross-section as well as at the support cross-section. The transverse locations of the rebar strain gauges were aligned with those of the concrete strain gauges.

Fig.5 illustrates the loading protocols. The monotonic loading consisted of two stages: (1) Preloading was performed using force-controlled loading up to 20 kN, followed by unloading. This stage was employed to verify the proper functioning of the testing equipment. (2) “Actual” loading: Firstly, force-controlled loading was applied at a rate of 10 kN per increment until yielding was reached at the U-rib bottom, identified through the thereby positioned strain gauges. Subsequently, the control was shifted to displacement, and vertical deflection of the loading actuator was applied at a rate of 0.1 mm/s until ultimate failure.

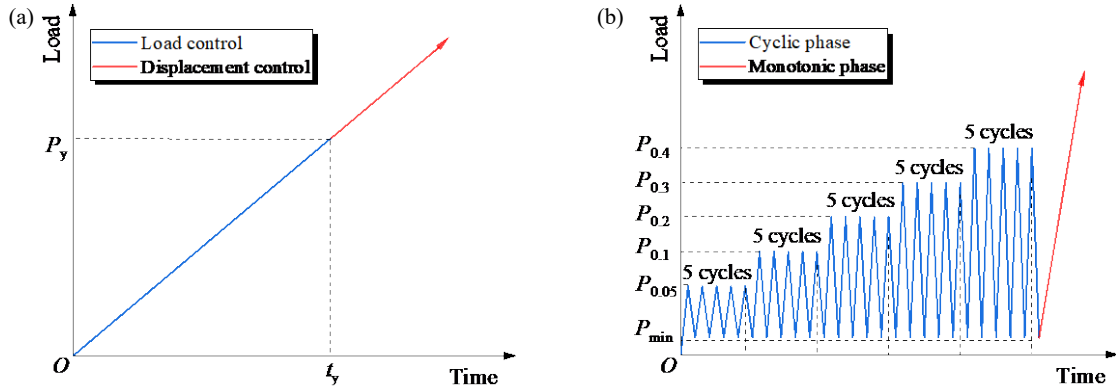


Fig.5. Loading protocols: (a) monotonic; and (b) cyclic.

As for the cyclic loading protocol, the preloading stage was identical to the monotonic loading. During the actual loading stage, force-controlled loading was applied up to $P_{0.05}$, which was defined as the force at a maximum concrete crack width of 0.05 mm. Subsequently, the load was decreased down 5 kN and then increased back to $P_{0.05}$ for a total of 4 cycles. The loading-unloading cycles were similarly repeated 5 times each for maximum crack widths of 0.1 mm, 0.2 mm, 0.3 mm, and 0.4 mm. Then, force-controlled monotonic loading was applied until the yielding at the U-rib. Finally, the loading was switched to a displacement-controlled type until ultimate failure.

After each loading increment was completed, the crack developments of the concrete overlay at the pure bending zone were visually observed and recorded. Crack widths were measured using crack observation devices with an accuracy of 0.01 mm.

2.1.4 Material properties characterization

As listed in Table 2, the CA-UHPC consists of reactive powders, river sand, basalt aggregates (with a maximum particle size equal to 8 mm), water, superplasticizer, and steel fibers. The steel fiber reinforcement with a total volume fraction of 2.5% consisted of straight fibers (length of 13 mm and diameter of 0.2 mm, dosage of 1%) and hooked-end ones (length of 20 mm and diameter of 0.25 mm, dosage of 1.5%). The NC contained gravel of 1080 kg/m^3 , sand of 780 kg/m^3 , cement of 450 kg/m^3 , water of 154 kg/m^3 , and water reducer of 4.5 kg/m^3 .

Axial tension tests on $50 \text{ mm} \times 100 \text{ mm} \times 560 \text{ mm}$ dog-bone-shaped specimens [27], elastic modulus tests (on prism specimens $100 \text{ mm} \times 100 \text{ mm} \times 300 \text{ mm}$ for CA-UHPC and $150 \text{ mm} \times 150 \text{ mm} \times 300 \text{ mm}$ for NC), compressive strength tests (same specimen as for elastic modulus test), and 4-point bending test on $100 \text{ mm} \times 100 \text{ mm} \times 400 \text{ mm}$ prism specimens (only for CA-UHPC) for concrete, were conducted. The obtained average mechanical properties of three identical samples are summarized in Table 3. All these material specimens were cured for 28 days under the same outdoor environment as the composite deck specimens. The first author has developed the tensile constitutive model of CA-UHPC [27], as plotted in Fig.6(a), which exhibits strain softening upon reaching the elastic tensile strength.

Table 2. Material compositions of 1 m^3 CA-UHPC (unit: kg).

| Reactive | Sand | Basalt | Steel fibers | Superplasticizer | Water |
|----------|------|--------|--------------|------------------|-------|
|----------|------|--------|--------------|------------------|-------|

| | | | | | | |
|--------|-----|------------|----------|--------|------|-----|
| powder | | aggregates | straight | hooked | | |
| 1173 | 616 | 472 | 89 | 109 | 25.7 | 138 |

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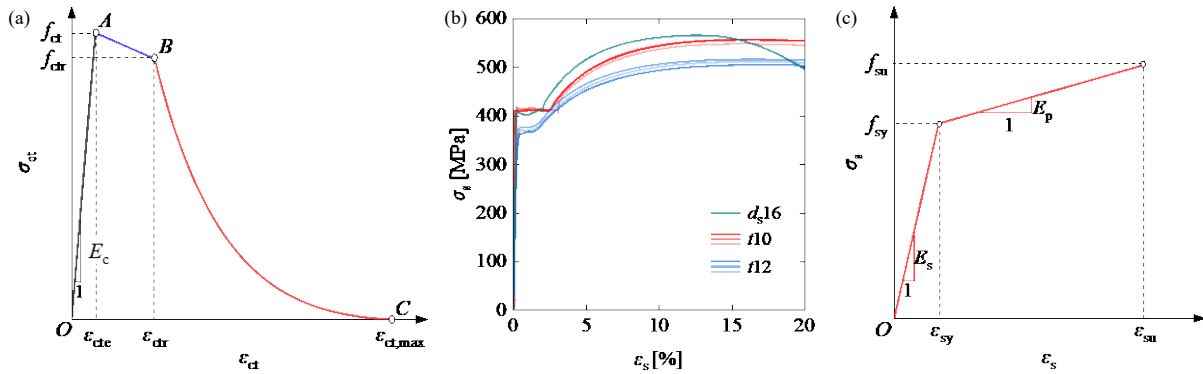
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Table 3. Mechanical properties of concrete (unit: MPa).

| | | | | | | |
|----------|-------|-------|------------|----------|-------------|-------------|
| Concrete | E_c | f_c | $f_{c,cu}$ | f_{ct} | $f_{cr,fl}$ | $f_{ct,fl}$ |
| NC | 36633 | 49 | 62 | 2.59 | — | — |
| CA-UHPC | 48733 | 96 | 108 | 7.45 | 11.53 | 22.38 |

187 Notes: $E_c, f_c, f_{c,cu}, f_{ct}, f_{cr,fl}, f_{ct,fl}$ denote elastic modulus, axial compressive strength (on prisms),
 188 cubic compressive strength, tensile strength, first cracking strength under flexural tension; and
 189 flexural tensile strength, respectively.

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192 **Fig.6.** Axial tensile constitutive models: (a) of CA-UHPC [28]; (b) tensile stress-strain
 193 response of steel rebar and steel plate; and (c) simplified tension constitutive model of steel
 194 rebar and steel plate.

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196 The steel plate and steel rebar were made of Q345 and HRB400, respectively. The tensile
 197 stress-strain curves of the steel plate and steel rebar are shown in Fig.6(b), and the simplified
 198 bilinear constitutive model is plotted in Fig.6(c). The characteristic mechanical properties of
 199 the bilinear constitutive model are summarized in Table 4.

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Table 4. Mechanical properties of steel.

| Material | t or d_s [mm] | f_{sy} [MPa] | f_{su} [MPa] | ϵ_{sy} [$\times 10^{-6}$] | ϵ_{su} [$\times 10^{-6}$] | E_s [MPa] | E_p [MPa] |
|----------|----------------------|-------------------|-------------------|---|---|----------------|----------------|
| Q345 | 8 | 411 | 554 | 1957 | 158269 | 209877 | 917 |
| | 12 | 370 | 511 | 1761 | 170963 | 209530 | 837 |
| HRB400 | 16 | 407 | 566 | 1958 | 124925 | 207880 | 1296 |

202 Note: t is thickness, d_s is diameter.

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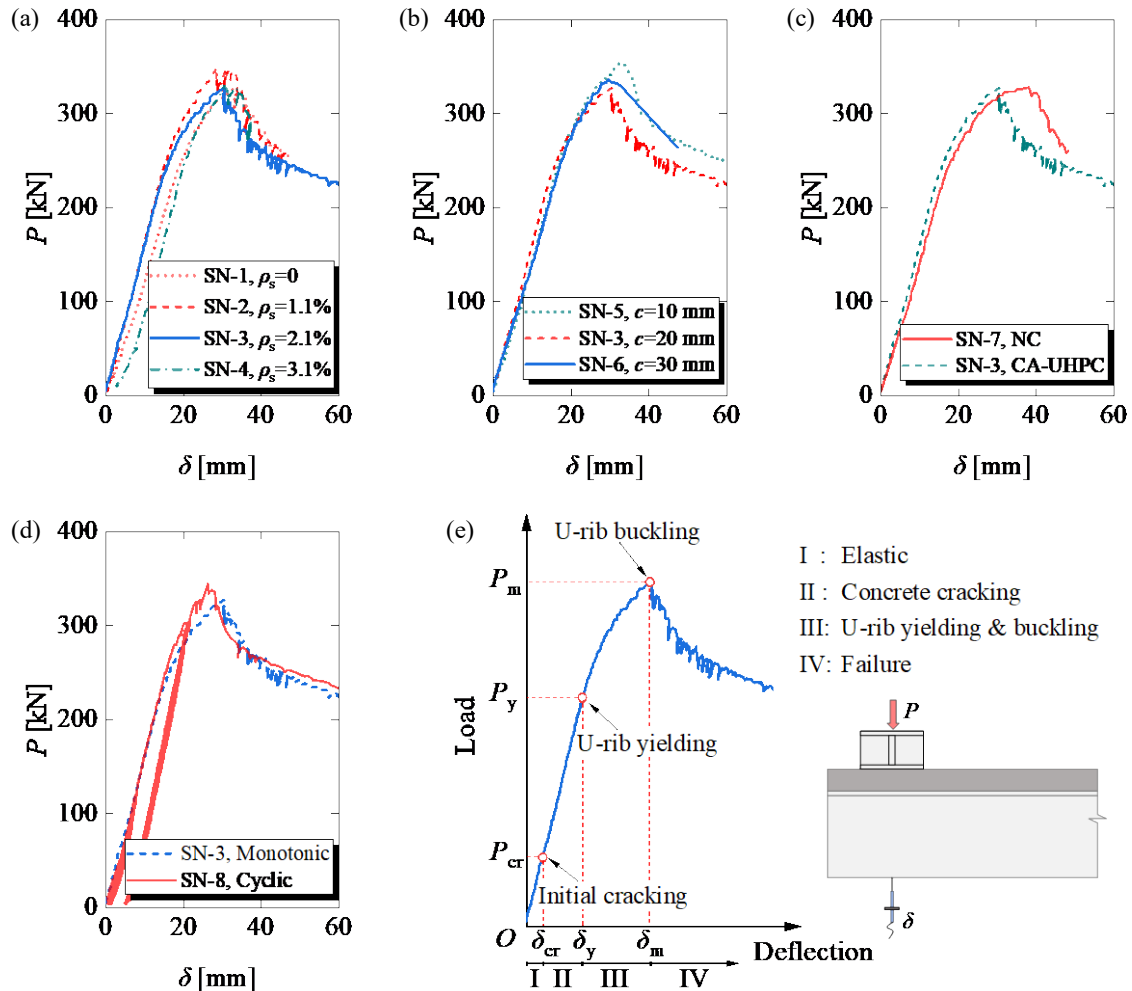
204 2.2 Test results and analysis

205 2.2.1 Flexural-tension response and failure modes

206 Fig.7(a)~(e) shows the flexural-tension response of the specimens, where P represents
 207 the load applied to one loading point, δ denotes the measured deflection from the

208 displacement sensor at the loading-point U-rib bottom. Overall, all specimens featured similar
 209 flexural-tension responses no matter of different reinforcement ratios, concrete covers,
 210 concrete types, and loading methods.

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213 **Fig.7.** Load-deflection responses: (a) reinforcement ratios; (b) concrete covers; (c) concrete
 214 types; (d) loading methods; and (e) schematic flexural-tension response.

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216 Fig.7(e) presents a schematic flexural-tension response of the steel-concrete composite
 217 deck specimens, which can be divided into four stages:

218 Stage I: Elastic stage, which ends with the initial cracking of concrete overlay.

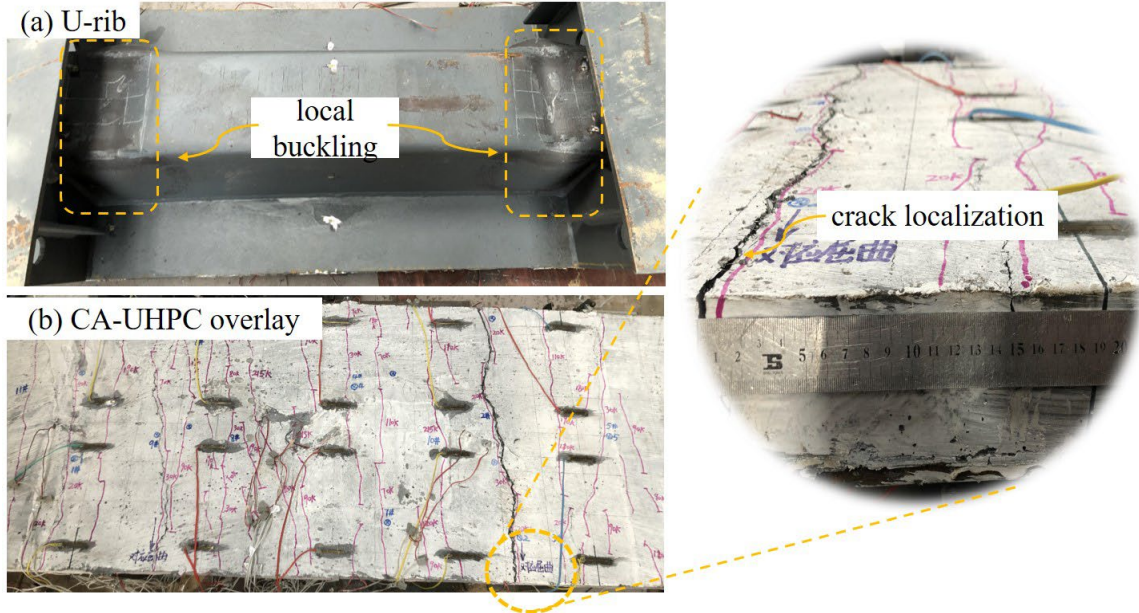
219 Stage II: Concrete cracking stage. With the increase in external loads, the crack numbers
 220 increased and the crack widths widened. This stage concludes with the compressive yielding
 221 at the U-rib bottom plate. Despite the crack-induced weakened tension contribution of the
 222 concrete overlay, the load-deflection curve still exhibited a linear response owing to the
 223 dominant bending stiffness contributed by the steel elements. The compressive yielding of the
 224 U-rib bottom plate corresponded to the linear deviation point in the load-deflection curve.

225 Stage III: U-rib yielding and buckling stage. With external loads increased, the yielding
 226 in the U-rib gradually progressed from the bottom plate to the web plate. Finally, local
 227 buckling of the U-rib bottom plate developed at the support cross-section. This phenomenon

228 was similar to the experimental results of the relevant existing study [28] on steel-UHPC
 229 composite decks. During this stage, the crack widths of concrete overlay further developed,
 230 while the crack numbers remained relatively stable.

231 Stage IV: Post-peak failure stage. The local buckling of the U-rib was continuously
 232 deformed, and a localized crack developed in the concrete overlay at the support cross-section.
 233 The ultimate failure modes are presented in Fig.8.

234



235

236 **Fig.8.** Ultimate failure modes: (a) local buckling of U-rib; and (b) crack localization at
 237 concrete overlay.

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239 2.2.2 Characteristic loads and deflections

240 **Table 7** summarizes loads and deflections at characteristic points, including the initial
 241 cracking point (δ_{cr} , P_{cr}), the yielding point (δ_y , P_y), and the peak point (δ_m , P_m).

242

243 **Table 7.** Characteristic loads and deflections (load unit: kN, deflection unit: mm).

| No. | Mark | Initial cracking | | | Yielding | | Peak | |
|------|------------------------------|------------------|---------------|---------------|----------|------------|-------|------------|
| | | P_{cr} | $P_{cr,theo}$ | δ_{cr} | P_y | δ_y | P_m | δ_m |
| SN-1 | $\rho_s 0\% - U - M$ | 20 | 68 | 1.75 | 211 | 16.23 | 327 | 32.71 |
| SN-2 | $\rho_s 1.1\% - c20 - U - M$ | 15 | 70 | 1.04 | 233 | 14.20 | 349 | 28.56 |
| SN-3 | $\rho_s 2.1\% - c20 - U - M$ | 20 | 72 | 0.92 | 196 | 12.15 | 327 | 30.43 |
| SN-4 | $\rho_s 3.1\% - c20 - U - M$ | 40 | 74 | 1.30 | 246 | 15.21 | 347 | 29.96 |
| SN-5 | $\rho_s 2.1\% - c10 - U - M$ | 30 | 72 | 1.86 | 210 | 14.33 | 353 | 32.56 |
| SN-6 | $\rho_s 2.1\% - c30 - U - M$ | 20 | 71 | 1.05 | 224 | 12.99 | 337 | 27.99 |
| SN-7 | $\rho_s 2.1\% - c30 - N - M$ | 35 | 29 | 2.25 | 220 | 15.31 | 328 | 38.06 |
| SN-8 | $\rho_s 2.1\% - c20 - U - C$ | 30 | 72 | 2.31 | 231 | 14.16 | 345 | 26.26 |

244 Notes: $\rho_s 0\%/1.1\%/2.1\%/3.1\%$ represent the longitudinal reinforcement ratio of 0, 1.1%, 2.1%,
 245 and 3.1%, respectively; $c10/20/30$ represent the concrete cover of 10 mm, 20 mm, and 30 mm,
 246 respectively; U/N represent CA-UHPC and NC, respectively; M/C represent monotonic

247 loading and cyclic loading, respectively.

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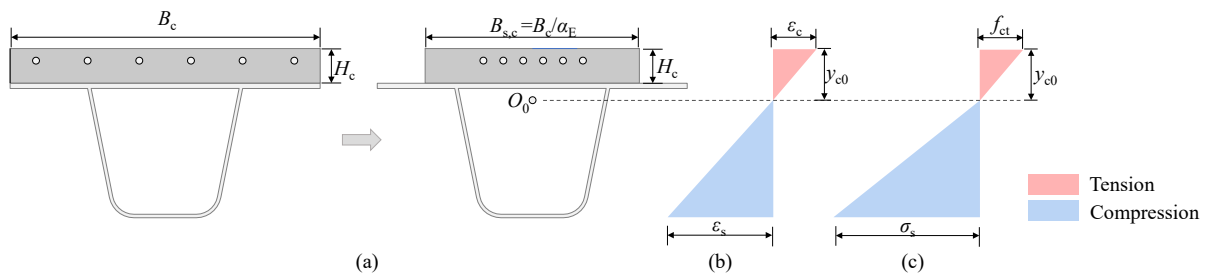
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Fig.9. (a) Schematic diagram of the transformed composite section; (b) strain distribution; and (c) stress distribution.

$$B_{s,c} = \frac{B_c}{\alpha_E} \quad (1)$$

where B_c is the width of the concrete overlay; $B_{s,c}$ is the transformed section width of the concrete overlay into steel; α_E is the elastic modulus ratio of steel to concrete, $\alpha_E = E_s / E_c$.

$$P_{cr,Theo} = \frac{f_{ct} I_0 \alpha_E}{L_0 y_{c0}} \quad (2)$$

where I_0 is the moment of inertia of the transformed composite section; y_{c0} is the vertical distance from the tensile edge of the concrete overlay to the centroid of the transformed composite section; L_0 is the distance from the cantilever loading point to the corresponding support point.

In contrast, the experimental cracking load observed in the NC specimen was close to the theoretical value. However, for the CA-UHPC specimens, the experimental cracking loads were notably below the theoretical predictions. This discrepancy can be attributed to the greater early-age autogenous shrinkage of CA-UHPC compared to NC. As a result, the shrinkage of CA-UHPC was restrained by the presence of steel elements, resulting in the development of tensile stress within the CA-UHPC overlay and subsequent premature cracking. A detailed mechanism analysis will be further elaborated in the following section.

279 2.2.3 Load-strain curves and strain distributions

280 **Fig.10** shows the load-strain curves for the representative specimens, the benchmark
 281 specimen SN-3, the NC specimen SN-7, and the cyclic loading specimen SN-8. The strain
 282 measuring points for concrete were selected from undamaged strain gauges, while the strain
 283 values for steel rebar and steel plates were the average value of strain gauges at the same
 284 section depth.

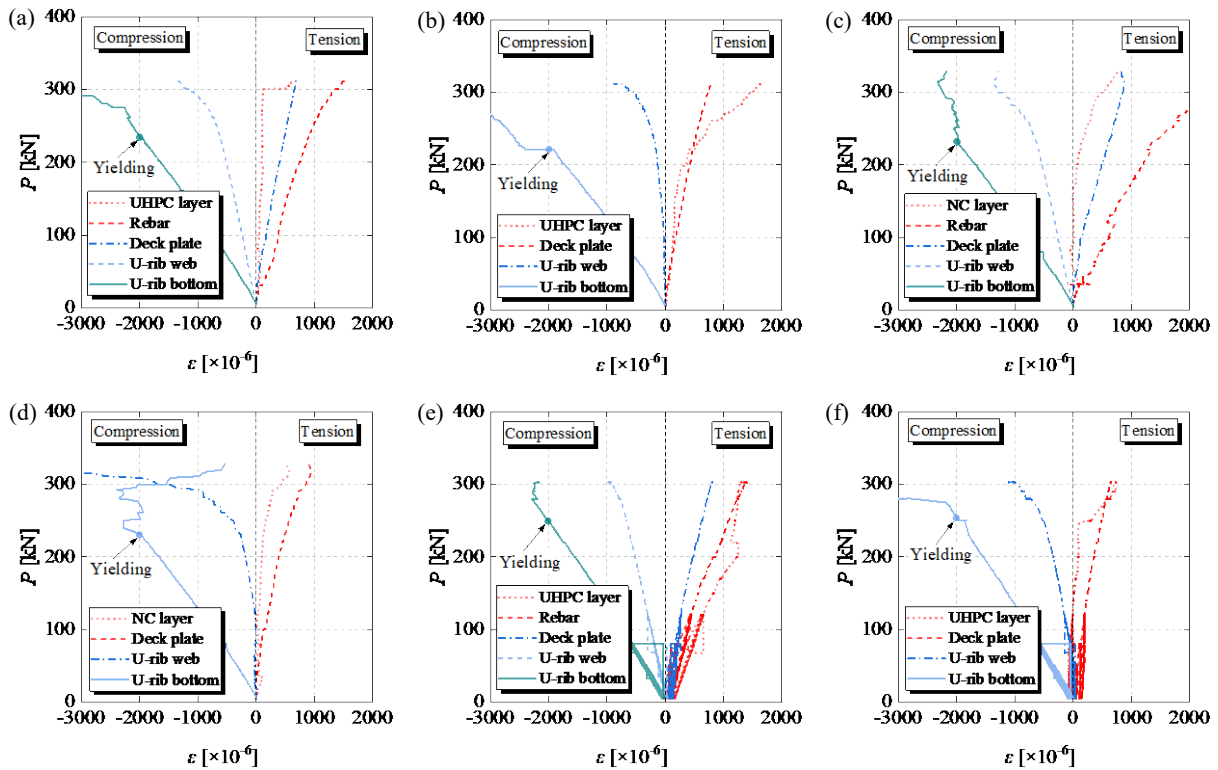
285 Specimens SN-3, SN-7, and SN-8 had the same reinforcement ratio ($\rho_s = 2.1\%$) and
 286 concrete cover ($c = 20$ mm). It can be observed that:

287 (1) Overall, the steel deck plate, steel rebar, and concrete overlay were subjected to
 288 tension, while the U-rib side was at compression. Additionally, the U-rib bottom reached
 289 yielding strain.

290 (2) The strain development in the cyclic loading specimens was generally similar to that
 291 of the monotonic loading specimen.

292 (3) The rebars in CA-UHPC specimens did not yield, while those in the NC specimen
 293 yielded. This discrepancy arises from the fact that NC loses its ability to withstand tension
 294 after cracking, transferring all the tension load to the rebars. Conversely, CA-UHPC maintains
 295 its capacity to sustain tension owing to the fiber-bridging effect, thereby delaying the onset of
 296 rebar yielding.

297



298

299 **Fig.10.** Load-strain curves: (a) SN-3-benchmark at mid-span cross-section; (b)

300 SN-3-benchmark at support cross-section; (c) SN-7-NC at mid-span cross-section; (d)

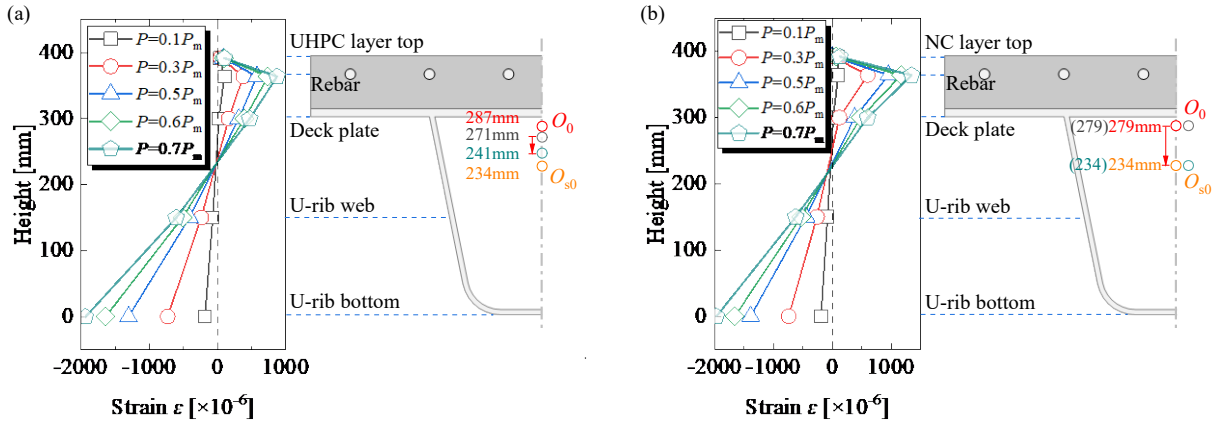
301 SN-7-NC at support cross-section; (e) SN-8-cyclic at mid-span cross-section; and (f)

302 SN-8-cyclic at support cross-section.

303

304 **Fig.11** shows the strain distributions along the section height at the mid-span
 305 cross-section. In the figure, O_0 and O_{s0} represent the centroid positions of the uncracked
 306 steel-concrete composite section (with SN-3 at 287 mm and SN-7 at 279 mm), and of the steel
 307 section (including steel rebar and steel plate, with SN-3 and SN-7 both at 234 mm),
 308 respectively.

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310

311 **Fig.11.** Strain distribution along the section height: (a) SN-3-benchmark; and (b) SN-7-NC.

312

313 It can be observed that:

314 As the load increased from $0.1P_m$ to $0.7P_m$, the strain distribution along the height
 315 direction followed a linear pattern (neglecting the concrete strains considering the significant
 316 scatter caused by concrete cracking). This indicated that the strain distribution conformed to
 317 the plane section assumption, and the arrangement of weld studs in the study can achieve a
 318 sound connection between the concrete overlay and the steel plate.

319 For the CA-UHPC specimen, as the load increased from $0.1P_m$ to $0.7P_m$, the neutral axis
 320 of the composite section obtained based on the strain distribution gradually decreased from
 321 271 mm to 241 mm, approaching the centroid location of the steel section (234 mm).
 322 Similarly, the neutral axis of the corresponding NC specimen dropped from 279 mm to 234
 323 mm. This demonstrated that CA-UHPC still contributes flexural stiffness to the composite
 324 section even after cracking compared to NC.

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326 3. Cracking behavior of CA-UHPC overlay

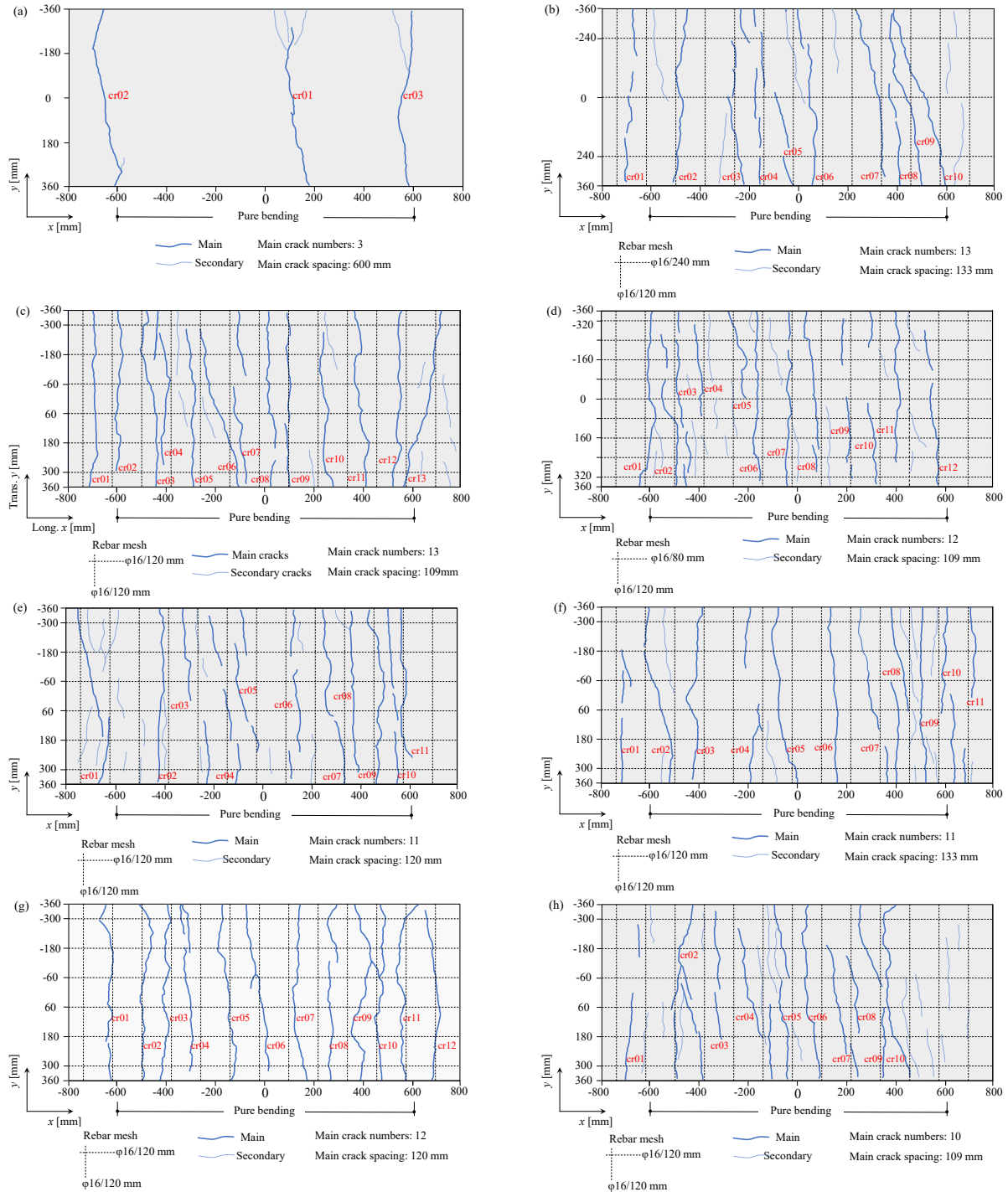
327 3.1 Crack patterns

328 No cracks at the concrete overlays were observed prior to the enforcement of external
 329 loads. **Fig.12** plots the overall crack distribution at the concrete top surface corresponding to
 330 the yielding point. In the figure, "cr+No." represents the main crack numbers, but does not
 331 indicate the emerging sequences. It was shown that:

332 (1) The rebar-reinforced CA-UHPC (R-CA-UHPC) overlays presented similar crack
 333 patterns, with uniformly distributed main cracks and densely distributed secondary cracks.
 334 Only three localized cracks developed at the CA-UHPC overlay without steel rebars. This

335 indicated that steel rebars are conducive to the transfer of tensile stress in the CA-UHPC
 336 overlay, preventing crack localization.

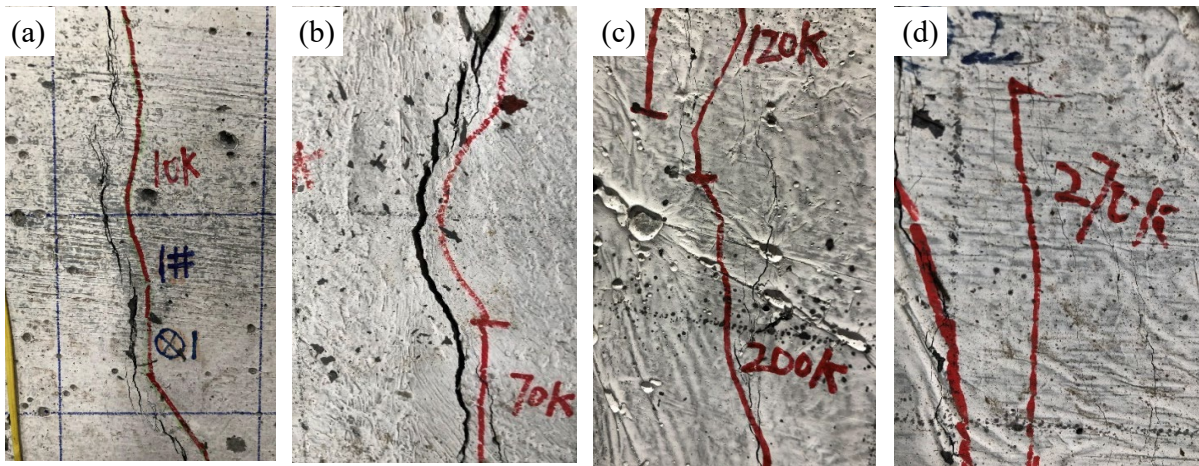
337 (2) The rebar-reinforced NC (R-NC) overlay displayed prominent primary cracks that
 338 fully penetrated in the transverse direction. Notably, there were no secondary cracks observed
 339 in the R-NC overlay. The different crack patterns observed between NC and CA-UHPC can
 340 be attributed to the fiber-bridging effect, which facilitates transferring tensile stress from local
 341 matrix cracks to the surrounding areas.



342
 343 **Fig.12.** Global crack patterns of the concrete overlays: (a) SN-1, no rebar; (b) SN-2, $\rho_s=1.1\%$,
 344 $c=20$ mm; (c) SN-3-benchmark, $\rho_s=2.1\%$, $c=20$ mm; (d) SN-4, $\rho_s=3.1\%$, $c=20$ mm; (e) SN-5,

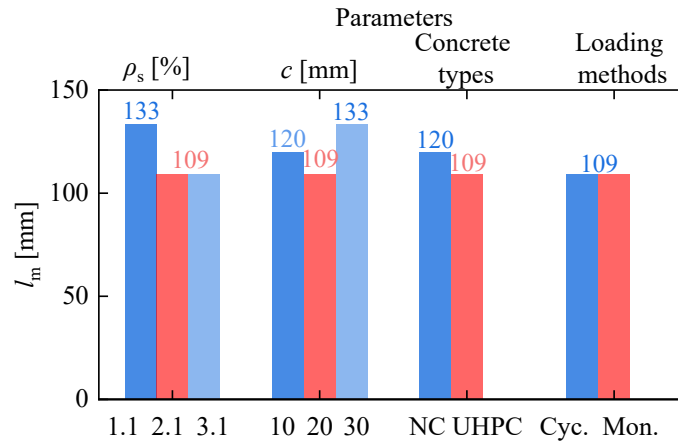
345 $\rho_s=2.1\%$, $c=10$ mm; (f) SN-6, $\rho_s=2.1\%$, $c=30$ mm; (g) SN-7, NC; and (h) SN-8, cyclic
346 loading.

347
348 **Fig.13** shows the local crack patterns of the concrete overlays. The R-NC overlay
349 exhibited a single localized feature with clear outlines. By comparison, the CA-UHPC overlay
350 performed a single crack accompanied by locally distributed micro-cracks, resulting in a more
351 dispersed crack outline and difficulties in crack width measurement. Moreover, the local crack
352 pattern of the R-CA-UHPC overlay can be further subdivided into two types. One exhibited a
353 "river bifurcation" characteristic, where one main crack was bifurcated into 2~3 fine cracks,
354 as shown in **Fig.13(c)**. The other was characterized by the smeared crack band composed of
355 multiple fine cracks, as plotted in **Fig.13(d)**. The distinctive crack features in the R-CA-UHPC
356 overlay were owing to the reinforcement-induced (including steel fibers as well as steel rebars)
357 stress redistribution in the CA-UHPC matrix.
358



359
360 **Fig.13.** Local crack patterns of the concrete overlays: (a) CA-UHPC without rebar; (b) R-NC;
361 (c) bifurcation feature for R-CA-UHPC; and (d) smeared feature for R-CA-UHPC.

362
363 **Fig.14** compares the average main crack spacing. Due to the random steel fiber
364 orientations and distributions, the main cracks of the R-CA-UHPC overlay were stochastically
365 distributed. Therefore, the selecting criteria for determining the main cracks were set as: (1)
366 locating at the pure bending zone; (2) exhibiting stable crack width widening; (3) for
367 bifurcation cracks or smeared cracks, only the main crack was considered and the
368 corresponding crack width should be greater than or equal to 0.05 mm.
369



370
371 **Fig.14.** Comparison of average main crack spacing.

372

373 As the reinforcement ratio increased, the average main crack spacing tended to decrease.
374 This can be explained by enhancing the reinforcement ratio helped reduce stress transfer
375 length between cracks. However, specimens with reinforcement ratios of 2.1% and 3.1% had
376 the same average main crack spacing of 109 mm, which may be influenced by factors such as
377 fiber distributions, shrinkage, and creep. The average main crack spacing increased with the
378 concrete cover, indicating a weakened constraint effect of steel rebars on the concrete top
379 surface. The influences of reinforcement ratio and concrete cover on the average main crack
380 spacing of CA-UHPC overlays are consistent with the conclusions obtained in previous
381 studies [28,29].

382 The average main crack spacing of CA-UHPC was relatively smaller than that of NC, as
383 mentioned earlier, due to the stress transfer by steel fibers. Moreover, cyclic loading had a
384 negligible effect on the average main crack spacing of the CA-UHPC overlay. Furthermore,
385 the average main crack spacing obtained in this experiment ranged from 109 to 133 mm,
386 which was close to the spacing of transverse rebars (120 mm). Although the transverse rebars
387 were placed below the longitudinal rebars in the study, it cannot be denied that the average
388 crack spacing was also affected by the transverse rebar arrangement. Some scholars [30] have
389 pointed out that the cracking of concrete bridge decks in steel-concrete composite beams
390 primarily occurred at the position of transverse rebars. In their experiments, the transverse
391 rebars were arranged closer to the tensile edge of the concrete deck than the longitudinal
392 rebars.

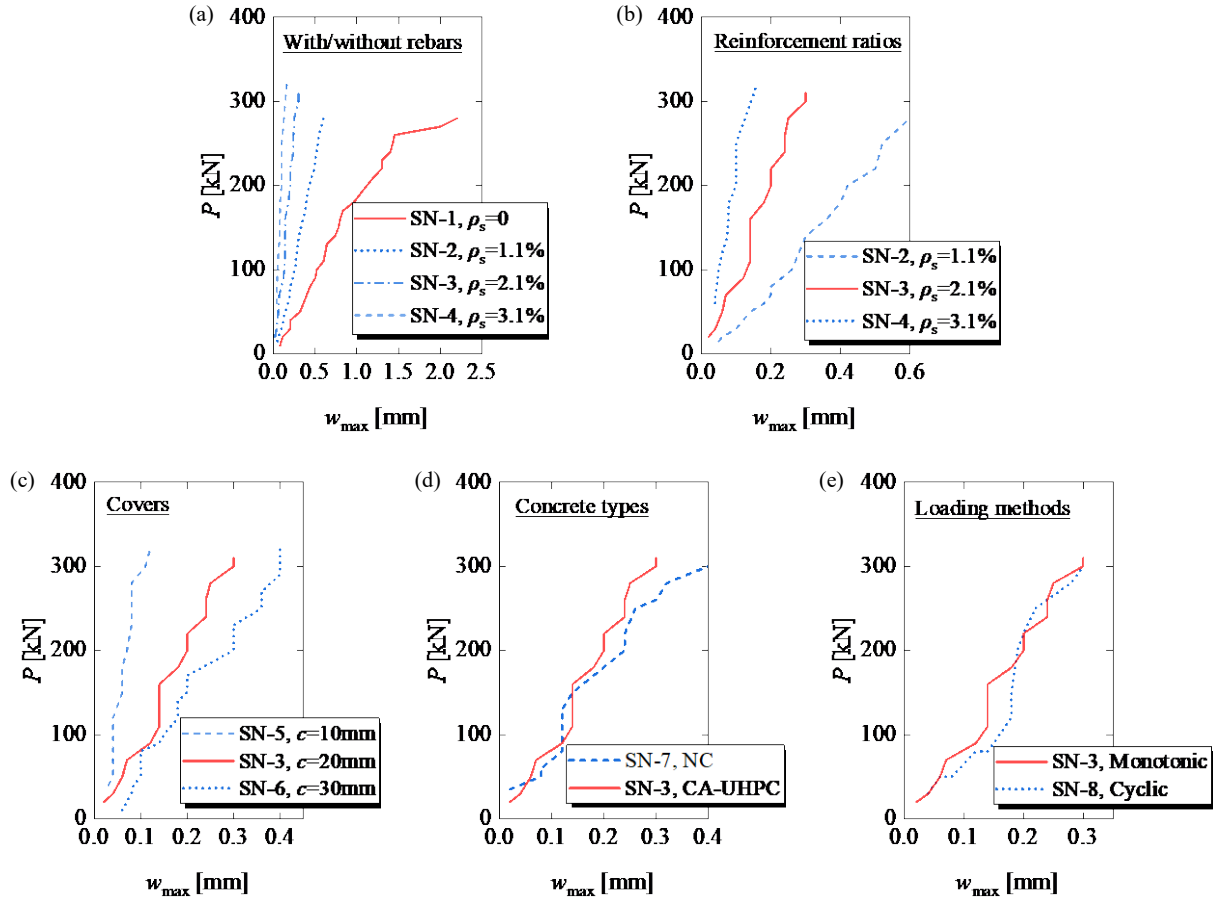
393 *3.2 Load-maximum crack width responses*

394 **Fig.15** compares the load-maximum crack width responses for specimens with different
395 parameters. It can be observed that:

396 (1) the crack width of reinforced specimens was significantly smaller than that of
397 unreinforced specimens. With an increase in reinforcement ratio (with the same concrete
398 cover), the maximum crack width gradually decreased.

399 (2) The maximum crack width increased along with the concrete cover due to the
400 weakened restraint effect of rebar on cracks. When reinforcement ratios exceed 2.1%,

401 maximum crack widths of CA-UHPC remain below 0.2 mm prior to U-rib yielding. (3) Under
 402 the same load (with the same reinforcement ratio and concrete cover), the maximum crack
 403 width of CA-UHPC was close to that of NC. (4) There was no significant difference in the
 404 maximum crack width development at cyclic tension compared to monotonic tension.
 405

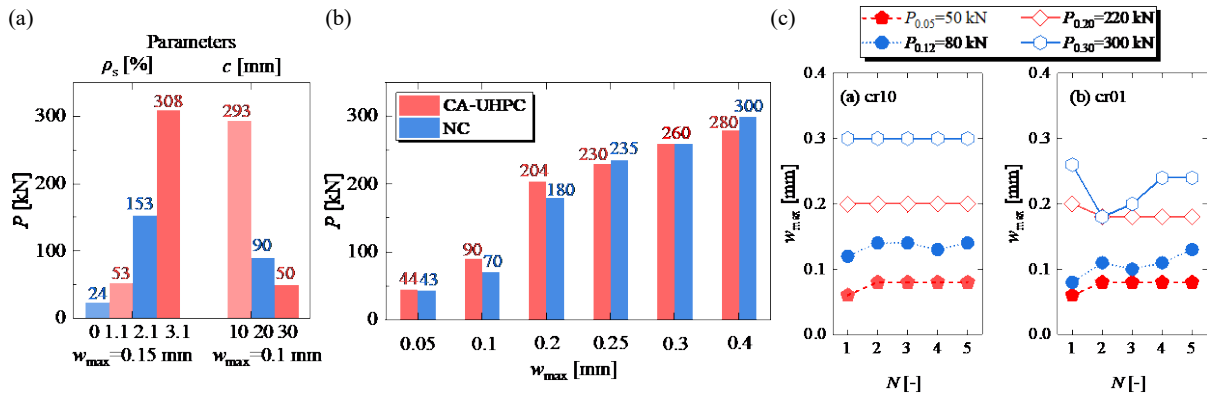


406
 407 **Fig.15.** Comparison of load-maximum crack width responses.
 408

409 **3.2.1 Parameter: reinforcement ratios and concrete covers**

410 **Fig.16(a)** compares the loads at characteristic maximum crack widths regarding
 411 reinforcement ratios and concrete covers. The loads for specimens with reinforcement ratios
 412 of 3.1%, 2.1%, and 1.1% were 13 times, 6 times, and 3 times the load of the unreinforced
 413 specimen, respectively. This indicated that increasing the reinforcement ratios significantly
 414 helps control the crack widths in the CA-UHPC overlay.

415 As the concrete cover decreased successively from 30 mm to 20 mm and 10 mm, the
 416 loads at maximum crack width of 0.1 mm increased by 80% and 486%, respectively. It was
 417 demonstrated that reducing the concrete cover contributes to restraining crack development.



418

419

420

421

422

Fig.16. Investigated parameters analysis: (a) influence of reinforcement ratios and concrete covers on characteristic loads; (b) influence of concrete types on characteristic loads; and (c) maximum crack width-cyclic number relationships at the peak loads.

423 3.2.2 Parameter: concrete types

424

425

426

427

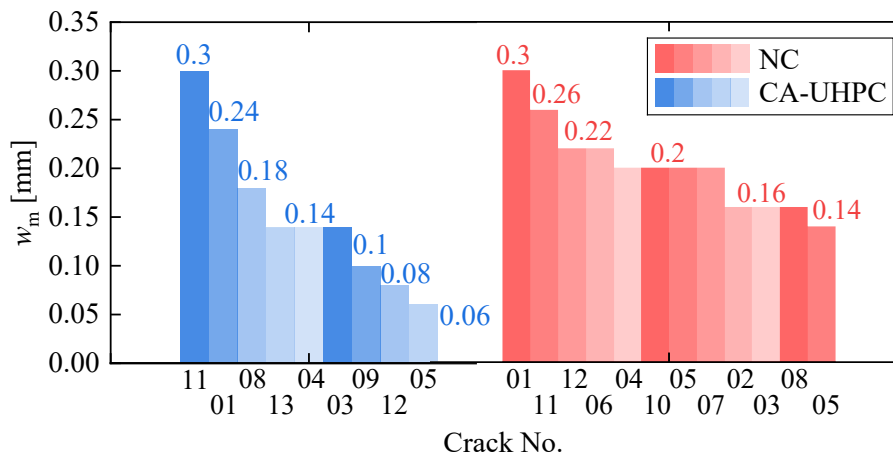
428

429

430

431

Fig.16(b) shows the load comparison between NC and CA-UHPC specimens at the same maximum crack widths. Notably, the disparity in loads appeared negligible. Moreover, **Fig.17** presents statistics on crack widths when the maximum crack width reaches 0.3 mm. The NC specimen exhibited 8 cracks with widths equal to or exceeding 0.2 mm, whereas the CA-UHPC specimen had only 2 such cracks. Considering both the loads and the overall number of cracks at characteristic widths, it becomes evident that CA-UHPC demonstrated significantly superior crack resistance compared to NC.



432

433

Fig.17. Crack statistics at a maximum crack width of 0.3 mm.

434

435 3.2.3 Parameter: loading methods

436

437

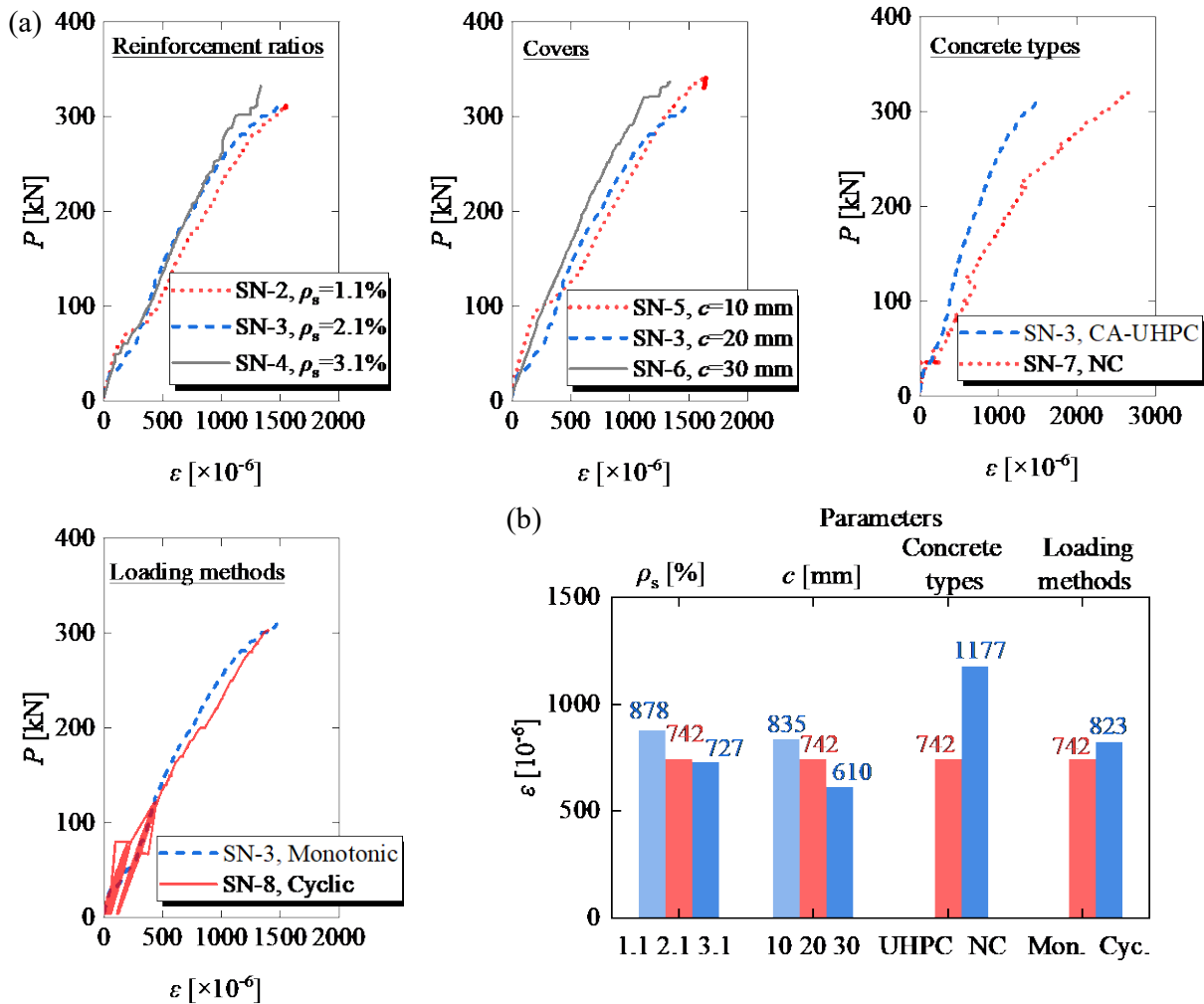
438

439

Fig.16(c) plots the maximum crack width against cyclic numbers at the peak load for cracks cr10 and cr01. It is clear that despite undergoing cyclic unloading and reloading, the maximum crack width at the peak load remained nearly constant. This suggests that finite cyclic loading-unloading has a negligible effect on the maximum crack width.

440 3.3 Load-rebar strain responses

441 Rebar strain can serve as an indirect indicator of the cracking behavior of reinforced
 442 concrete elements. Fig.18(a) compares the load-rebar strain curves of the tested specimens. In
 443 CA-UHPC specimens, the development of rebar strain remained relatively consistent with
 444 increasing loads, and the rebar did not yield. As for the NC specimen, the rebar strain
 445 demonstrated multiple instances of rebound owing to the cracking instability of NC.
 446 Moreover, the rebar yielded prior to reaching the peak load, indicating a more substantial
 447 involvement of rebar in tension in NC.
 448



449
 450 **Fig.18.** Comparisons of investigated parameters on: (a) load-rebar strain curves; and (b)
 451 rebar strain at $P=200$ kN.

452 Fig.18(b) illustrates the rebar strain comparison at $P=200$ kN (approximately
 453 corresponding to the yielding at the U-rib bottom). It can be observed that:

454 (1) Appropriately increasing the reinforcement ratio can reduce the rebar strain,
 455 mitigating the role of single reinforcement in restraining crack propagation.

456 (2) Increasing the concrete cover leads to the rebar closer to the neutral axis of the
 457 composite section, resulting in smaller strain and a corresponding weakening of its role in
 458 restraining crack development.

459 (3) The rebar strain in NC specimens was approximately 1.6 times that of the CA-UHPC
 460 specimens, indicating once again that NC contributes less to tensile resistance, and CA-UHPC
 461 can still provide excellent tensile resistance after cracking.

462 (4) Under cyclic loading, the rebar strain was slightly higher than that under monotonic
 463 loading, indicating the influence of the loading method was insignificant.

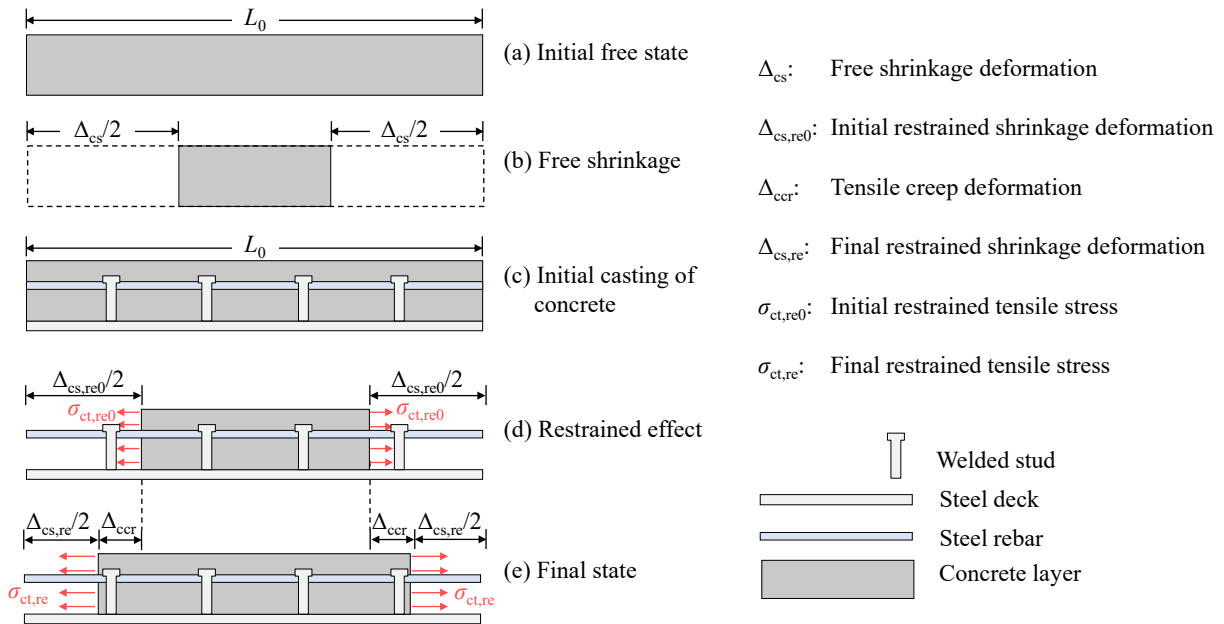
464

465 4. Restrained shrinkage effect analysis

466 4.1 Restrained shrinkage effect

467 **Fig.19** presents the schematic restrained shrinkage effect in the steel-UHPC composite
 468 deck. When casting UHPC overlay on the steel deck, the free shrinkage of UHPC is restrained
 469 by the steel deck as well as the embedded steel rebar. It should be noted that UHPC exhibits
 470 extremely high autogenous shrinkage but insignificant drying shrinkage at early ages, owing
 471 to a low w/b ratio and high fineness of its constituents [14,16]. Consequently, initial restrained
 472 tensile stress $\sigma_{ct,re0}$ develops in the UHPC. Moreover, the developed shrinkage deformation is
 473 further decreased due to the tensile creep properties of concrete material. The restrained
 474 shrinkage and tensile creep continue to develop over time, leading to the final restrained
 475 tensile stress $\sigma_{ct,re}$ and final restrained shrinkage strain $\epsilon_{cs,re}$ in the UHPC overlay. This
 476 mechanism provides a good explanation for the premature cracking of the CA-UHPC overlay
 477 stated in sec 2.2.2.

478



479

480

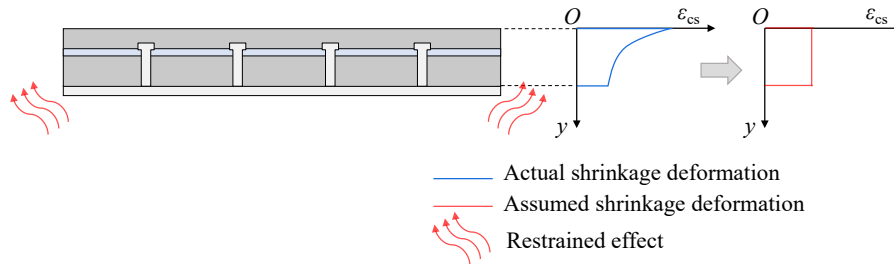
481

Fig.19. Schematic restrained shrinkage effect.

482 4.2 Theoretical derivation

483 To quantify the influence of the restrained shrinkage effect on the internal force
 484 redistribution in the tested specimens, theoretical derivation was conducted based on the

485 Trost-Bazant algebraic equations [31]. The lower-depth CA-UHPC overlay withstands
 486 stronger restraint from the steel deck compared with the upper overlay, therefore the
 487 non-uniform shrinkage develops over the CA-UHPC depth, as plotted in Fig.20. Considering
 488 the CA-UHPC overlay has a thick depth of 80 mm, a uniform shrinkage was assumed in the
 489 theoretical analysis. Additionally, the analysis exclusively addressed the impact of restrained
 490 shrinkage on axial strain, with the effect on cross-sectional curvature neglected.

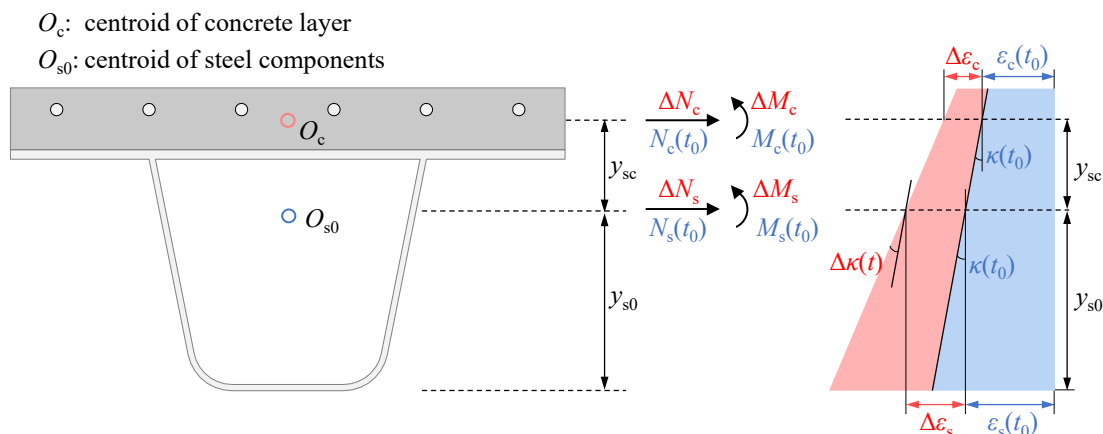


491
 492 **Fig.20.** Assumed shrinkage profile over the depth.
 493

494 **Fig.21** illustrates the schematic restrained-shrinkage-effect-induced internal force
 495 redistributions in a composite bridge deck, where O_c and O_{s0} represent the centroids of the
 496 CA-UHPC overlay and the steel component (including steel plates and rebars) respectively,
 497 and y_{sc} denotes the vertical distance between the two centroids. The cross-sectional area,
 498 moment of inertia, and elastic modulus for the concrete overlay are denoted as A_c , I_c , and E_c ,
 499 respectively, while those of the steel component are marked as A_s , I_s , and E_s , respectively.

500 At the onset of the steel-concrete composite interaction, denoted as time t_0 , the curvature
 501 of the cross-section is $\kappa(t_0)$, and the initial axial force and bending moment carried by the
 502 CA-UHPC overlay are denoted as $N_c(t_0)$ and $M_c(t_0)$ respectively, while that borne by the steel
 503 component is marked as $N_s(t_0)$ and $M_s(t_0)$ respectively. At this moment, the axial force and
 504 bending moment of the composite section are represented as $N(t_0)$ and $M(t_0)$ respectively, and
 505 their relations can be expressed as:

506



507

508 **Fig.21.** Schematic internal force redistributions in composite bridge deck induced by
 509 restrained shrinkage effect.

510

$$511 \quad N_c(t_0) + N_s(t_0) = N(t_0) \quad (3)$$

$$512 \quad M_c(t_0) + M_s(t_0) + N_s(t_0) \cdot y_{sc} = M(t_0) \quad (4)$$

513

514 As curing time progresses from t_0 to t , the internal forces distribution develops in the
 515 composite section due to the restrained shrinkage effect. Consequently, $N_c(t_0)$, $M_c(t_0)$, $N_s(t_0)$,
 516 and $M_s(t_0)$ become $N_c(t)$, $M_c(t)$, $N_s(t)$, and $M_s(t)$, respectively. However, the axial force and
 517 bending moment of the composite section remain unchanged. Therefore, the expression below
 518 is derived:

$$519 \quad \Delta N_c(t, t_0) + \Delta N_s(t, t_0) = 0 \quad (5)$$

$$520 \quad \Delta M_c(t, t_0) + \Delta M_s(t, t_0) + \Delta N_s(t, t_0) \cdot y_{sc} = 0 \quad (6)$$

521 where:

$$\Delta N_c(t, t_0) = N_c(t) - N_c(t_0)$$

$$522 \quad \Delta N_s(t, t_0) = N_s(t) - N_s(t_0) \quad (7)$$

$$\Delta M_c(t, t_0) = M_c(t) - M_c(t_0)$$

$$\Delta M_s(t, t_0) = M_s(t) - M_s(t_0)$$

523 The specimens were not subjected to external loads at the curing stage. The self-weight
 524 of the steel plates, rebars, and CA-UHPC overlays were carried by the steel structures. The
 525 self-weight can be neglected due to its relatively small effect. Therefore, $N(t_0)$, $N_c(t_0)$, $N_s(t_0)$,
 526 $M(t_0)$, $M_c(t_0)$, and $M_s(t_0)$ are all equal to 0. Hence, the following equations can be derived:

$$527 \quad N_c(t) + N_s(t) = 0 \quad (8)$$

$$528 \quad M_c(t) + M_s(t) + N_s(t) \cdot y_{sc} = 0 \quad (9)$$

529 According to the Trost-Bazant method, the algebraic equation represents the relationship
 530 between the strain increment induced by shrinkage and creep and the stress increment in
 531 concrete, as given by:

$$532 \quad \Delta \varepsilon_c(t, t_0) = \frac{\sigma_c(t_0)}{E_c} \cdot \varphi(t, t_0) + \frac{\Delta \sigma_c(t, t_0)}{E_c} \cdot [1 + \chi(t, t_0) \cdot \varphi(t, t_0)] + \varepsilon_{cs}(t, t_0)$$

533 (10)

534 where: $\sigma_c(t_0)$ is the concrete stress at time t_0 ; $\Delta \sigma_c(t, t_0)$ is the stress increment of concrete from
 535 t_0 to t ; $\chi(t, t_0)$ is the aging coefficient for concrete, a parameter less than 1.0; $\varphi(t, t_0)$ is the creep
 536 coefficient for concrete; $\varepsilon_{cs}(t, t_0)$ is the free shrinkage strain.

537 As demonstrated in Sec.2.2.3, the designed stud arrangement ensures a perfect
 538 connection between the steel component and the CA-UHPC overlay. Therefore, two
 539 deformation compatibility conditions are satisfied:

540 (1) The strain increment of CA-UHPC overlay at the centroid of the steel component
 541 should be equal to the strain increment of steel;

542 (2) The curvature increment of the CA-UHPC overlay should be equal to that of the steel
 543 component.

544 These conditions can be expressed as:

$$545 \quad \Delta \varepsilon_{cN}(t, t_0) + \Delta \varepsilon_{cM}(t, t_0) + \varepsilon_{cs}(t, t_0) = \Delta \varepsilon_s(t, t_0) \quad (11)$$

546
$$\Delta\kappa_c(t, t_0) = \Delta\kappa_s(t, t_0) \quad (12)$$

547 The Trost-Bazant-algebraic-equation-based deformation compatibility equations are
548 given as:

549
$$\frac{N_c(t)[1 + \chi(t, t_0) \cdot \varphi(t, t_0)]}{E_c A_c} + \frac{y_{sc} \cdot M_c(t)[1 + \chi(t, t_0) \cdot \varphi(t, t_0)]}{E_c I_c} + \varepsilon_{cs}(t, t_0) = \frac{N_s(t)}{E_s A_s}$$

550 (13)

551
$$\frac{M_c(t)[1 + \chi(t, t_0) \cdot \varphi(t, t_0)]}{E_c I_c} = \frac{M_s(t)}{E_s I_s} \quad (14)$$

552 From Eq.(9), $M_s(t) = -(M_c(t) + N_s(t)y_{sc}) = N_c(t)y_{sc} - M_c(t)$ was obtained. Substituting it into
553 Eq.(14), gives the bending moment of the CA-UHPC overlay at time t :

554
$$M_c(t) = \frac{N_c(t) \cdot y_{sc} \cdot E_c I_c}{[1 + \chi(t, t_0) \cdot \varphi(t, t_0)] E_s I_s + E_c I_c} \quad (15)$$

555 Substituting Eq.(15) into Eq.(13), gives the axial force of the CA-UHPC overlay at time
556 t :

557
$$N_c(t) = \frac{-\varepsilon_{cs}(t, t_0)}{\frac{1 + \chi(t, t_0) \cdot \varphi(t, t_0)}{E_c A_c} + \frac{[1 + \chi(t, t_0) \cdot \varphi(t, t_0)] y_{sc}^2}{[1 + \chi(t, t_0) \cdot \varphi(t, t_0)] E_s I_s + E_c I_c} + \frac{1}{E_s A_s}}$$

558 (16)

559 Hence, the restrained tensile stress generated in the CA-UHPC overlay can be expressed
560 as:

561
$$\sigma_{ct, re}(t) = \frac{N_c(t)}{A_c} \pm \frac{M_c(t) \cdot y_c}{I_c} \quad (17)$$

562 Where: y_c is the vertical distance from any point in the CA-UHPC overlay to its neutral
563 axis.

564 4.3 Discussions and verification

565 It should be noted that the Trost-Bazant algebraic equation is suitable for predicting
566 long-term strain and stress increments caused by shrinkage and creep (long-term performance)
567 in NC structural elements. Consequently, the elastic modulus of concrete E_c in the equation is
568 commonly assumed to remain constant under standard curing for 28 days. Moreover, given
569 the progressive aging of concrete during service life, the aging coefficient $\chi(t, t_0)$ typically
570 tends to be less than 1. Furthermore, the tension capacity of NC is often disregarded, resulting
571 in the adoption of compressive creep coefficient $\varphi(t, t_0)$.

572 Compared with conventional NC structural members, the investigated steel-CA-UHPC
573 composite bridge deck has distinct characteristics as follows:

574 (1) The shrinkage observed in CA-UHPC during the curing stage is predominantly
575 autogenous shrinkage, rather than long-term drying shrinkage. Throughout this period, the
576 elastic modulus of CA-UHPC evolves continuously with age, leading to a non-constant elastic
577 modulus.

578 (2) During the curing stages, CA-UHPC remains in a state of fresh concrete, thus the

579 consideration of aging characteristics is unnecessary.

580 (3) Creep refers to the tensile creep due to the restrained tensile stress.

581 The basic parameters in Eq.(16) can be obtained:

582 Parameter 1: The initial interactive time t_0 for steel and CA-UHPC was taken as 0.5d
 583 (half a day), according to the firth author's previous study [32]. The end of curing time t was
 584 37 days.

585 Parameter 2: Elastic modulus E_c was taken as the equivalent average elastic modulus
 586 $E_{c,eq}$ at the curing stage [32], $E_{c,eq}=0.962E_{c,28}$, where $E_{c,28}$ is the elastic modulus under
 587 standard curing for 28 days. Here, $E_{c,28}$ was taken from Table 3. The definition of equivalent
 588 average elastic modulus is shown in Fig.22(a).

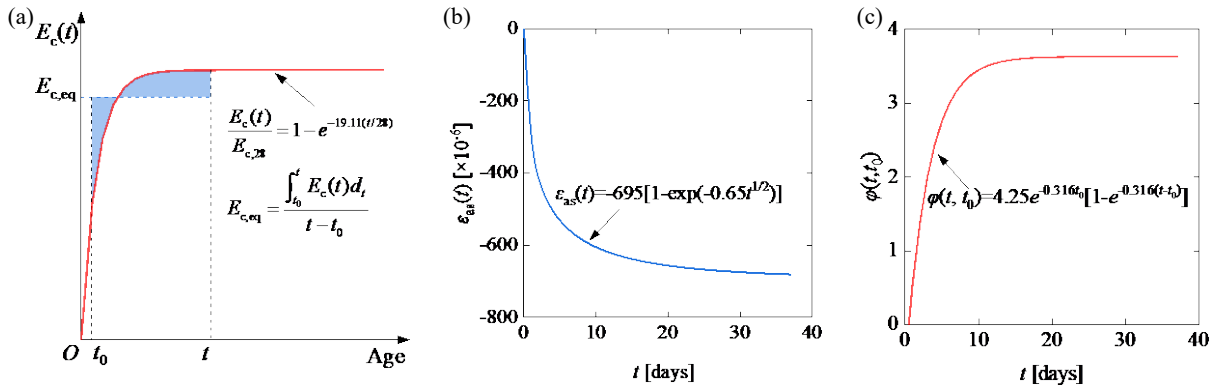
589 Parameter 3: Free shrinkage $\varepsilon_{cs}(t, t_0)$ was taken as $-681\mu\epsilon$ [32], shown in Fig.22(b).

590 Parameter 4: Tensile creep coefficient $\varphi(t, t_0)$ was taken as 3.629 [32], shown in Fig.22(c).

591 Parameter 5: Aging coefficient $\chi(t, t_0)$ was assumed to be 1.0 considering without aging
 592 process at the curing stage.

593 Substituting the parameters 1~5 into Eq.s(15)~(17), the theoretical restrained tensile
 594 stresses can be obtained.

595



596

597 **Fig.22.** Time-dependent models for CA-UHPC [32]: (a) elastic modulus; (b) autogenous
 598 shrinkage; and (c) Tensile creep coefficient.

599

600 According to Eq.(2) and the measured initial cracking load P_{cr} listed in Table 7, the
 601 initial cracking strength of the CA-UHPC overlay is given:

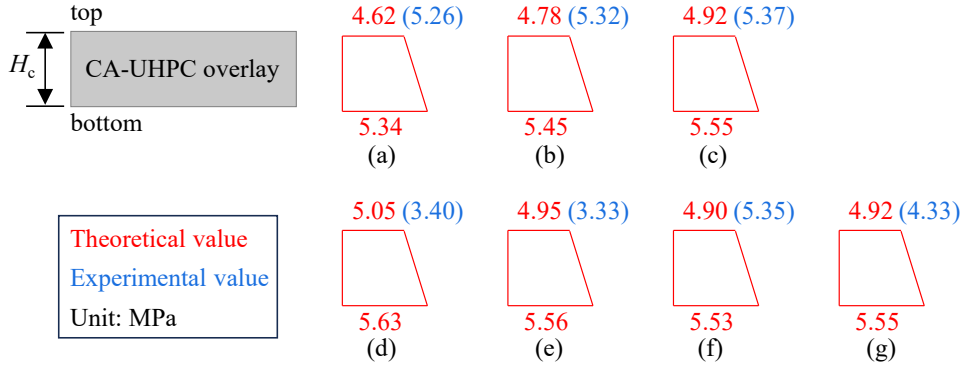
602
$$f_{cr} = \frac{P_{cr} L_0 y_{c0}}{\alpha_E I_0} \quad (18)$$

603 Therefore, the experiment-based restrained tensile stress can be calculated as:

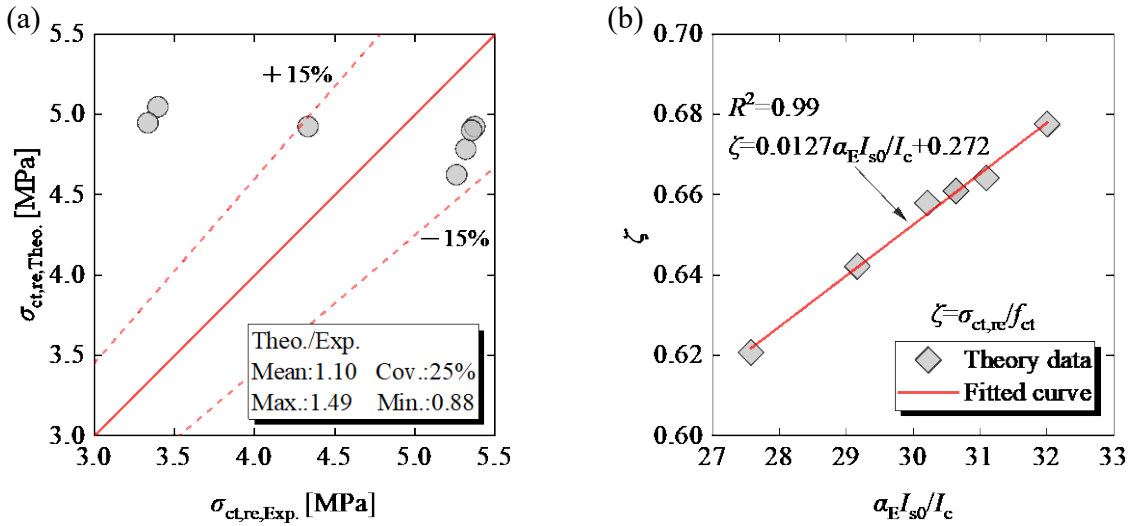
604
$$\sigma_{ct, re} = f_{ct} - f_{cr} \quad (19)$$

605 The restrained tensile stress distribution over the depth is plotted in Fig.23. Fig.24(a)
 606 compares the theoretical and experimental restrained tensile stresses. As indicated, the mean
 607 value of the ratio between theoretical and experimental restrained tensile stresses was 1.10,
 608 with a coefficient of variation of 23%, thereby confirming the validity of the theoretical
 609 derivation.

610



611
 612 **Fig.23.** Restrained tensile stress distribution over the depth: (a) SN-1, no rebar; (b) SN-2,
 613 $\rho_s=1.1\%$, $c=20$ mm; (c) SN-3-benchmark, $\rho_s=2.1\%$, $c=20$ mm; (d) SN-4, $\rho_s=3.1\%$, $c=20$ mm;
 614 (e) SN-5, $\rho_s=2.1\%$, $c=10$ mm; (f) SN-6, $\rho_s=2.1\%$, $c=30$ mm; and (g) SN-8, $\rho_s=2.1\%$, $c=20$ mm,
 615 cyclic loading.



617
 618 **Fig.24.** Theoretical analysis: (a) comparison between experimental and theoretical
 619 restrained tensile stresses; (b) fitted relation between restrained degree and steel-concrete
 620 bending stiffness ratio.

621
 622 To further quantify and predict the restrained effect of the composite deck, the concept of
 623 restrained degree ζ , which was defined as the ratio of restrained tensile stress (theoretical
 624 values) to the tensile strength of concrete was proposed, as expressed below.

625

$$\zeta = \frac{\sigma_{ct, re}}{f_{ct}} \quad (19)$$

626 The relationship between the restrained degree ζ and the ratio of steel-concrete bending
 627 stiffness $\alpha_E I_{s0}/I_c$ was formulated and illustrated in Fig.24(b). A fitted function, denoted as the
 628 restrained shrinkage model and described by Eq.(20), was derived for this purpose. Given the
 629 specified material properties (E_s , E_c , and f_{ct}) and geometric properties (I_{s0} and I_c), the
 630 restrained shrinkage model can be applied to predict the restrained tensile stresses and the
 631 initial cracking loads of the composite deck.

632
$$\zeta = 0.0127\alpha_E I_{s0} / I_c + 0.272 \quad (20)$$

633 **5. Conclusions**

634 Based on the above investigations, the main conclusions are:

- 635 (1) The flexural-tension behavior of steel-concrete composite decks is characterized by
636 four distinct stages: elastic response, concrete cracking, U-rib yielding and buckling,
637 and ultimate failure. Notably, the yielding of U-ribs, rather than concrete cracking,
638 significantly contributes to stiffness reduction. Furthermore, the buckling of U-ribs at
639 support sections determines the load-bearing capacity of the composite deck.
- 640 (2) The synergistic reinforcement of steel fibers and steel rebars in the R-CA-UHPC
641 overlay promotes the formation of uniform global crack patterns and distinctive local
642 crack distributions characterized by river bifurcation or crack bands. Conversely, the
643 R-NC overlay displays prominent main cracks with well-defined outlines.
644 Additionally, while steel rebars in the NC overlay undergo yielding, those in the
645 CA-UHPC overlay remain unyielded.
- 646 (3) Increasing reinforcement ratios or reducing concrete covers helps to control the
647 maximum crack widths of the CA-UHPC overlay. When reinforcement ratios exceed
648 2.1%, maximum crack widths of CA-UHPC remain below 0.2 mm prior to U-rib
649 yielding. Limited numbers of cyclic tension yield a negligible impact on crack
650 patterns and maximum crack widths of the CA-UHPC overlay.
- 651 (4) The presence of steel plates and rebars restrains the free shrinkage of the CA-UHPC
652 overlay, resulting in restrained tensile stress at the curing stage and premature
653 cracking under external loads. The Trost-Bazant-algebraic-equations-based
654 theoretical analysis was conducted to quantify the restrained shrinkage-induced
655 internal force/stress redistributions in the composite section. Subsequently, a
656 restrained shrinkage model was developed to predict both the restrained tensile
657 stresses and the initial cracking loads of the composite deck.

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