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This is the peer reviewed version of the following article: Borrotti, M., Pievatolo, A., Critelli, I., Degiorgi, A., and Colledani, M. (2016) A computer-aided methodology for the optimization of electrostatic separation processes in recycling. *Appl. Stochastic Models Bus. Ind.*, 32: 1 133– 148, which has been published in final form at <https://doi.org/10.1002/asmb.2128>. This article may be used for non-commercial purposes in accordance with Wiley Terms and Conditions for Use of Self-Archived Versions.

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# **A computer-aided methodology for the optimization of electrostatic separation processes in recycling**

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(Dated: February 9, 2015)

## Abstract

The rapid growth of technological products has lead to an increasing volume of waste electrical and electronic equipments (WEEE) which could represent a valuable source of critical raw materials. However, current mechanical separation processes for recycling are typically poorly operated, making it impossible to modify the process parameters as a function of the materials under treatment, thus resulting in untapped separation potentials. Corona Electrostatic Separation (CES) is one of the most popular process for separating fine metals and nonmetals particles derived from WEEE. In order to optimize the process operating conditions (i.e. variables) for a given multi-material mixture under treatment, several technological and economical criteria should be jointly considered. This translates into a complex optimization problem that can be hardly solved by a purely experimental approach. As a result, practitioners tend to assign process parameters by few experiments based on a small material sample and to keep these parameters fixed during the process life-cycle. The use of *computer experiments* for parameter optimization is a mostly unexplored area in this field. In this work, a computer-aided approach is proposed to the problem of optimizing the operational parameters in CES processes. Three metamodels, developed starting from a multi-body simulation model of the process physics, are presented and compared by means of a numerical and simulation study. Our approach proves to be an effective framework to optimize the CES process performance. Furthermore, by comparing the predicted response surfaces of the metamodels, additional insight into the process behavior over the operating region is obtained.

Keywords: Design of computer experiments; Kriging; Artificial neural networks; Response surface; WEEE

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## I. INTRODUCTION

In recent years, the use of rules that govern experiments for technological improvement (i.e. Design of Experiments - DoE) [1] has received renewed momentum through the utilization of *Computer Experiments* [2]. These experiments are run on a computer code implementing a simulation model of a physical system of interest such as in the process of recovering waste printed circuit boards or in enzyme kinetics. In general a simulation model, or simulator, consists of a set of many linear or nonlinear, ordinary and/or differential simultaneous equations, whose solutions may not be amenable to analytical expression. Furthermore, runs of the simulator can be expensive and/or time-consuming. In this case, the use of a surrogate model (metamodel) is suggested. These metamodels are simpler models which represent a valid approximation of the original simulator and usually are statistical interpolators built from the simulated input-output data. Predictions at untried experimental points can then be made by metamodels and optimization techniques can be applied in order to find best settings. The selection of a metamodel to approximate the true model as accurately as possible is a crucial problem. Generally, polynomial surrogates are widely used to model computer experiments [3]. However, the behavior of the data often cannot be explained by these models. An alternative method is known as the neural network technique which allows the data to be fitted in a less constrained form [4, 5]. Another popular technique is kriging, which has been widely used for the design and analysis of computer experiments [6, 7]. With the aim of a detailed comparison between metamodels, in this work we build experimental designs based on these three different techniques (i.e. polynomial regression, kriging and neural network models).

This analysis is applied to the Corona Electrostatic Separation (CES), which is a process widely used in recycling for separating conductive from non-conductive fine particles obtained from the shredding of waste electrical and electronic equipments (WEEE). The main goal is to understand advantages and disadvantages of each model in support of the optimization of the process parameters, ultimately aiming and implementing an in-line process control framework. CES is defined as the selective sorting of charged or polarized bodies in an electric field [8–10] and it represents one of the most effective ways for recycling metals and nonmetals from WEEE with limited environmental impact. For example, this process has been proposed as a viable alternative to pyrometallurgical processes in the recovery of

metals from waste Printed Circuit Board (PCB).

WEEE is currently considered to be one of the fastest growing waste streams in the world, growing at 3-5 % per year [11]. Electronic waste can represent a very important source of key-metals for advanced technological products. For example, PCBs are called urban mineral resources since 25% - 30% in weight of their composition is made of valuable metals such as copper, tin, nickel, gold and silver. However, in order to successfully apply CES processes to the separation of complex multi-material mixtures such as granular flows from finely shredded PCBs, a tighter control of the process parameters need to be implemented. In order to optimize the process parameters (i.e. variables) for a given multi-material mixture under treatment, several technological and economical criteria should be jointly considered. This translates into a complex optimization problem that can be hardly solved by a purely experimental approach. As a result, practitioners tend to assign process parameters by few experiments based on a small material sample and to keep these parameters fixed during the process life-cycle. This is mainly due to the lack of knowledge-based engineering models and tools to support the design and operation of separation processes able to capture, with an acceptable level of confidence, all the major phenomena affecting the quality of the output. In the literature attempts to implement different control procedures have been developed in order to optimize specific objectives functions [12, 13] based on simplified process models and computer experiments [14, 15].

In this study, a reliable multi-body simulation model of roll-type Corona Electrostatic Separation (CES) [16] is used to build a set of metamodels in order to conduct computer-aided experiments for optimizing the process parameters. This solution will provide the ability to optimize the process parameters with respect to the specific material mixture under treatment, thus providing a degree of adaptability to these processes that is currently not available in the recycling industry.

The paper is structured as follows. The engineering problem is described in Section 2. Then, in Section 3, three metamodels for the response of physical experiments are introduced and discussed. Section 4 presents the computer-aided approach to generate sampling plans and its application is illustrated by the case study based on the CES simulator. The predictive abilities of the three metamodels are investigated and compared. A final discussion concludes the paper in Section 5.

## II. ENGINEERING PROBLEM

Corona electrostatic separator is mainly used to separate conductors from insulators, like copper from plastics, in shredded multi-material mixtures. The process physics is briefly explained in the following. Particles are transported by a feeder on the rotating drum and they are charged as they pass through an electrostatic field. More specifically, the separator uses corona charging or ion discharging to establish a negative charge on particles when particles pass between two high-voltage electrodes. Particles receive a discharge of electricity, which gives the non-metals a high surface charge, causing them to be attracted to the rotor surface until they are brushed down into the left bin. Metal particles do not get charged, as the charge rapidly dissipates through the particles to the earthed rotor, so they fall into the right bin under the effect of the centrifugal and gravitational forces. Ideally, if the separation process were perfectly accurate, all the particles would be correctly classified. However, due to the presence of mixed non-liberated particles and to random particle impacts, a non-classified material flow is generated (middlings) consisting of particles that drop in the central bin. The quality of the separation process depends on two set of process parameters, namely design parameters and controllable parameters. The design parameters include the drum diameter, the position and the shape of the electrodes. The operating parameters include the drum rotational speed, the electrostatic potential, the feed rate, and the splitters' position. Moreover the distribution of the input material characteristics (shape, density, conductivity, degree of liberation) also affects the separation performance. Due to these complex particle flow dynamics, the particles' trajectories are far from being deterministic, but a statistical distribution of the particles' falling points at the bin quota is usually observed.

Since the process physics is complex, modeling the trajectories of particles within CES is of practical engineering interest. In the literature, several attempts have been made to simulate particle trajectories in roll-type electrostatic separators [17, 18]. However, existing recycling process models only focus on single particle trajectories and fail to model two major causes for loss of efficiency in the separation process, i.e. (i) particle-particle and particle-equipment interactions and impacts, and (ii) the presence of un-liberated particles in the material flow. These limitations undermine the applicability of existing models in industrial settings. More realistic models are needed to better capture the real behavior of the process and to provide an accurate prediction of separation process performance. These motivations

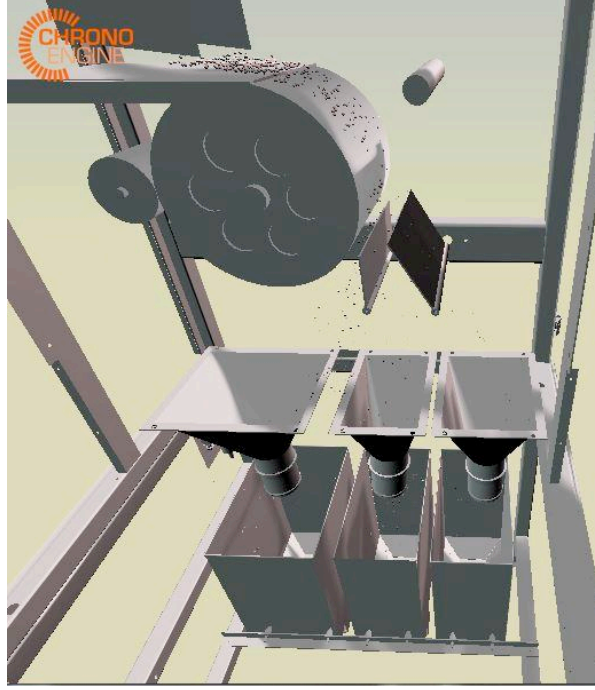


FIG. 1: Example of particle behaviour simulated by the CES simulation model.

has led to the development of a new multi-body simulation model [16, 19]. The simulation is based on the Chrono::Engine (<http://projectchrono.org>) C++ simulation libraries, which implement the Differential Variational Inequalities (DVI) approach. The non-smooth dynamics method used for the simulator, rooted in the recent theory of DVI, can handle up to millions of contacts between particles without requiring short integration time steps [20]. Within the simulation each particle is randomly generated with its own characteristics by sampling from a particle flow "DNA", characterized by multiple attributes, such as shape, material, orientation, and liberation degree. External forces, including aerodynamic, electrical, centrifugal and gravitational forces are applied on these particles, determining their trajectories. These realistic simulations, that have been validated in real industrial settings, can support the designer to perform virtual experiments to test the behavior of the system under specific mixture conditions and machine parameters, instead of running real experiments. From an application point of view, this approach can reduce drastically the number of real experiments and make the process flexible and adaptable to changes within the material flow. An example of separation process computed by the CES simulator is reported in Fig. 1.

However, simulations are usually time-consuming and it still unpractical to rely on simula-

tions for implementing in-line process control schema. In this scope, the use of metamodeling is particularly appealing for enabling “fast” in-line applications.

In this work we consider a typical industrial CES machine (Hamos KWS electrostatic separator) with fixed design parameters, whose performance depends on the following controllable parameters:

- 1) Electrostatic potential, or voltage, which ranges between 25.000 to 35.000 Volt;
- 2) Drum speed, or simply speed, which ranges between 32 to 128 rpm;
- 3) Feed rate, which ranges between 0.0028 to 0.028 kilograms per seconds (kg/s).

Furthermore the position of two splitters,  $S_1$  and  $S_2$ , separating the collecting boxes of conductive, middling and nonconductive products are considered. They have a fixed height and can move along the horizontal coordinate with a range of variation between 0 and 20 cm for both, divided into 60 possible positions. In the case under analysis the splitters are not considered as physical bodies, unlike the particles or the drum, and the interaction of the particles with these volumes is neglected. The positions of  $S_1$  and  $S_2$  are only considered in the post-processing phase: knowing the coordinates of the falling point of each particle after each simulation, the best position that maximizes an objective function is found, testing all feasible combinations of  $S_1$  and  $S_2$ . The outcomes (i.e. system responses) of the process are: the recovery of conductive products in its collecting box ( $R_{c,c}$ ), the grade of conductive products in its collecting box ( $G_{c,c}$ ), the recovery of non-conductive products in its collecting box ( $R_{nc,nc}$ ) and the grade of non-conductive products in its collecting boxes ( $G_{nc,nc}$ ). For the case of conductive products, the recovery is defined as follows:

$$R_{c,c} = \frac{m_{c,c}}{m_{c,c} + m_{c,m} + m_{c,nc}}, \quad (1)$$

where  $m_{c,c}$  is the mass of conductive products in its collecting box,  $m_{c,m}$  is the mass of conductive products in middling box and  $m_{c,nc}$  is the mass of conductive products in non-conductive box. Instead, the grade is:

$$G_{c,c} = \frac{m_{c,c}}{m_{c,c} + m_{nc,c}}, \quad (2)$$

where  $m_{nc,c}$  is the mass of non-conductive products in conductive box. Similarly,  $R_{nc,nc}$  and  $G_{nc,nc}$  are defined as the mass of non-conductive products in its collecting box divided



by the sum of the mass of non-conductive products in all the boxes and the mass of non-conductive products in its collecting box divided by the total mass in the non-conductive box, respectively.

These system responses are in trade-off and different possible solutions can arise while searching for a process optimization. For instance an optimal solutions for recovery  $R_{c,c}$  can negatively influence the performance of the separation process in terms of grade  $G_{c,c}$ . For this reason, we selected a utility function, which assesses the material recycling potential of a product. This approach is similar to Sherwood's characterization of the relationship between the price of a material and its concentration in its feed stream [11, 21], described in Gutowski et al. (2008) [22]. The utility function,  $u$ , has been defined as:

$$u(\phi_1, \phi_2) = \phi_1(R_{c,c}, G_{c,c}) + \phi_2(R_{nc,nc}, G_{nc,nc}), \quad (3)$$

where:

$$\phi_1(R_{c,c}, G_{c,c}) = (3.0649 \times (G_{c,c})^2 + 1.5747 \times G_{c,c} + 1.6673) \times R_{c,c} \quad (4)$$

and

$$\phi_2(R_{nc,nc}, G_{nc,nc}) = 0.1 \times (3.0649 \times (G_{nc,nc})^2 + 1.5747 \times G_{nc,nc} + 1.6673) \times R_{nc,nc}. \quad (5)$$

The constant values are chosen in order to fit copper economic values.

The utility function  $u(\phi_1, \phi_2)$  is then used to calculate the final system response,  $y_i$  with  $i = 1, \dots, E$ , where  $E$  is the total number of experimental points given by all controllable parameters combinations, and should be maximized in order to optimize the electrostatic separation process.  $R_{c,c}$ ,  $G_{c,c}$ ,  $R_{nc,nc}$  and  $G_{nc,nc}$  are computed using the simulators of the CES process [16], previously described.

### III. METAMODELS

#### A. Polynomial regression model

Polynomial regression models [23] are often used to approximate the dependence relation between a set of variables and a response. This response represents the output of the system and is measured by an identified variable  $Y$  and the  $v$  input variables  $(x_1, x_2, \dots, x_v)$  describe the features of the problem. This relation can be written as follows:

$$Y = f(x_1, x_2, \dots, x_v) + \epsilon; \quad (6)$$

where  $f$  may be a smooth function of  $x_1, x_2, \dots, x_v$  and  $\epsilon$  represents a random noise in the observable response.

The simplest polynomial model to explore the space approximating the function (6) is the first-order polynomial model,

$$Y = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \dots + \beta_v x_v + \epsilon; \quad (7)$$

where  $v$  variables are assumed to affect the response in a linear way without interactions. The first-order polynomial model is likely to be appropriate when we are interested in approximating the true response surface over a relatively small region of the independent variable space in a location where there is little curvature in  $f$ . Often the curvature in the true experimental surface is strong enough that the first-order model is inadequate. A second-order polynomial model will likely be required in these situations. The second-order polynomial model is a flexible model to describe experimental data in which nonlinear terms are present. The nature of the experimental surface depends on the signs and magnitudes of the coefficients in the following model:

$$Y = \beta_0 + \sum_{i=1}^v \beta_i x_i + \sum_{i=1}^v \beta_i x_i^2 + \sum_{i < j} \beta_{ij} x_i x_j + \epsilon \quad (8)$$

The approach of least squares estimation for the  $\beta$  parameters is then generally used and the adequacy of the fitted model is evaluated with the typical linear model diagnostics such residual analysis, coefficient of determination and/or more graphical methods.

## B. Artificial Neural Network (ANN)

An Artificial Neural Network (ANN) [24] is an information processing paradigm that is inspired by the way biological nervous systems, such as the brain, process information. The structure of the information processing system is composed by a large number of highly interconnected processing elements (neurons) working in unison to solve specific problems. An ANN is configured through a learning process, which, as in biological systems, involves adjustments to the synaptic connections that exist between the neurons.

The usual type of ANN consists of three groups, or layers, of units: a layer of *input units* (i.e. variables) is connected to a layer of *hidden units*, which is connected to a layer

of *output units* (system responses). When all the units are connected to one another and information travel one way only, from input to output, the ANN has a single-layer feed-forward architecture as represented in Fig. 2. Each hidden layer can be composed by a different number of nodes.

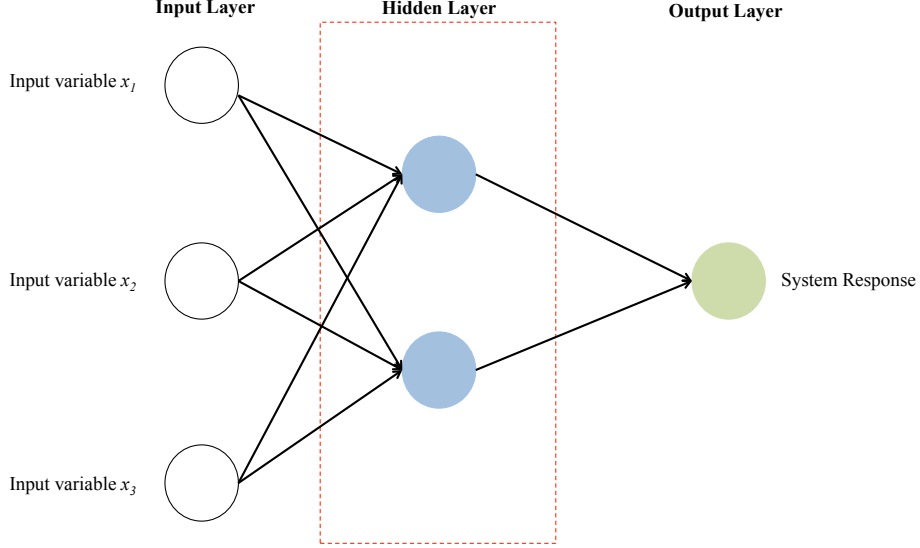


FIG. 2: Example of a single layer feed-forward neural network.

The influence of the inputs on the outputs is determined by the connection weights. The connection weights are real numbers associated with each connection between units and they determine whether it is possible for one unit to influence another. In order to train an ANN, the weights of each unit should be adjusted in such a way that the error between the expected output and the actual output is reduced. The most widely used method to determine the best weights is the back-propagation algorithm [25], which minimise this error by means of a gradient descent method that selects the best combination of weights. The performance of the algorithm depends on a weight decay parameter,  $\lambda$ , which is a regularization term that tends to decrease the magnitude of the weights and avoids over fitting [24].

After the training, the output of an ANN is equal to:

$$Y = f\left(\sum_{i=1}^v w_i \times x_i\right); \quad (9)$$

where  $w_i$  is the connection weight of the input variable  $x_i$ , with  $i = 1, \dots, v$ . The function  $f$ , which is called activation function or transfer function, is chosen before the training among

a range of functions [26]. Here we have employed the sigmoid function defined as follows:

$$f(x) = \frac{1}{1 - e^{-x}} \quad (10)$$

where  $x$  is a real number.

### C. Kriging Model

Kriging methodology was originally proposed by a South Africa geologist, D. G. Krige (1951) [27], for the analysis of geostatistical data and, nowadays, has become very popular in several applied context [28, 29].

Following Sacks et al. (1989) [30], the kriging approach consists in treating the output of a simulator as a realization of a stochastic process  $Y(\mathbf{x})$  such that  $Y(\mathbf{x}) = \mu(\mathbf{x}) + Z(\mathbf{x})$ . The global trend is denoted by  $\mu(\mathbf{x})$  and  $Z(\mathbf{x})$  represents the departure of the system response  $Y(\mathbf{x})$  from the trend. More precisely,  $Z(\mathbf{x})$  is usually assumed to be a Gaussian stationary process with  $E(Z(\mathbf{x})) = 0$ , a constant variance  $\sigma_Z^2$ , and a non-negative correlation function between two experimental points  $\mathbf{x}_1$  and  $\mathbf{x}_2$ :

$$\text{Corr}[Z(\mathbf{x}_1), Z(\mathbf{x}_2)] = R(\mathbf{x}_1, \mathbf{x}_2). \quad (11)$$

The correlation function should reflect the characteristics of the system response and one of special interest is the *power exponential family*, which is defined coordinatewise to form the correlation function in the  $v$ -dimensional space under the assumption of separability:

$$R(\mathbf{x}_1, \mathbf{x}_2 | \psi) = \exp \left\{ - \sum_{i=1}^v \left| \frac{x_{1i} - x_{2i}}{\theta_i} \right|^{p_i} \right\}, \quad (12)$$

where, for  $i = 1, \dots, v$ ,  $\theta_i$  is a scale parameter,  $p_i$  is the power parameter and  $\psi$  is the vector having  $\psi_i = (\theta_i, p_i)$  as its  $i$ -th entry. A popular choice for the estimation of  $\psi$  is the maximum likelihood estimate (MLE).

Two different types of kriging metamodels should be considered depending on the functional form of the trend function [7]:

- Ordinary kriging: the trend is constant  $\mu(\mathbf{x}) = \mu$  but unknown.

- Universal kriging: the trend component depends on  $\mathbf{x}$  and is modeled in a regressive way

$$\mu(\mathbf{x}) = \sum_{i=1}^v f_i(\mathbf{x})\beta_i, \quad (13)$$

where  $f_1(), \dots, f_v()$  are known functions and  $\beta = (\beta_1, \dots, \beta_v)$  is the vector of unknown parameters.

In other words, in ordinary kriging, the trend is a simple unknown constant whereas in universal kriging trend varies (i.e. second order polynomial trend) and the coefficients of the regression equation that describes this trend are unknown. In this work, we have employed the universal kriging modeling approach.

#### IV. COMPUTER-AIDED EXPERIMENTAL APPROACH

Following the general framework for computer experiments we proposed a computer-aided experimental approach (see Fig. 3) which is based on the following main steps:

- (i) Select the initial experimental batch of size  $n$  based on a sampling-based design [2];
- (ii) Evaluate the design points with the simulator;
- (iii) Estimate the metamodel on the simulated input-output data;
- (iv) Select from the experimental region the best point which yields the highest predicted system response value;
- (v) Evaluate the best design point with the simulator and use it as the best setting.

##### A. Sampling-based design: Latin Hypercube Sampling (LHS)

Computer Experiments differ from traditional physical experiments in that repeated observations at the same set of input variables yield identical system response [2], therefore, sampling techniques that spread design points are needed. Different sampling-based designs are described in literature [31] and one of the most used is the Latin Hypercube Sampling (LHS) technique [32] or Latin Hypercube Design. Generally, to obtain an LHS design consisting of  $n$  points, each dimension of the experimental region is divided into  $n$  equally

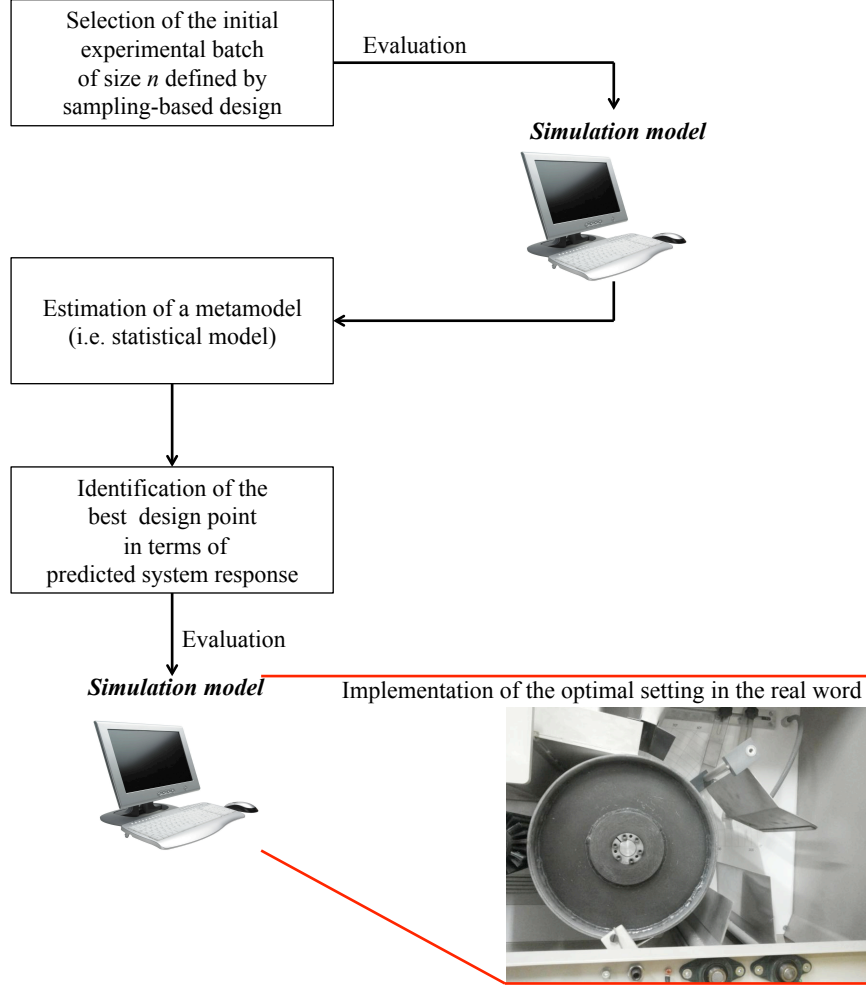


FIG. 3: Computer-aided experimental approach.

spaced intervals (e.g.  $[0, (1/n)], \dots, [(n-1)/n, 1]$ ), an interval is randomly sampled without replacement from each dimension and a value is uniformly sampled from the interval, obtaining one design point. This procedure is then repeated  $n$  times (see Fig. 4).

The uniform sampling of the co-ordinates of the design points meets the S-optimality criterion, which consists in maximizing the harmonic mean distance from each design point to all the other points in the design [33], in order to spread them as much as possible in the experimental region.

In this work, the Latin hypercube design is applied and a batch of size  $n = 50$  is selected based on the S-optimal criterion. The batch is then tested on the CES simulator.

As a first exploratory analysis, a set of descriptive statistics have been computed in order to get some insights into the frequency distribution of the system response. The maximum

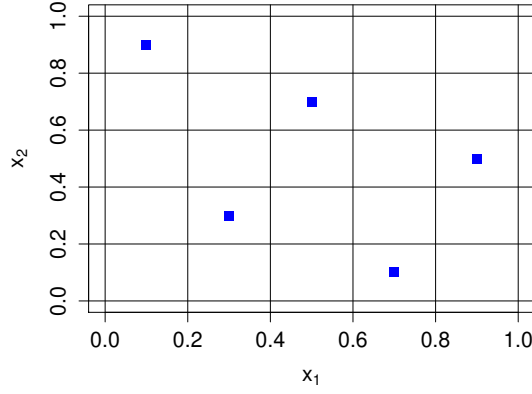
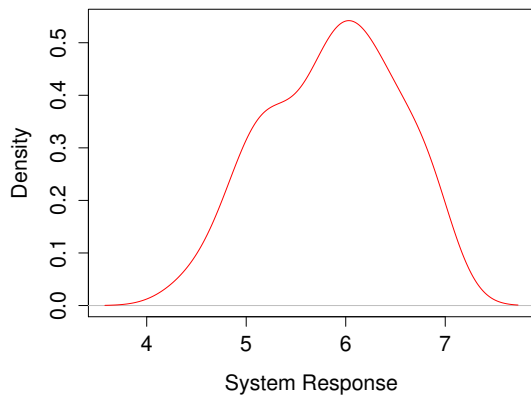


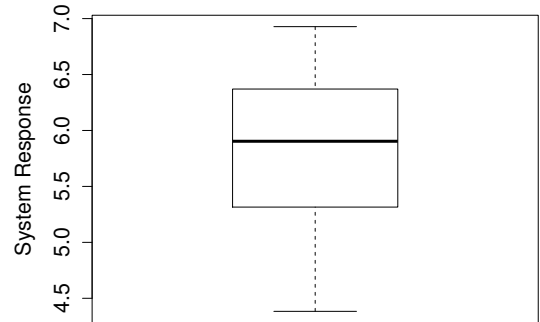
FIG. 4: A Latin hypercube design with two variables,  $x_1$  and  $x_2$ .

value of the utility function reached with the Latin hypercube design is 6.928 and the minimum is 4.383. The mean is 5.866 and the median is equal to 5.904; the first quartile is 5.319 and the third quartile is 6.358.

These values indicate a slightly left-skewed distribution and this particular shape can be seen in Fig. 5(a). In Fig. 5(b) a box-plot is shown which summarizes the distribution of the system response. The upper side of the box is the third quartile, instead the lower side of the box is the first quartile. The line inside the box represents the median. The upper and lower whisker are, respectively, the maximum and minimum values.



(a) Density plot



(b) Box plot

FIG. 5: Analysis of the system response

## B. Optimised model selection procedure

In order to fine-tune the three metamodels, we applied different approaches to each.

For the polynomial model, starting from Eq. (8), we used a stepwise selection procedure based on the Akaike Information Criterion (AIC) [34] in order to identify the significant variables.

The resulting best model is:

$$Y = \beta_0 + \beta_1 x_2 + \beta_2 x_3 + \beta_3 x_2^2 + \beta_4 x_3^2 + \beta_5 x_1 x_2 + \epsilon, \quad (14)$$

where  $x_1$  is the voltage,  $x_2$  the speed and  $x_3$  the feed rate,  $\beta_i$  (with  $i = 0, \dots, 5$ ) are the regression coefficients and  $\epsilon$  the random noise in the observable response,  $Y$ .

For the neural network and kriging models we applied a bootstrap procedure [35]. In the case of the neural network, the bootstrap procedure is used to identify the best number of nodes in the hidden layer and to set the decay parameter,  $\lambda$ . For the kriging model, it is used to select the correlation function family.

The bootstrap procedure works as follows: from a subset of the initial data set ( $n_t = 40$ ), the parameters of a range of different model specifications are estimated. Then, the different estimated models are used for predicting the system response associated with the remaining experimental points ( $n_v$ ). At this point, the Mean Square Error (MSE) is calculated for each specification. The MSE is defined as:

$$MSE = \frac{1}{n_v} \sum_{i=1}^{n_v} \left( \hat{Y}_i - Y_i \right)^2, \quad (15)$$

where  $\hat{Y}_i$  is the  $i^{th}$  predicted value of the system response. The procedure is repeated  $B = 20$  times, each one with a different re-sample of the initial subset. Finally, the specification of each statistical model with the minimum averaged MSE is selected.

The best selected network topology (see Fig. 6) involves one hidden layer with seven neurons, a sigmoid activation function between the input and the hidden layer and a linear activation function between the hidden layer and the output. The training algorithm for the weight selection is the back-propagation algorithm with  $\lambda = 0.1$ .

The best type of kriging model is based on the universal kriging approach and the selected most representative correlation function is the power exponential family.



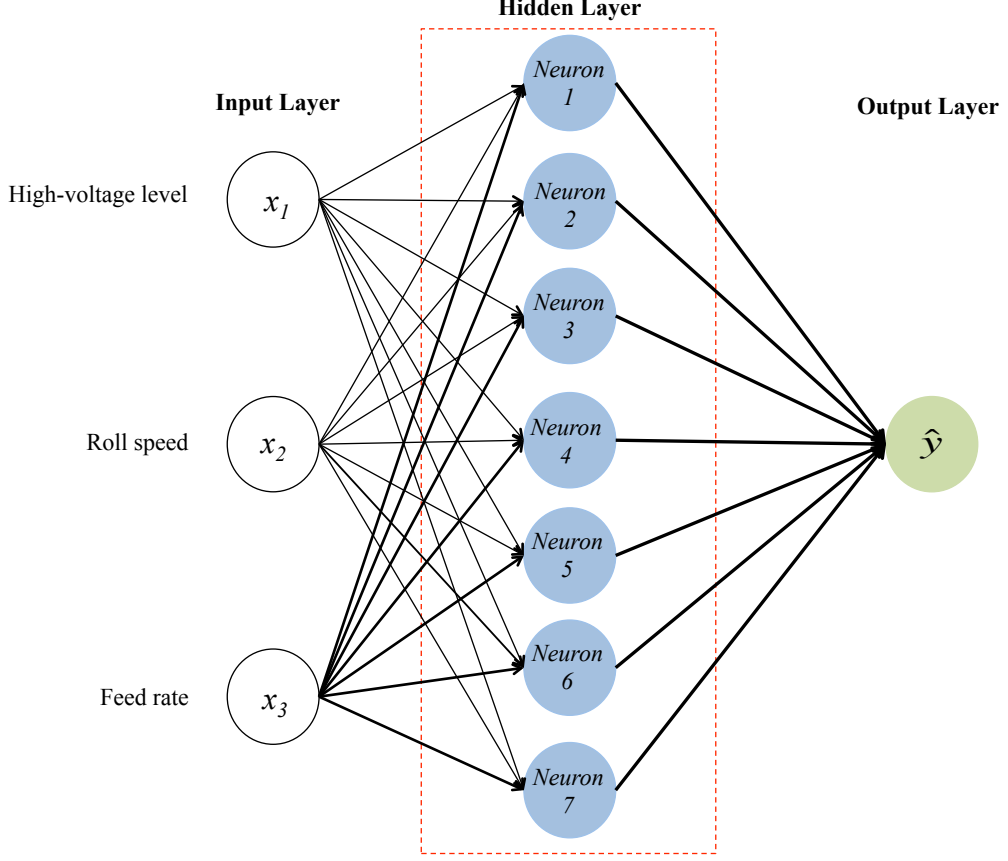


FIG. 6: Best feed-forward ANN with 7 neurons in the hidden layer. The different line thickness represents the importance of the connection arcs.

### C. Results

The three metamodels have been compared in terms of prediction accuracy by means of a cross-validation approach. In our case, we randomly divided  $R = 50$  times the initial dataset in two subset: a training set of size  $n_t = 40$  and a validation set of size  $n_v = 10$ . At each time, the training set is used to estimate the coefficients and/or parameters of the metamodels. The resulting metamodels are used to predict the system response of the validation set and then to evaluate their performance. The predictive performance indicators selected to compare the metamodels are: the mean squared error ( $MSE$ ), the mean absolute error ( $MAE$ ), the standard deviation of absolute error ( $St. AE$ ), the mean absolute percentage error ( $MAPE$ ) and the standard deviation of absolute percentage error ( $St. APE$ ).

$$AE = \left| \hat{Y}_i - Y_i \right|, \quad i = 1, \dots, n_v \quad (16)$$

$$MAE = \frac{1}{n_v} \sum_{i=1}^{n_v} AE_i, \quad (17)$$

$$St. AE = \sqrt{\frac{1}{n_v - 1} \sum_{i=1}^{n_v} (AE_i - MAE)^2} \quad (18)$$

$$APE = \left| \frac{\hat{Y}_i - Y_i}{Y_i} \right|, \quad i = 1, \dots, n_v \quad (19)$$

$$MAPE = \frac{1}{n_v} \sum_{i=1}^{n_v} APE_i, \quad (20)$$

$$St. APE = \sqrt{\frac{1}{n_v - 1} \sum_{i=1}^{n_v} (APE_i - MAPE)^2} \quad (21)$$

where  $\hat{Y}_i$  is the  $i^{th}$  predicted value of the response system in the  $r^{th}$  re-sample.

From the results, reported in Table I, the neural network shows better performance in terms of prediction accuracy. Besides that, the ability of kriging model to predict the unknown system responses is comparable with the neural network. The selected polynomial model seems to perform worse but still acceptably. In Fig. 7, the MSE distribution is shown.

Given these results, we estimated the three metamodels on the  $n = 50$  available data points selected by the LHS technique (see Sec. IV A).

	polynomial model	neural network	kriging model
<i>MSE</i>	0.0940	<b>0.0906</b>	0.0911
<i>MAE</i>	0.6421	<b>0.6034</b>	0.6063
<i>St. AE</i>	0.7618	<b>0.7291</b>	0.7332
<i>MAPE</i>	0.1113	0.1056	<b>0.1055</b>
<i>St. APE</i>	0.1325	0.1285	<b>0.1282</b>

TABLE I: Prediction performance for the three metamodels.

In Fig. 8, 9 and 10, we show the different predicted response surfaces by means of contour plots. Each contour plot represent the behaviour of the response system varying two of the three variables. The third variable is just kept fixed at the central value of its range.

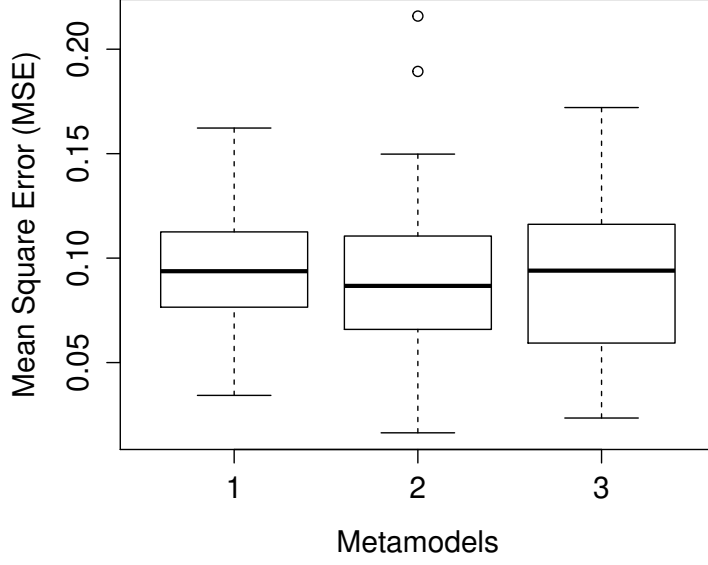


FIG. 7: Comparison of the MSE distribution for polynomial model (1), neural network (2) and kriging model(3).

The three metamodels give different levels of smoothness. In Fig. 8(a), the polynomial model identifies a concave surface with a maximum response value in the region of the minimum values for voltage and drum speed. The maximum is found in the same region by the other two response surfaces obtained with the Neural Network (Fig. 8(b)) and the kriging model (Fig. 8(c)), respectively. This result can be explained using forces balance. More specifically, by increasing the magnitude of the voltage, the electric force acting on booth particles is also increased, pushing metals far from the drum and attracting non-metals on the drum surface. Reducing the drum speed, the contribution of the centrifugal force, which is a significant term, is reduced too, making the effects of the electrostatic forces more evident.

In Fig. 9 the response surfaces as functions of feed rate and voltage are considered. The polynomial model (9(a)) is still a concave surface which leads to a specific region of optimality. In other words, the feed rate, given minimum values of voltage, influences the performance of the system. The neural network (9(b)) identifies a slope surface with maximum values when voltage is set at the minimum, and minimum values when voltage is set at the maximum. In this case, the response surface is not affected by variations of

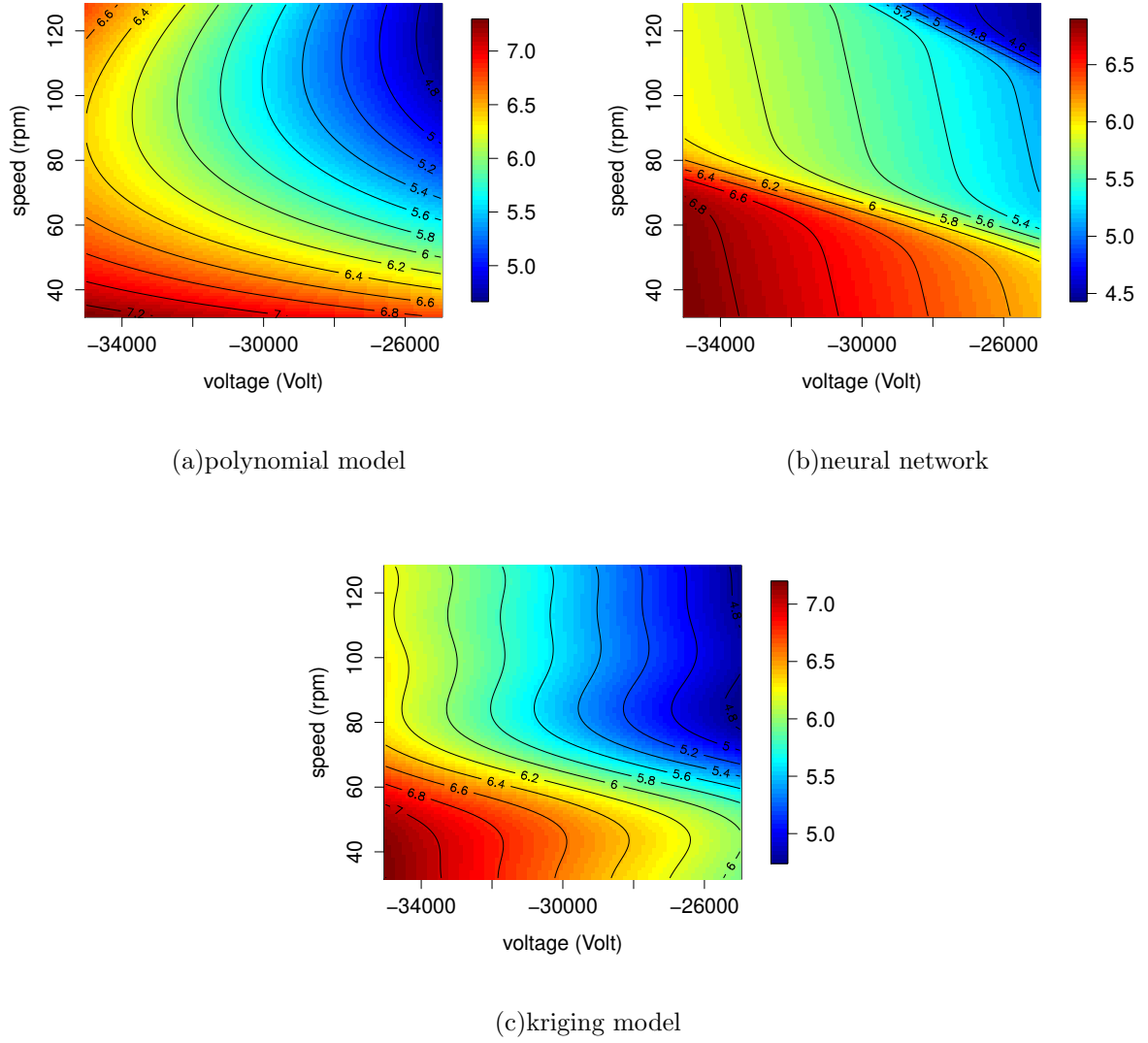
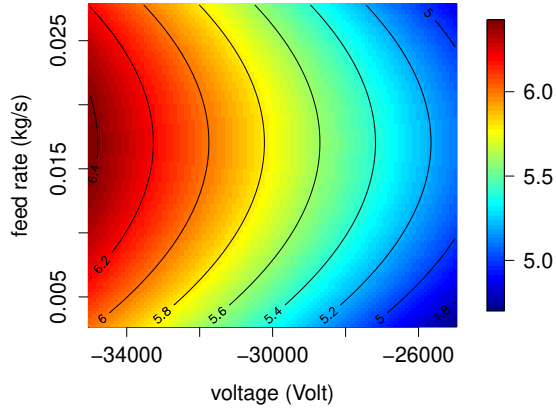


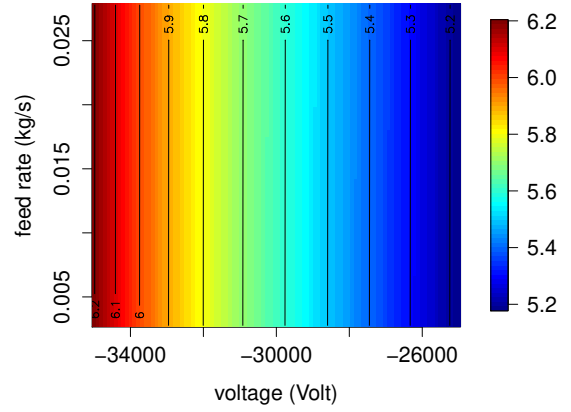
FIG. 8: Contour plots of voltage and drum speed, or simply speed.

the feed rate. The same situation occurs with the kriging model (9(c)) which identifies less straight contour lines but with the same feature.

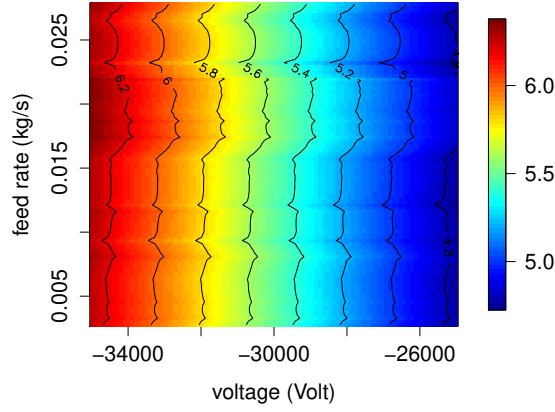
In Fig. 10, drum speed and feed rate are studied. In Fig. 10(a) (polynomial model), a stationary point is identified between 90 and 110 rpm and 0.015 and 0.018 kg/s. From 65 to 32 rpm the response system constantly increases towards maximum values when feed rate is between 0.015 and 0.020 kg/s. Instead, neural network (10(b)) considers the feed rate non influential for the behavior of the response system and a slope between 50 and 75 rpm is identified. A similar slope is identified by the kriging model (10(c)). However, the feed rate affects the response system and there is also interaction between drum speed and feed rate,



(a)polynomial model



(b)neural network



(c)kriging model

FIG. 9: Contour plots of voltage and feed rate.

a feature absent from the other models. In fact, given minimum values of speed, maximum values of response system are reached in correspondence of higher values of feed rate.

The weak dependence of the response from the feed rate suggests two main remarks. Probably, the effect on the distribution of particles in the simulated flows, and consequently on the objective function, is noticeable for very high values of the feed rate. These values have not been tested. In fact, the experiments were carried out in the range expected from the normal use of the machine. In addition, it is not possible to generalize this behavior of the separation process because it is strictly linked to the specific properties of the material used in simulations. The problem needs to be studied in greater depth, for a better understanding

of the physics of granular flows in terms of feed rate interaction with flow variability.

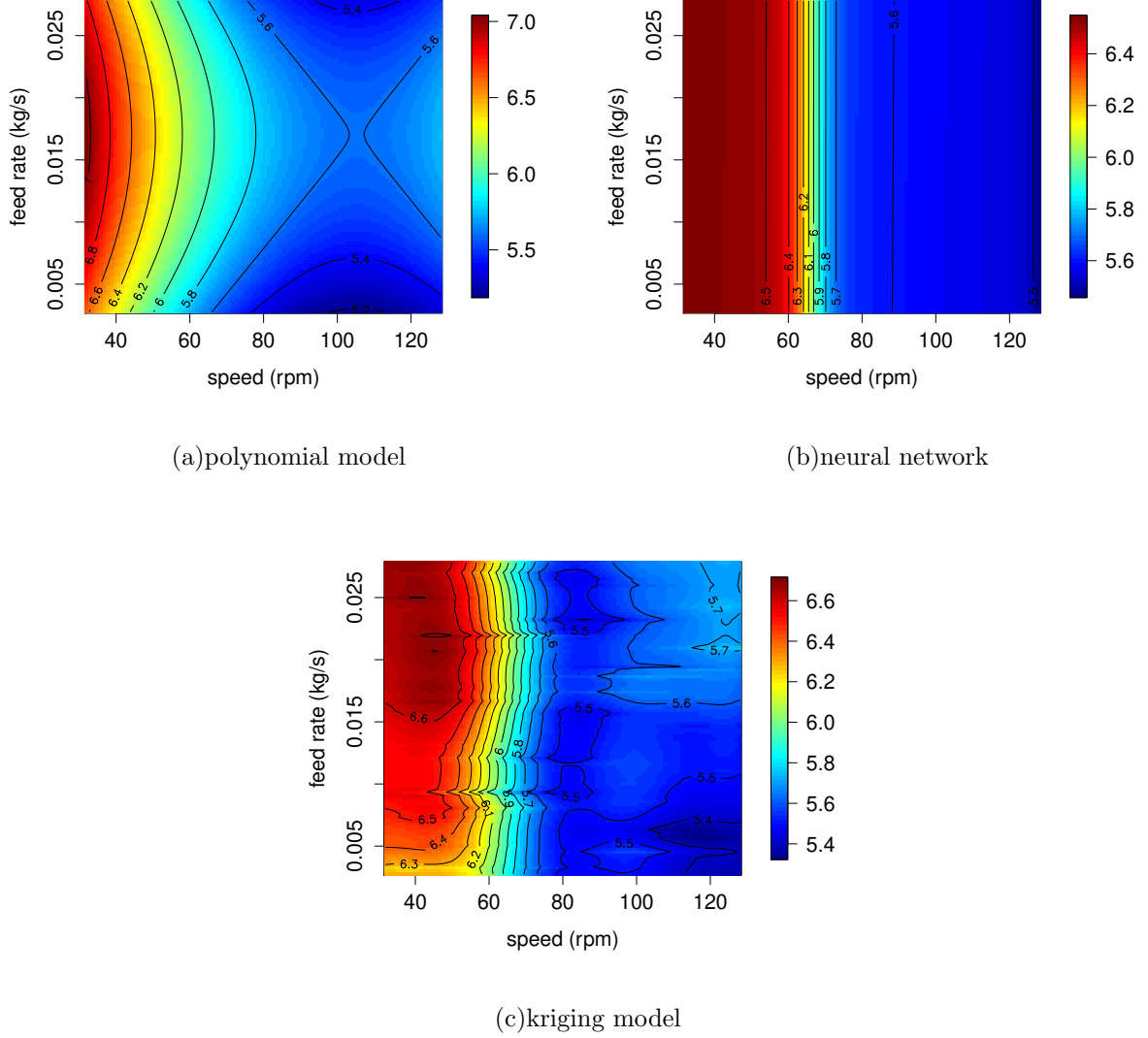


FIG. 10: Contour plots of drum speed, or simply speed, and feed rate.

The three metamodels are slightly different in terms of predicted response surfaces. All of them have individuated a similar behaviour of the predicted response as a function of voltage and drum speed but, concerning the influence of the feed rate, they have predicted different situations.

In order to understand which of the three metamodels better locates the optimal controllable parameters combination, we applied a Simulated Annealing (SA) [36, 37] optimization algorithm.

We ran the SA over the three metamodels obtaining identical results for the neural

network and the kriging models. The optimal setting of the controllable parameters found in the polynomial response surface reflects the previous considerations and a different best value for the feed rate has been selected.

Subsequently, the CES simulator was used to calculate the response of the all optimal settings. Results reported in Table II show that the response from the simulated model is the same. This suggests that the feed rate does not affect the response system, given the minimum values of voltage and speed, as the neural network and the kriging model were correctly predicting.

	<b>Optimal setting</b>	<b>Predicted response</b>	<b>Simulated response</b>
polynomial model	-35000   32   0.01704	7.304	6.925
neural network	-35000   32   0.02778	6.899	6.925
kriging model	-35000   32   0.02778	7.312	6.925

TABLE II: Optimal settings for voltage, speed and feed rate.

#### D. Kriging model Vs Neural Networks

Artificial Neural Networks (ANNs) are well-known models which have exhibited excellent behavior in the resolution of complex problems. It is demonstrated that feedforward ANNs are universal approximators, which means that an ANN can approximate, to any desired degree of accuracy, any real-valued continuous function [38].

Despite the success of ANNs, one of the most common criticism of ANNs is that there is no satisfactory interpretation of their behavior because they capture relations between inputs and outputs with a highly accurate approximation, but no definitive answer has been given about their inner workings.

However, Benítez et al. (1997) [39] demonstrated the equivalence between fuzzy rule-based systems (FRBS), developed using fuzzy logic, and ANNs. In their work it is shown that ANNs can be encoded by a continuous FRBS.

Following a similar reasoning, we show that it is possible to empirically obtain a *equivalence-by-approximation* between kriging models and ANNs. In other words, given a simple single layer feed-forward neural network with a sigmoid activation function in hidden neurons and linear in output neurons, there exists at least one universal kriging model

with power exponential correlation function which approximates the same real function in way similar to the neural network. This is possible by tuning the  $\theta$  and  $p$  parameters of the power exponential correlation function and the trend coefficients. In Fig. 11, it is shown that an universal kriging model, correctly tuned, can approximate the response surface predicted by the ANN fitted to our simulator output. In particular, the kriging model has been estimated using the ANN predicted values of the first batch of data ( $n = 50$ ) selected by the LHS as response.

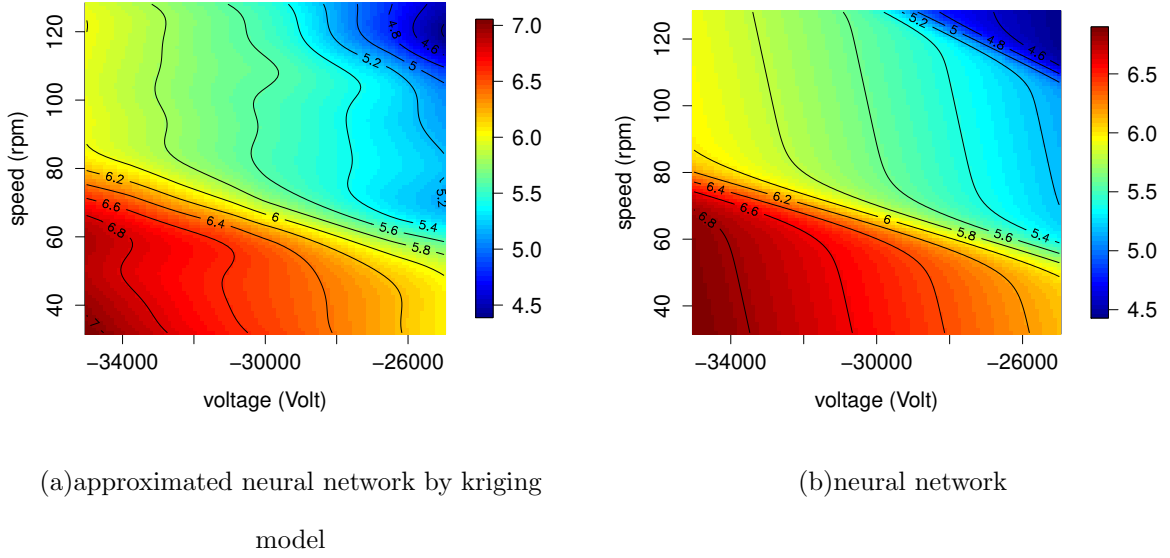


FIG. 11: Comparison between neural network response surface and the one approximated by the kriging model.

This approximation provides a handle to interpret the artificial neural network fitted on our CES data. In fact,  $\theta$  and  $p$  parameters have a clear influence on the power exponential correlation function [40] and, consequently, on the universal kriging model. Furthermore, as the two metamodels have shown a similar performance while optimizing the controllable parameters combinations, this approximation is important for understanding whether a different behavior in the whole experimental region reflects limitations of the metamodels themselves or actual characteristics of the simulator.

In Table III, all the parameters of the models are reported. Model 1 collects the trend coefficients, scale and power parameters and variance of the universal kriging model estimated on the LHS design and Model 2 collects the same information for the universal kriging model



that approximates the single layer feed-forward neural network.

TABLE III: Estimated trend coefficients, scale and power parameters and variances of the two universal kriging models. Model 1 is the universal kriging model estimated on the first batch of data ( $n = 50$ ) selected by the LHS and Model 2 is the approximation of the artificial neural network by means of the universal kriging model.

	Trend				Scale			Power			Variance
	coefficients				parameters			parameters			
	$\beta_0$	$\beta_1$	$\beta_2$	$\beta_3$	$\theta_1$	$\theta_2$	$\theta_3$	$p_1$	$p_2$	$p_3$	$\sigma^2$
<b>Model 1</b>	2.503	-0.0001	-0.012	10.151	12612.404	18.796	0.049	2.000	2.000	0.117	0.128
<b>Model 2</b>	3.583	-0.0001	-0.014	0.381	12409.871	12.597	0.049	1.186	1.994	2.000	0.048

Two of the power parameters in the two models,  $p_1$  and  $p_3$ , change significantly, showing a different degree of smoothing along the directions of voltage and feed rate: the larger the power parameter, the smaller the degree of smoothing. The power parameter for the feed rate of Model 1 changes from  $p_3 = 0.117$  to  $p_3 = 2.000$  in Model 2, while the corresponding trend coefficient is reduced by two orders of magnitude. This indicates that Model 2 estimate of the feed rate effect on the predicted response at any given point depends mostly on a very weak linear trend, not taking into account the observed responses at the remaining experimental points, unlike Model 1 which seems to exploit the effect of larger feed rates to obtain information on smaller ones through a higher degree of smoothing (so that contour lines in Fig. 10(c) are not straight in the direction of feed rate). The power parameter of voltage in Model 2 smooths out local variations with respect to Model 1, while the trend parameter is unchanged, so that Model 1 shows greater sensitivity to voltage variations.

This analysis leads to two important conclusions. First of all, an ANN may be expressed in a more comprehensible way by means of a universal kriging model. Secondly, from the application point of view, it provides a suggestion in the choice of the most suitable model for CES applications. In fact, a greater sensitivity to voltage can be crucial for the real CES process, because small variations over the dielectric strength can cause an electrical discharge (by electric arch) and, consequently, they can alter the electric field in the real CES machine, thus affecting the quality of output. Therefore, the kriging model seems preferable to the ANN model, because it seems to reflect this latter property and it also seems to give

some more information on the effect of feed rate.

## V. CONCLUSIONS

The rapid growth of waste electrical and electronic equipments (WEEE) has led to an increasing demand from experimental fields for efficient methods to improve material separation processes, such as the corona electrostatic separation.

This work has addressed this issue by proposing a computer-aided methodology, derived by computer experiments, and comparing three different modeling techniques: polynomial regression, kriging and artificial neural network (ANN) models. Our numerical results in Section IV C suggest that kriging and ANN models are equivalent in terms of optimization. In fact, the optimal setting of the controllable parameters (voltage, drum speed and feed rate) obtained by the two metamodels is the same.

However, a more careful analysis of the two metamodels (see Section IV D) has also shown different abilities in describing the actual characteristics of the process. In particular, the kriging and the ANN models mainly differ in how they treat voltage and feed rate. On the one hand, ANN considers the effect of feed rate on the predicted response as weakly linear and as not-interacting with voltage or drum speed and shows a strong degree of smoothing in terms of voltage variations. On the other hand, the kriging model reveals the effect of larger feed rates on the predicted response and shows greater sensitivity to voltage variations. Therefore, considering the known physical properties of CES, the most suitable metamodel seems to be the kriging model, which better describes some properties of the CES process.

Another interesting finding of our analysis of the two metamodels is that it is possible to empirically obtain a *equivalence-by-approximation* between the kriging and the ANN models. In fact, by fine tuning the  $\theta$  and  $p$  parameters of the power exponential correlation function and the trend coefficients in the kriging model, an approximation of the response surface close to that predicted by an ANN can be obtained, which can aid interpretation of the ANN fit.

Finally, we remark that our computer-aided methodology can be successfully applied to CES to handle experiments with a higher number of process variables, with a different level of accuracy, based on the chosen metamodel. More generally, we believe that further exploration in this direction may generate valuable contributions to the optimization and

description of the recycling process of WEEE, because also other stages of this process, taking place before separation, require modelling and optimization.

### Acknowledgments

This work has been carried out as a part of the FIDEAS project (Fabbrica Intelligente per la Deproduzione Avanzata e Sostenibile) co-funded within the Framework Agreement between Regione Lombardia and CNR.

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