

Fig. 2. Time-based boost converter.

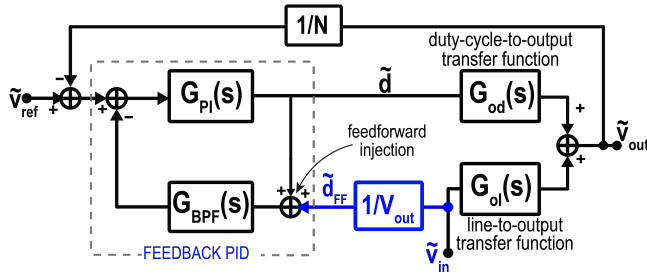


Fig. 3. Small signal model of the boost converter employing the proposed F-PID.

for time-based control is introduced in [7] to solve this issue. Although effective, the reported feedforward scheme requires a wide-range linear differential delay line, which introduces a considerable delay in the loop and occupies a significant amount of area. To overcome these drawbacks, an alternative time-based compensator, referred to as feedback-PID (F-PID), has been used in this paper. The proposed F-PID exploits an additional path to introduce a feedforward without modulating the PD. Basically, the F-PID additional path can be used to modify the converter's duty-cycle, as it generates an additional transfer function, with unity gain, from the injection node to the PD inputs.

This paper is organized as follows. In Sect. II the proposed F-PID is introduced and the analytical expression of the relevant transfer function are provided; in Sect. III the circuit implementation and the behavior are described; measurement results of the boost converter employing the proposed control method are shown in Sect. IV, then, conclusions are drawn in Sect. V.

II. FEEDBACK-PID COMPENSATOR

The small-signal model of a boost converter employing feedback-PID is shown in Fig. 3. The F-PID is composed of a forward path, $G_{PI}(s)$, and a feedback path, $G_{BPF}(s)$, that can be used as an injection point for the input voltage signal (\tilde{v}_{in}). In the forward path, a proportional-integral (PI) compensator

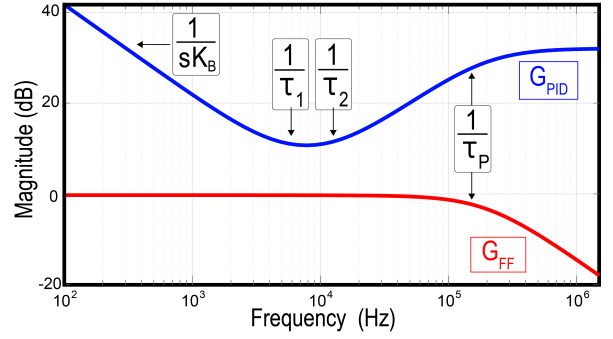


Fig. 4. Bode diagram of the magnitude of the F-PID transfer functions G_{F-PID} (blue) and G_{FF} (red).

is employed, with transfer function

$$G_{PI}(s) = \frac{K_I}{s} \left(1 + \frac{s}{\omega_{PI}} \right), \quad (1)$$

with K_I being the gain and ω_{PI} being the radiant frequency of the high frequency pole. The feedback block is a band-pass filter (BPF) with transfer function

$$G_{BPF}(s) = \frac{sK_B}{\left(1 + \frac{s}{\omega_1} \right) \left(1 + \frac{s}{\omega_2} \right)} \quad (2)$$

with gain $K_B = K_0/\omega_1$ and two poles at ω_1 and ω_2 . For this implementation, assuming $K_I \cdot K_B \gg 1$, the structure is equivalent to a PID with transfer function G_{F-PID} equal to:

$$G_{F-PID}(s) = \frac{G_{PI}(s)}{1 + G_{PI}(s)G_{BPF}(s)} \simeq \frac{\left(1 + \frac{s}{\omega_1} \right) \left(1 + \frac{s}{\omega_2} \right)}{s \cdot K_B \left(1 + \frac{s}{\omega_p} \right)}, \quad (3)$$

where a pole-zero cancellation occurs through the interaction between the BPF and the PI. The F-PID also shows a high frequency pole at angular frequency, ω_p :

$$\omega_p = \frac{K_I K_B \cdot \omega_1 \omega_2}{\omega_{PI}}, \quad (4)$$

and its Bode diagram is shown in Fig. 4.

The feedforward signal $\tilde{d}_{FF} = -\tilde{v}_{in}/V_{out}$, induced by an input voltage variation \tilde{v}_{in} , is injected at the BPF input. The transfer function from the feedforward injection point to the PD output, $G_{FF}(s) = \tilde{d}/\tilde{v}_{in}$, is

$$G_{FF}(s) = -\frac{G_{BPF}(s) \cdot G_{PI}(s)}{1 + G_{PI}(s) \cdot G_{BPF}(s)} \quad (5)$$

which shows a unity gain at low frequency and a high frequency pole at ω_p , as shown in Fig. 4. Referring to the state-space averaged model of the boost converter [3], the *duty-cycle-to-output* and the *line-to-output* transfer functions, G_{od} and G_{ol} , respectively, can be written as:

$$G_{od}(s) = G_{od}(0) \cdot \frac{\left(1 - \frac{s}{\omega_{z,rhp}} \right) \left(1 + \frac{s}{\omega_{z,lhp}} \right)}{\left(\frac{s^2}{\omega_0^2} + \frac{2s\zeta}{\omega_0} + 1 \right)} \quad (6)$$

and

$$G_{ol}(s) = \frac{1}{D'} \frac{RD'^2}{(RD'^2 + r)} \cdot \frac{\left(1 + \frac{s}{\omega_{z,lhp}} \right)}{\left(\frac{s^2}{\omega_0^2} + \frac{2s\zeta}{\omega_0} + 1 \right)}, \quad (7)$$

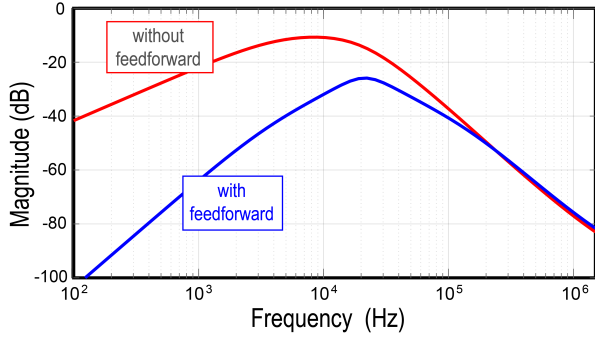


Fig. 5. Closed loop line-to-output transfer function of the boost converter with F-PID controller with (blue) and without (red) the line-feedforward.

where

$$G_{od}(0) = \frac{V_{out}}{D'} \cdot \frac{(RD'^2 - r)}{(RD'^2 + r)}; \quad (8a)$$

$$D' = 1 - D = \frac{V_{in}}{V_{out}} \cdot \eta; \quad (8b)$$

$$\omega_0 = \frac{1}{\sqrt{LC}} \cdot \sqrt{\frac{RD'^2 + r}{R}}; \quad (8c)$$

$$Q = \frac{\sqrt{LC} \cdot (R + r_c) \cdot (RD'^2 + r)}{C(r(R + r_c) + RD'^2 r_c) + L}; \quad (8d)$$

$$\omega_{z,thp} = \frac{1}{C \cdot r_c}; \quad (8e)$$

$$\omega_{z,rhp} = \frac{(RD'^2 - r)}{L}. \quad (8f)$$

In the above equations, R is the load resistance, D the converter's duty-cycle of the converter, ω_0 and Q denote LC filter angular frequency and quality factor respectively, r_c is the series resistance of the output capacitor, and η is the conversion efficiency. The term $r = r_L + R_{on,LS} \cdot D + R_{on,HS} \cdot (1 - D)$ represents the equivalent average resistance (EAR) [11] which accounts the parasitic resistances of the inductor, r_L and of the high-side and low-side power MOSFETS, $R_{on,HS}$ and $R_{on,LS}$, respectively. By employing the F-PID, the closed-loop line-to-output transfer function, $G_{ol,FF-CL}$, becomes:

$$G_{ol,FF-CL}(s) = \frac{G_{ol}(s) - G_{od}(s)/V_{out}G_{FF}}{1 + G_{LOOP}(s)}, \quad (9)$$

where $G_{LOOP}(s) = G_{F-PID}(s)G_{od}(s)/N$, being $1/N$ the resistive divider ratio at the converter's output. With the adoption of the F-PID structure, the input voltage information can be directly injected into the compensator network at the BPF input, obtaining a wide bandwidth feedforward action. The simulated closed-loop line-to-output transfer function, $G_{ol,FF-CL}(s)$, is shown in Fig. 5, also compared with the closed-loop line-to-output obtained without the proposed feedforward. The Bode diagrams of the two transfer functions are shown in blue and red, respectively. The comparison shows that the audiosusceptibility of the system adopting line-feedforward is lower over the entire frequency range up to the pole frequency ω_p .

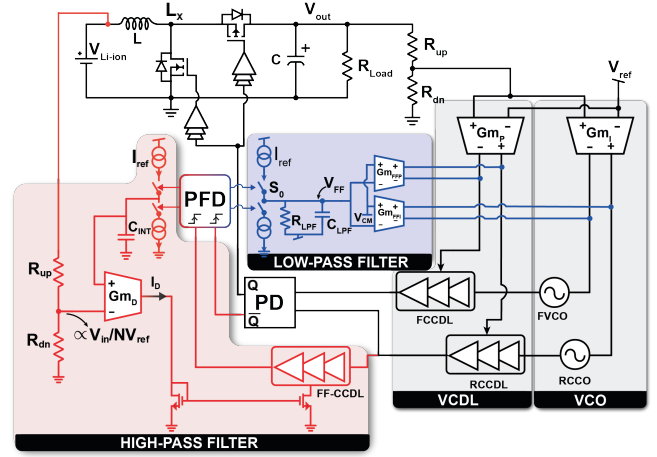


Fig. 6. Simplified circuit diagram of the proposed time-based F-PID controller with delay-line based line-feedforward.

III. CIRCUIT IMPLEMENTATION

The circuit diagram of the F-PID is shown in Fig. 6. The forward path implements a time-based PI controller through the cascade of integral and proportional stages. The integral stage is realized by injecting current from the integral transconductor into two current-controlled oscillators (CCOs), while the proportional stage uses the proportional transconductor to drive two current-controlled delay lines (CCDLs), leading to a transfer function G_{T-PI} , that is,

$$G_{T-PI}(s) = \frac{G_{mI} \cdot K_{CCO}}{s} + G_{mP} \cdot K_{CCDL}, \quad (10)$$

where G_{mI} and G_{mP} are the integral and proportional transconductors' gains, respectively, and K_{CCO} and K_{CCDL} are the CCO and CCDL gains, respectively.

The feedback path implements a band-pass filter, split into a high-pass and a low-pass filter. The low-pass filter, R_{LPF} , C_{LPF} , receives as input the charge-pump current and, by means of the transconductors G_{mFFI} and G_{mFFP} , injects currents into the CCOs and CCDLs. The high-pass filter (HPF) is realized as an integrator in feedback and is composed of the transconductor G_{mD} , an additional CCDL, denoted as feedforward CCDL (FF-CCDL), a phase and frequency detector (PFD), a charge-pump (CP), and an integrator capacitance C_{INT} . The capacitance voltage is connected to the positive node of the transconductor G_{mD} , thereby closing the feedback loop. The HPF transfer function, $G_{HPF} = \tilde{i}_{int}/\tilde{d}$, i.e., the gain from the duty-ratio, \tilde{d} , to the current over the integral capacitor, \tilde{i}_{int} , can be written as:

$$G_{HPF}(s) = \frac{s \cdot G_{mD} K_{FF-CCDL} G_{PFD} / C_{INT}}{1 + s \cdot G_{mD} K_{FF-CCDL} G_{PFD} / C_{INT}} \cdot I_{ref}, \quad (11)$$

where G_{mD} is the transconductor gain, $K_{FF-CCDL}$ is the gain of the feedforward CCDL, G_{PFD} and I_{ref} are the PFD gain and the charge-pump current respectively. The charge-pump output is replicated at the input of the low-pass filter (LPF), so that the overall BPF transfer function G_{BPF} is:

$$G_{BPF}(s) = \frac{s \cdot G_{mD} K_{FF-CCDL} G_{PFD} / C_{INT}}{1 + s \cdot G_{mD} K_{FF-CCDL} G_{PFD} / C_{INT}} \cdot \frac{I_{ref} \cdot R_{LPF}}{1 + s C_{LPF} R_{LPF}}. \quad (12)$$

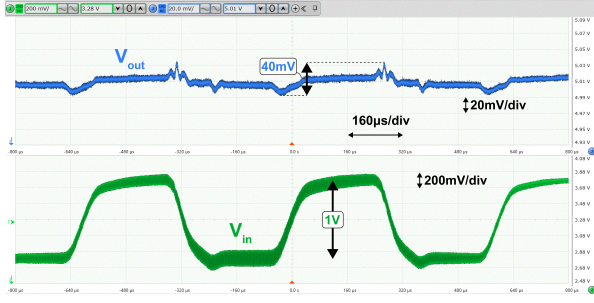


Fig. 11. Measured line transient response to a 1 V input voltage variation in $50 \mu\text{s}$ ($I_{\text{LOAD}}=300 \text{ mA}$).

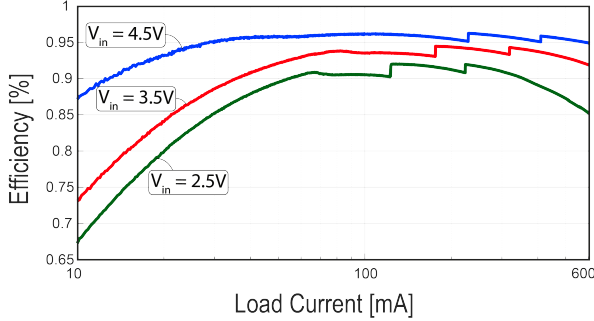


Fig. 12. Measured efficiency of the boost converter at different input voltages. The peak efficiency is 96.1%

shows the efficiency vs. load current of the boost converter at different values of V_{in} . The converter shows a peak of 96.1% and, overall, higher than 80% for all input voltages and across a wide load range (20 to 600 mA). Finally, Table I compares the proposed converter with other boost converters reported in the literature and commercially available products for the AMOLED application. The proposed structure provides similar load and efficiency performance while offering superior line transient responses, comparable to those of the boost converter in [12], which also inherently incorporates line transient improvement through current-mode control. The proposed boost converter achieves these performances with a 30% reduction in the controller area occupation.

V. CONCLUSIONS

In this paper, a time-based boost converter with feedback-PID has been presented. The prototype, realized in a 180nm BCD technology operates at 1.5 MHz switching frequency, 2.5-to-4.8 V input voltage, and delivers up to 600 mA load current. The die active area is 4.09 mm^2 , while the controller area is only 0.23 mm^2 , about 30% less area than that of state-of-the-art controllers. When subject to a 1 V input voltage variation in $50 \mu\text{s}$, it shows a peak-to-peak variation of only 40 mV. The load transient response shows an 80 mV peak-to-peak variation, and about $60 \mu\text{s}$ recovery time. Moreover, the proposed implementation of the HPF in the F-PID feedback path gives an intrinsic low duty-cycle jitter of 1.5 ns, equal to only 0.2% of the switching period.

TABLE I
PERFORMANCE SUMMARY AND COMPARISON WITH THE
STATE-OF-THE-ART

	This work	[6] TPEL '22	[12] STMP30	[13] MAX18000
Technology	180-nm	180-nm	180-nm	N/A
V_{in} [V]	2.5 - 4.8	2.5 - 4.8	2.5 - 4.8	2 - 4.8
V_{out} [V]	5	5	5	5
$I_{\text{load,max}}$ [mA]	600	800	550	1000
L [μH]	2.2	2.2	2.2	0.47
C [μF]	44	44	44	44
f_{sw} [MHz]	1.5	1.5	1.5	2
η_{peak} [%]	96.1	96	96.5	95*
Ctrl method	VM F-PID	ICF	CM	N/A
Ctrl Area [mm^2]	0.23	0.29	0.3	N/A
ΔI_{load} [mA]	300	300	300	985
$\Delta V_{\text{out,pp}}$ [mV]	80	80	140	200*
ΔV_{in} [V]	1	1	1	0.7
$\Delta V_{\text{out,pp}}$ [mV]	40	87	36	80

*estimated from figure.

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