

emerged as an effective method (Frenge et al. 2019; Zadeh et al. 2020).

Recent deep learning applications have shown promise for various soil-related processes, including nutrient levels (Sapkota et al. 2023).

In soil temperature prediction, a study compared Multiple Linear Regression (MLR) with Artificial Neural Networks (ANN) and Fuzzy Inference System (ANFIS) (Sapkota et al. 2023). Subsequent studies have demonstrated various applications, including crop yield prediction (Sapkota et al. 2023).

Most recent studies have shown that deep learning models, such as Gradient Boosting (XGBoost) and Random Forest (RF), outperform traditional models like Multiple Linear Regression (MLR) and Support Vector Machines (SVM) in soil temperature prediction (Sapkota et al. 2023).

Conventional AI approaches for soil temperature forecasting primarily focus on time series data, often overlooking the complex relationships between variables. This issue is addressed through copula mathematical framework for multivariate dependencies by coupling marginal distributions (De Michele and Salvadori 2003; De Michele et al. 2007).

Recent applications demonstrate copulas' unique ability to handle multivariate dependencies in environmental systems (Zhang et al. 2019; Lü et al. 2020).

While offering improved accuracy, these methods often require extensive data and computational resources. However, despite the proliferation of deep learning models (e.g., LSTMs, CNNs) and their application in environmental modeling, no comprehensive study has yet compared their relative efficacy for soil temperature prediction at multiple depths and time horizons.

This study addresses the knowledge gap, as existing standalone AI approaches (like ANNs) or Deep ESNs (Alizamir et al. 2021) rely solely on copula applications without considering the

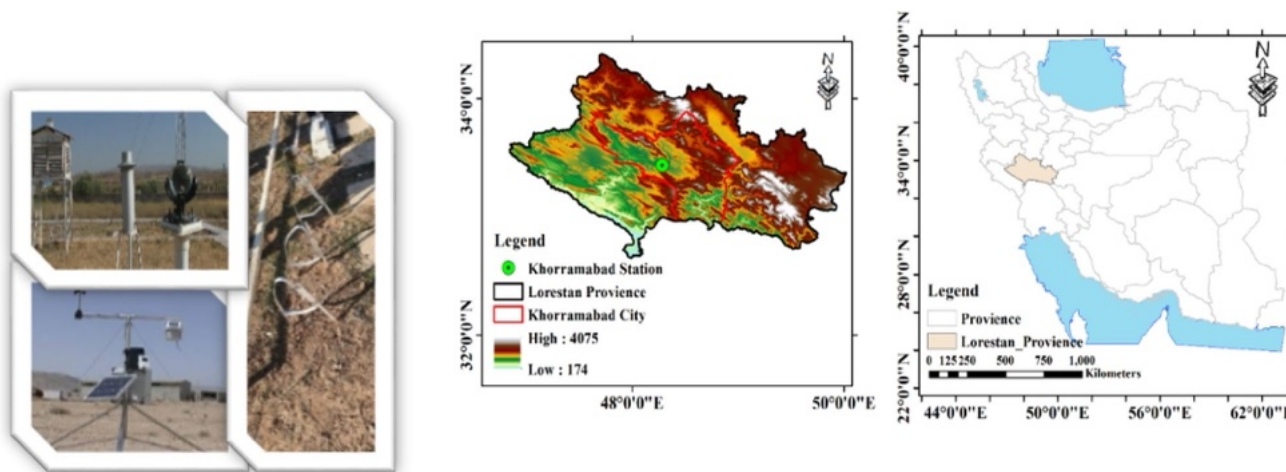


Fig. 1 Location of Khorramabad station in Iran

Table 1 Statistics of the considered variables observed at a daily station for the Khorramabad station

Variables	Depth	Mean	Standard deviation	Skewness
Soil temperature (°C)	10 cm	21.18	1.43	0.21
	30 cm	20.08	1.07	0.08
	50 cm	20.17	0.97	0.08
	Air temperature (°C)	17.33	3.94	0.02
Relative humidity (%)	44.80	9.96	0.24	
Wind speed – (m/s)	6.22	2.39	1.50	
Sunny hours (hr)	8.44	3.60	-0.85	
Rain (mm)	-	1.29	5.02	6.95

variations, with a mean of 17.33°C, indicating a mild thermal gradient. The relative humidity is at 44.80%, reflecting a relatively moderate and humid environment, while wind speed averages 6.22 m/s, with a skewness of 1.50, indicating occasional strong gusts. The average of 8.44 sunny hours per day, combined with a significant positive skewness (6.95) in rainfall, suggests the region experiences long but intense rainfall events.

2.2 Deep learning models

Deep learning is a specialized machine learning approach that focuses on learning from data by emphasizing multiple levels of abstraction (Chollet 2017; Alzubaidi et al. 2021). This study utilizes three deep learning models: Convolutional Neural Network (CNN), Long Short-Term Memory (LSTM), and Recurrent Neural Network (RNN).

Short-Term Memory (LSTM), and Recurrent Neural Network (RNN).

2.2.1 Convolutional neural network (CNN) model

Convolutional Neural Networks (CNNs) have shown success in computer vision, but their application in analyzing time-series data is limited due to the spatial dimensionality of the input. CNNs include convolutional filters to process input data, which are applied across the time series, reducing the risk of overfitting (Ghani et al. 2025).

2.2.2 Long Short-Term Memory (LSTM) model

The LSTM model is designed to handle time lags that traditional RNNs cannot, as it overcomes the issue of vanishing gradients by introducing a novel unit structure called the LSTM cell (Hochreiter and Bengio 1997). This architecture enables LSTM to capture long-term dependencies in time-series data (Kizito et al. 2021; Al-Musa et al. 2025).

Fig. 2 Schematic of a Convolutional Neural Network (CNN) architecture. The network processes input data through successive layers, including convolution with ReLU activation, pooling and fully connected layers for feature extraction and classification.

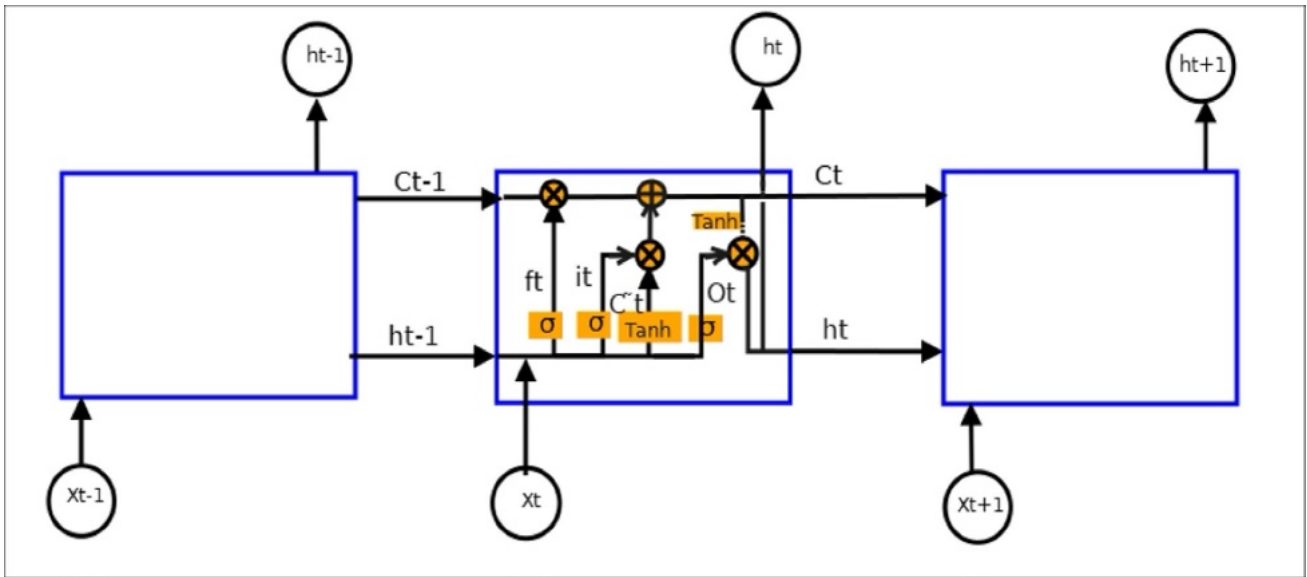
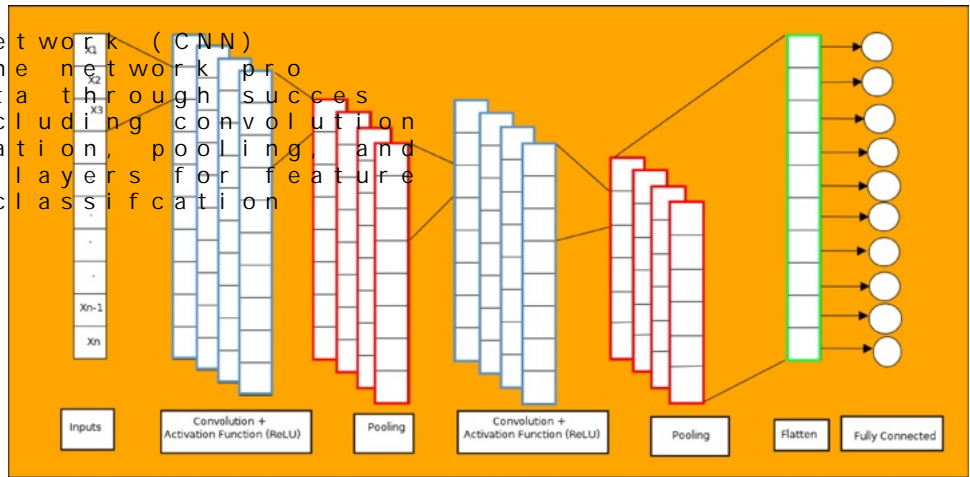


Fig. 3 Structure of an LSTM unit, highlighting the flow of information between hidden states (h_{t-1} , h_t , h_{t+1}) and cell states (C_{t-1} , C_t , C_{t+1}). The architecture highlights the flow of information through the LSTM unit.

LSTM architecture, and how information flows through the hidden states and gates. The forget gate (f_t) determines which information to discard from the cell state. The input gate (i_t) determines which new information to store in the cell state. The output gate (o_t) determines which part of the cell state to output. The cell state (C_t) is updated based on the forget gate, the input gate, and the current cell state. The hidden state (h_t) is calculated based on the cell state and the output gate.

2.2.3 Gated recurrent unit (GRU) model

The GRU is a variant of gated recurrent unit (GRU) model. It simplifies the design by combining the forget and input gates.

Table 2 Comparative analysis of LSTM, GRU, and CNN architectures for soil temperature prediction

Component	LSTM	GRU	CNN
Input features	Air temperature, sunshine duration, relative humidity (Kendall's Tau-selected)	Same as LSTM	Same as LSTM
Data preprocessing	Handle missing values, Data-target variable creation	Same as LSTM	Same as LSTM
Model architecture	3 layers, 1 Dropout (50%), 1 Dense output	GRU layers, 1 Dropout (50%), 1 Dense output	1D Conv, 1D Pool, 1D Global Average Pooling
Key parameters	Units: 50, Dropout: 50%, Adam optimizer, MAE loss	Units: 50, Dropout: 50%, Adam optimizer, MAE loss	Filters: 1, 3, 5, Pool sizes: 2, 2, Adam optimizer, MAE loss
Training	Batch size: 5, Epochs: 50	Same as LSTM	Same as LSTM

Each tree represents the trees that are constructed for each tree. In the D-vine, nodes are connected to more than two edges, and each node is connected to $n-j$ edges, and each tree. The n -dimensional

$$\prod_{k=1}^n f(x_k) \prod_{j=1}^{n-1} \prod_{i=1}^{n-j} c_{i,j+i|1,\dots,j-1} \{F(x_j|x_1, \dots, x_{j-1}), F(x_{j+i}|x_1, \dots, x_{j-1})\} \tag{3}$$

2.5.1 Conditional density in the 4-dimensional case

Upon selecting the vine copula, the conditional density function and assess soil temperature at chosen dependent variables (Rachdawong et al., 2020). The conditional probability density function can be determined using the following formula. This method enables a more accurate representation of temperature variations at different locations by capturing the interdependencies among the

variables $U_j = F_{X_j}(x_j)$ that are d-dimensional copula function:

$$C_{U_1, \dots, U_n}(F_{X_1}(x_1), \dots, F_{X_n}(x_n)) = F_{X_1, \dots, X_n}(x_1, \dots, x_n) \tag{1}$$

According to Nelsen (2006), parameter estimation is crucial in implementing copula functions.

This challenge can be addressed by using the diagonal section of the copula, as suggested by Salvadori et al. (2007) and Jaworski and Ebrahimi (2010). Bivariate copulas are typically employed. However, higher dimensions, more complex structures like nested vine copulas are recommended (Samarayasinghe et al., 2020; Nazeri et al., 2022). In this study, vine copulas can be constructed in various ways, categorized into D-type, C-type, and R-type (Rambaldi et al., 2013). Among these, the D-vine is the most commonly identified and described in the literature (Samarayasinghe et al., 2020). They are used to model the joint density of an n -dimensional random vector (X_1, \dots, X_n) corresponding to a D-vine structure as follows:

$$\prod_{k=1}^n f(x_k) \prod_{j=1}^{n-1} \prod_{i=1}^{n-j} c_{i,j+i|1,\dots,i+j-1} \{F(x_i|x_{i+1}, \dots, x_{i+j-1}), F(x_{j+i}|x_{i+1}, \dots, x_{i+j-1})\} \tag{2}$$

$$c(u_4|u_1, u_2, u_3) = \frac{\partial^4 C(u_1, u_2, u_3, u_4)}{\partial u_1 \partial u_2 \partial u_3 \partial u_4} \Big|_{u_1, u_2, u_3} \tag{4}$$

Specifically, u_1, u_2, u_3 are T, Sun, and RH, respectively, and u_4 is soil temperature. To obtain u_1 sample pairs, the following dependency

is used: Sample $u_j \sim U[0,1]$, $j=1, \dots, 3$, then $u_4 = C_{2,1,1}^{-1}(u_2|u_1, u_3)$. However, for $n > 3$, the diagonal section of the copula is used to estimate the parameters of the bivariate copulas. For example, $u_4 = C_{1,1,1,1}^{-1}(u_4|u_1, u_2, u_3)$.

Among these, the D-vine is the most commonly identified and described in the literature (Samarayasinghe et al., 2020). They are used to model the joint density of an n -dimensional random vector (X_1, \dots, X_n) corresponding to a D-vine structure as follows: complex, high-dimensional dependencies. They decompose multivariate distributions into bivariate copulas (pairwise dependencies) and a graphical model called a "vine representation of asymmetric,

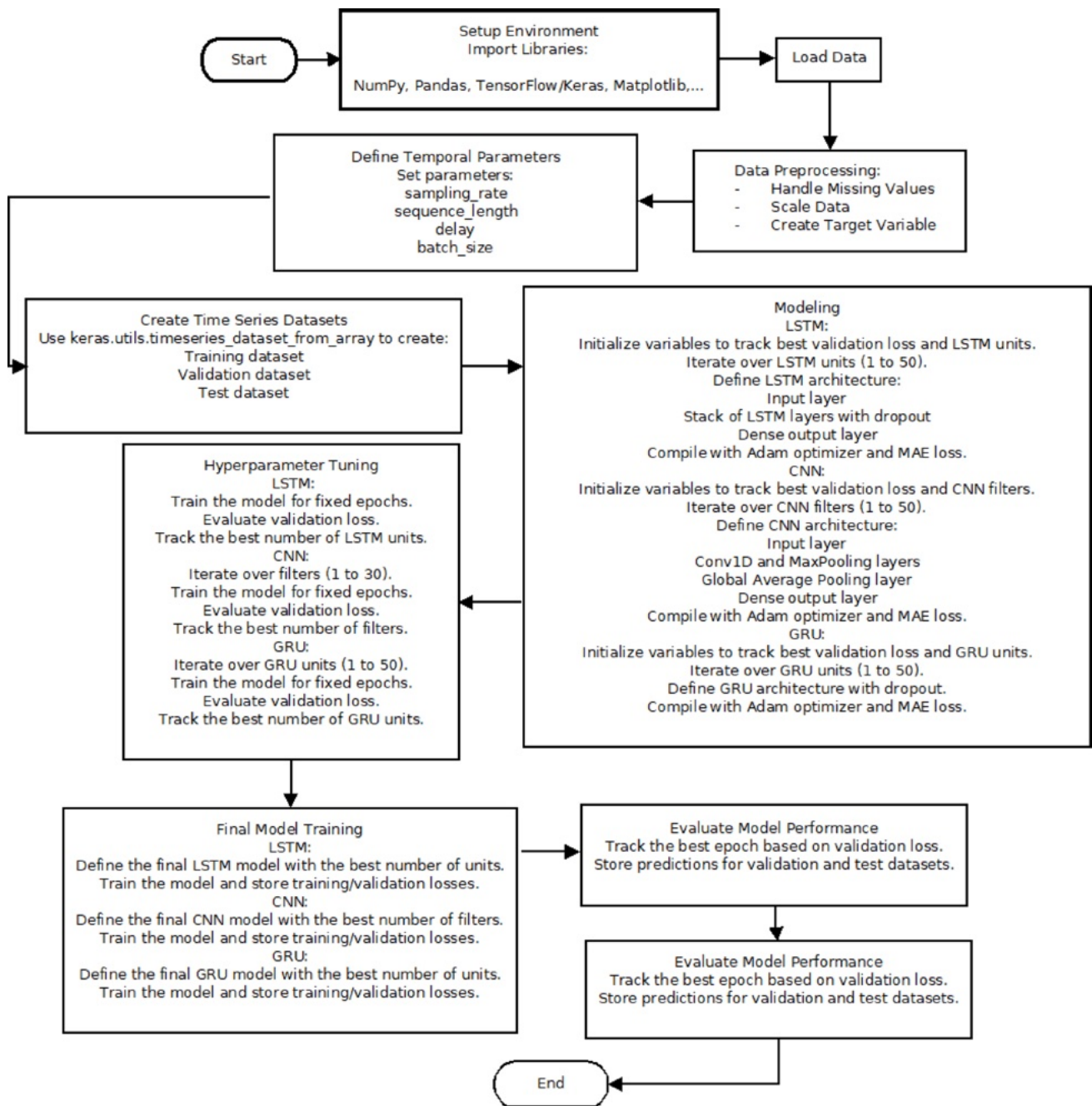


Fig. 5 End-to-end workflow for time series models (LSTM, CNN, and GRU architectures). The diagram illustrates the process from data loading and preprocessing to final model training and evaluation. It includes steps for defining temporal parameters, creating time series datasets, modeling (LSTM, CNN, and GRU), hyperparameter tuning, final model training, and evaluating model performance.

relationships that traditional models (e.g., Gaussian) cannot capture. These relationships often involve nonlinear interactions across different time windows (e.g., deeper layers in neural networks). The proposed model is designed to surface variations in these nuanced dependencies.

Unlike conventional time-series models (e.g., ARIMA) or machine learning (e.g., ANN), vine copulas

2.6 Model evaluation criteria

3 Results and discussion

The Root Mean Square Error (RMSE), Nash-Sutcliffe efficiency coefficient (NSE), and Mean Absolute Error (MAE) are widely used metrics for comparing the performance of studied models and evaluating their forecast results. These statistical measures provide insights into the accuracy and reliability of the forecasting model (Zhang and Singh 2008).

$$RMSE = \sqrt{\frac{1}{N} \sum_{i=1}^N (x_i - y_i)^2} \tag{6}$$

$$MAE = \frac{1}{N} \sum_{i=1}^N |x_i - y_i| \tag{7}$$

$$NSE = 1 - \frac{\sum_{i=1}^N (x_i - y_i)^2}{\sum_{i=1}^N (x_i - x_{ave})^2} \tag{8}$$

where y_i and x_{ave} are equal to the simulated and observed values, respectively. x_{ave} is also the average of observed values. The analysis is focused on the study area, covering a period of 365 days on a daily scale. Forecasting horizons of 1, 3, 5, and 7 days were examined and validated for forecasting meteorological variables and soil temperature. Based on the highest Kendall's tau-B correlation coefficient (0.6), the model was selected for air temperature and solar radiation influencing predictions of precipitation can be excluded from the trend analysis. The model was determined based on a Kendall's tau-B correlation coefficient of 0.4 (Nazeri et al. 2023). The model was selected for variables with a dependence on the meteorological and forecasting of soil temperature intervals (1, 3, 5, and 7 days) in the deep learning models and tree

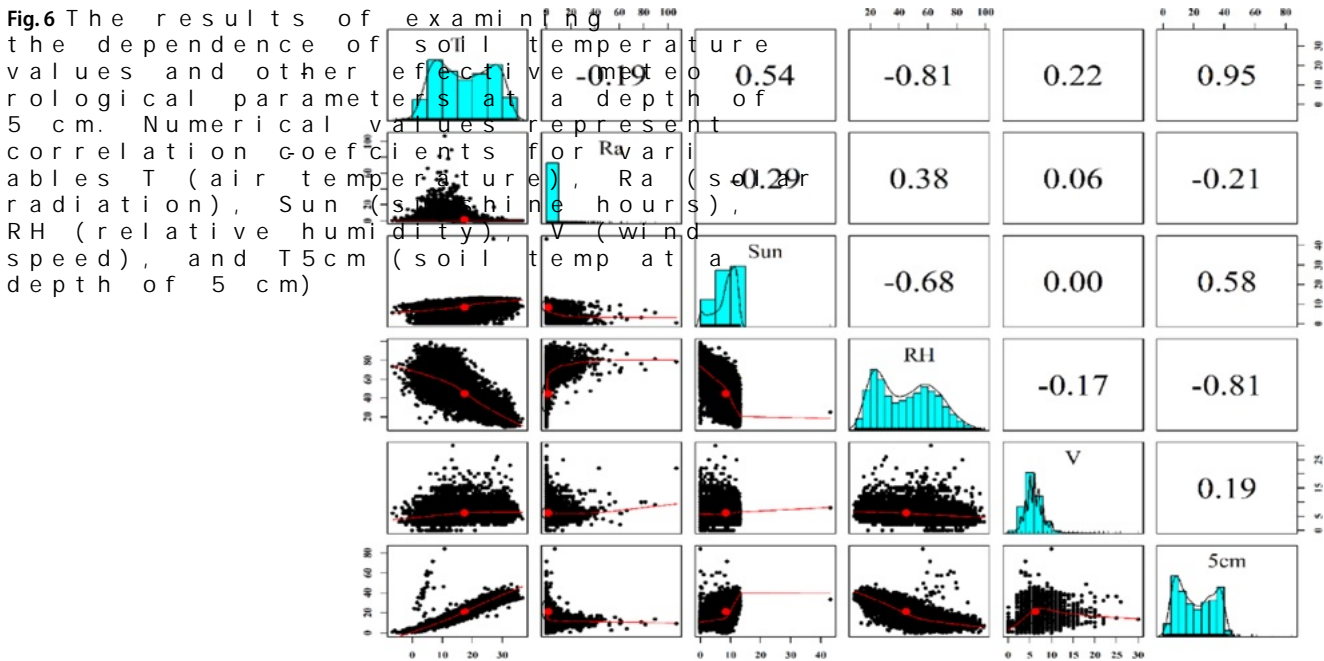


Fig. 6 The results of examining the dependence of soil temperature values and other meteorological parameters at a depth of 5 cm. Numerical values represent correlation coefficients for variables T (air temperature), Ra (solar radiation), Sun (sunshine hours), RH (relative humidity), V (wind speed), and T5cm (soil temperature at a depth of 5 cm)

3.1 Forecasting soil temperature at different depths using deep learning models

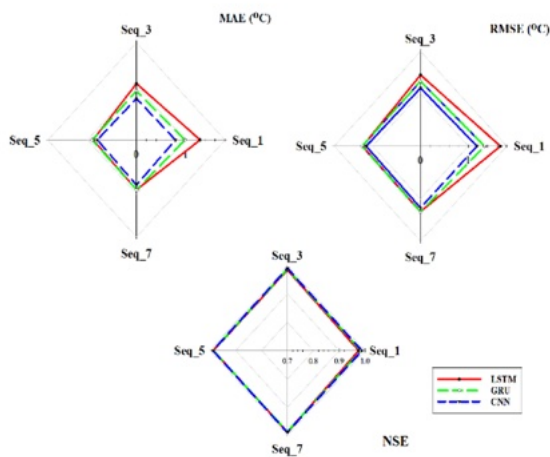
3.1.1 The performance of deep learning models at a depth of 5 cm

The performance of deep learning models in predicting daily soil temperature at a depth of 5 cm was evaluated using sequence lengths of 1, 3, 5, 7, and 15 days. The results are shown in Fig. 7.

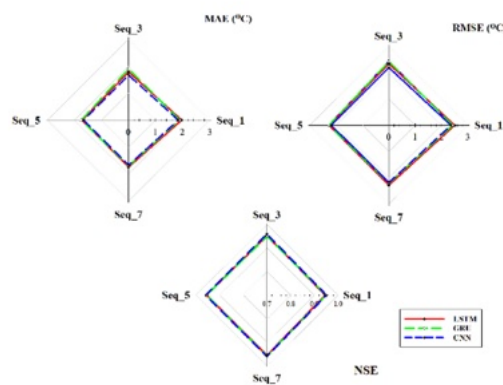
It can be observed that for the 15-day forecast, CNN outperformed LSTM and GRU. As the prediction period extended from 1 to 15 days, the models' efficiency decreased. CNN consistently outperformed LSTM and GRU across all sequence lengths and forecast horizons.

for one-day-ahead forecasting respectively, indicating the models' performance in predicting one day ahead. CNN maintained its lead with the lowest error rate (95–96%) and the lowest RMSE (0.1–0.2 °C) across all sequence lengths and forecast horizons. LSTM and GRU performed similarly, with LSTM showing slightly better performance than GRU in some cases.

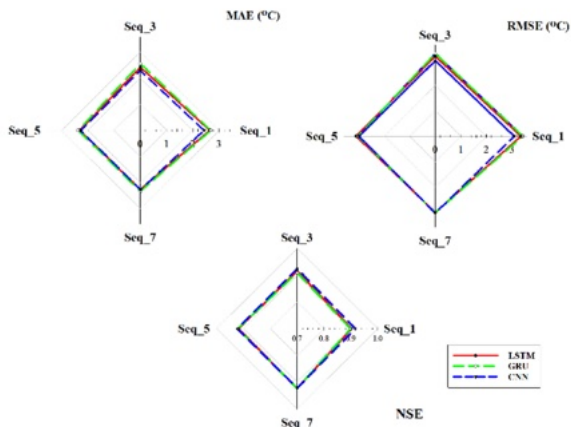
GRU (with a 7-day sequence length) showed the best performance for the 30-day forecast, with an RMSE of 0.3 °C and an NSE of 99%. The difference in performance between this model and the best LSTM model was minimal.



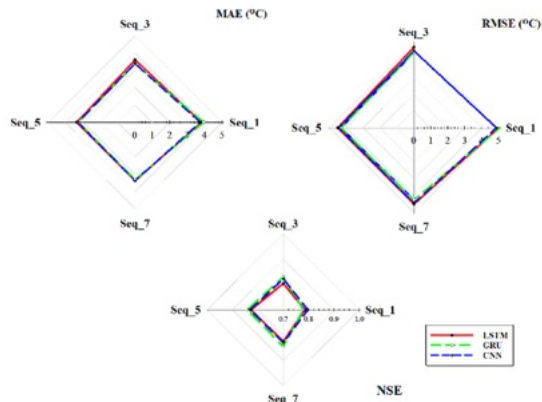
forecasting soil temperature for one day ahead



forecasting soil temperature for 7 days ahead



forecasting soil temperature for 15 days ahead



forecasting soil temperature for 30 days ahead

Fig. 7 Performance evaluation of deep learning models for soil temperature across prediction horizons (1/7/15/30 days). Key metrics: RMSE (

3.30, NSE: 85%), despite its lower accuracy, robustness compared to shorter horizons. The RMSEs of this model were 4% and 5% slower than those of performing CNN and LSTM models (2021). Alotaibi et al. (2019) emphasized the importance of sequence length in enhancing model performance, highlighting that a 3-day sequence length is emerging as a promising choice for medium-term forecasting. CNNs have been widely applied as an effective model for forecasting time series data (Chen et al. 2021a,b). Wang et al. (2018) found that CNNs effectively extract temporal features from load sequences (2021). Cheng et al. (2021) proposed a probabilistic residential load forecasting method using a novel deep learning model (GRU-Net). The GRU-Net is integrated with meteorological data (Güçlüoğlu et al. 2024) introduced a Multi-Dimensional Variational

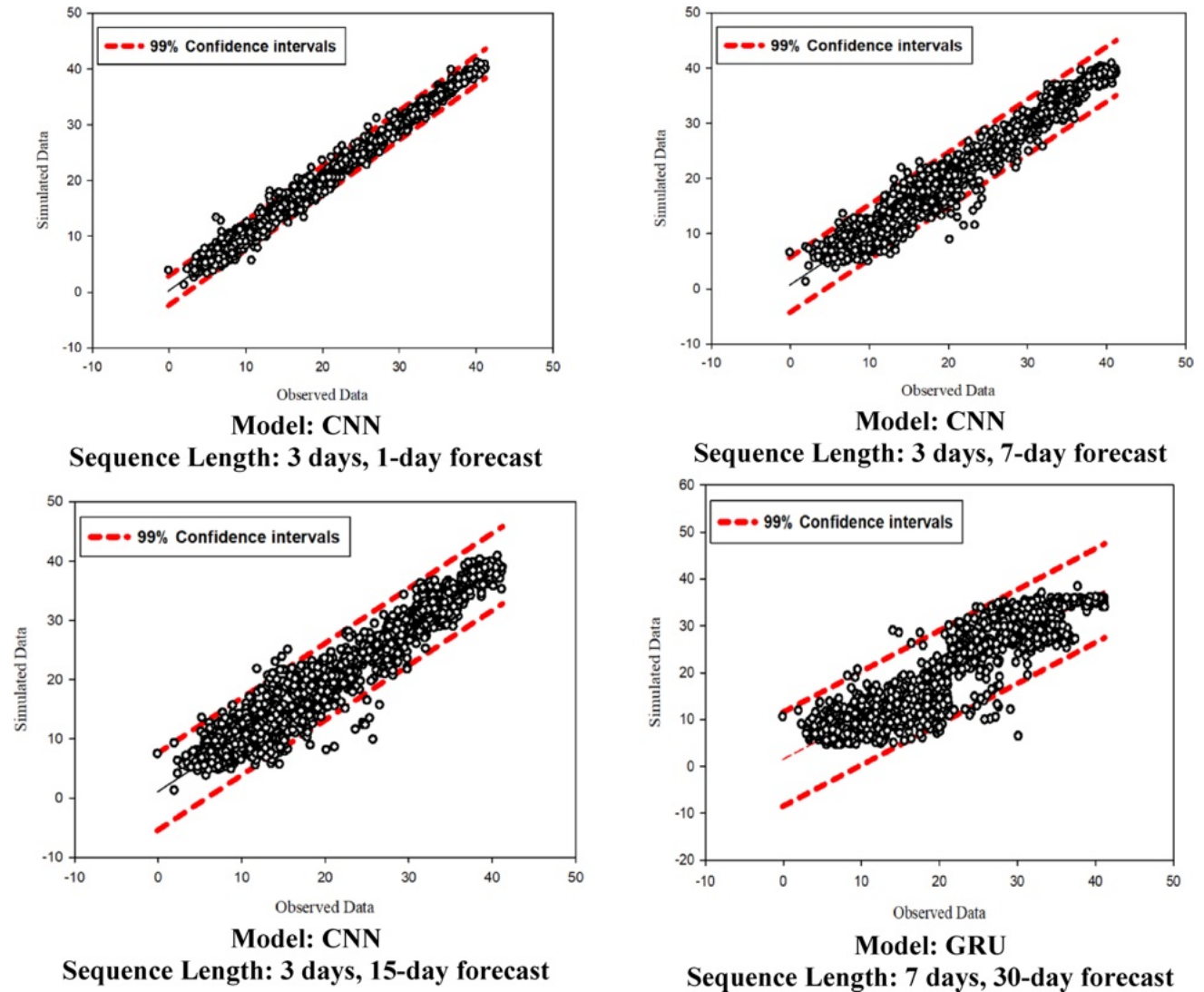


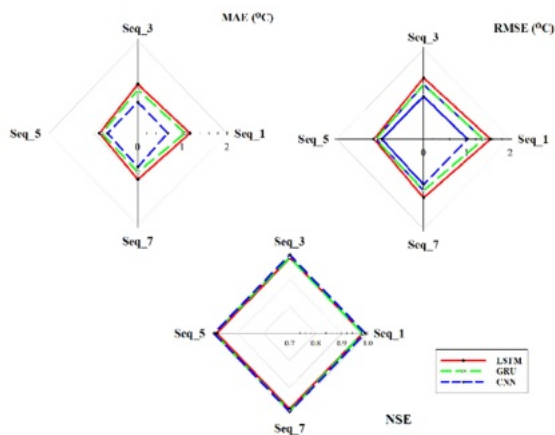
Fig. 8 99% Confidence interval of soil temperature forecasting at a observed values falling predominantly within the predicted confd

despite their wider inter-vaadhsie, the ubbe for, for RMSA: c
 ning, risk assessment, and 2.002, a NSB: a 9.6%) siss. lightly ou
 GRU. Notably, similar to the

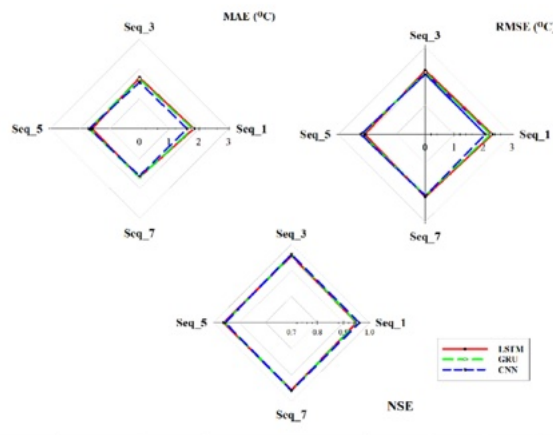
3.1.2 The performance of deep learning models at a depth of 10 cm

The performance of deep leaemg thg ang adien se'ic, e, p, RMSE (C, MAE (C, NSE: 2.1
 soil temperature at a 10 cm) e, p, th shows a signseq us concenbe g e
 1, 3, 5, and 7 days for f omancas was soviez onsl of se 1 to 7 th a 5, c
 days, is il9, illustrated in Figo. recasts, GRU with a 7-day s

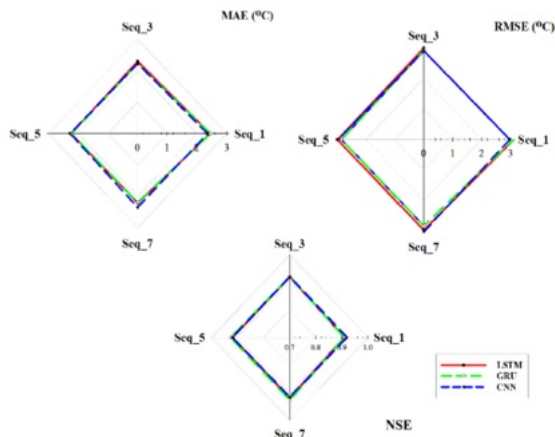
As shown9, in o F ig.-day for etchas ttop - QNf w ir th n g, m RMSE (C, (MAE
 3-day sequence length ac NISE. Ev ed 8.6%) he hieght l i p g h r t f i o r g m a i n t c s e s
 (MAE: °C, 6 RMSE C, ON 9.5: 99%), ti o n s o n N o r t a b l y, the RMSE of t
 ing near-perfect accuracy. l o t w h e r R M S A e n v t h a u t e s o f f t h e h i l S T M o f
 were 17% and 13% lower thaan d h 0.8 N N o f v i t h e a b e 7 s - t d a l y S T M e o u e r t o
 a 5-day sequence length) a t r i d e g R y U (O w i e t r a l a, 5 s d a y l a e q u e n t h
 length) models, respectively, s y o p f o m a l o n e d a y h e a d t o m e d i a
 ing. For 7-day forecasts, 1 C 5 N - N d a w j) t, h w h i 3 l - d a y R e q s e p r e f e n



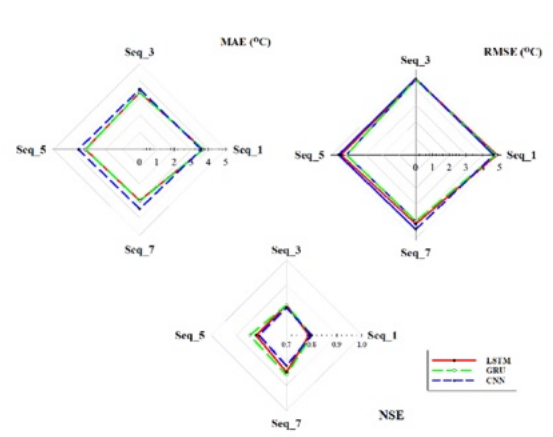
forecasting soil temperature for one day ahead



forecasting soil temperature for 7 days ahead



forecasting soil temperature for 15 days ahead



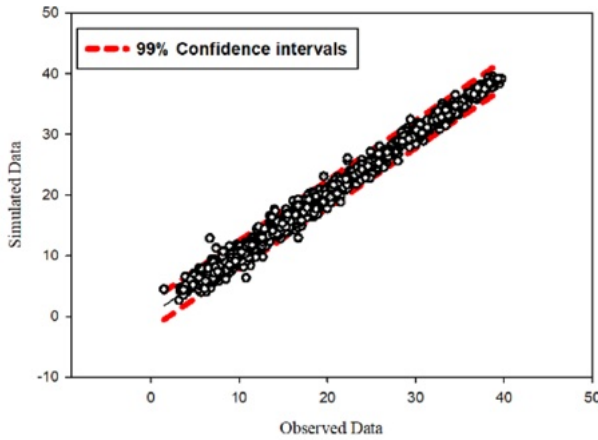
forecasting soil temperature for 30 days ahead

Fig. 9 The performance of deep learning models in forecasting soil te for forecast horizons of 1, 7, 15, and 30 days. Key metrics: RMS

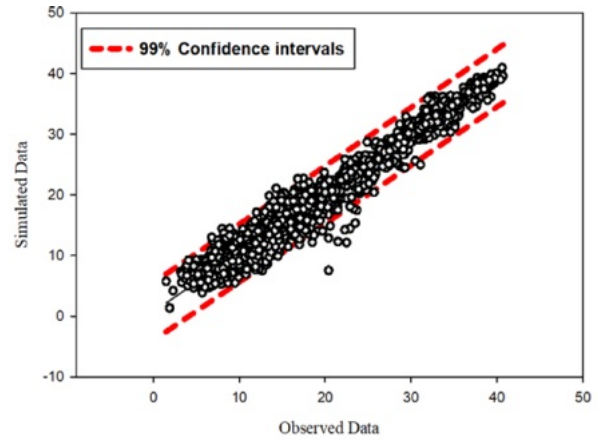
(30-day). The results of the performance comparison between the LSTM and GRU models for forecasting soil temperature at a 10 cm depth, based on the RMSE and MAE metrics, are presented in Table 10. The LSTM model demonstrated superior performance compared to the GRU model, with the LSTM achieving lower RMSE and MAE values. The LSTM model's performance was consistently better than the GRU model across all metrics, demonstrating its effectiveness in capturing the underlying patterns in the soil temperature data. The LSTM model's performance was also evaluated using the RMSE and MAE metrics, and the results showed that the LSTM model achieved lower values than the GRU model, indicating better forecasting accuracy. The LSTM model's performance was also evaluated using the RMSE and MAE metrics, and the results showed that the LSTM model achieved lower values than the GRU model, indicating better forecasting accuracy.

3.1.3 Performance of deep learning models at a depth of 30 cm

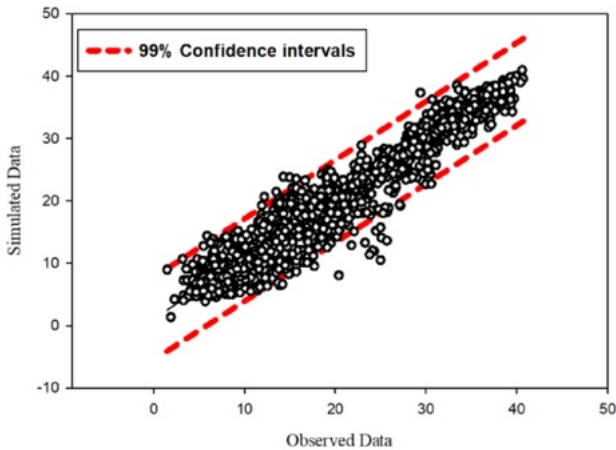
The performance of deep learning models in forecasting daily soil temperature at a depth of 30 cm is shown in Fig. 10. As shown, for 1-day sequence length achieved the best performance (NSE of 94%, RMSE of 1.1, MAE of 0.8) for the CNN model with a 3-day sequence length. For 7-day sequence length, the CNN model achieved the best performance (NSE of 94%, RMSE of 1.1, MAE of 0.8) for the CNN model with a 3-day sequence length. For 15-day sequence length, the CNN model achieved the best performance (NSE of 94%, RMSE of 1.1, MAE of 0.8) for the CNN model with a 3-day sequence length. For 30-day sequence length, the GRU model achieved the best performance (NSE of 94%, RMSE of 1.1, MAE of 0.8) for the GRU model with a 7-day sequence length.



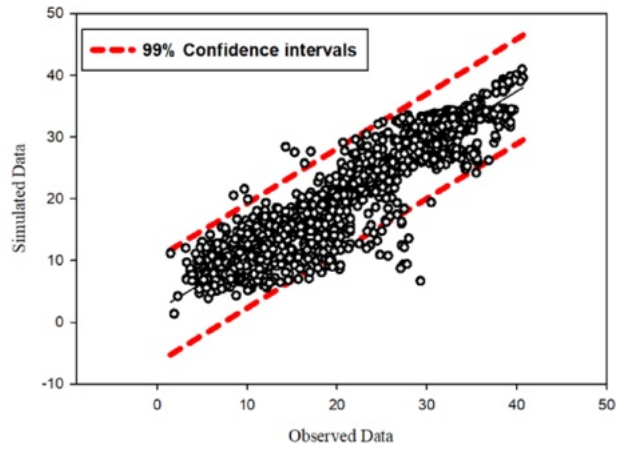
Model: CNN
Sequence Length: 3 days, One-day forecast



Model: CNN
Sequence Length: 3 days, 7-day forecast



Model: CNN
Sequence Length: 3 days, 15-day forecast



Model: GRU
Sequence Length: 7 days, 30-day forecast

Fig. 10 99% Confidence interval of soil temperature forecasting at a observed values falling predominantly within the predicted confd

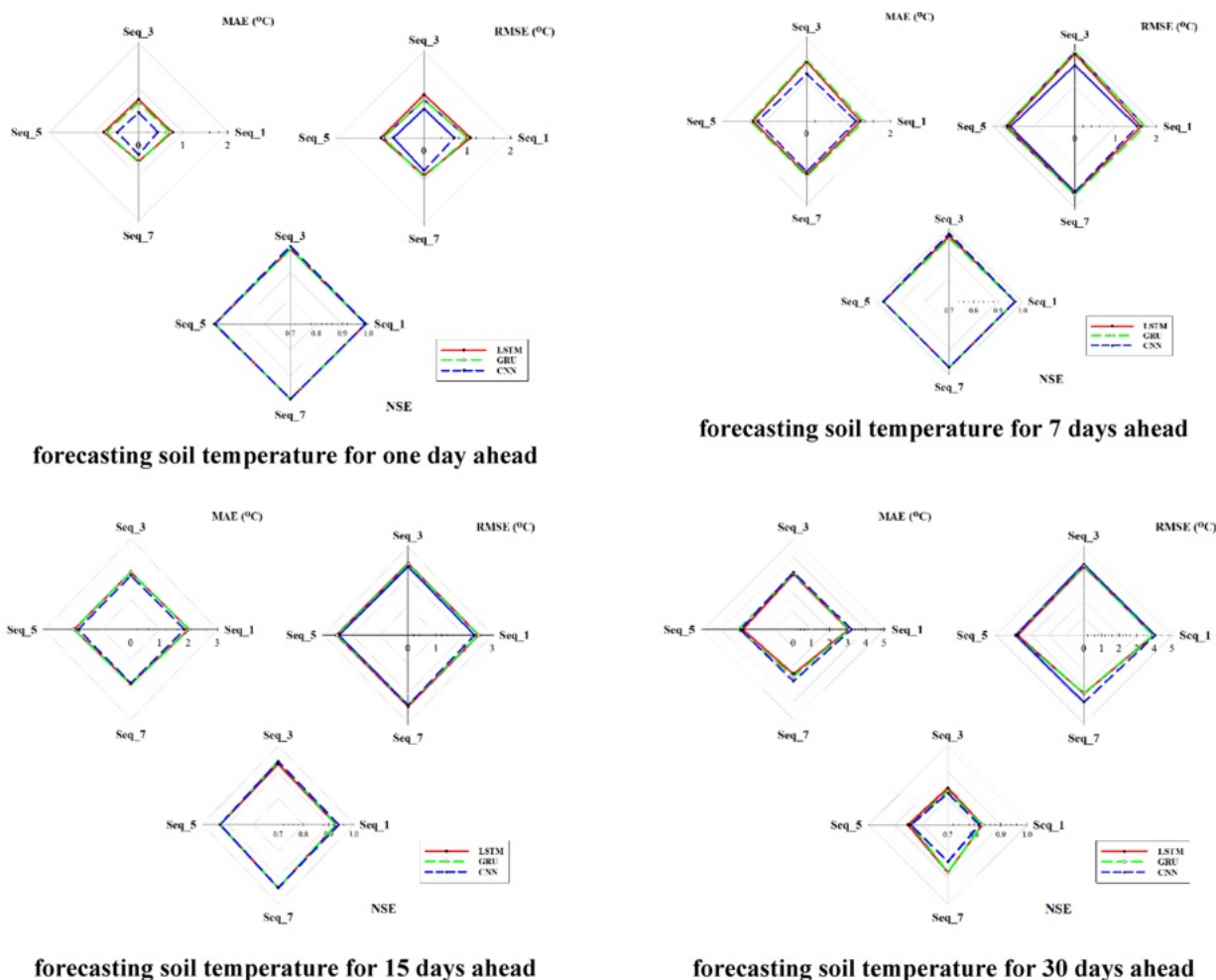
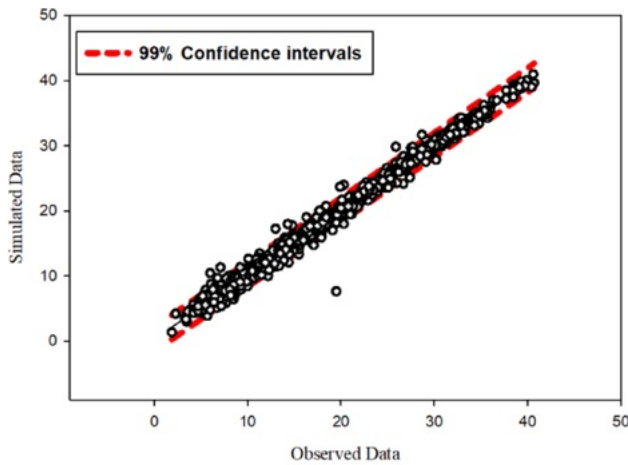


Fig. 11 The performance of deep learning models in forecasting soil temperature for forecast horizons of 1, 7, 15, and 30 days. Key metrics: RMSE

model for short- to medium-term forecasting (1–15 days) while GRU is preferred for long-term forecasting. (Ford and Similar to the trends observed with depth, the best models at this depth are LSTM and GRU. The performance of the best models at this depth is also shown in Fig. 10. In general, the performance of the best models at this depth is also shown in Fig. 10. In general, the performance of the best models at this depth is also shown in Fig. 10.

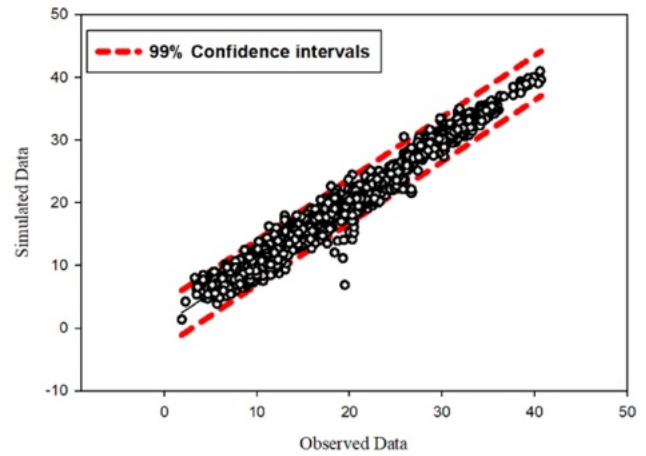
3.1.4 Performance of deep learning models at a depth of 50 cm

The simulation results of deep learning models for forecasting daily soil temperature at a depth of 50 cm for forecast lengths of 1, 3, 5, and 7 days are shown in Fig. 11. Unlike other depths, As shown in this Figure, the performance of the best models at this depth is also shown in Fig. 11. Unlike other depths, the performance of the best models at this depth is also shown in Fig. 11.



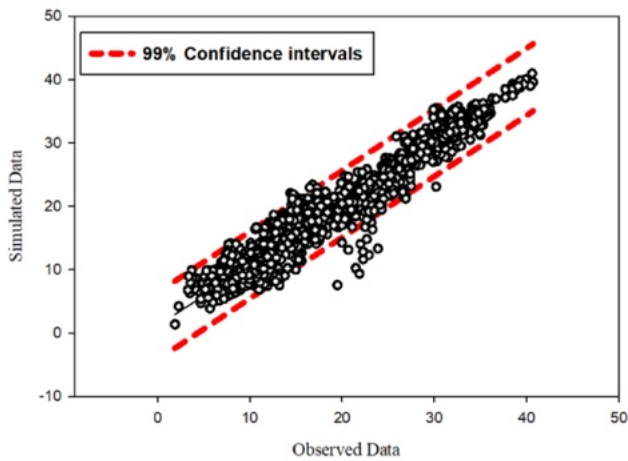
Model: CNN

Sequence Length: 3 days, 1-day forecast



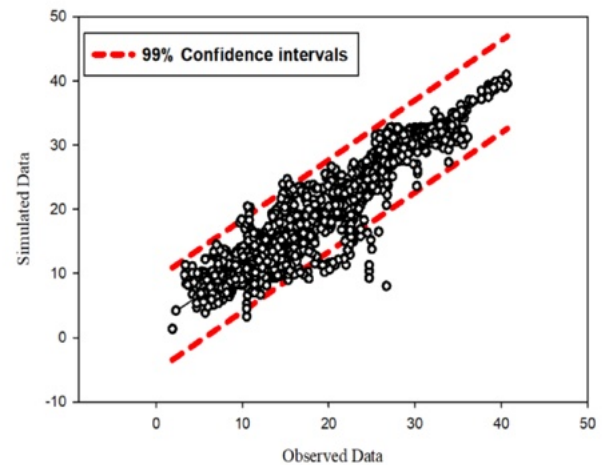
Model: CNN

Sequence Length: 3 days, 7-day forecast



Model: CNN

Sequence Length: 3 days, 15-day forecast



Model: GRU

Sequence Length: 7 days, 30-day forecast

Fig. 12 99% Confidence interval of soil temperature forecasting at a observed values falling predominantly within the predicted confd

the GRU model with a 7-day sequence is better than the LSTM model (NSE: 78%, RMSE: 3.98 °C). The 2p4f of the GRU model is the best model across different depths and forecast horizons. The performance of the best models across different depths and forecast horizons is shown in Fig. 12.

3.1.5 Comparing the performance of the best deep learning models across different depths and forecast horizons

The performance of the best deep learning model (CNN, GRU, and LSTM) in forecasting soil temperature at different depths and forecast horizons is shown in Fig. 13. The performance of the best model across different depths and forecast horizons is shown in Fig. 13. The performance of the best model across different depths and forecast horizons is shown in Fig. 13.

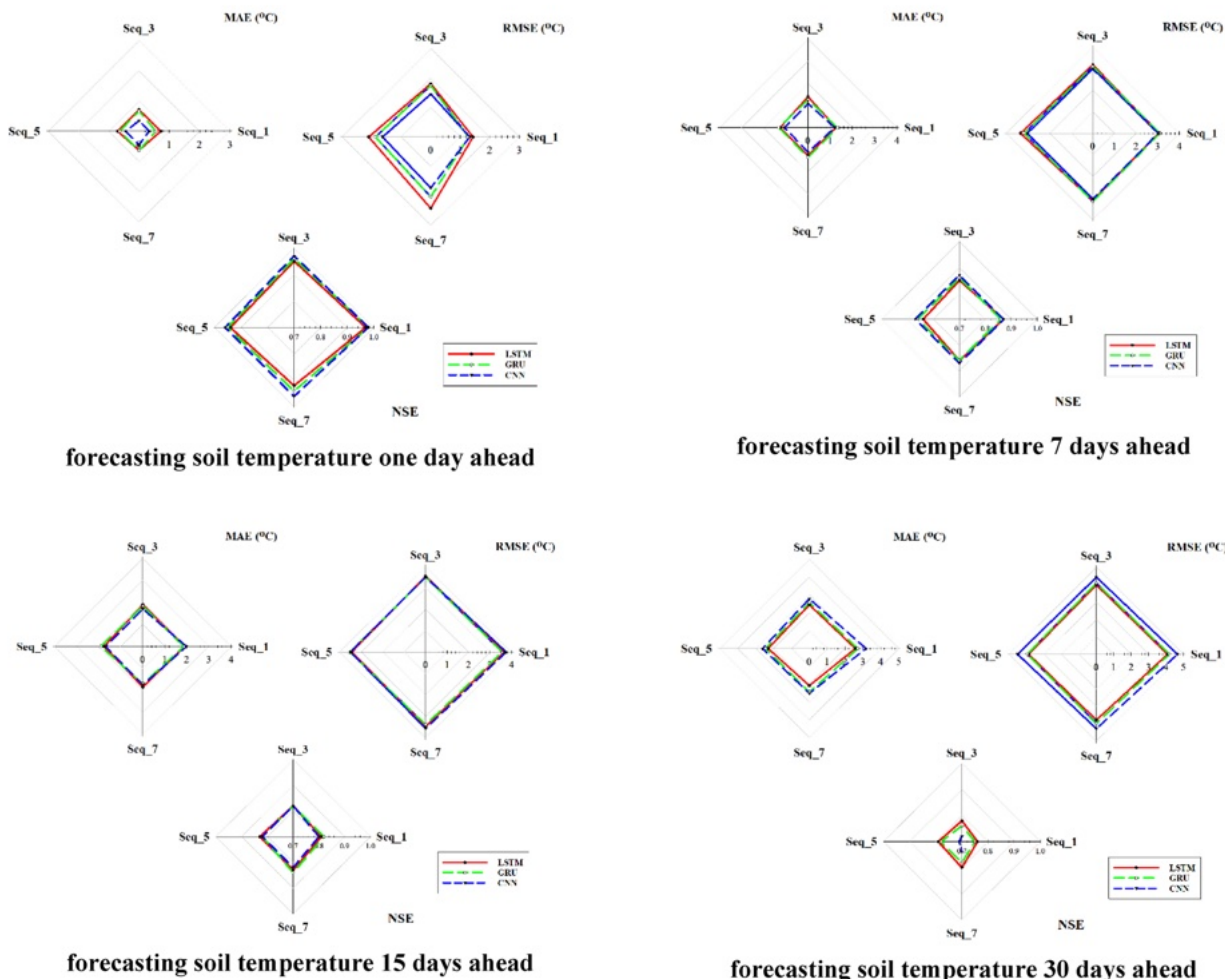
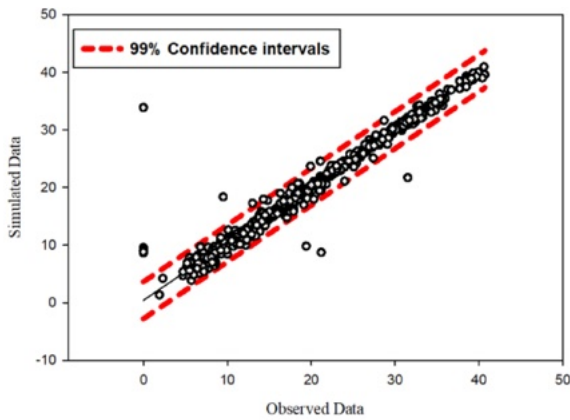


Fig. 13 The performance of deep learning models in forecasting soil temperature for forecast horizons of 1, 7, 15, and 30 days. Key metrics: RMS

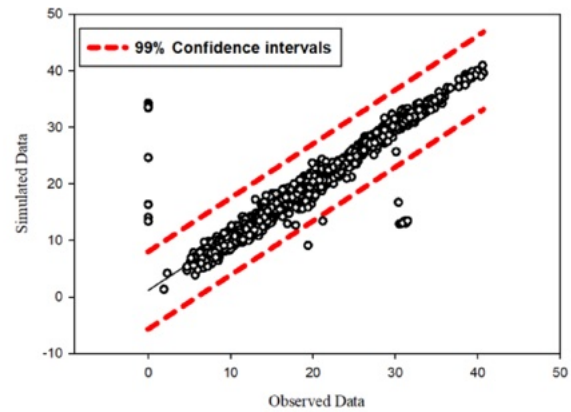
to higher prediction errors over time.

Forecasting accuracy also decreases with soil depth. For short- to medium-term forecasts, accuracy is high (e.g., 99% for a 1-day forecast at 5 cm depth) but drops significantly for longer horizons (e.g., 70% at 5 cm depth for a 30-day forecast). Previous studies (Kisi et al. (2015) and Nadeem et al. (2020)) noted that deep learning models perform better at shallower depths. However, the current study (2024a,b) found that BiLSTM performs well at 100 cm depth, a discrepancy likely due to differences in model architectures and climate data used. For shorter sequence lengths (1–3 days), CNN is effective, while LSTM and GRU are more effective for long-term forecasts (5–30 days), as noted by Alshaiji et al. (2020) and (2021). Overall, the performance of models like LSTM, GRU, and CNN for daily soil temperature prediction is highly dependent on forecast horizon and soil depth.



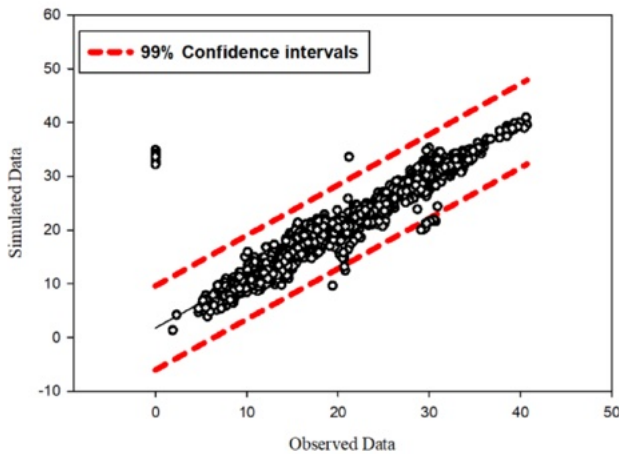
Model: CNN

Sequence Length: one day, One-day forecast



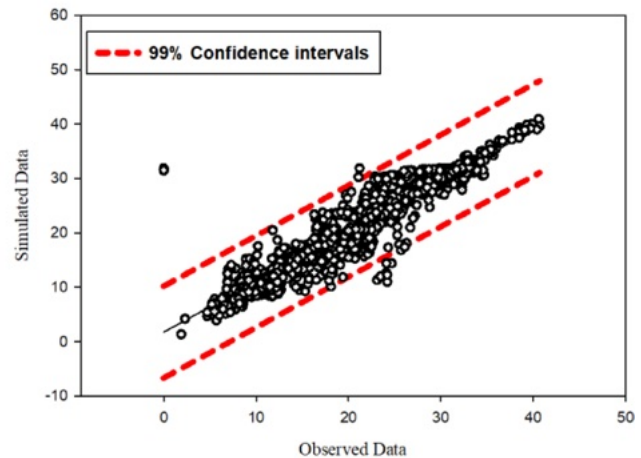
Model: CNN

Sequence Length: 3 days, 7-day forecast



Model: CNN

Sequence Length: 3 days, 15-day forecast



Model: LSTM

Sequence Length: 7 days, 30-day forecast

Fig. 14 99% Confidence interval of soil temperature forecasting at a observed values falling predominantly within the predicted confid

horizons can be attributed to the inherent limitations of each model architecture. CNNs are particularly effective at capturing short-term trends and local dependencies, while LSTMs excel at long-term dependencies and global context. The CNN model's performance is generally superior for short-term forecasts, while LSTMs show better performance for long-term forecasts. Shorter forecast horizons require less reliance on long-term dependencies, while longer horizons require the model to retain or forget information over time. The CNN model's ability to process fixed-length input sequences is a significant advantage for short-term forecasting, while LSTMs' ability to process variable-length sequences is a key strength for long-term forecasting. The CNN model's performance is generally superior for short-term forecasts, while LSTMs show better performance for long-term forecasts. Shorter forecast horizons require less reliance on long-term dependencies, while longer horizons require the model to retain or forget information over time. The CNN model's ability to process fixed-length input sequences is a significant advantage for short-term forecasting, while LSTMs' ability to process variable-length sequences is a key strength for long-term forecasting.

Table 3 The performance of the best deep learning models (CNN, GRU, and LSTM) at different soil depths (10 cm, 30 cm, and 50 cm) and forecast horizons (1, 7, 15, and 30 days)

Soil depth (cm)	Forecast horizon (days)	Model	Sequence length	Performance metrics (per day)		
				MAE (°C)	RMSE (°C)	NSE
5	1	CNN	3	0.77	1.11	0.99
	7	CNN	3	1.6	2.19	0.96
	15	CNN	3	2.29	2.96	0.92
	30	GRU	7	3.3	4.26	0.85
10	1	CNN	3	0.67	0.95	0.99
	7	CNN	3	1.55	2.07	0.96
	15	CNN	3	2.23	2.9	0.92
	30	GRU	7	3.01	3.96	0.86
30	1	CNN	3	0.67	0.43	0.99
	7	CNN	3	1.14	1.51	0.98
	15	CNN	3	1.79	2.34	0.94
	30	GRU	7	2.59	3.29	0.88
50	1	CNN	1	1.2	3.02	0.87
	7	CNN	3	1.09	2.99	0.87
	15	CNN	3	1.7	3.5	0.82
	30	LSTM	7	2.08	3.78	0.8

CNNs, which are better suited for identifying spatial patterns.

In the domain of soil temperature forecasting, several studies have explored this field. Nanda (2020) examined the spatiotemporal variability of soil temperature in the Lesser Himalaya region.

3.2 Forecasting soil temperature at different depths and lags using vine copulas

Several machine learning techniques for estimating soil temperature in scarce areas. Their results are compared with the existing method: boosting algorithm (XGBoost), support vector machines (SVM), other methods, including random forests (RF), and support vector perceptron (MLP), and support vector machines (SVM). Meanwhile, Li et al. (2022) developed a long short-term temporal dependency (LSTM)-based model to capture the temporal dependencies from multiple predictors. Instead of using traditional attention mechanisms, they used a novel attention mechanism to predict soil moisture and temperature. In this study, the LSTM model outperformed several traditional models, such as Random Forest (RF), Support Vector Machine (SVM), Elastic-Net (ENET), standard LSTM, and LSTM with attention (A-LSTM), in most tests.

Imanian et al. (2024) conducted a comparative analysis of various deep learning models, including CNN, and MLP, for predicting the soil temperature of various sites across Canada, from the northwest to the southeast. The study found that traditional methods struggled with accurate soil temperature predictions, particularly in extremely cold regions. The LSTM model with shuffled input data achieved superior performance, with

The results of the vine copula selection procedure are presented in Table 4 for all scenarios with a lag of 30 days. Similarly, the tree sequence for the temperature differences (and 7) were evaluated using the Akaike Information Criterion, and these results are presented in Table 5. The analysis across different depths is shown in Table 6. R- and C-vine copulas performed best in the empirical models. Figure 15 illustrates the transition rates between R- and C-vines, highlighting the temperature variable as an indicator of the complex dependencies between different lags.

By examining the tree sequence of different copulas, including C, D, R, as well as the vine copulas at 5 cm depth, their Gaussian mode, the best sequences regarding the dependence of the studied variables in 4 dimensions are identified for the

The results of the analysis for 10 and 30 cm, R-vine sequence was chosen as the best sequence. Regarding the internal copulas, results showed that in the 0–10 cm range, internal copulas of Frank (270 degrees) were selected as the best copulas in the 0–5 cm range.

In order to fully cover the range of different vine-copulas, it was tried (RMSE) at different depths.

Table 4 Selected vine copulas for different depths: R: Rotated Gumbel copula (90 degrees), N: Gaussian copula

	Tree	Edge	Internal copula	AIC	Log likelihood	Best tree sequence
5 cm	1	3, 2	G270	-41, 050	20, 531	R-vine
		1, 3	G270			
		4, 1	F			
	2	1, 2 3	F			
		4, 3 1	F			
		4, 2 1, 3	F			
10 cm	1	3, 2	G270	-39, 545	19, 778	R-vine
		1, 3	G270			
		4, 1	F			
	2	1, 2 3	F			
		4, 3 1	F			
		4, 2 1, 3	F			
30 cm	1	3, 2	G270	-38, 153	19, 083	R-vine
		1, 3	G270			
		4, 1	F			
	2	1, 2 3	F			
		4, 3 1	G270			
		4, 2 1, 3	C			
50 cm	1	1, 2	F	-32, 876	16, 444	C-vine
		1, 3	G270			
		4, 1	F			
	2	3, 2 1	C90			
		4, 3 1	F			
		4, 2 3, 1	N			

Fig. 15 R and C tree sequences in the forecasting of soil temperature values at different depths (R - vineC - vine), T: Temperature, Sun: Sunshine hours, RH: relative humidity

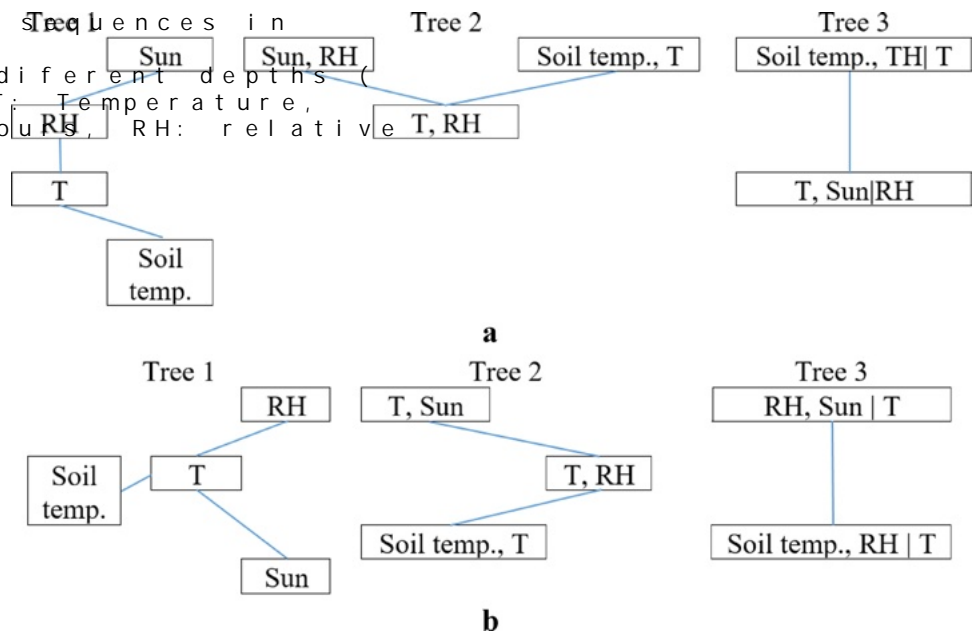


Table 5 The results of forecasting soil temperature values at a depth of 5 cm with different lags and forecast horizons using the vine-based approach and R-vine copula-based approach 15-day forecast performance

Simulation	Sim_Lag1	Sim_Lag2	Sim_Lag3	Sim_Lag4
RMSE (°C)				
1 - day	0.33	0.19	1.53	2.70
7 - day	1.25	2.20	1.90	2.66
15 - day	1.37	2.03	1.56	2.96
30 - day	1.21	1.92	1.63	2.49
MAE (°C)				
1 - day	0.33	0.19	1.53	2.70
7 - day	0.87	1.73	1.48	2.21
15 - day	1.14	1.53	1.28	2.46
30 - day	0.96	1.52	1.29	2.01
NSE				
1 - day	0.99	0.99	0.87	0.90
7 - day	0.96	0.87	0.90	0.85
15 - day	0.97	0.91	0.95	0.77
30 - day	0.98	0.95	0.96	0.90

of 15.96 °C, which is about average. This forecast period Apart from the one-day forecast related to the 30-day forecast with one-day lag, which shows error rate of 1.21 °C (RMSE).

To validate the simulation a confidence interval for the forecast values at a depth of 5 cm, using 30-day forecast period, as shown in the figure, for lags of 1 and 7-day prediction confidence interval while the other falls below the 7-day lag, only one instance in the forecasting of soil temperature.

the soil temperature forecast results that all the forecasts 30-day forecast window are better than the other. This day of Also, according to Table 4, it can be seen that the vine-based approach increases of the forecasting period, the error values are increasing in general and the efficiency coefficient of the model is also decreasing.

3.2.2 Forecasting soil temperature at different lags using

vine copulas at 10 cm depth 5 cm, the best performance was observed in lag 3.

Apart from the one-day forecast periods, one-day lag and 7-day lag are the best lags in forecasting soil temperature at a depth of 5 cm, with a performance coefficient of 0.99 according to NSE statistic. The highest forecast error is the RMSE statistic in forecasting the soil temperature

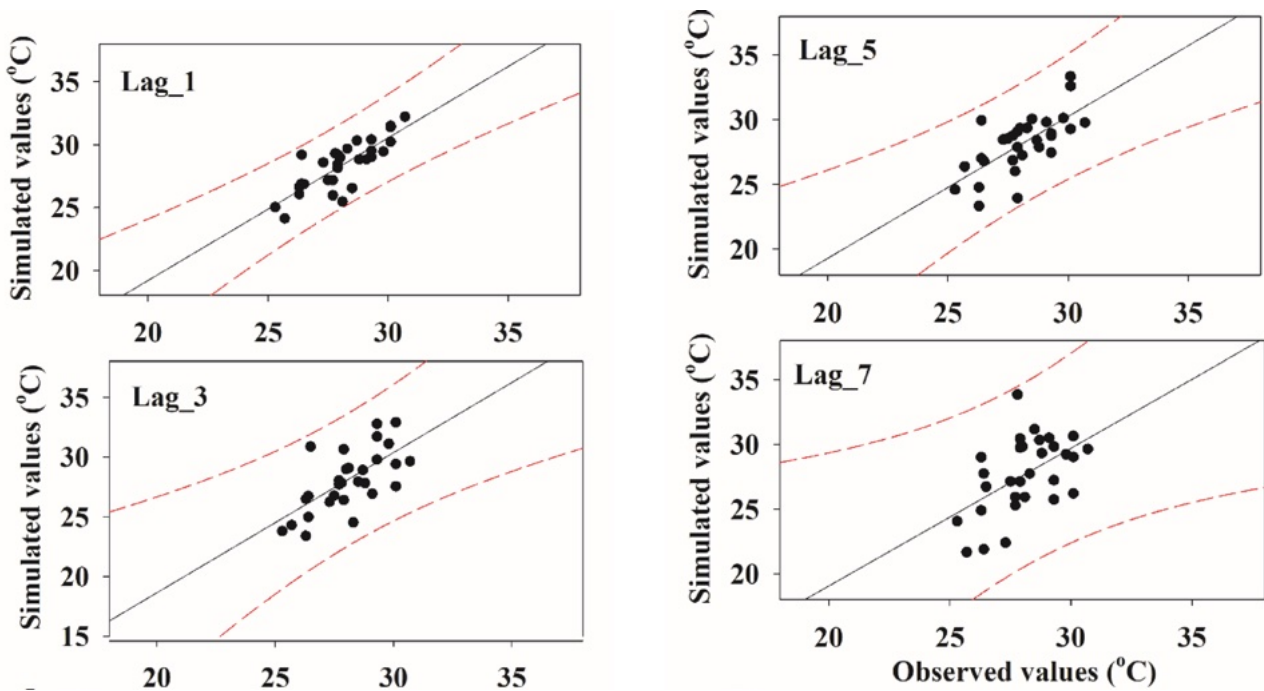


Fig. 16 99% confidence interval of soil temperature forecasting at a depth of 10 cm using the R-vine copula-based approach

Table 6 The results of forecasting and spot soil temperature values at a depth of 10 cm with different lags and forecasting windows using the R-vine copula-based approach and R-vine copula-based approach. It can be seen that the forecasting performance is generally better for shorter forecasting periods and smaller lags.

Simulation	Sim_Lag_1	Sim_Lag_3	Sim_Lag_5	Sim_Lag_7
RMSE (°C)				
1 - day	0.68	1.81	0.71	2.25
7 - day	0.93	0.93	0.99	3.97
15 - day	0.98	1.16	1.94	3.71
30 - day	1.13	1.18	2.21	3.34
MAE (°C)				
1 - day	0.68	1.81	0.71	2.25
7 - day	0.79	0.79	0.80	3.29
15 - day	0.90	0.99	1.29	3.01
30 - day	1.01	1.00	1.70	2.71
NSE				
1 - day	0.99	0.95	0.98	0.93
7 - day	0.98	0.98	0.98	0.81
15 - day	0.98	0.98	0.92	0.80
30 - day	0.98	0.98	0.93	0.87

The results of forecasting and spot soil temperature values at a depth of 10 cm using the R-vine copula-based approach and R-vine copula-based approach. It can be seen that the forecasting performance is generally better for shorter forecasting periods and smaller lags. The amount of error value (RMSE) is also increases. However, unlike the pattern of forecasting soil temperature at a depth of 5 cm, in a five-day forecasting window, the error rate and also, the NSE is not better than three-day forecasting window.

of the long-term mean soil temperature varied show the performance of 81%. Considering the importance of the evolutions of the forecast period, the forecasting of the soil temperature is examined by the period and in the seven-day lag, the move base change of forecasting confidence interval, so that it is also clear that the interval of the upper bound and the interval of the lower bound, which indicates an increase in the accuracy used by the model. In the case of a five-day lag, the soil temperature is not as accurate as the estimation was observed in the five-day lag. It is also observed that at a depth of 10 cm using the five-day lag, the average error is not as high as the sequence. No overestimation is observed in the five-day lag. Overall, apart from one case in the seven-day lag, the 95% confidence interval (RMSE) is not as accurate as the performance of the model. The RMSE is not as accurate as the performance of the model over a 30-day lag, highlighting its reliability in forecasting of soil temperature.

3.2.3 Forecasting soil temperature at different lags using vine copulas at 30 cm depth

According to the forecast results at the depths of 5 and 10 cm, the RMSE, MAE and MAPE statistics for the depth of 30 cm and the results are on a daily basis, highlighting its reliability in forecasting of soil temperature.

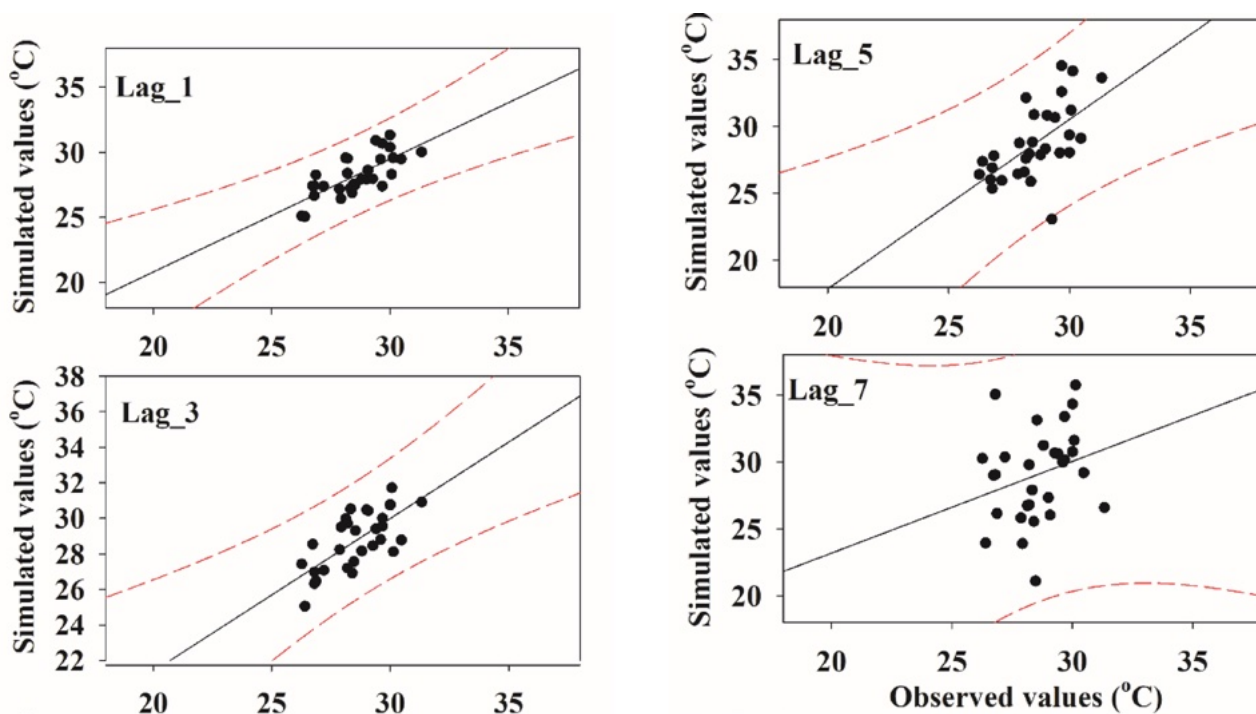


Fig. 17. 99% confidence interval of soil temperature forecasting at a depth of 30 cm using vine copulas approach

Table 7 The results of forecasting soil temperature on values at 30 cm depth of 30 cm with different lags and forecasting windows using the vine based approach and R-vine copula based sequence predicted values across different confidence interval. This under and reliability of the studied, while maximum overestimation occurred in two cases during temperatures at depths of 5 cm not observed at the 30 cm depth and consistency of the vine forecasting soil temperature at great

Simulation	Sim_Lag_1	Sim_Lag_3	Sim_Lag_5	Sim_Lag_7
RMSE (°C)				
1 - day	1.65	1.05	1.65	7.19
7 - day	1.47	1.56	2.38	3.29
15 - day	1.21	1.58	2.69	3.29
30 - day	1.38	1.61	2.51	3.06
MAE (°C)				
1 - day	1.65	1.05	1.65	7.19
7 - day	1.26	1.31	2.25	2.40
15 - day	0.96	1.41	2.45	2.74
30 - day	1.04	1.33	2.09	2.49
NSE				
1 - day	0.90	0.98	0.89	0.73
7 - day	0.95	0.96	0.85	0.82
15 - day	0.98	0.96	0.88	0.86
30 - day	0.97	0.96	0.91	0.89

RMSE statistic, the lowest error for soil temperature at a depth of 30 cm, a 15-day forecast, is about 1.21 °C. At a depth of 50 cm, the results are similar to those at 30 cm, with a 15-day forecast period.

Based on the Nash-Sutcliffe coefficient of vine copulas in the forecasting of soil temperature, it is evident that for forecasting soil temperature at a depth of 30 cm, a 15-day forecast with the R tree sequence approach is the best sequence based on

confidence interval. This under and reliability of the studied, while maximum overestimation occurred in two cases during temperatures at depths of 5 cm not observed at the 30 cm depth and consistency of the vine forecasting soil temperature at great

3.2.4 Forecasting soil temperature at different lags using vine copulas at 50 cm depth

The forecasting results at a depth of 50 cm on a daily scale with five-day, and seven-day, considering the Nash-Sutcliffe coefficient of vine copulas in the forecasting of soil temperature, it is evident that for forecasting soil temperature at a depth of 50 cm, a 15-day forecast with the R tree sequence approach is the best sequence based on

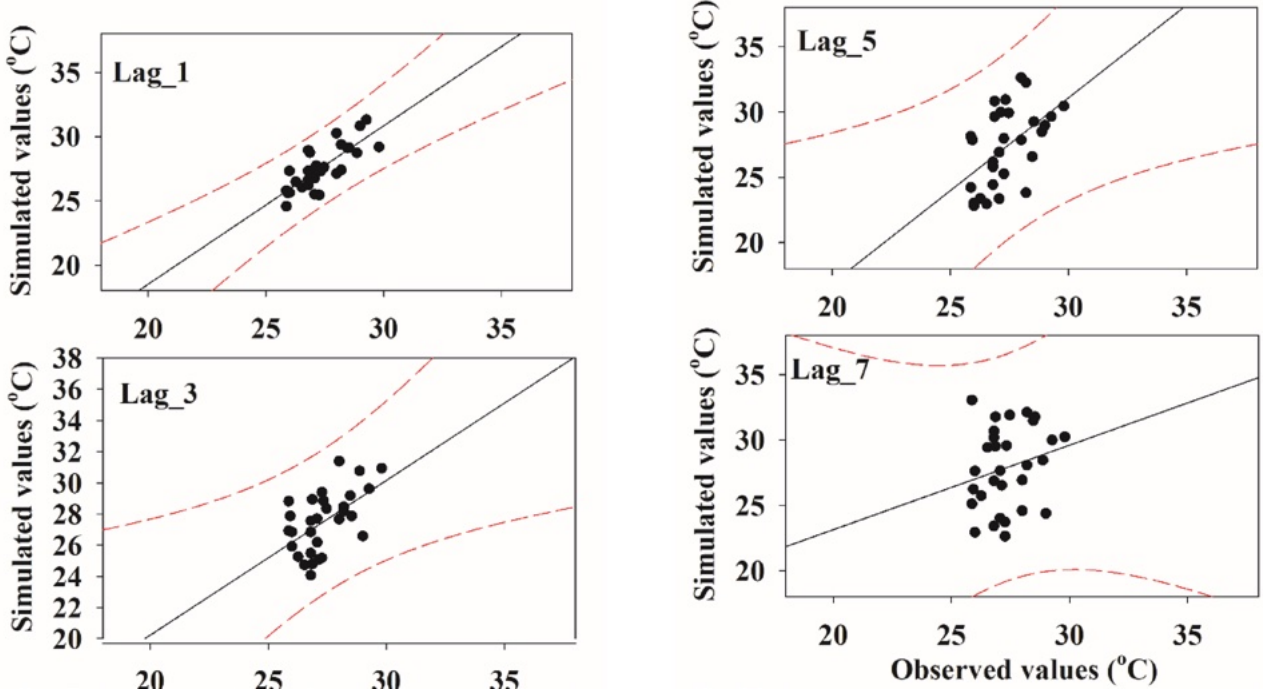


Fig. 18 99% confidence interval of soil temperature forecasting at a depth of 30 cm using the vine based approach

Table 8 The results of forecasting soil temperature detail values relative depth of 50 cm with different lags and forecasting windows using the vine-based approach and C-vine copula-based sequence

Simulation	Sim_Lag1	Sim_Lag3	Sim_Lag5	Sim_Lag7
RMSE (°C)				
1-day	0.73	2.13	4.12	1.00
7-day	0.97	1.91	3.02	3.24
15-day	0.99	1.84	2.72	3.30
30-day	1.05	2.13	2.66	2.96
MAE (°C)				
1-day	0.73	2.13	4.12	1.00
7-day	0.78	1.72	2.54	2.86
15-day	0.79	1.56	2.43	2.87
30-day	0.83	1.78	2.33	2.47
NSE				
1-day	0.99	0.88	0.89	0.98
7-day	0.99	0.93	0.88	0.88
15-day	0.99	0.95	0.91	0.85
30-day	0.99	0.95	0.92	0.91

selected tree sequence. At a depth of 50 cm, rotational copulas studied lags. At a depth of 50 cm, the Frank copula all lags, but in the second Clayton's copula (90 and according to the Table

According to the results of forecasting soil temperature at a depth of 50 cm using the vine-based approach and the C-vine copula-based approach, it can be seen that with increasing lags, the RMSE (RMSE) increased approximately 1.5 times. As the lag increases, the amount of RMSE value decreases. It can be seen that the RMSE values compared to the depths of 5, 10 and 30 cm only in lags of one day and three-day, which is better than the other lags. In forecasting soil temperature across different depths and forecast horizons, the amount of RMSE and MAE has a slight decrease. In forecasting of the soil temperature at a depth of 50 cm, the best performance was observed at one-day lag. It can also be seen that in three-day lag approach, the RMSE values of 7, 15 and 30 days, the vine-based approach and the C-vine copula-based approach temperature forecasting at a depth of 50 cm is 95%, which is better than the other approaches. Based on the MAE and RMSE values, it can be seen that in forecasting the soil temperature at a depth of 50 cm, the vine-based approach and the C-vine copula-based approach at seven-day lag, which is better than the other forecast periods of 7 to 30 days. The forecast with a 3-day time window was drawn and presented in the form of Fig.

It can be seen that, in other cases (one-day lags) no points were observed in the acceptable interval. It can be seen that, in the 30-day forecasting of soil temperature, it is confirmed that the vine-based model and the C-vine copula-based model in the simulation and that the forecasted values are better than the observed values.

By examining the forecasting results for different time windows, the results show that in the 30-day window, the best performance was observed with lags of one-day, three-day, five-day and seven-day. In RMSE statistics, the RMSE values are 95% and 98% for the one-day and three-day lags, respectively.

In general, the results of forecasting soil temperature at different depths and forecast horizons using the vine-based approach and the C-vine copula-based approach are as follows: (1) In forecasting soil temperature at a depth of 50 cm, the best performance was observed at one-day lag. (2) In forecasting soil temperature at a depth of 50 cm, the RMSE values of 7, 15 and 30 days, the vine-based approach and the C-vine copula-based approach are 95%, which is better than the other approaches.

3.2.5 Comparing the performance of the best vine copulas in forecasting soil temperature across different depths and forecast horizons

Table 9 summarizes the soil temperature forecasting results for different depths and forecast horizons. It can be seen that in three-day lag approach, the RMSE values of 7, 15 and 30 days, the vine-based approach and the C-vine copula-based approach temperature forecasting at a depth of 50 cm is 95%, which is better than the other approaches. Based on the MAE and RMSE values, it can be seen that in forecasting the soil temperature at a depth of 50 cm, the vine-based approach and the C-vine copula-based approach at seven-day lag, which is better than the other forecast periods of 7 to 30 days. The forecast with a 3-day time window was drawn and presented in the form of Fig.

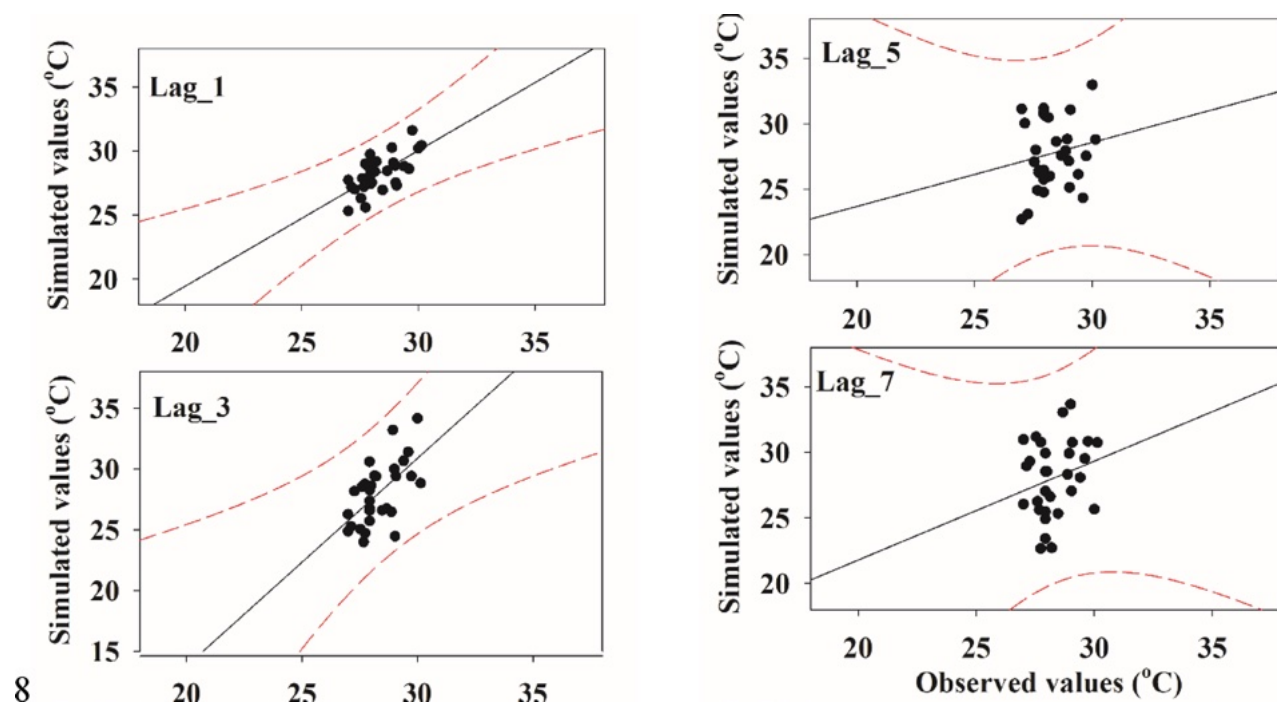


Fig. 19 99% confidence interval of soil temperature forecasting at a deep learning approach

Table 9 The performance of the best vine based model in soil temperature forecasting across different depths (5 cm, 10 cm, 30 cm, and 50 cm) and forecast horizons (1, 3, 5, 7, and 30 days) for model

Soil depth (cm)	Forecast horizons (days)	Lag	Metrics		
			MAE (°C)	RMSE (°C)	NSE
5	1	3	0.19	0.19	0.99
	7	1	0.87	1.25	0.96
	15	1	1.14	1.37	0.97
10	30	1	0.96	1.21	0.98
	1	5	0.71	0.71	0.98
	7	3	0.79	0.93	0.98
30	15	1	0.9	0.98	0.98
	30	1	1.01	1.13	0.98
	1	3	1.05	1.05	0.98
50	7	1	1.26	1.47	0.98
	15	1	0.96	1.21	0.98
	30	1	1.04	1.38	0.97
50	1	1	0.73	0.73	0.99
	7	1	0.78	0.97	0.99
	15	1	0.79	0.99	0.99
	30	1	0.83	1.05	0.99

3.2.6 Comparing the performance of the best vine copulas and deep learning models in forecasting soil temperature

Vine copulas and deep learning approaches to modeling data have their own weaknesses. Vine copulas, as demonstrated by Chen et al. (2020), decompose multivariate dependence into bivariate components. In contrast, deep learning models are highly complex and often lack interpretability. This study compares the performance of these two approaches in forecasting soil temperature. The results show that the vine copula model performs better than the deep learning model in most cases, especially in terms of accuracy and interpretability. The vine copula model is able to capture the complex dependencies between soil temperature variables at different depths and horizons, while the deep learning model struggles to do so. This is likely due to the high dimensionality and non-linear nature of the data, which is better suited to the vine copula approach. The deep learning model, on the other hand, is often a black box, making it difficult to understand how it is making its predictions. This lack of interpretability is a significant drawback in many applications, particularly in risk assessment and decision-making. Therefore, the vine copula model is recommended for soil temperature forecasting in this context.

Table 10 Comparative performance of deep learning (CNN/GRU/LSTM) and vine-based models at different soil depths and time horizons

Soil depth (cm)	Forecast horizon (days)	Deep learning model	Sequence length (days)	Performance metrics (days)		
				MAE (°C)	RMS E (°C)	NSE
5	1	CNN	3	0.77	1.11	0.99
	7	CNN	3	1.6	2.19	0.96
	15	CNN	3	2.29	2.96	0.92
	30	GRU	7	3.3	4.26	0.85
10	1	CNN	3	0.67	0.95	0.99
	7	CNN	3	1.55	2.07	0.96
	15	CNN	3	2.23	2.9	0.92
	30	GRU	7	3.01	3.96	0.86
30	1	CNN	3	0.67	0.43	0.99
	7	CNN	3	1.14	1.51	0.98
	15	CNN	3	1.79	2.34	0.94
	30	GRU	7	2.59	3.29	0.88
50	1	CNN	1	1.2	3.02	0.87
	7	CNN	3	1.09	2.99	0.87
	15	CNN	3	1.7	3.5	0.82
	30	LSTM	7	2.08	3.78	0.8
Vine-based models						
			Lag time (days)			
5	1	Vine-Based	3	0.19	0.19	0.99
	7	Vine-Based	1	0.87	1.25	0.96
	15	Vine-Based	1	1.14	1.37	0.97
	30	Vine-Based	1	0.96	1.21	0.98
10	1	Vine-Based	5	0.71	0.71	0.98
	7	Vine-Based	3	0.79	0.93	0.98
	15	Vine-Based	1	0.9	0.98	0.98
	30	Vine-Based	1	1.01	1.13	0.98
30	1	Vine-Based	3	1.05	1.05	0.98
	7	Vine-Based	1	1.26	1.47	0.98
	15	Vine-Based	1	0.96	1.21	0.98
	30	Vine-Based	1	1.04	1.38	0.97
50	1	Vine-Based	1	0.73	0.73	0.99
	7	Vine-Based	1	0.78	0.97	0.99
	15	Vine-Based	1	0.79	0.99	0.99
	30	Vine-Based	1	0.83	1.05	0.99

superior performance in forecasting soil temperature compared to LSTM models. However, among the deep learning models, the CNN model performs best at depths of 5, 10, and 50 cm, while the GRU model performs best at 30 cm depth. The error rate for forecasting soil temperature for one day ahead is approximately 5%, 10%, and 50% at depths of 5, 10, and 50 cm, respectively, compared to the vine-based approach, while at 30 cm depth, the CNN model performs best. The error rate for forecasting soil temperature for one day ahead is approximately 5%, 10%, and 50% at depths of 5, 10, and 50 cm, respectively, compared to the vine-based approach, while at 30 cm depth, the CNN model performs best.

In the 7-day soil temperature forecasting, the CNN model shows the best performance at depths of 5, 10, and 30 cm, while the GRU model performs best at 30 cm depth. In the 15-day soil temperature forecasting, the CNN model shows the best performance at depths of 5, 10, and 30 cm, while the GRU model performs best at 30 cm depth.

temperature at multiple depths (5, 10, 30, and 50 cm) in Khorramabad, Iran. The study highlights the strengths and limitations of various models, particularly CNNs, in capturing temporal patterns and demonstrating superior performance at shallow depths (5 cm) using a sequence length of 3. However, the Vine copula-based approach and deep learning models across different horizons, achieving significant accuracy (RMSE) and demonstrating superior performance. By leveraging lags of 1, the model effectively modeled complex interactions, making it a reliable choice for uncertainty quantification. The findings underscore the effectiveness of these approaches: deep learning models are well-suited for scalable, data-driven tasks requiring high-dimensional data processing, while Vine-based models are preferred where interpretability, performance on smaller datasets are critical. For soil temperature forecasting, the Vine-based approach is recommended as the most

Appendix A: Tree sequence in different lag and different depth

Table 11 The results of evaluation between deep learning models and best tree sequence

	Tree	Edge	Internal Copula	AIC	Log Likelihood	Best tree sequence
5 cm	1	3, 2	G270	-35, 522	17, 767	R-vine
		1, 3	G270			
		4, 1	F			
	2	1, 2 3	F			
		4, 3 1	F			
		4, 2 1, 3	F			
10 cm	1	3, 2	G270	-35, 158	17, 585	R-vine
		1, 3	G270			
		4, 1	F			
	2	1, 2 3	F			
		4, 3 1	F			
		4, 2 1, 3	F			
30 cm	1	3, 2	G270	-39, 859	19, 936	R-vine
		1, 3	F			
		4, 1	F			
	2	1, 2 3	F			
		4, 3 1	G270			
		4, 2 1, 3	C			
50 cm	1	1, 2	F	-34, 775	17, 393	C-vine
		1, 3	F			
		4, 1	G270			
	2	3, 2 1	C270			
		4, 3 1	C90			
		4, 2 3, 1	C270			

Table 12 The results of examining three nested stepwise methods of vine copula as a tree sequence

	Tree	Edge	Internal Copula	AIC	Log Likelihood	Best tree sequence
5 cm	1	3, 2	G270	-33, 978	16, 995	R-vine
		1, 3	G270			
		4, 1	F			
	2	1, 2 3	F			
		4, 3 1	F			
		4, 2 1, 3	F			
10 cm	1	3, 2	G270	-33, 631	16, 821	R-vine
		1, 3	G270			
		4, 1	F			
	2	1, 2 3	F			
		4, 3 1	F			
		4, 2 1, 3	F			
3 @ m	1	3, 4	G270	-38, 809	19, 411	R-vine
		2, 3	F			
		4, 1	F			
	2	1, 2 3	F			
		4, 3 1	G270			
		4, 2 1, 3	F			
50 cm	1	1, 2	F	-35, 170	17, 592	C-vine
		1, 3	F			
		4, 1	t			
	2	3, 2 1	C270			
		4, 3 1	C90			
		4, 2 3, 1	C270			

Table 13 The results of examining three nested stepwise methods of vine copula as a tree sequence

	Tree	Edge	Internal copula	AIC	Log Likelihood	Best tree sequence
5 cm	1	3, 2	G270	-32, 738	16, 376	R-vine
		1, 3	G270			
		4, 1	F			
	2	1, 2 3	F			
		4, 3 1	t			
		4, 2 1, 3	F			
10 cm	1	3, 2	G270	-32, 380	19, 196	R-vine
		1, 3	G270			
		4, 1	F			
	2	1, 2 3	F			
		4, 3 1	F			
		4, 2 1, 3	F			
3 @ m	1	3, 2	F	-31, 142	18, 182	R-vine
		1, 3	G270			
		4, 1	F			
	2	1, 2 3	C90			
		4, 3 1	F			
		4, 2 1, 3	N			
50 cm	1	1, 2	F	-36, 913	18, 463	C-vine
		1, 3	F			
		4, 1	F			
	2	3, 2 1	C270			
		4, 3 1	C90			
		4, 2 3, 1	C270			

Appendix B

Results of additional accuracy evaluation criteria for evaluating the performance of studied models (Willmott's Index, Absolute Percentage Bias and Explained Variance Score)

Willmott's Index of performance (prediction)
 Absolute Percentage Bias (prediction)
 Explained Variance Score (prediction)
 See Tables 15, 16, 17, 18, 19, 21, and 22

Note:

Table 14 The results of forecasting of 5 cm with different lags and for based approach and R-vine copula-based approach

Lag	Willmott's Index	Absolute Percentage Bias	Explained Variance Score
<i>30-day</i>			
Sim_Lag_1	0.99	3.42	0.28
Sim_Lag_3	0.99	5.43	-0.92
Sim_Lag_5	0.99	4.61	-0.37
Sim_Lag_7	0.98	7.23	-2.10
<i>15-day</i>			
Sim_Lag_1	0.98	4.02	0.21
Sim_Lag_3	0.97	5.65	-2.09
Sim_Lag_5	0.98	4.73	-0.83
Sim_Lag_7	0.96	9.07	-5.85
<i>7-day</i>			
Sim_Lag_1	0.91	3.33	-7.61
Sim_Lag_3	0.87	6.60	-26.20
Sim_Lag_5	0.87	5.64	-19.76
Sim_Lag_7	0.87	8.47	-34.00

Table 16 The results of forecasting of 30 cm with different lags and for based approach and R-vine copula-based approach

Lag	Willmott's Index	Absolute Percentage Bias	Explained Variance Score
<i>30-day</i>			
Sim_Lag_1	0.99	3.77	0.37
Sim_Lag_3	0.99	4.90	-1.30
Sim_Lag_5	0.98	7.73	-4.67
Sim_Lag_7	0.98	9.44	-7.64
<i>15-day</i>			
Sim_Lag_1	0.97	3.62	-1.64
Sim_Lag_3	0.96	5.30	-6.33
Sim_Lag_5	0.95	9.20	-22.12
Sim_Lag_7	0.94	10.61	-33.36
<i>7-day</i>			
Sim_Lag_1	0.88	4.84	-18.94
Sim_Lag_3	0.81	5.04	-20.28
Sim_Lag_5	0.86	8.65	-46.08
Sim_Lag_7	0.75	9.50	-118.42

Table 15 The results of forecasting of 10 cm with different lags and for based approach and R-vine copula-based approach

Lag	Willmott's Index	Absolute Percentage Bias	Explained Variance Score
<i>30-day</i>			
Sim_Lag_1	0.99	3.52	0.31
Sim_Lag_3	0.99	3.51	0.21
Sim_Lag_5	0.98	5.88	-1.87
Sim_Lag_7	0.98	9.55	-5.42
<i>15-day</i>			
Sim_Lag_1	0.98	3.24	0.16
Sim_Lag_3	0.98	3.57	-0.13
Sim_Lag_5	0.96	4.56	-2.54
Sim_Lag_7	0.93	10.90	-12.39
<i>7-day</i>			
Sim_Lag_1	0.92	2.98	-9.58
Sim_Lag_3	0.86	2.96	-10.88
Sim_Lag_5	0.86	2.98	-9.19
Sim_Lag_7	0.82	12.33	-122.71

Table 17 The results of forecasting of 50 cm with different lags and for based approach and R-vine copula-based approach

Lag	Willmott's Index	Absolute Percentage Bias	Explained Variance Score
<i>30-day</i>			
Sim_Lag_1	0.99	2.95	0.46
Sim_Lag_3	0.98	6.28	-4.91
Sim_Lag_5	0.97	8.25	-8.00
Sim_Lag_7	0.97	8.77	-10.55
<i>15-day</i>			
Sim_Lag_1	0.96	2.84	0.02
Sim_Lag_3	0.94	5.64	-21.96
Sim_Lag_5	0.93	8.83	-52.84
Sim_Lag_7	0.92	10.38	-76.20
<i>7-day</i>			
Sim_Lag_1	0.89	2.87	-11.13
Sim_Lag_3	0.88	6.30	-27.91
Sim_Lag_5	0.83	9.35	-115.10
Sim_Lag_7	0.83	10.45	-130.53

Table 18 The results of forecasting g_5 cm will th ednipfeerratrutres evqaul eunecse sa ta nad dfeoprte learning models (CNN, GRU, and LSTM)

Lag	Willmott's index			Absolute percentage of xpilasi ned variance s c					
Model	CNN	GRU	LSTM	CNN	GRU	LSTM	CNN	GRU	LSTM
<i>30-day</i>									
Sim_Seq_0.941	0.941	0.937	0.940	28.269	29.575	28.940	0.797	0.780	0.785
Sim_Seq_0.950		0.955	0.946	24.162	24.697	25.588	0.825	0.830	0.810
Sim_Seq_0.953	0.953	0.956	0.954	23.516	22.940	24.348	0.834	0.846	0.828
Sim_Seq_0.952		0.958	0.953	24.857	22.363	23.552	0.832	0.854	0.828
<i>15-day</i>									
Model	CNN	GRU	LSTM	CNN	GRU	LSTM	CNN	GRU	LSTM
Sim_Seq_0.977	0.977	0.974	0.975	17.988	18.240	18.455	0.919	0.904	0.904
Sim_Seq_0.980		0.976	0.978	17.002	17.464	17.279	0.926	0.918	0.918
Sim_Seq_0.980	0.979	0.979	0.979	17.391	17.557	16.344	0.923	0.923	0.922
Sim_Seq_0.979	0.979	0.979	0.980	17.364	16.385	16.378	0.923	0.928	0.926
<i>7-day</i>									
Model	CNN	GRU	LSTM	CNN	GRU	LSTM	CNN	GRU	LSTM
Sim_Seq_0.987	0.987	0.987	0.986	13.782	13.753	14.796	0.954	0.949	0.946
Sim_Seq_0.989		0.986	0.988	13.209	13.856	12.957	0.958	0.953	0.956
Sim_Seq_0.989	0.988	0.988	0.989	13.023	13.268	12.801	0.959	0.956	0.957
Sim_Seq_0.989	0.989	0.989	0.988	13.277	12.761	12.842	0.959	0.959	0.958

Table 19 The results of forecasting g_{10} cm will th ednipfeerratrutres evqaul eunecse sa ta nad dfeoprte learning models (CNN, GRU, and LSTM)

Lag	Willmott's index			Absolute percentage of xpilasi ned variance s c					
Model	CNN	GRU	LSTM	CNN	GRU	LSTM	CNN	GRU	LSTM
<i>30-day</i>									
Sim_Seq_0.943	0.943	0.943	0.941	26.945	26.668	27.795	0.806	0.797	0.789
Sim_Seq_0.945		0.950	0.952	25.739	24.175	23.258	0.817	0.820	0.818
Sim_Seq_0.943	0.943	0.958	0.955	29.563	23.149	22.136	0.809	0.846	0.823
Sim_Seq_0.947	0.947	0.961	0.960	27.733	22.121	21.258	0.822	0.860	0.849
<i>15-day</i>									
Model	CNN	GRU	LSTM	CNN	GRU	LSTM	CNN	GRU	LSTM
Sim_Seq_0.978	0.978	0.977	0.977	17.328	17.278	16.916	0.920	0.912	0.913
Sim_Seq_0.979	0.980	0.980	0.979	17.138	15.890	16.242	0.921	0.924	0.921
Sim_Seq_0.979	0.980	0.980	0.979	17.593	16.514	15.762	0.921	0.928	0.922
Sim_Seq_0.978	0.981	0.981	0.979	18.227	15.355	15.250	0.917	0.932	0.927
<i>7-day</i>									
Model	CNN	GRU	LSTM	CNN	GRU	LSTM	CNN	GRU	LSTM
Sim_Seq_0.990	0.988	0.988	0.988	12.381	12.635	12.836	0.960	0.953	0.951
Sim_Seq_0.990	0.989	0.989	0.989	12.438	12.109	12.073	0.961	0.958	0.956
Sim_Seq_0.988	0.989	0.989	0.990	13.777	12.035	12.003	0.955	0.959	0.960
Sim_Seq_0.990	0.990	0.990	0.989	12.079	11.798	11.698	0.960	0.961	0.959

Table 20 The results of forecasting 30 cm will the deep feed networks equivalent to a random forest learning models (CNN, GRU, and LSTM)

Lag	Willmott's index			Absolute percentage error			Explained variance score		
	CNN	GRU	LSTM	CNN	GRU	LSTM	CNN	GRU	LSTM
<i>30-day</i>									
Sim_Seq_01955	0.956	0.955	0.955	22.814	22.395	22.293	0.833	0.838	0.834
Sim_Seq_03954	0.958	0.958	0.958	23.337	22.558	21.902	0.834	0.846	0.846
Sim_Seq_05958	0.959	0.961	0.961	22.012	22.130	20.231	0.850	0.847	0.853
Sim_Seq_07960	0.969	0.970	0.970	21.034	20.170	17.972	0.850	0.889	0.883
<i>15-day</i>									
Model	CNN	GRU	LSTM	CNN	GRU	LSTM	CNN	GRU	LSTM
Sim_Seq_01984	0.983	0.982	0.982	13.778	14.159	14.817	0.942	0.933	0.933
Sim_Seq_03985	0.983	0.984	0.984	13.878	14.420	13.606	0.943	0.939	0.936
Sim_Seq_05982	0.982	0.982	0.982	15.063	14.493	14.143	0.938	0.934	0.931
Sim_Seq_07984	0.984	0.983	0.983	14.509	14.028	13.901	0.939	0.941	0.937
<i>7-day</i>									
Model	CNN	GRU	LSTM	CNN	GRU	LSTM	CNN	GRU	LSTM
Sim_Seq_01993	0.992	0.993	0.993	9.359	9.384	9.543	0.977	0.969	0.971
Sim_Seq_03994	0.991	0.991	0.991	9.188	10.318	9.731	0.976	0.969	0.966
Sim_Seq_05993	0.992	0.992	0.992	9.697	10.052	10.083	0.973	0.970	0.972
Sim_Seq_07993	0.992	0.993	0.993	9.939	10.319	9.579	0.972	0.971	0.972

Appendix C

The mathematical formulations governing our deep learning architecture are presented below the CNN model

The CNN architecture for regression tasks comprises the following key components.

The input usually consists of a 1D time series data, expressed as:

$$Input = [x_1, x_2, \dots, x_T]$$

where T denotes the duration. X_t represents the value at the operation utilizes a 1D filter to extract features. The result is:

$$output(i) = \sum_{n=0}^{N-1} Kernel(n) \cdot input(i+n) \tag{9}$$

$Kernel(n)$ 1D filter sequence, $input(i+n)$ represents the input sequence at position $i+n$, and $output(i)$ indicates the resulting of the convolution.

Table 21 The results of forecasting 50 cm will the deep feed networks equivalent to a random forest learning models (CNN, GRU, and LSTM)

Lag	Willmott's index			Absolute percentage error			Explained variance score		
	CNN	GRU	LSTM	CNN	GRU	LSTM	CNN	GRU	LSTM
<i>30-day</i>									
Sim_Seq_01929	0.938	0.940	0.940	18.135	16.376	15.716	0.717	0.762	0.768
Sim_Seq_03935	0.943	0.944	0.944	15.942	14.965	14.408	0.742	0.774	0.781
Sim_Seq_05931	0.944	0.947	0.947	15.571	14.724	13.979	0.726	0.790	0.795
Sim_Seq_07935	0.946	0.948	0.948	15.169	14.235	12.538	0.753	0.786	0.800
<i>15-day</i>									
Sim_Seq_01951	0.954	0.953	0.953	11.694	11.239	10.882	0.807	0.821	0.818
Sim_Seq_03956	0.956	0.957	0.957	10.629	11.200	11.020	0.832	0.833	0.825
Sim_Seq_05957	0.957	0.958	0.958	10.495	11.111	10.506	0.831	0.831	0.834
Sim_Seq_07954	0.958	0.957	0.957	11.062	10.460	11.103	0.825	0.840	0.837
<i>7-day</i>									
Sim_Seq_01968	0.967	0.967	0.967	7.235	7.764	7.333	0.870	0.860	0.866
Sim_Seq_03968	0.965	0.965	0.965	6.948	7.739	8.096	0.871	0.864	0.857
Sim_Seq_05966	0.964	0.960	0.960	7.132	7.729	7.527	0.869	0.856	0.840
Sim_Seq_07967	0.965	0.965	0.965	7.155	7.878	7.457	0.869	0.858	0.862

convolution, an activation function such as ReLU (6) Sigmoid, Tanh, or Linear functions is applied to introduce non-linearity. For regression tasks, ReLU (Rectified Linear Unit) is common (2019; a parallel with dropout represents input gate which to update the candidate memory information to potentially store

$$ReLU(x) = \max(0, x); Sigmoid(x) = \frac{1}{1 + e^{-x}}; \quad (10) \quad C_t = f_t \cdot C_{t-1} + i_t \cdot \tilde{C}_t \quad (17)$$

$$\tanh(x) = \frac{e^x - e^{-x}}{e^x + e^{-x}}; Linear(x) = x$$

Pooling decreases the dimensionality of the input maps. In the case of 1D CNNs, max pooling is employed, as described below:

$$MaxPooling(i) = \max(output(i + m)) \quad (11) \quad o_t = \sigma(W_f \cdot (h_{t-1}, x_t) + b_o) \quad (18)$$

Here m denotes the size of the pooling window. Following multiple convolution and pooling layers, the output is flattened and passed through one or more fully connected (dense) layers. The output is then passed through a linear layer expressed as

$$y = W \cdot x + b \quad (12)$$

Here x represents the flattened input, W is the weight matrix, b is the bias vector, and y is the output of the fully connected layer. The loss function measures the discrepancy between the forecasted and actual values. The weights are adjusted using gradient descent. The update rule is as follows:

$$W_{update} = W_{old} - \left(Learning\ Rate \cdot \frac{\partial Loss}{\partial W} \right) \quad (13)$$

where $\frac{\partial Loss}{\partial W}$ is the gradient of the loss with respect to the weight matrix. Learning rate determines the step size during the training process as described by Shi et al. (2021):

$$r_t = \sigma(W_r \cdot (h_{t-1}, x_t) + b_r) \quad (20)$$

The LSTM model

The equations of the LSTM model operations are as follows: the previous time step's input and hidden state are used to calculate the forget gate, input gate, and candidate hidden state.

$$f_t = \sigma(W_f \cdot (h_{t-1}, x_t) + b_f) \quad (14)$$

Here σ represents the sigmoid function, which produces values between 0 and 1. W_f is the weight matrix for the forget gate, h_{t-1} is the previous hidden state, x_t is the input at time t , and b_f is the bias term for the forget gate.

$$i_t = \sigma(W_i \cdot (h_{t-1}, x_t) + b_i) \quad (15)$$

- Feng Y, Cui N, Hao W, Gao L, Gong R (2019) Interrelationships of soil temperature from meteorological data and ground temperature prediction models. *Geoderma* 338:67–74. <https://doi.org/10.1016/j.geoderma.2019.03.014>
- Genest C, Favre AC (2007) Everything we know about copula modeling but we were afraid to ask. *Journal of the Royal Statistical Society B* 69(4):651–676. <https://doi.org/10.1111/j.1467-9868.2007.00556.x>
- Ghimire S, Nguyen-Huy T, Al-Musayih MS, Shorideh R, Chaostolvaalst-Appenzeller D, Salcedo-Sanz S (2023) Integrating deep learning-based self-attention transformer model for electricity load forecasting. *Energy* 378:124763. <https://doi.org/10.1016/j.energy.2023.124763>
- Ghimire S, Al-Musayih MS, Nguyen-Huy T, Acharya R, Casillas-Pérez D, Yaseen Z-M, Nadeem M, Samizadeh J (2025) A novel deep learning-based neural network for predicting river flow using probabilistic confidence interval. *Energy* 378:124763. <https://doi.org/10.1016/j.energy.2023.124763>
- Guo J, Chen C, Wen H, Cai G, Liudyn A (2024) Prediction of coal temperature based on PSO-GRU-based deep neural network. *Stud Therm Eng* 53:103813. <https://doi.org/10.1016/j.stther.2024.103813>
- Hao H, Yu F, Li Q (2020) Soil temperature prediction using convolutional neural network based on empirical mode decomposition. *IEEE Access* 9:40844–40851. <https://doi.org/10.1109/ACCESS.2020.3010233>
- Hochreiter S, Schmidhuber J (1997) Long short-term memory. *Neural Comput* 9(8):1735–1780. <https://doi.org/10.1162/NECO.1997.9.8.1735>
- Imanian H, Hiedra Cobo J, Payeur J, Mohammadian A (2022) A comprehensive study of soil temperature prediction using deep learning models and extremely hot events. *Journal of Applied Meteorology and Climatology* 61(1):1–12. <https://doi.org/10.1175/JAMC-D-21-0111.1>
- Imanian H, Mohammadian A, Farhadi M, Payeur J, Hiedra Cobo J, Shirkhani H (2024) A comparative analysis of deep learning models for soil temperature prediction in semi-arid climates. *Theor Appl Climatol* 150(4):2575–2587. <https://doi.org/10.1007/s00137-024-02575-7>
- Jaworski P, Durante F, Hardle WK (2010) Copula theory and its applications, vol 19. *Springer*, New York
- Khashei-Siuki A, Shahidi A, Ramezani S, Hamedani GG (2023) Simulation of potential evapotranspiration using a bivariate copula. *Meteorol Appl* 28(5):e202301-023-01929-y. <https://doi.org/10.1002/met.2023.01929-y>
- Kisi O, Tombul M, Kermani MZ (2015) Soil temperature prediction at different depths by using three deep neural computing techniques. *Theor Appl Climatol* 121(3):777–787. <https://doi.org/10.1007/s00137-015-0777-7>
- Kizito R, Scruggs P, Li X, Devlin M, Jbaansseedn M, deKlrsos R (2021) Short-term memory networks for wildfire risk assessment of remaining useful life prediction. *IEEE Access* 9:6585–6594. <https://doi.org/10.1109/ACCESS.2021.3010233>
- Lai G, Chang W, Yang Y, Lin L, He M, Li J (2018) Soil temperature prediction using deep learning model with data augmentation. *In The 41st International ACM SIGKDD Conference on Knowledge Discovery and Data Mining* (2018):1–10. <https://doi.org/10.1145/3214131.3214139>
- Lee T, Shin JY, Kim JS, Singh R (2020) Soil temperature prediction using deep learning model. *Journal of Hydrology* 587:125450. <https://doi.org/10.1016/j.jhydrol.2020.125450>
- Li C, Zhang Y, Ren X (2020) Modeling soil temperature using deep BiLSTM neural network. *Applied Mathematics* 11(7):1373–1383. <https://doi.org/10.1007/s11464-020-07313-9>
- Li Z, Liu F, Yang W, Peng S, Zhou J (2021) A novel deep learning-based neural networks: analysis, applications, and prospects. *IEEE Trans Neural Netw Learn Syst* 32(9):999–1010. <https://doi.org/10.1109/TNNLS.2021.3010233>
- Li Q, Zhu Y, Shanguan W, Wang X, Li H, Ge Y (2022) A novel soil temperature aware LSTM model for soil moisture and soil temperature prediction. *Geoderma* 409:115651. <https://doi.org/10.1016/j.geoderma.2022.115651>
- Lü TJ, Tang XS, Li DQ, Qi XH (2020) Prediction of multiple soil parameters using a deep learning model. *Geotech* 118:103340. <https://doi.org/10.1016/j.geotech.2020.103340>
- Ma L, Pan SB, Dai XG, Song S, Shiva A (2020) Deep learning-based forecasting model of working face temperature. *Journal of Xi'an Univ Sci Technol* 40:363–368. <https://doi.org/10.1029/2004WR003133>
- Mampitiya L, Rozumbetov K, Ratsanayake R, Gerdke M, Velasco R, Arachchi S, Kantamaneni K, Hettiarayo A, Ratahntaiyak J (2024) En

