

# Novel beamline for attosecond transient reflection spectroscopy in a sequential two-foci geometry

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We present an innovative beamline for extreme ultraviolet (XUV)-infrared (IR) pump-probe reflection spectroscopy in solids with attosecond temporal resolution. The setup uses an actively stabilized interferometer, where attosecond pulse trains or isolated attosecond pulses are produced by high-order harmonic generation in gases. After collinear recombination, the attosecond XUV pulses and the femtosecond IR pulses are focused twice in sequence by toroidal mirrors, giving two spatially separated interaction regions. In the first region, the combination of a gas target with a time-of-flight spectrometer allows for attosecond photoelectron spectroscopy experiments. In the second focal region, an XUV reflectometer is used for attosecond transient reflection spectroscopy (ATRS) experiments. Since the two measurements can be performed simultaneously, precise pump-probe delay calibration can be achieved, thus opening the possibility for a new class of attosecond experiments on solids. Successful operation of the beamline is demonstrated by the generation and characterization of isolated attosecond pulses, the measurement of the absolute reflectivity of SiO<sub>2</sub>, and by performing simultaneous photoemission/ATRS in Ge.

## I. INTRODUCTION

In the last twenty years, the exploitation of high-order harmonic generation (HHG) in gases has opened new possibilities for the investigation of fundamental processes in atoms, molecules and solid-state materials with extreme temporal resolution<sup>1,2</sup>. High-order harmonics originate from the interaction of an intense ( $\sim 10^{14}$  W/cm<sup>2</sup>) infrared (IR) femtosecond pulse with a nonlinear medium (typically a noble gas). Under particular conditions, harmonic emission occurs every half optical cycle of the IR field (about 1 fs), hence the XUV light is naturally emitted in the form of an attosecond pulse train (APT)<sup>3</sup>. By gating the HHG process, it is possible to isolate single attosecond pulses (SAPs) from the train<sup>4</sup>. This sets the foundation for the development of a new branch of ultrafast spectroscopy: Attosecond Science. The low efficiency of the HHG process (typically of the order of  $10^{-6} - 10^{-7}$ ) limits the intensity of standard attosecond light sources, which are usually combined with a portion of the fundamental IR pulses in order to perform pump-probe spectroscopy without compromising the time resolution. First pioneering experiments based on time-resolved photoelectron spectroscopy have shown the capability of such a configuration to resolve ultrafast dynamics like Auger decay after inner core excitation in atoms<sup>4</sup>, tunnelling by strong field ionization<sup>5</sup>, electron motion in atoms<sup>6</sup> and molecules<sup>7</sup> by using single attosecond pulses<sup>8</sup> or attosecond pulse trains<sup>9</sup>. More recently, attosecond photoelectron spectroscopy has been used to study the ultrafast dynamics involved in the photoionization process<sup>10</sup>, with

particular attention to photoemission from solid targets<sup>11–16</sup>. Complementary aspects of light-matter interaction can be studied with all-optical techniques<sup>17,18</sup>. In this framework, attosecond transient absorption spectroscopy (ATAS)<sup>19,20</sup> has established as a powerful tool for the investigation of sub-fs electron dynamics in insulators<sup>21–24</sup>, semiconductors<sup>25,26</sup> and metals<sup>27</sup>. One of the key elements is the possibility to combine ATAS with a simultaneous, in-situ, calibration measurement of the IR pump electric field. This is normally done by injecting a noble gas as close as possible to the solid target and collecting the spectrum of the electrons photoemitted by the XUV radiation in the presence of the delayed IR pulse (see Sec. III A) while performing the ATAS measurement. In this way, it is possible to study the precise timing between the observed dynamics in the solid and the pump electric field<sup>28</sup>, potentially revealing new physical phenomena<sup>29</sup>.

Despite the outstanding results discussed above, the combination of high absorption coefficient in the XUV spectral range and relatively low photon flux of standard attosecond light sources, forces the samples to have thickness of the order of few tens of nanometers. Since this is not always possible, the applicability of the ATAS technique is strongly limited. Very recently, C. J. Kaplan and coworkers have shown that equivalent information can be obtained by looking at transient changes in the sample reflection rather than absorption<sup>30–34</sup>. Therefore, attosecond transient reflection spectroscopy (ATRS) candidates as a powerful tool to investigate ultrafast carrier dynamics in solids, which cannot be manufactured in thin membranes. While the applicability of ATRS in the few-fs domain has been already demonstrated<sup>31</sup>, a clear observation of sub-fs dynamics is still missing. Furthermore, the more complex geometry needed to collect reflected rather than transmitted XUV radiation, makes it impossible to easily combine a reference gas target with ATRS.

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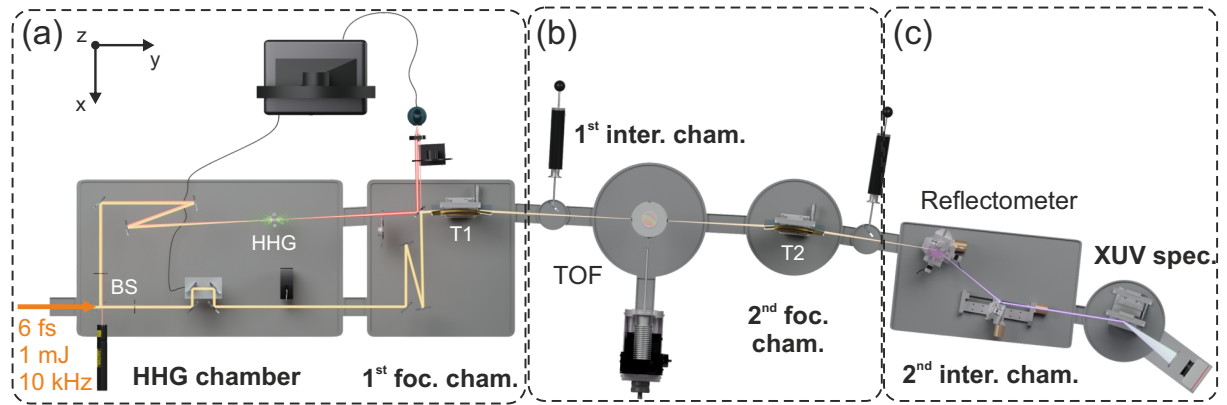


FIG. 1: Orthogonal projection of the beamline setup. (a) HHG chamber and first focusing chamber which compose the actively stabilized interferometer. (b) First interaction chamber equipped with a TOF spectrometer, followed by the refocusing chamber. (c) Reflectometer for solid samples placed in the second interaction chamber together with an XUV spectrometer.

As a consequence, this hinders the possibility to access the attosecond timing of the observed dynamics with respect to the pump field. Here we report on the development and application of the first attosecond beamline for ATRS in a sequential double-foci geometry<sup>35</sup>, which allows to overcome this limit. The beamline is composed by two separate interaction regions. The first region is equipped with a time-of-flight (TOF) spectrometer for photoelectron spectroscopy in gas targets. The second focus hosts a versatile XUV reflectometer. After a precise measurement of the phase delay induced by light propagation between the two foci<sup>36</sup> (see Sec. III B), the beamline enables direct calibration of the pump-probe delay without introducing any additional geometrical limitation on the solid target, thus opening the possibility to investigate light-matter interaction in bulk samples with attosecond all-optical spectroscopy.

This paper is organized as follows: Section II presents the innovative beamline addressing separately each of its main constituents. In Sec. III we report on the results of some experimental measurements which validate our setup.

## II. EXPERIMENTAL SETUP

The primary laser system is a commercial, 10-kHz laser system (AURORA, Amplitude Technologies), which generates pulses at a central wavelength of 800 nm, with an energy of 2 mJ, a full-width-half-maximum (FWHM) temporal duration of 25 fs and stable carrier-envelope phase (CEP). The shot-to-shot CEP standard deviation is 320 mrad<sup>37</sup>, while the average rms deviation measured with a f-to-2f interferometer placed in front of the pump-probe setup and sampled every 150 ms with 1-ms integration time is of 105 mrad. Additional temporal pulse shortening is achieved through a hollow-core fiber compression system<sup>38</sup> in combination with a battery of chirped mirrors. At the output of this stage, we obtain IR pulses with bandwidth ranging between 500 and 1200 nm, a time duration of less than 6 fs and pulse energy of about 1 mJ. The compressed pulses enter the beamline (Fig. 1), composed

of three main blocks: (a) HHG chamber and actively stabilized interferometer, (b) first interaction region for gas phase targets and (c) second interaction region with an XUV reflectometer for solid samples.

### A. HHG and actively stabilized interferometer

Figure 2(a) shows the first main block of the beamline. After compression, the IR pulses enter a first evacuated chamber where they are split by a 70-30 broadband beam splitter (BS). The reflected part of the IR radiation (70%) is focused by a converging mirror (FM1,  $ROC = 1$  m) onto a gas target (GT) for HHG. This latter is composed by three interchangeable 1-cm-thick gas cells, which are closed on both sides by an aluminum tape and filled with a noble gas (typically Ar). The IR laser drills an entrance and exit hole in the tape, providing efficient gas confinement (beam spot size on the target is  $\sim 150 \mu\text{m}$ ). The cells are mounted on a motorized xyz-translation stage allowing for fine alignment. This, in combination with a motorized iris (II) placed on the beam path before HHG, allows to optimize the phase matching in real time. After XUV generation the beam enters a second evacuated chamber where the residual IR radiation is removed by a proper metallic filter. The filters are mounted on a filter wheel (FW) which enables different filter selection without breaking the vacuum.

The transmitted part of the IR radiation (30%) follows a delay line before being collinearly recombined with the harmonic radiation by a double-drilled mirror at 45° (DM), placed in the second chamber. The pulse energy is controlled through a motorized iris (I2), while the delay between the XUV and IR pulses is controlled by a retro-reflector mounted on a translation stage (TS) with nanometer resolution (Smart SLC-2445-S-HV). A mechanical shutter (MS) placed on the delay line is used to achieve efficient noise subtraction in the measurement. The mechanical design of the shutter is based on the voice-coil actuator used in hard disk drivers<sup>39</sup>, which can be driven at a frequency of 1 Hz in vacuum for

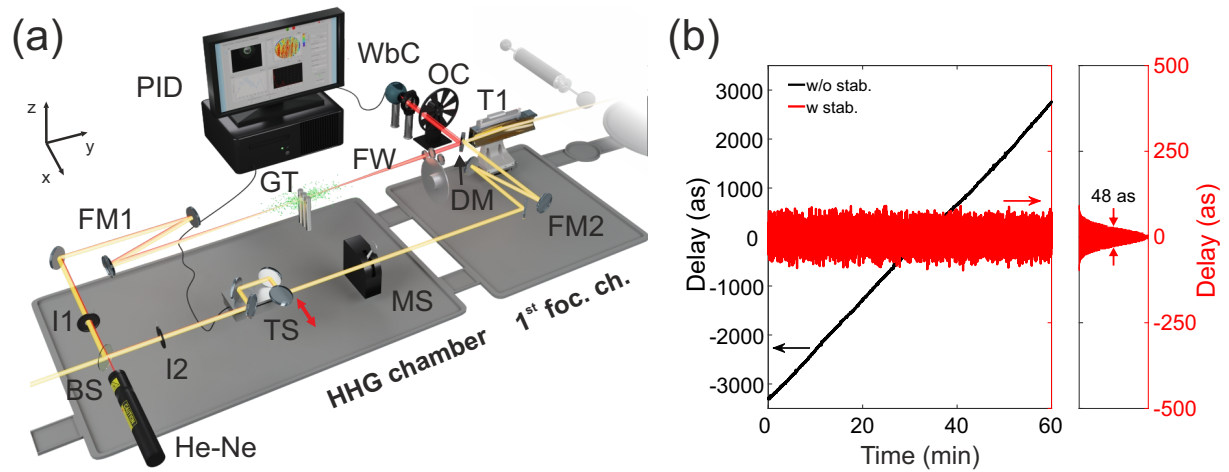


FIG. 2: (a) Schematic drawing of the HHG interferometer composed by two vacuum chambers (Fig. 1(a)). The IR beam is represented in orange, the XUV in violet and the He-Ne used for active stabilization in red. The meaning of the labels which mark the optical elements is discussed in the text. (b) Comparison between the phase variation recorded by the webcam (WbC) with (red) and without (black) the active stabilization system, over a period of 60 minutes. The active stabilization system manages to correct the interferometer instabilities down to a standard deviation  $\sigma$  of about 24 as.

hours without overheating. A diverging mirror (FM2,  $ROC = 1.2$  m), placed in the second chamber before recombination, is used to match the IR beam divergence to the one of the XUV beam. In this way the two beams are focused onto the same plane by the first toroidal mirror (T1).

In order to perform time-resolved experiments with attosecond temporal resolution, very precise relative timing between pump and probe pulses is required. Any mechanical instability or thermal drift can introduce uncontrolled delay between the two interferometer arms, hence compromising the success of the experiment. Therefore, we implemented an active stabilization system. A frequency-stabilized helium-neon (He-Ne in Fig. 2) laser beam (at  $\sim 633$  nm) enters the interferometer through initial beamsplitter and follows the same paths of pump and probe pulses up to the double-drilled mirror. To avoid the He-Ne beam to be blocked by the metallic filters in the XUV path, we exploit the different propagation properties of this beam. Being characterized by a stronger spatial divergence, an annular part of the He-Ne beam passes through the glass support of the metallic filter<sup>40</sup>. This portion of the beam is then reflected by the back of the double-drilled mirror and recombined with the He-Ne radiation which comes from the other arm of the interferometer and passes through the second hole in the mirror. The spatial interference fringes of these two beams are then measured by a web-cam (WbC), that is placed after an optical chopper (OC) suitably synchronized to remove the residual IR radiation. Figure 2(b) shows the interferometer stability measured under the same conditions as for a real pump probe experiment (main laser at 800 nm passing through the beamline). Using a digital PID controller acting on the delay stage, it is possible to stabilize the pump-probe relative delay with a residual standard deviation  $\sigma = 24$  as. In order to ensure that the active stabilization system is not affected by the shutter action, we monitor the He-Ne fringes contrast. Whenever the shutter is closed and the contrast falls

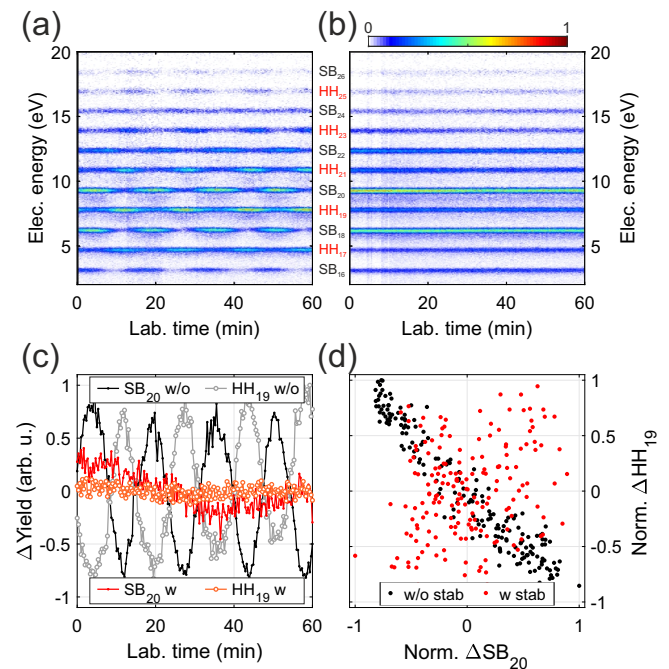


FIG. 3: In-situ temporal stability measurement. (a) Photoelectron spectra obtained by ionizing Ne atoms with an attosecond pulse train and an IR pulse at a fixed relative delay without active stabilization. (b) Same as (a) but with active stabilization of the interferometer. (c) Yield variation for SB20 and HH19, centered respectively at 9.3 and 7.7 eV, without (black-gray) and with (red-orange) active stabilization. (d) Correlation between SB20 and HH19 normalized variations around their average value without (black dots) and with (red dots) active stabilization.



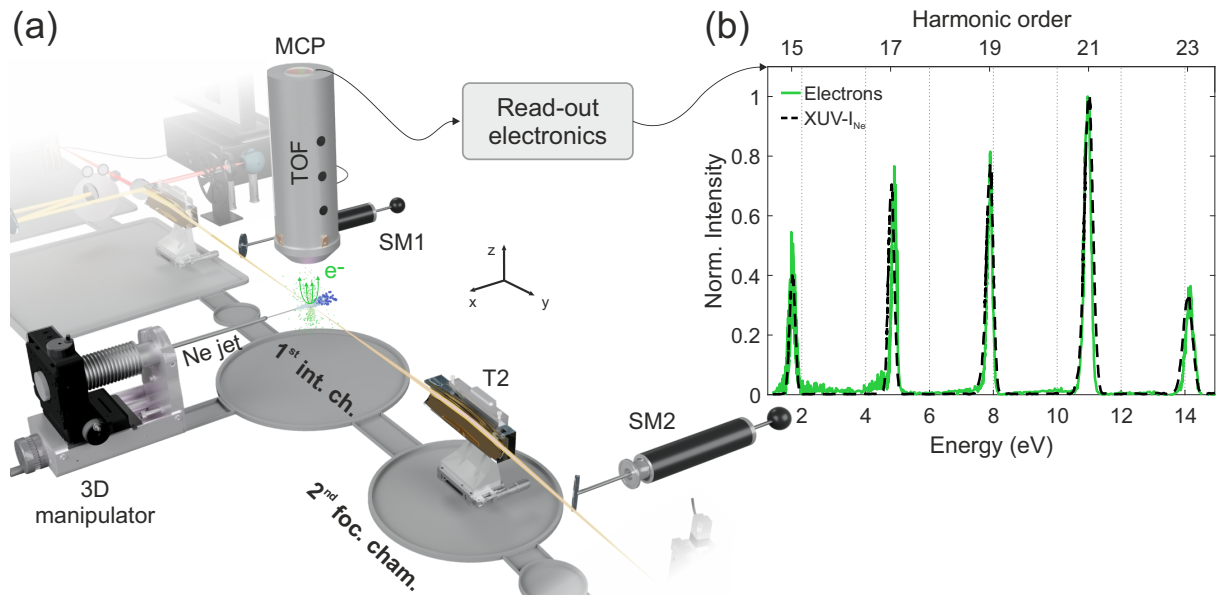


FIG. 4: **(a)** Schematic of the first interaction chamber and second refocusing mirror. A gas target is placed through an open needle in the first focus. The photoelectrons coming from the gas target are accelerated by static fields into a flying tube of a TOF before impinging on a micro-channel plate (MCP). The time evolution of the MCP current is recorded by a read-out electronics, leading to the photoelectron spectrum in **(b)** (green curve). The black dashed curve represents the ionizing XUV radiation as measured by the XUV spectrometer at the end of the line. The photon energy axis has been shifted by the gas ionization potential (in this case Ne,  $I_{Ne} \simeq 21.56$  eV).

below a threshold value we block the feedback and store the current fringes phase value. When the shutter opens, the contrast rises and the stabilization feedback is turned back on. If the unmonitored phase variation during the “shutter off” state is smaller than  $2\pi$  (equivalent to  $\simeq 4.7$  fs), the absolute reference is not lost. We find this condition to be always verified in our experiments.

It is worthy to point out that any fluctuation of the double-drilled mirror is not sampled by the He-Ne beam. Therefore, the delay stability measured by the fringes does not necessarily coincides with the stability of the real pump-probe interferometer at the target position. To prove the goodness of our approach, we ionized Ne atoms with an XUV pulse train at the presence of an IR pulse and acquired the photoelectron spectrum every 30 seconds for a total time frame of one hour. The results are reported in Figs. 3(a) and (b) without and with the active stabilization. The photoelectron spectrum is characterized by discrete peaks which correspond to direct XUV ionization (high-harmonics, labeled with HH) or to two-color ionization involving one XUV and one IR photon (sidebands, labeled with SB). For a perfectly stable interferometer we expect HH and SB yields to stay constant in laboratory time (see discussion in Sec. III B). An unstable delay between the two arms will instead result in a variation of the SB signals followed by an opposite change in the HH signals. As an example, Fig. 3(c) shows the time evolution of HH19 and SB20 without (gray scale) and with (red scale) active stabilization. Without stabilization HH19 and SB20 evolve in time with almost perfect anti-correlation (black dots in Fig. 3(d), Pearson correlation coefficient  $r = -0.9616$ ). When the sta-

bilization system is turned on, HH19 and SB20 yields are almost constant in time and the correlation degree is strongly decreased (red dots in Fig. 3(d), Pearson correlation coefficient  $r = 0.2576$ ). The residual positive correlation may originate from laser instabilities or acquisition noise which affect HH and SB signals in the same way.

## B. First interaction region and refocusing

After recombination, XUV and IR pulses are focused by a gold-coated toroidal mirror (T1 in Fig. 4(a)) with radii  $R_{mer} = 14335$  mm and  $R_{sag} = 69.8$  mm. Working at an incidence angle of  $86^\circ$  we obtain one-to-one imaging with an arm length of 1000 mm. A silver mirror (SM1) mounted on a push-pull manipulator can be inserted into the beam path soon after the first focusing chamber to extract the converging beams and control their spatial properties. Furthermore, removing the metallic filter from the XUV arm, it is possible to exploit spatial and spectral interferometry between the IR pump and the residual IR from the probe to set their temporal overlap. The focus of the first toroidal mirror coincides with the center of a dedicated vacuum chamber equipped with an electron TOF spectrometer (eTOF v6 by Stefan Kaesdorf) which acquires the XUV photoelectron energy spectrum with a resolution of about 10 meV. The target gas is injected in front of the TOF head with a stainless-steel needle (internal diameter of  $500 \mu\text{m}$ ), mounted on a 3D manipulator for fine spatial adjustment. Figure 4(b) shows an example of photoelectron spectrum (green-solid curve) obtained by ionizing neon



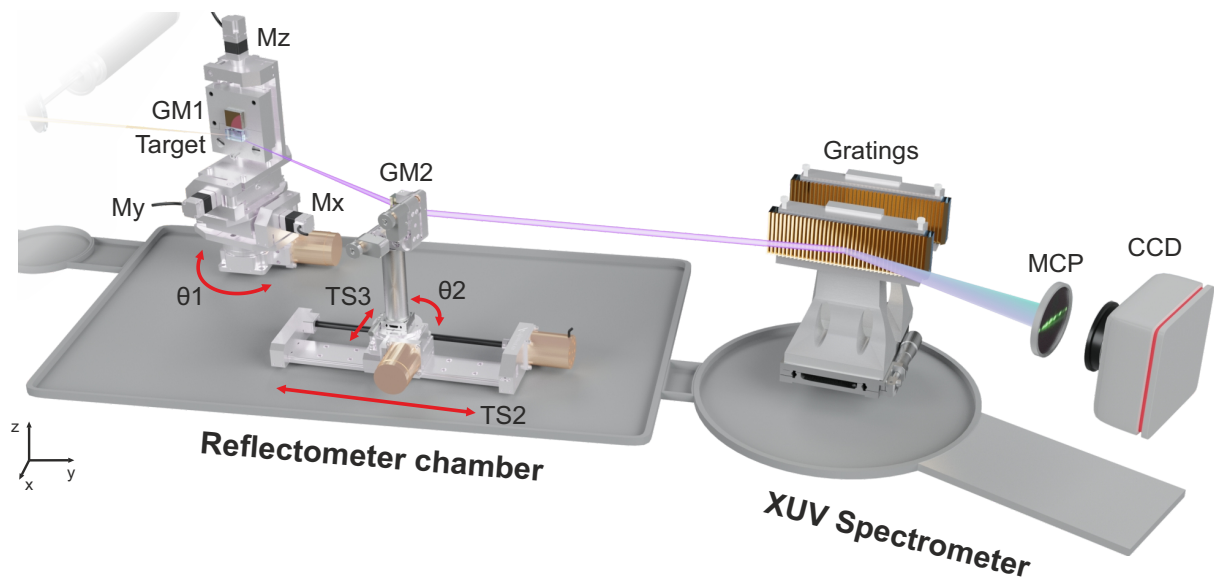


FIG. 5: Schematic of the XUV reflectometer. The solid sample is mounted on an holder that can be rotated along its vertical axis and translated in the three spatial directions. A reference gold mirror (GM1) is placed on top of the sample. A second gold mirror (GM2), mounted onto a roto-translational stage, is used to collect the reflected radiation and steer it into the XUV spectrometer composed by a dispersive grating, an MCP and a phosphor screen. The image of the XUV spectrum which is formed on the phosphor is finally read by a CCD camera.

with a comb of harmonics (black-dashed curve). After proper correction for the transfer function of the TOF spectrometer and the Ne cross-section, electron and photon spectra can be nicely superimposed to one another. The TOF chamber is followed by a second gold-coated toroidal mirror (T2) with radii  $R_{mer} = 11500$  mm and  $R_{sag} = 59$  mm, incidence angle of  $86^\circ$ , focal length 800 mm, which collects the radiation and makes a one-to-one image of the first focus onto the solid target placed in the reflectometer. A second silver mirror (SM2) mounted on a push-pull manipulator allows for beam extraction for the diagnostics of the second focus.

### C. Second interaction region: XUV reflectometer

The second focus coincides with the sample position of the XUV reflectometer (Fig. 5). It consists of two main elements which allow reflectivity measurements to be performed in a wide range of angles of incidence. The first element is a motorized sample holder which can translate along the  $x$ ,  $y$  and  $z$  directions thanks to three linear motors (Mx, My, and Mz) with a resolution of  $0.1 \mu\text{m}$ , and rotated around the vertical axis ( $\theta_1$ ) with a resolution of  $0.01^\circ$ . The sample support is a steel plate with a 13-mm groove, designed to host an additional reference gold-coated mirror (GM1). This mirror can be moved in place of the sample to collect background or reference data during the experiment. The remaining degree of freedom, the vertical tilt, can be adjusted manually when a new sample is mounted for the first time in order to have the sample surface laying in the plane defined by the reference gold mirror surface.

In order to improve the versatility of the XUV reflectome-

ter, we intercept the reflected beam with a second gold-coated mirror (GM2) mounted onto a roto-translational stage. In this way, we can set the incident angle on the target in a range between  $40^\circ$  and  $80^\circ$  without the need for a major rearrangement of the optics. The mirror is mounted on a motorized holder for fine horizontal and vertical tilt. Between the mirror holder and the rotator ( $\theta_2$ ) we placed a manual translation stage (TS3) used to precisely align the rotation axis with the gold mirror surface. Finally, the whole support is mounted onto a long-range translator (TS2, model MP-21 by Micronix, with a resolution of  $0.1 \mu\text{m}$ ), able to shift the mirror by 200 mm. Small variations of the angle of incidence onto the sample may produce a large change in the beam position alongside the propagation direction before the spectrometer. With this setup, we can precisely correct the beam position without the need to vent the chamber.

The XUV spectrometer is composed by a diffraction grating, which spatially disperses the attosecond radiation, and a space sensitive detector consisting in a micro-channel plate (MCP) followed by a phosphor screen<sup>41</sup>. Finally, a CCD camera records an image of the signal on the phosphor screen. The spectrometer chamber can host two different gratings, which can be moved into the beam path with an external manipulator. The first grating is an Hitachi model 001-0693 with central groove density of 600 groves/mm, allowing for detection of photons in the range between 14 eV and 62 eV with a spectral dispersion of 18 meV/pixel at 30 eV (the pixel size is  $30 \mu\text{m}$  on the phosphor screen). The second grating is an Hitachi model 001-0640 with a central groove density of 1200 groves/mm and it is optimized for radiation in the spectral range between 27.5 eV and 124 eV, with a spectral dispersion of 11 meV/pixel at 30 eV.

### III. EXPERIMENTAL RESULTS

In this section a few experimental measurements will be presented, which demonstrate the functionality and versatility of the beamline. In Sec. III A we report on the generation and temporal characterization of SAPs. Section III B describes a simultaneous double RABBITT (Reconstruction of Attosecond Burst By Two-photon Transitions)<sup>3,42</sup>, which both demonstrates the high fidelity of the re-imaging and allows us to measure the phase difference between the two foci. Finally, Sec. III C contains an example of static and dynamical reflectivity measurements on an insulator (silicon dioxide) and a semiconductor (germanium).

#### A. Single attosecond pulse generation and characterization

We generated SAPs by employing the ionization gating technique<sup>43</sup>. For sub-6-fs pulse duration, due to the relatively tight focusing, the driving IR pulses have enough intensity to ionize almost all the gas during their leading edge. When combined with CEP stabilization, this can lead to the direct generation of SAPs without the need for additional spectral or temporal manipulation. We characterized the pulses by performing a streaking measurement<sup>44</sup> in combination with FROG-CRAB (frequency resolved optical gating for the complete reconstruction of attosecond burst)<sup>45</sup> reconstruction. We injected Ne gas in the first interaction chamber. The SAP photons are energetic enough to ionize the atoms and emit an electron in the continuum. The photoelectron spectrum is recorded by the TOF spectrometer. If a delayed IR pulse is added to the process, it behaves as an ultrafast phase modulator, changing the electron momentum. The collection of photoelectron spectra measured at different relative delays between the SAP and the IR pulse (Fig. 6(a)) is a spectrogram which is called streaking trace. As the information it encodes is highly redundant, it is possible to retrieve both the IR and XUV temporal characteristics with an appropriate iterative reconstruction algorithm. Figure 6(b) shows the reconstructed trace after 2000 iterations of the extended Ptychographic Iterative Engine (ePIE)<sup>46</sup>, while the associated SAP and IR temporal characteristics are shown in Figs. 6(c) and 6(d), respectively. In order to evaluate the uncertainty of our reconstruction procedure, we run the iterative code 20 times with different initial guesses for the pulses. The solid lines in Figs. 6(c) and 6(d) represent the average value of the reconstruction outputs while the shaded area marks twice the standard deviation. Considering only the uncertainty of the reconstruction method, the SAP has a FWHM time duration of  $211 \pm 3$  as and a residual quadratic chirp of  $-0.2981 \text{ as}^2$ . We note that the weak interference pattern appearing at big negative and positive delays originates from the presence of a satellite pulse which reconstructed intensity is less than 0.3% of the main pulse. As expected, the reconstructed IR vector potential (red solid curve in Fig. 6) follows the raw center of mass of the spectrogram (black dashed curve in Fig. 6) and lasts for  $4.7 \pm 0.3$  fs (FWHM of the IR intensity envelope). Due to the fact that our streaking trace is centered at rela-

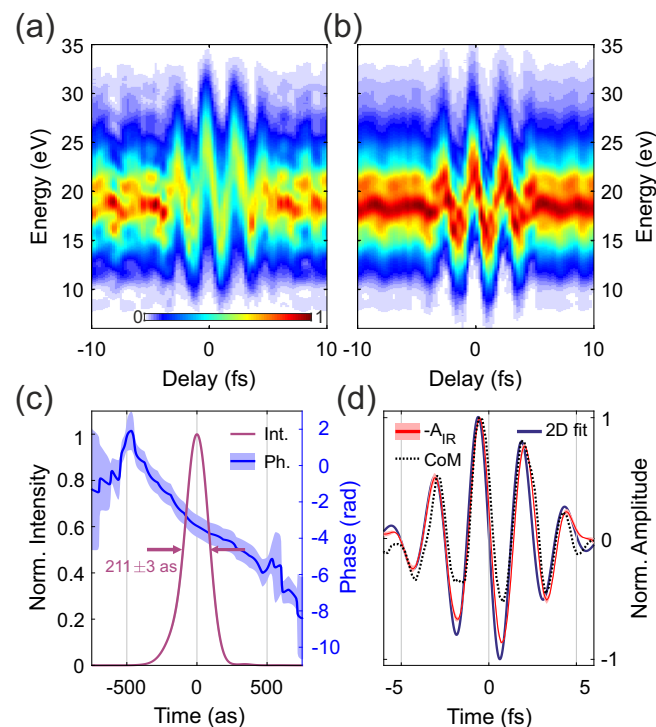


FIG. 6: **(a)** Experimental streaking trace generated in Ne with an IR intensity of  $(5.2 \pm 0.3) \times 10^{12} \text{ W/cm}^2$ . **(b)** Reconstructed trace after 2000 iterations of the ePIE algorithm. **(c)** Intensity (violet curve) and phase (blue curve) temporal profiles of the SAP. **(d)** IR vector potential reconstructed by the iterative algorithm (red curve), extracted from the center of mass of the trace in (a) (black-dotted curve) or from an analytical 2D fitting procedure (blue solid curve). The solid lines in the reconstruction results of (c) and (d) represent the average over 20 reconstructions performed with different initial conditions. The shaded areas extend over twice the standard deviation.

tively low electron kinetic energies, both the streaking trace in Fig. 6(a) and the black-dotted curve in Fig. 6(d) show an up-down asymmetry which is not caught by the reconstruction because of the central momentum approximation upon which the iterative algorithm is based. While slower reconstruction algorithms can overcome this problem<sup>47</sup>, corrections to the standard ePIE approach have shown that the error deriving from the central momentum approximation is severe only for photoelectron energies next to few electronvolts<sup>48</sup>. As an alternative approach, it is worth to notice that a direct fit of the 2D streaking trace with an analytical model<sup>49</sup> gives a faster way to estimate the IR vector potential (blue curve in Fig. 6(d)).

#### B. Simultaneous double RABBITT

One of the main advantages of the sequential double-foci geometry adopted for this beamline is the possibility to run simultaneous measurements in the two interaction regions. In

this way, one can perform an ATRS experiment while acquiring a spectrogram. The advantage of this approach is twofold. Not only it is possible to obtain a live characterization of the temporal properties of pump and probe pulses with the FROG-CRAB technique described above, but it is also possible to precisely calibrate the pump-probe delay axis with respect to the IR pulse field. In particular, the latter is necessary to access the attosecond timing of the observed dynamics and exploit the full potentials of the beamline. Since beam propagation between the two foci introduces an additional delay between the IR and XUV pulses, a precise calibration of this propagation delay (or equivalently, propagation phase) is necessary in order to obtain an absolute pump-probe delay axis.

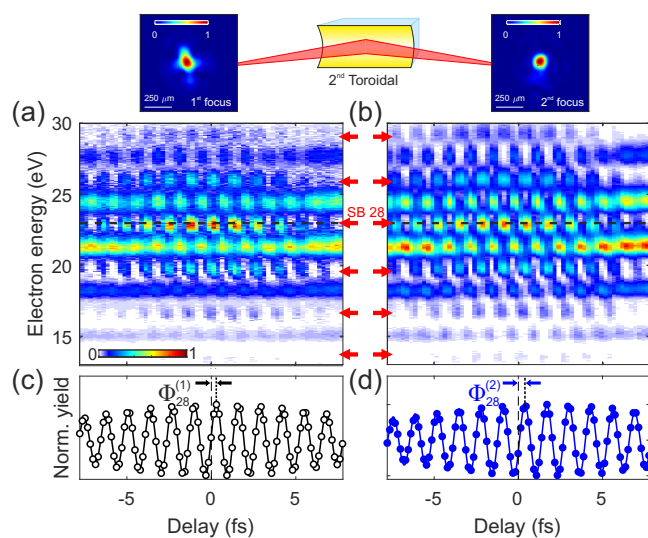


FIG. 7: (a), (b), RABBITT traces acquired in the first and second focus, respectively. The signals appearing for small pump-probe delays and marked with the red arrows correspond to SB22 to SB32. (c), (d), SB28 yield obtained integrating the RABBITT trace in an energy band of 0.6 eV around the black dashed horizontal line in (a) and (b), respectively. Open and close circles represent the data. The continuous line is the result of a fit with the function  $SB(\tau) = ae^{-\left(\frac{\tau}{\sigma}\right)^2} \cos(\omega_{IR}\tau - \Phi_{SB})$  where  $\tau$  is the pump-probe delay,  $\omega_{IR}$  is the IR field angular frequency and  $\Phi_{SB}$  is the SB phase. The cartoon on top of the figure shows the IR beam profile measured in the two foci.

We measured the propagation phase with a double-RABBITT experiment. To this end, we placed a second TOF spectrometer, identical to the first one, in the second focal position. We generated an APT by using 25-fs IR pulses and used the harmonic comb to ionize two Ne targets and collect simultaneously two spectrograms (Figs. 7(a), (b)). In the absence of the IR field, the photoelectron spectra are characterized by discrete peaks corresponding to the direct ionization by each odd harmonic. When the IR field is added, sideband (SB) peaks in between the main bands appear (red arrows in Figs. 7(a), (b)). These peaks correspond to a two-color two-photon process, which involves the absorption of

an XUV photon and the additional emission or absorption of an IR photon. As it originates by two energetically degenerate quantum paths, the SB intensity oscillates with the pump-probe delay at a frequency which is twice the IR frequency  $\omega_{IR}$  (period of about 1.25 fs). As an example, Figs. 7(c), (d) show the electron yield associated to SB28 in the two foci. In the framework of the second order perturbation theory, it is possible to demonstrate that the harmonic phase is imprinted in the phase of the SB oscillation. Therefore, a direct comparison between the SB phases extracted in the first and second focus measures the effect of pulse propagation as reported by F. Schlaepfer et al.<sup>36</sup>. In particular, the phase of the SB of

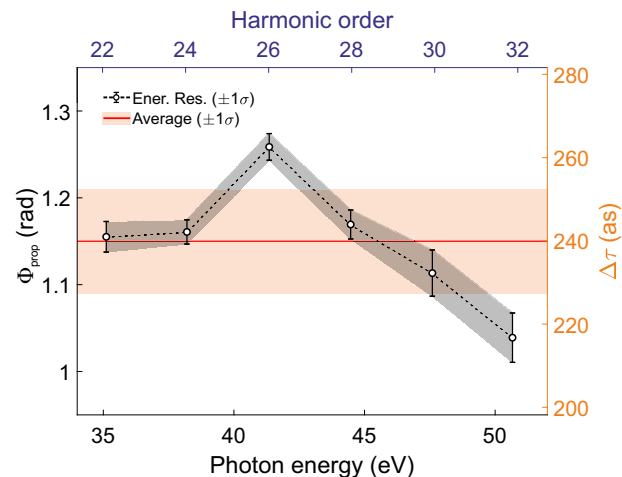


FIG. 8: Propagation phase/delay extracted from simultaneous double-RABBITT experiments as the one reported in Fig. 7. Since no particular dispersive optics are present in the beamline between the first and second focus, the propagation phase stays almost flat in the energy region under investigation (max variation of  $\sim 25$  as). Therefore, we can evaluate its effect by taking the average value of  $240 \text{ as} \pm 13 \text{ as}$  (red curve and shaded area).

order  $2q$ ,  $\Phi_{2q}$ , can be decomposed in the sum of three terms:  $\Phi_{2q} = \Delta\theta_{2q} + \Delta\theta_{at} - \theta_{IR}$ . The first term originates from the phase difference between consecutive harmonics (it is the so called attochirp<sup>50</sup>). The second term,  $\Delta\theta_{at}$ , is a target specific phase associated with the photoemission process. The last term accounts for the phase of the IR field. Since the two RABBITT traces are simultaneously recorded and with the same gas target (Ne),  $\Delta\theta_{2q}$  and  $\Delta\theta_{at}$  are the same in the two foci. Therefore, a non vanishing difference between  $\Phi_{2q}^{(1)}$ , measured in the first focus, and  $\Phi_{2q}^{(2)}$ , measured in the second focus, gives directly any additional phase which is imprinted onto the radiation upon propagation. Figure 8 shows the extracted phase difference  $\Delta\Phi_{2q} = \Phi_{2q}^{(2)} - \Phi_{2q}^{(1)}$  from SB 22 to 32. Black open circles represent the average over 7 repeated measurements while the error bars extend over twice the standard deviation. Since  $\Delta\Phi_{2q}$  originates from the difference in IR and XUV reflection phase on the second toroidal mirror, and from a geometrical (Gouy phase) term, we expect it to be almost flat in the energy region of interest. Indeed our results



show a maximum variation of  $\Delta\Phi_{2q}$  of about 25 as around its average value. Therefore, we can describe the propagation phase with a unique, energy-independent value given by the average of the different  $\Delta\Phi_{2q}$  measured and amounting to  $\langle\Delta\Phi_{2q}\rangle = \Phi_{prop} = 1.15 \pm 0.06$  rad (red line and shaded area in Fig. 8). Dividing by  $2\omega_{IR}$ , we obtain a propagation delay  $\tau_{prop} = 240 \pm 13$  as, which can be used to calibrate the delay axis in the second interaction region. The weak energy dependence of  $\Phi_{prop}$  could originate from a non-zero energy derivative of the gold reflection phase or from the different divergence of each harmonic<sup>51,52</sup>, causing an energy dependent Gouy phase term for the XUV radiation. As the derivative of the gold reflection phase is contained in 2 as, the energy trend observed in Fig. 8 must originate from the different focusing properties of the harmonics. Finally, we note that the value of the propagation phase depends on the actual beam paths. If the relative position of the second focus changes, for example, the propagation phase can vary up to 50 as per mm<sup>36</sup>. In order to ensure reproducibility, we have taken some references along the beamline which guarantee that beam paths are preserved on a daily base. In this way the beamline throughput is optimized and the propagation phase has to be calibrated only if a major change is made.

### C. Reflectivity measurements

Once the SAPs are generated and the beamline has been fully characterized, it is possible to perform ATRS with high temporal resolution. In order to prove the flexibility of our spectrometer and validate our calibration approach, we first measured the static reflectivity of a known target as amorphous silicon dioxide ( $\text{SiO}_2$ ). The absolute sample reflectivity  $R_s$  is given by the ratio of the reflected,  $I_s$ , and the incident,  $I_0$ , XUV intensities. While  $I_s$  is proportional to the signal measured by the XUV spectrometer at the end of the beamline, there is no direct way to measure  $I_0$ . Nevertheless, this problem can be solved by measuring the beam intensity,  $I_{Au}$ , reflected by a calibration target like a gold mirror. Since the gold reflectivity,  $R_{Au} = I_{Au}/I_0$ , is known from literature<sup>56</sup>, the unknown sample reflectivity can be derived as follows:

$$R_s = \frac{I_s}{I_0} = \frac{I_s}{I_{Au}} R_{Au} = \frac{S_s}{S_{Au}} R_{Au}, \quad (1)$$

where  $S_s$  and  $S_{Au}$  are the XUV spectra measured after reflection onto the sample or the gold mirror, respectively. If the two spectra are measured under identical conditions, the procedure is justified. Figure 9 presents the static reflectivity of  $\text{SiO}_2$ ,  $R_{\text{SiO}_2}$ , measured with the procedure described above for four incidence angles ranging from  $55^\circ$  to  $70^\circ$ . The blue solid lines indicate  $R_{\text{SiO}_2}$  obtained by averaging over 100 independent measurements, while the shaded area represents the measurement uncertainty (twice the standard deviation). In this case, as the sample is a very large fused silica plate (size of  $25 \times 50 \text{ mm}^2$ ), we deposited a layer of 50 nm of gold onto a corner of the sample and used this gold layer as reference in order to assure high reproducibility of the measurements. The other solid curves in Fig. 9 show  $R_{\text{SiO}_2}$  as computed from

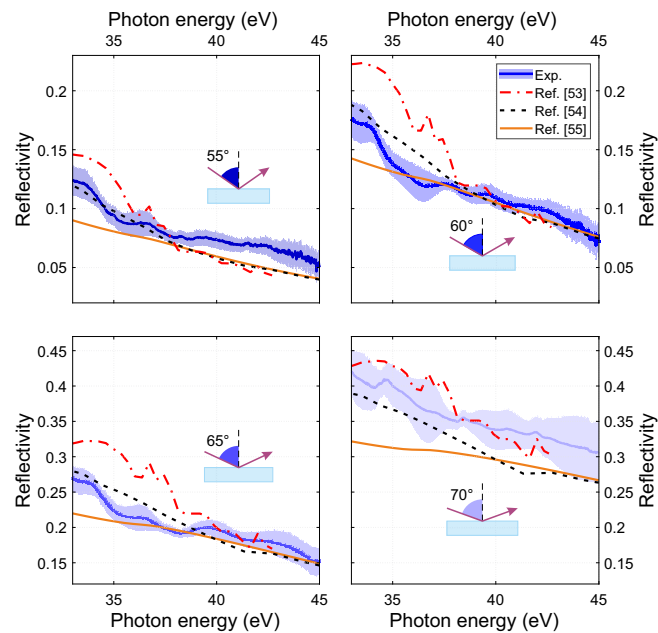


FIG. 9: Measured static reflectivity of fused silica,  $R_{\text{SiO}_2}$ , at an incidence angle of: (a)  $55^\circ$ , (b)  $60^\circ$ , (c)  $65^\circ$  and (d)  $70^\circ$ . In all panels the experimental reflectivity is marked by the blue solid curve (the shaded area represents the standard deviation for repeated measurements), while red dash-dotted, black dashed and yellow solid curves display literature data as derived from the  $\text{SiO}_2$  refractive index published in Refs.<sup>53,54</sup> and<sup>55</sup>, respectively.

literature data<sup>53–55</sup>. Within the experimental error, we can conclude that our procedure for the measurement of energy-resolved absolute reflectivity is correct.

As a further validation of the setup, we performed an ATRS experiment of a known sample. In particular, we measured the effect of a relatively strong IR pump in bulk germanium as reported by Kaplan et al.<sup>31</sup>. We used a relatively short pulse train and recorded the IR-induced relative changes in the sample reflectivity defined as the difference between the Ge reflectivity with and without the IR pump, divided by the static Ge reflectivity without the pump:  $\frac{\Delta R}{R}(E_{ph}, \tau) = [R_{Ge}^{IR}(E_{ph}, \tau) - R_{Ge}^{wo}(E_{ph})] / R_{Ge}^{wo}(E_{ph})$ . The results we obtained at an incidence angle of  $66^\circ$  (critical angle for Ge) and XUV photon energies ranging from 27 to 32 eV, are reported in Fig. 10(a) together with the intensity envelope of the IR vector potential  $A_{IR}(t)$  as extracted from the simultaneous photoemission measurement. Our findings fully reproduce what observed by Kaplan and co-authors. The IR field promotes electrons from the valence band (VB) to the conduction band (CB) initiating the dynamics, which are subsequently probed by the XUV pulse through the  $M_{4,5}$  edge located at  $\sim 30$  eV below the VB top (Fig. 10(b)). We observe a slow increase in reflectivity which develops on a picosecond time scale around 30.1 and 30.7 eV, together with a slow decrease at 28–29 eV. Between 29 and 30 eV we find, instead, a prompt increase in reflectivity, which decays within 3 ps. These features are associated to complex mechanisms of band-gap renormalization,

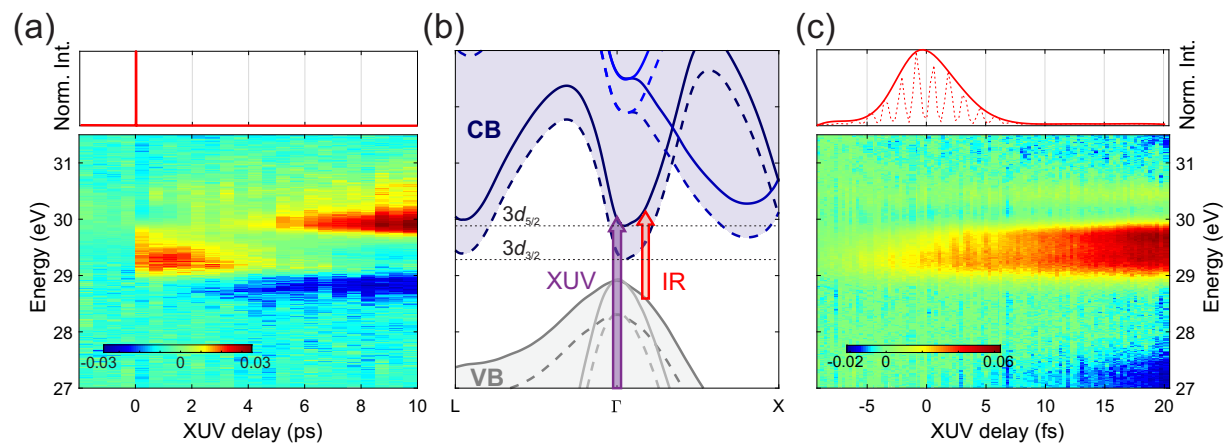


FIG. 10: **(a)** Transient reflectivity  $\Delta R/R$  measured from a Ge sample pumped with an IR intensity of  $1.27 \cdot 10^{13} \text{ W/cm}^2$  at an angle of incidence of  $66^\circ$ . The top panel shows the square of the IR vector potential as retrieved from a simultaneous photoemission experiment. **(b)** Cartoon of the pump-probe mechanism. The IR photons promote electrons from the top of the valence band (VB) into the conduction band (CB). The dynamics thus initiated are then probed by the attosecond radiation via a transition from the Ge  $3d$  level to the VB and CB ( $M_{4,5}$  edge). **(c)** Temporal zoom of (a). The upper panel in (a) and (c) report the IR intensity envelope as extracted from the simultaneous photoelectron measurements. The red-dotted curve in (c) shows the square of the center of mass of the high energy part of the photoelectron spectrogram.

hot electron and hole relaxation via inter-valley scattering and electron-phonon coupling via acoustic phonons. Since  $\Delta R/R$  is sensitive to both the real and imaginary part of the dielectric function, a direct assignment of the observed features to these mechanisms is not trivial and requires a detailed analysis as reported in Ref.<sup>31</sup>. Figure 10(c) shows a temporal zoom of  $\Delta R/R$  in the region of pump-probe overlap. Since we used an APT to perform ATRS, the information on the IR CEP is lost and therefore it is not possible to extract the time-dependent IR amplitude from the simultaneous photoelectron spectrogram. Nevertheless, we can retrieve the IR pulse envelope (upper panel in Figs. 10(a), (c)) which can be used to independently calibrate the pump-probe delay axis. We note the presence of some fast oscillations in the region of pump-probe overlap, between 29 and 30 eV. These oscillations are probably related to the pumping mechanism observed in Ref.<sup>26</sup>, but their discussion is beyond the scope of this work.

These results prove that this setup is a reliable tool for assessing electron dynamics in solids with attosecond transient reflection measurements in a pump-probe configuration.

#### IV. SUMMARY

We presented and validated a unique beamline for attosecond transient reflection spectroscopy in a sequential double-foci geometry. The attosecond streaking measurement reported in Sec. III A demonstrates the capability of this setup to generate and characterize single attosecond pulses. Precise temporal calibration between the two interaction points was achieved by performing a simultaneous double-RABBITT experiment. The static absolute reflectivity of silicon dioxide reported in Sec. III C is in good agreement with what previously reported in literature, both showing the flexibility of this setup

and confirming the experimental approach. Finally, the measured pump-induced relative changes in the reflectivity of germanium crystals demonstrate the possibility to perform simultaneous experiments in two different physical systems located in the two interaction regions. In particular, the possibility to perform a simultaneous calibration of the pump-probe delay with attosecond resolution fills the gap between transient absorption and reflection measurements, thus opening new perspectives for the investigation of ultrafast dynamics in solid with attosecond all-optical techniques.

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#### DATA AVAILABILITY

The data that support the findings of this study are available from the corresponding author upon reasonable request.

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