

Reinforcement Learning-Based Bezier Airship Hull Optimization: A Data-Driven Framework for Shape Adaptation Under Aerodynamic Constraints

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Abstract. This paper proposes a data-driven reinforcement learning framework for aerodynamic optimization of airship hulls. It combines Deep Deterministic Policy Gradient (DDPG) with Bezier curve parameterization to adjust the shape of the classic airship "Lotte" [1,2,3]. A volume-preserving constraint ensures buoyancy consistency. Different from previous studies focused solely on drag minimization, we target lift-to-drag ratio (L/D) and robustness [4,5]. Simulations in SILCROAD [6,7,8,9] demonstrate significant improvement in L/D while preserving volume and smoothness. The approach offers a modular, scalable framework for future multi-objective extensions..

Introduction

Airships are regaining attention for applications like surveillance, communication relay, and environmental monitoring [12]. A key design challenge is aerodynamic shape optimization of the hull, which affects drag, L/D , energy use, and mission range.

Traditional airship shapes often rely on empirical formulas or fixed parametric models, limiting flexibility for mission-specific designs. Prior aerodynamic optimization focused primarily on drag at constant angles, overlooking L/D , a critical factor for propulsion and endurance [11].

Reinforcement learning (RL) offers a flexible alternative for high-dimensional, constraint driven problems. Unlike gradient-based methods, RL learns from interaction and handles noisy evaluations.

This work introduces an RL framework integrating DDPG and Bezier parameterization for airship optimization [10]. The agent modifies control points to maximize L/D while preserving volume. Evaluation is performed using SILCROAD [6,7,8,9].

Main contributions include: (1) reinforcement learning with embedded physical constraints, (2) continuous shape control via Bezier parameters, and (3) performance improvements in L/D and robustness.

Methodology

The upper hull is modeled with a Bezier curve using $n + 1$ control points $\{P_0, \dots, P_n\}$. The curve is:

$$R(x) = \sum_{i=0}^n B_{i,n}(x)P_i, \quad B_{i,n}(x) = \binom{n}{i} (1-x)^{n-i} x^i \quad (1)$$

where $x \in [0, 1]$ is the normalized axial coordinate. Endpoints P_0, P_n are fixed at zero and the agent adjusts the $n - 1$ interior points.



Volume is maintained via scaling factor λ :

$$\lambda = \sqrt{\frac{V_0}{V'}}, \quad P_i^{\text{scaled}} = \lambda P_i, \quad (2)$$

where V_0 is the volume of the original hull and V' is the volume of the perturbed shape, both computed via

$$V = \pi \int_0^L R(x)^2 dx \quad (3)$$

Here, L denotes the length of the hull.

RL formulation. The state is the set of current radii; the action is a perturbation vector on the interior control points. The reward is:

$$r = \omega_1 \left(\frac{L}{D} \right)_{avg} - \omega_2 \sigma_{\frac{L}{D}} - \omega_3 \|\Delta P\|_1 \quad (4)$$

The weights in (4) trade off performance and regularity. ω_1 scales the primary objective $(L/D)_{avg}$ (suggested range 0.5–1; we use $\omega_1 = 1$ to keep the natural scale and emphasize aerodynamic merit). ω_2 would penalize the variability $\sigma_{L/D}$ across α to promote robustness (typical 0–0.5), but is set to $\omega_2=0$ here because our solver interface returns only the mean L/D . ω_3 regularizes shape smoothness via $\|\Delta P\|_1$ (implemented as the mean absolute first difference of control-point radii), for which 0.05–0.2 keeps the penalty one order below $(L/D)_{avg}$; we choose $\omega_3=0.1$ as it curbs oscillatory updates without suppressing beneficial adjustments. Hence, $(\omega_1, \omega_2, \omega_3) = (1, 0, 0.1)$, matching the implementation $reward = AvgLD - 0.1 * smoothPenalty$.

Learning algorithm. Training uses MATLAB Reinforcement Learning Toolbox's rlDDPGAgent, the built-in implementation of the Deep Deterministic Policy Gradient (DDPG) algorithm—an off-policy, model-free actor–critic method for continuous-action control with a deterministic policy, experience replay, and target networks. Actor and critic networks are two-layer multilayer perceptrons. At each episode, the agent queries SILCROAD to compute the L/D curve over an angle-of-attack grid spanning 0°–30°; the resulting mean (and, when used, dispersion) of L/D across this range feeds the reward in (4).

Result and Discussion

Trained over 10,000 episodes, the agent consistently outperforms the baseline.

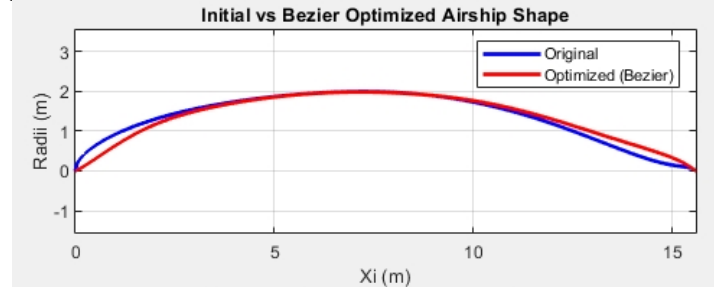


Figure 1: Original and optimized Bezier-based hull shapes.

Figure 1 shows original vs optimized shapes. The optimized hull has a smoother profile with gradual tapering.

The shape preserves volume:

$$V_0 = V_{final} = 107.5273 \text{ m}^3, \quad \lambda = 1.16$$

Figure 2 shows the L/D improvement. Average values:

$$\left(\frac{L}{D}\right)_{\text{initial}} = 4.7766, \quad \left(\frac{L}{D}\right)_{\text{optimized}} = 5.3044, \quad \text{Gain} = +11.05\%$$

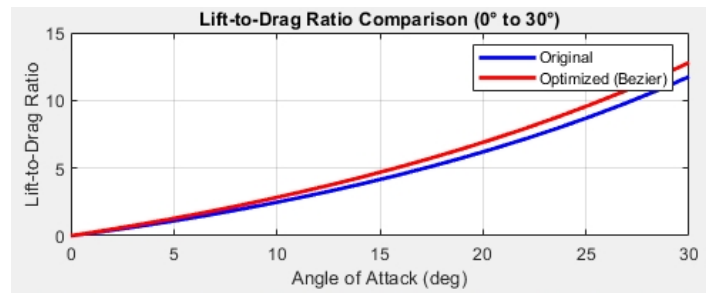


Figure 2: Lift-to-drag ratio comparison (0° – 30° angle of Attack).

Perturbation tests showed reduced standard deviation in L/D . Shape smoothness was retained via $\|\Delta P\|_1$.

Conclusion

This study presented a reinforcement-learning-based framework for airship shape optimization. The DDPG agent adjusted Bezier control points while preserving volume. Evaluation in SILCROAD confirmed an 11.05% L/D improvement with retained robustness and smoothness [13]. The framework is modular, supporting future extensions such as tail design and stability control.

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