

# Design and Modeling of a Periodic Single-Phase Sandwich Panel for Acoustic Insulation Applications

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# 2 ABSTRACT

Sandwich and composite panels are widely adopted in acoustic applications due 3 to their sound insulation properties that overcome mass-law-based partitions in 4 the medium-high frequency regions. A key aspect in the design procedure of 5 acoustic panels is the control of the resonance dominated region of the Sound 6 Transmission Loss (STL) curve. Within that frequency range such systems usually 7 show acoustic weakness and poor insulation performances with respect to standard 8 single layer solutions. In the present contribution we want to highlight an innovative 9 approach for the sandwich partitions concept. A novel single-phase sandwich 10 panel is realized adopting a periodic repetition of a properly designed unit cell. The 11 resulting internal truss structure is self-sustained and its mechanical stiffness can 12 be tuned to maximize the STL in the resonance dominated region. A series of 13 parametric analysis is reported to show how the topology of the unit cell affects the 14 noise reduction properties of the panel. An experimental validation is performed 15 on a Nylon 3D printed prototype. The proposed panel is then integrated with 16 some Locally Resonant elements that can be adopted to further improve the low 17 frequency STL of the solution. Industrial and production considerations are also 18 taken into account during the design process to make the solution industrially valid 19 with a circular economy focus. 20

21 Keywords: sandwich panel; periodic panel; Sound Transmission Loss; circular economy

# **1 INTRODUCTION**

The widespread adoption of sandwich-like acoustic panels in many sectors and applications 22 is linked to their significant sound insulation performances combined with low weight and 23 good mechanical strength. Mass-Air-Mass (MAM) and Mass-Spring-Mass (MSM) systems 24 overcome single panel noise reduction performances over a wide frequency range. Multi-25 layered partitions are however characterized by a Mass-Spring-Mass resonance where clear 26 weakness in terms of acoustic performances arise. For this reason such frequency range must 27 be considered and rigorously analyzed during the design process. This resonance is strictly 28 related to the stiffness of the multi-layered panel, which is determined by the geometry and 29 material composition of the latter (C. W. Isaac and Wrona, 2020) (M. R. Zarastvand, 2021). 30

Different kind of cores for such panels have been investigated in the recent literature, 31 including air cavities, porous or fibrous materials, honeycomb, truss or lattices structures. 32 Honeycomb sandwiches are usually adopted in applications where high stiffness, good 33 shock resistance and low mass is required. However, the latter features usually lead to an 34 35 increase in the noise transmission through the structure (M. Radestock, 2019). Sandwich panels with truss-core demonstrate interesting dynamic, acoustic and mechanical properties 36 that strongly depend on the core configuration (e.g. pyramids, tetrahedrons, hourglass) 37 (Zhi-Hui Wen and Ma, 2021)(Dong-Wei Wang, 2017)(Zhen-Kun Guo and Tang, 2021). 38

The design process of the panel internal core is still a point of intense research (L. Quinteros and Ruiz, 2021) (C. Shen, 2013) (A. Spadoni, 2006). The main issue remains related to find an effective compromise between sound insulation performances and mechanical strength of the panel.

The aim of the present contribution is to propose a new sandwich panel concept with an engineered shape that match significant noise reduction performances and a structure with self-standing properties. The proposed innovative core is a modification of the one proposed in (C. Gazzola, 2021). It has been designed from the acoustic point of view to not overstiffen the panel and leave to the airgap the main stiffness contribution that defines the system resonance.

A series of parametric analysis has been carried out to optimize the acoustic performances of the sandwich panel in the resonance dominated region and to define the more promising configuration in terms of internal beam dimensions and presence of holes digged on the massive elements of the unit cell.

53 An additional aim of this work is to show further developments that can be implemented 54 to improve the low frequency performances of the proposed panel with a Metamaterial

based approach, coupling its core with Locally Resonant elements, similarly to the strategy
proposed in (Filho et al., 2019) (de Melo Filho et al., 2019)(Lin et al., 2016) (de Melo Filho

57 et al., 2020). Inclusions that act as Locally Resonant elements are introduced in the panel

58 core, increasing the STL response in the 200-250 Hz region.

Another point taken into account in the design process is the industrialization of the panel through a circular economy approach. The panel core is conceived as a single-phase structure, which can be entirely produced through injection molding technique. This makes possible the realization of an acoustic insulating solution entirely made in regenerated plastic material.

The paper is structured as follows: the panel unit cell geometry and the numerical design 64 65 approach are described in section 2. Results of numerical simulations and parametric analyses are reported in section 3 as well as the analytical lumped mass model to predict the 66 MSM resonance frequency. In section 4 experimental results and validation of performances 67 of the final selected design on a 3D printed panel are presented. In section 5 a Metamaterial 68 approach for the panel is introduced from the numerical point of view. The proposed 69 solution, *i.e.* the introduction of local resonators embedded in the unit cell, can be 70 implemented to improve the STL response of the partition in critical parts of the spectrum 71 at low frequencies. Finally, in section 6 conclusions are drawn. 72

# 2 MATERIALS AND METHODS

73 In this section a detailed description of the acoustic panel unit cell is presented along with74 the numerical tools exploited for the SPL estimation.

## 75 2.1 Acoustic Panel Geometry

The acoustic panel core is composed by a periodic structure with an in-plane repetition of a primitive cell.

78 The unit cell geometry is a modification of the one proposed in (C. Gazzola, 2021). The latter was composed by six massive pyramidal elements connected by a 3D frame and it was 79 80 designed according to the principle of separation of modes (D'Alessandro et al., 2017) to obtain an ultrawide band gap at low frequencies (Fig. 1). This ensured that the mechanical 81 modes of the core do not interfere with the acoustic transmission loss performances of the 82 83 panel. The lumped parameter model proposed for this configuration showed the needed modifications in the geometry of the unit cell to optimize the STL performance at low 84 frequencies. In particular, it was shown that the massive elements can be redistributed to 85 maximize the lateral mass of the unit cell and minimize the internal one, which does not 86

contribute to the modal mass of the MSM resonance mode. Moreover, the frame stiffness
can be further reduced in order to make the mechanical stiffness negligible with respect
to the air stiffness. These considerations have been taken into account to propose the

90 innovative unit cell of this contribution.

The unit cell here analysed consists of two massive elements (Fig. 1a) connected by four elastic ligaments placed on a cross shaped frame that give structural stiffness to the panel (Fig. 1b). The aforementioned internal core is then integrated with a couple of 3.0 mm thick planar elements to create the final acoustic partition (Fig. 1d).

95 The working principle of the beam elements has been designed integrating the geometry 96 proposed in (C. Gazzola, 2021) with industrial and production considerations for plastic 97 injection molding. The flexural behaviour of the ligaments, from the dynamic and acoustic 98 point of view, allows to play with an additional degree of freedom in the panel mechanical 99 stiffness definition. At the same time, the panel can be conceived as a monolithic sandwich 100 structure with both massive and ligament elements made of the same material, thus obtaining 101 a suitable configuration for plastic molding manufacturing.

This type of production approach brings some additional constraints in the definition 102 103 of the geometry of the unit cell *e.g.* undercuts must be avoided and holes are needed in the massive elements to facilitate the cooling process after the molding of the plastic. The 104 unit cell has global dimensions of 60x60x46 mm. The fundamental geometrical features 105 of the cell are highlighted in Fig. 2. In particular,  $l_{mass} = 0.057 \ m, \ b_{mass} = 0.016 \ m,$ 106  $h_1 = h_2 = 0.0255 m$ ,  $l_{beam} = 0.026 m$ ,  $w_1 = 0.004 m$ ,  $w_2 = 0.002 m$ , d = 0.008 m and 107 a = 0.060 m. The material adopted for the prototype and for all the numerical simulations 108 reported in what follows, is Nylon PA12, characterized by a Young's modulus E=1.586 109 GPa, Poisson's ratio  $\nu$ =0.4, volumetric mass density  $\rho$ =1000 kg/m<sup>3</sup> and loss factor  $\eta$ =0.05. 110 This lead to an overall partition mass of  $26 \text{ kg/m}^2$ . 111

## 112 2.2 Acoustic Panel Modeling

The Sound Transmission Loss (STL) of the proposed solution is determined numerically adopting a FEM plane wave model (Langfeldt and Gleine, 2019) implemented in COMSOL Multiphysics v5.6, by coupling the Pressure Acoustics and Structural Mechanics modules. As shown in Fig. 3, a primitive cell is modeled and the performances of the entire panel are reproduced due to the application of Bloch-Floquet boundary conditions, both at the lateral boundaries of the unit cell (see Fig. 3b) and at the air domain along the tube.

- 119 Perfectly matched layers (PML) are placed on the tube terminations.
- 120 The calculation of the STL is computed as:



**Figure 1.** Dispersion diagram of the unit cell proposed in (C. Gazzola, 2021) with schematic of the investigated Irreducible Brillouin Zone. The red dotted lines identify the opening and closing frequencies of the first band gap, respectively,  $f_o = 184$  Hz and  $f_c = 1437$  Hz. The gap to mid-gap ratio is also reported.

$$STL = 20log_{10} \left( \frac{|P_{in}|}{|P_{out}|} \right),\tag{1}$$

with  $P_{in}$  and  $P_{out}$  representing the sound pressure computed at two sections before and 121 122 after the sound insulation module. A normal incidence pressure wave model (without structural damping) is adopted for the simulations reported in section 3. In that section a 123 124 lumped mass analytical model is presented with the aim of predicting the low frequency resonances by means of a simplified tool. In section 4, instead, the numerical STL is 125 computed with a complete FEM model that takes into account both diffuse incidence 126 equations and panel finite size correction, in order to have the best agreement between 127 numerical and experimental data. The complete model formulation is here summarized: 128

$$STL_{diff,corr} = -10log_{10} \left( \frac{\int_0^{\theta_{lim}} |T(\theta)|^2 \sigma_{R,avg}(\theta) \cos(\theta)^2 \sin(\theta) d\theta}{\int_0^{\theta_{lim}} \cos(\theta) \sin(\theta) d\theta} \right)$$
(2)

129 being  $T(\theta)$  the transmission coefficient,  $\theta_{lim} = 90$  deg and  $\sigma_{R,avg}$  the averaged geometrical 130 efficiency with its dependency on the incidence angle. Eight frequencies in each 1/3 octave 131 band and twenty incidence angles between 0 and 89 degrees. A Standard Linear viscoelastic 132 behavior is adopted in the FEM model which results are reported in section 4.





**Figure 2.** Unit cell geometry: (a) Massive elements connected by (b) four ligaments placed on a cross shaped frame. (c) Masses and internal frame assembly and (d) complete external view of the unit cell 60x60x46 mm.



**Figure 3.** (a) Complete acoustic panel view and identification of the modeled unit cell. (b) Plane wave FEM model for sound transmission loss calculation.

133 The complete formulation of the constitutive law can be found in previous works
134 (D'Alessandro et al., 2019)(D'Alessandro et al., 2016), while further details about the
135 numerical formulation are reported in (C. Gazzola, 2021) and (Bonfiglio et al., 2016).
136

## **3 NUMERICAL RESULTS**

In what follows, a set of parametric studies is presented, to show the panel acoustic 137 performances at varying some geometrical features of the unit cell. In particular, the effects 138 139 in terms of STL modifying the geometric dimensions of the elastic frame (subsection 3.1) and the number and position of holes in the massive element (subsection 3.2) are presented. 140 141 These studies allow to select the most effective unit cell configuration, then exploited to 142 build the prototype for the experimental validation. To limit the computational burden, 143 these preliminary simulations are performed adopting a normal incidence model setting  $\theta = 0$  in the formulation reported in subsection 2.2. 144

## 145 3.1 Geometric dimensions of the elastic ligament

146 One of the main geometrical features that characterize the acoustic partition performances is the beam elements dimension. The STL curves by varying the ligaments dimension  $w_2$ 147 148 (Fig. 2b) in the range 2.0-4.0 mm are reported in Fig.4. The effect of reducing the beams 149 thickness is a progressive shift at low frequency of the MSM resonance. For  $w_2=2.0$  mm 150 the latter occurs at 187 Hz. At medium-high frequency (between 500 Hz and 2000 Hz), the analysis on the ligaments dimension show a variation of the second resonance frequency 151 152 that arise due to the frame flexural mode as shown in Fig. 5. From the graph presented in Fig. 4 the green STL curve ( $w_1$ =4.0 mm and  $w_2$ =2.0 mm) is selected to proceed with 153 further analysis on the panel geometry. 154

## 155 **3.2** Number and positions of holes

156 As mentioned in subsection 2.1, the geometry of the panel is designed considering the adoption of injection printable recycled materials. For this purpose, the massive 157 elements that compose the panel core need to be holed to facilitate the mass production 158 159 with recycled plastic molding. This technique is adopted in the mold design phase to avoid strong temperature gradients that can lead to permanent deformations on the finite plastic 160 component. The geometry of the panel is hence modified as depicted in Fig. 6. In the 161 proposed holed configurations the thickness of the massive elements is adjusted to preserve 162 the core mass of the unholed configuration. In all the three configurations, the air volume 163 164 enclosed in the holes is the same to maintain constant the stiffness contribution related to



Figure 4. Sound Transmission Loss of the panel at varying beam dimensions.



Figure 5. Sound Transmission Loss of the panel considering  $w_1$ =4.0 mm and  $w_2$ =2.0 mm with focus on the Mass-Spring-Mass resonance occurring at 187 Hz and beam elements mode at 630 Hz.

- 165 the air inside the partition.
- 166 This will be better highlighted in subsection 3.3.
- 167 Due to the equivalence in mass and stiffness, the STL curves for the three holed
- 168 configurations are superimposed. The sixtyfour holes configuration is the one selected
- 169 for the experimental validation due to a better voids distribution on the massive elements
- 170 surfaces.



**Figure 6.** Different holes configuration analyzed: (a) four holes configuration, (b) sixteen holes configuration, (c) sixtyfour holes configuration.



**Figure 7.** Sound Transmission Loss of the proposed acoustic partition at varying holes position and dimensions.

#### 171 3.3 Lumped-parameter model

The Mass-Spring-Mass resonance frequency which appears at 187 Hz (Fig. 5) can be described by the lumped parameter model reported in Fig. 8a and following the procedure presented in (C. Gazzola, 2021). At this resonance the faceplates and the massive elements  $(m_1 = m_2=0.0042 \text{ kg})$  vibrate at the stiffness of the system, given by the air enclosed in the panel ( $k_a$ ) and by the elastic ligament ( $k_m$ ). The corresponding deformed shapes are reported in Fig. 8b for the lumped model and in Fig. 8c for the FEM model.



**Figure 8.** (a) Lumped-parameter model and (b) deformed shape corresponding to the Mass-Spring-Mass resonance at 187 Hz of the lumped model and (c) of the FEM model.

The air stiffness  $k_a$  is computed as  $BA_p/d_{eq} = 24640$  N/m.  $B = \rho_0 c^2$  represents the adiabatic bulk modulus of air,  $\rho_0 = 1.225$  kg/m<sup>3</sup> and c = 340 m/s are the air density and the speed of sound considered.  $A_p = 0.0036$  m<sup>2</sup> is the surface area of the unit cell and its equivalent thickness  $d_{eq} = 20.7$  mm is derived computing the air volume enclosed in one unit cell ( $V_a$ =7.4484 · 10<sup>-5</sup> m<sup>3</sup>) and dividing it by the single unit cell surface ( $A_p$ ).

The eight L shaped beams of the elastic frame determine the panel structural stiffness. In particular, the bending stiffness of the aforementioned ligaments is calculated considering a clamped-clamped beam scheme, whose bending stiffness reads  $k_{m,1B} = 12EI/l^3 =$ 3248N/m, with  $I = 1/12w_1^3w_2$  and  $l = l_{beam} - w_1/2$ .

187 The mechanical stiffness of the four beams forming one half of the frame is equal to 188  $k_g = 4 \cdot k_{m \, 1B} = 12993$  N/m. Hence, the stiffness of the whole elastic structure is equal to 189  $k_m = k_g/2 = 6496$  N/m, being the two grid in a series configuration.

According to D'Alambert's principle the lumped mass systems equation of motion are set:

$$\begin{cases} m_1 \ddot{x}_1 + (k_a + k_m) x_1 - (k_a + k_m) x_2 = 0, & \text{for } m_1 \end{cases}$$
(3a)

$$m_2\ddot{x}_2 + (k_a + k_m)x_2 - (k_a + k_m)x_1 = 0, \text{ for } m_2$$
 (3b)

190 The harmonic motion hypothesis is considered introducing:  $x = Xe^{i\omega t}$  to solve the linear 191 eigenvalue problem. The MSM resonance predicted by the lumped model is equal to 189 192 Hz (+1% with respect to the FEM prediction).

The same frequency can be predicted starting from the MAM formula for a standarddouble-leaf partition, which reads (de Melo Filho et al., 2019; Norton and Karczub, 2010):

$$f_{MAM} = \frac{1}{2\pi} \sqrt{\frac{\rho_0 c^2}{d} \frac{m_1' + m_2'}{m_1' m_2'}},\tag{4}$$

195  $m'_i$  is the areal weight of the *i*-th wall leaf and *d* is the air-gap distance between the closing 196 panels. Considering the definition of  $k_a$ , the aforementioned formula can be reinterpreted 197 as:

$$f_{MAM} = \frac{1}{2\pi} \sqrt{k_a \frac{m_1 + m_2}{m_1 m_2}},\tag{5}$$

198 with  $m_i$  the mass of the *i*-th wall leaf. For the panel under investigation there is also the 199 stiffness contribution of the elastic frame, the MSM resonance can then be determined as:

$$f_{MAM} = \frac{1}{2\pi} \sqrt{(k_a + k_m) \frac{m_1 + m_2}{m_1 m_2}} = 189 Hz.$$
 (6)

200 It is worth mentioning that the mechanical stiffness represents only the 20% of the total 201 stiffness.

## **4 EXPERIMENTAL RESULTS**

202 In this section the final comparison between the tested 3D printed prototype and the 203 complete numerical analysis of the panel is shown. The numerical STL curve is determined 204 through the complete diffuse field FEM model presented in subsection 2.2 considering  $\theta$ 205 varying through twenty incidence angles between 0 and 90 degrees and eight frequencies 206 for 1/3 octave band.

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The experimental acoustic sound insulation of the panel is determined through a measurements campaign on a 3D printed prototype in Nylon PA12. The panel consists of 12x12x1 unit cells that result in a total dimension of 800x800x46 mm. A unit cell detailed view is depicted in Fig. 10c. Due to SLS 3D printing technology, the whole unit cell is printed together (front panel, back panel and core) avoiding the assembly procedure.

The panel prototype has been characterized in a coupled chambers laboratory (Fig. 10b) 212 and the STL has been determined. Mastic sealing was arranged on the panel boundaries 213 during the installation on the window between the reverberant and the hemi-anechoic 214 chamber (see Fig. 10a). The total volume of the reverberant room is  $252 m^3$  and a tetrahedral 215 source of the type Genelec 8351A is adopted. Six microphones B&K 1/4" type 4135 for 216 sound pressure measurements in the source room are exploited, while the sound power in 217 the receiving room is measured by means of a B&K sound intensity PP probe type 2681. 218 The good agreement reached between the experimental test and the complete diffuse field 219

220 model is shown in Fig. 9.



**Figure 9.** Comparison between the numerical STL curve determined through the diffuse field FEM model and experimental STL curve performed in double chamber lab.

## 5 METASOLUTION AND LOCALLY-RESONANT ELEMENTS

The purpose of this section is to give an idea of the potentiality that a single-phase sandwich partition can obtain in terms of transmission loss improvement if coupled with

- 223 the metamaterial concept of locally resonant inclusions.
- 224 As mentioned in section 1, MSM panel show performances that exceed the sound insulation



(10c)

**Figure 10.** (a) Acoustic panel mounted and sealed on test window, (b) reverberant room view (c) and prototype unit cell detail.

- 225 power of a common mass-law-based partition, especially in the medium-high frequency
- range. The resonance of the MSM system however results in a dip, in this case set to 187
- 227 Hz (Fig. 5), where the STL has its minimum value. For this reason, effective solutions
- 228 based on locally resonant metamaterials principle to improve sandwich panels insulation at
- 229 their resonance frequency are extensively present in recent literature (Filho et al., 2019) (de
- 230 Melo Filho et al., 2019)(Lin et al., 2016) (de Melo Filho et al., 2020).
- 231 Coherently with the design process followed in the previous sections, a resonant element
- 232 design embedded in the partition geometry is proposed. The massive elements that compose
- 233 the panel core can be modified maintaining the injection moldable configuration, which is a
- 234 key aspect for industrial production. The hosted resonant elements are hence designed by



**Figure 11.** Unit Cell view of locally resonant hosting configuration. (a) Front view, (b) lateral view and (c) resonator geometry detail and first flexural eigenmode

- 235 tuning their own frequency with the one of the MSM system.
- 236 Resonators are composed of a beam element, linked to the main body of the unit cell,
- 237 and a cylindrical massive part. The following dimensions are adopted,  $d_{mass} = 0.014 m$ , 238  $h_{mass} = 0.014 m$ ,  $l_{beam} = 0.003 m$ ,  $h_{beam} = 0.0015 m$ ,  $w_{beam} = 0.003 m$  (see Fig. 239 11c).
- 240 The overall mass of the partition has been maintained to 26 kg/m<sup>2</sup> with the resonator mass 241 set to 5 kg/m<sup>2</sup> ( $m_{res}/M_{tot} = 19\%$ ).
- 242 Fig. 12 highlights the improvement in correspondence of the MSM dip of the baseline
- 243 system due to the locally resonant element introduction. Right after the resonators frequency
- 244 the sound transmission curve of the metamaterial panel converges towards the equivalent
- 245 mass configuration.

## 6 CONCLUSIONS

- The present contribution describes in detail the study, design, fabrication and experimental performances of an innovative acoustic sandwich panel. The peculiarity of the proposed
- 248 geometry is the internal core, an in-plane repetition of multiple engineered unit cells,



Figure 12. Normal incidence transmission loss comparison between baseline configuration and resonator hosting configuration.

- 249 coupled with two closing plane panels. The unit cell is composed by two principal massive
- elements supported by a frame of beams.
- 251 Such panel core is numerically and experimentally analyzed to give the partition a self-
- 252 sustaining capability and optimized sound insulation performances.
- 253 In particular, the frame has been designed from the acoustic point of view to not overstiffen
- the panel and leave to the airgap the main stiffness contribution that defines the system MSM resonance, which is accurately predicted by the lumped parameter model proposed.
- 256 During all the design process, considerations about the solution production via plastic
- 257 injection molding have been take into account. The acoustic transmission loss performances
- 258 are validated by an experimental campaign on a 3D-printed Nylon prototype, showing a
- 259 good agreement between the proposed numerical impedance tube model and the sound
- 260 insulation measured in double chamber lab. The last section introduces a further step in the
- 261 optimization process of the panel explaining how the unit cell can be easily coupled
- 262 with properly tuned locally resonant elements to improve the low frequency STL in
- 263 correspondence of the MSM resonance. A more detailed investigation of this Metasolution
- will be the object of a future work.

# **CONFLICT OF INTEREST STATEMENT**

The authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

# **AUTHOR CONTRIBUTIONS**

- 267 Conceptualization, methodology and validation, C.G. and S.C.; writing-original draft
- 268 preparation and figures preparation, C.G. and S.C.; writing-review and editing, S.C, C.G
- 269 and A.C; supervision A.C; funding acquisition, A.C. All authors have read and agreed to
- 270 the published version of the manuscript.

# ACKNOWLEDGMENTS

- The authors would like to thank Materiacustica S.r.l. and Paolo Bonfiglio for the precious support during the experimental tests.
- 273 The authors acknowledge the contribution of Fondazione Cariplo. The research has
- 274 been carried out within the framework of Project '2018-1743 META-matErials as new
- 275 teChnOlogy for high performing acoustic InSulatiOn paneLs, made of end of life
- 276 MATerials'.

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