# Medical & Biological Engineering & Computing

# Gaussian Mixture Models based 2D-3D registration of bone shapes for orthopaedic surgery planning --Manuscript Draft--

Article Type: Original article Keywords: Statistical Shape Models; Gaussian Mixture Models; 2D/3D registration; orthopedic surgery Corresponding Author: Marta Valenti Milano, Milano ITALY  Corresponding Author Secondary Information: Corresponding Author's Secondary Information: Corresponding Author's Secondary Information: Corresponding Author's Secondary Information: Corresponding Author's Secondary Information: Order of Authors:  Marta Valenti Giancarlo Ferrigno, professor Dario Martina Weimin Yu Guoyan Zheng, P.D. Mohsen Akbari Shandiz, PhD Carolyn Anglin, professor Elena De Momi, PhD  Order of Authors Secondary Information: Funding Information:  Funding Information:  In orthopaedic surgery, precise kinematics assessment helps the diagnosis and the planning of the intervention. The correct placement of the prosthetic component in the case of knee replacement is necessary to ensure a correct load distribution and to avoid revision of the implant. 3D reconstruction of the knee kinematics under weight bearing conditions becomes fundamental to understand existing in vivo loads and improve the joint motion tracking. Existing methods rely on the semi-automatic positioning of a shape previously segmented from a CT or MRI on a sequence of fluoroscopic images acquired during knee flexion. We propose a maleumatic positioning of a shape previously segmented from a CT or MRI on a sequence of fluoroscopic indiges acquired during knee flexion between the projected sillowette and the extracted calonour from the fluoroscopy image. We evaluated the algorithm using Digitally Reconstructed Radiographies of both healthy and diseased subjects, with a CT extracted shape and a SSM as the 30 model. In vivo lests were done with fluoroscopically acquired images and subject specie CT Shapes. The results obtained are in line with the literature, but the computational time is substantially reduced.	Manuscript Number:					
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Keywords Statistical Shape Models  $\cdot$  Gaussian Mixture Models  $\cdot$  2D/3D registration  $\cdot$  orthopedic surgery  $\cdot$  image processing

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#### 1 Introduction

Osteoarthritis is a highly debilitating pathology that affects knees primarily of older people. With this inflammation, the cartilage degenerates, the distance between bones is reduced and hypertrophy of the bones can occur, with the creation of osteophytes [1]. The Dutch Institute for Public Health estimates that worldwide almost 16% of men and 31% of women aged over 55 years have radiographic knee osteoarthritis [2]. In 12% of cases the pathology reduces the motion of the knee and causes pain to the patient, often requiring the use of ambulatory aids [3]. The most used treatment for severe osteoarthritis is surgery. However almost the 20% of the patients that undergo Total Knee Arthroplasty (TKA) are not satisfied with their operation [4].

A pre-operative study of knee kinematic under weight-bearing conditions can improve the outcome of the surgery [5]. The representation of the joint kinematics in 3D space allows for understanding pain zones and ligament tensions, determining the best implant positioning and thus correcting nonalignments of the bone segments [5–11]. The acquisition of pre-operative Computer Tomography (CT) or Magnetic Resonance Imaging (MRI) images gives a deep insight into the morphology of the structures, but these procedures are currently limited to static positioning and have high costs and radiation doses given to the patient. Mono and multi-plane fluoroscopy are the most accurate and used procedures to measure in vivo non-invasive kinematics of the knee [5, 10]. The current clinical technique is mainly based on the operator's ability to correctly position the shape on the images [4]. This technique is time-expensive and error-prone, as it is based on human ability. Regardless of the number of fluoroscopic projections, two main automatic methods have been implemented to recover the correct pose of the bones in 3D space: intensity based and feature based methods.

Intensity based methods need a pre-operative CT scan in order to acquire the density of the patient's bone. The 2D-3D matching is then achieved comparing the Digitally Reconstructed Radiograph (DRR) to the acquired fluoroscopic image and adjusting the rotation and translation parameters in order to minimize the differences between the two images in terms of pixel intensities [5,12,13]. Although very accurate, these methods require a previous CT to determine the bone density for the DRR creation, and are computationally expensive for the number of pixel intensity comparisons that must be made to find the correct pose.

Feature based methods are based on the contours of the bone shape that can be extracted from the fluoroscopic images using edge detector filters, such as Canny or Sobel [14–16]. These methods project the silhouette of the bone shapes and match it with the extracted edges. Usually, feature based methods necessitate a previous morphological 3D dataset of the bone shapes, such as MRI or CT [4,17,18]. Recently, some authors have addressed the problem of needing the morphological scan and substituting it with a Statistical Shape Model (SSM), a collection of shapes coming from atlas that can be deformed in order to represent accurately the target shape [9,19,20]. In this way, costs

are reduced and the patient is exposed to a lower radiation dose. However, computational time becomes an issue, as the whole sequence of poses takes some hours to be computed [21].

Our objective is to develop a new feature based algorithm based on Gaussian Mixture Models (GMMs) that is able to register a 3D point-set on a single or biplane image of the same object. We tested the algorithm with a SSM of the femur using a set of fluoroscopic images of the knee. The goal is twofold: we addressed the problem of accurately recovering the pose of the knee in 3D space in a completely automatic way and also of ensuring the correct parameters for the deformation of the shape. In [22, 23], the authors addressed the problem of the registration of two point-sets with a GMM fitting. The solution is given through an Expectation Conditional Maximization (ECM) procedure, that simplifies the original Expectation Maximization (EM) algorithm by Dempster et al. [24]. Both of these frameworks, however, assume working with point-sets lying in the same (2D or 3D) space.

The proposed algorithm extends the state of the art to registering a 3D shape of a femur on a set of fluoroscopic images acquired during flexion-extension of the knee.

#### 2 Materials and methods

The knee is imaged during a sequence of flexion-extension movements. A fluoroscopic tube returns a set of X-ray images. The source and the image plane are calibrated, and their pose in the world reference frame is known. The reconstruction of the femur kinematics is done through a series of features projection and back-projection from the fluoroscopic image plane to the 3D space. A 3D shape of the bone is used as a model to reconstruct the correct pose.

# 2.1 Datasets

#### 2.1.1 3D shape

The 3D shape is defined as a set of points  $(\mathbf{X}_s, s = 1, ..., S)$  and triangles that can be either derived from the segmentation of a volumetric image dataset (CT or MRI) [25] or a SSM [26]. We define the patient specific 3D shape as  $3DS_{CT/MRI}$  and the SSM as  $3DS_{SSM}$  (A). A Gaussian distribution  $(\mathbf{X}_s, \mathbf{\Sigma}_s)$  is associated to each 3D point of the model. The isotropic covariance can be expressed as  $\mathbf{\Sigma}_s = \sigma_s \mathbf{I}_3$ .

The silhouette of the model is made up of those points that share a contour edge, i.e. an edge shared by two facets with normals pointing in different directions from the source. The silhouette points are then a subset of the shape points  $\mathbf{X}_m, m = 1, \dots, M < S$ . The model silhouette is projected on the image plane  $\mathbf{x}_m, m = 1, \dots, M$ .

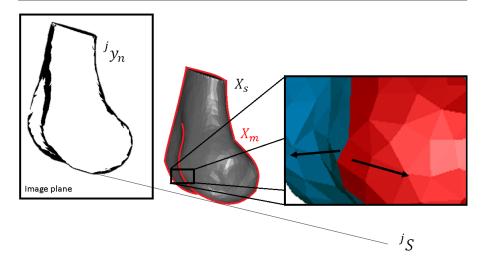


Fig. 1: The X-ray source  ${}^jS$  projects rays on the image plane. The image is processed and the contours  ${}^jy_n$  are extracted using a Canny edge detector (black points on the image). In the middle, the shape is formed by points  $X_s$  and triangles. The silhouette of the model,  $X_m$  in red, is made up of those points that share a contour edge, i.e. an edge shared by two triangles with normals (arrows) pointing in different directions from the source. The zoom on the right shows the normals of the triangles that point in different directions.

#### 2.1.2 2D contours

The segmentation of the contour of the shape on the images is performed using a semi-automatic algorithm based on gradient enhancement of the image and a spline interpolation between user picked points [20]. The selected pixels, belonging to the segmentation, can be transformed in 3D points using the known image calibration parameters  $(\mathbf{y}_n, n=1,\ldots,N)$ .

# 2.2 Registration

# 2.2.1 Initialization

A manual initialization is necessary to define the initial pose for the shape. Seven landmark points  $L_i$ , i = 1, ..., 7 are identified on the 3D shape 3DS. The user is asked to select the same points on the images [27]. The backprojected lines from the user-selected points to the corresponding source identify seven landmarks in the 3D space. Using corresponding points registration [28], we find the homogeneous transformation matrix  $\mathbf{T}$  that maps the shape in the calibrated image space.

#### 2.2.2 Expectation Conditional Maximization

The expectation step (E-step) involves the computation of the posterior probability  $p_{mn}$  that every point of the projected shape on the image plane  $(\mathbf{x}_m, m = 1, ..., M)$  is associated to a point of the contour  $(\mathbf{y}_n, n = 1, ..., N)$ :

$$p_{mn} = \mathcal{P}\left(Z : \mathbf{y}_n \to \mathbf{x}_m \,|\, \mathbf{y}_n; \theta, \sigma\right) \tag{1}$$

where Z is the association operator between a projected point  $\mathbf{x}_m$  of the shape's silhouette  $\mathbf{X}_m$  with a point of the contour  $\mathbf{y}_n$  extracted from the image (B). The set of unknown variables is composed by the registration parameters  $\theta[6\times1] = \{q_1, q_2, q_3, t_1, t_2, t_3\}$  where  $q_i, i=1,2,3$  are the Euler angles and  $t_i, i=1,2,3$  are the translation values, and the set of 3D points variances  $\sigma_1^2, \ldots, \sigma_M^2$ :

$$\psi = (\theta, \sigma_1^2, \dots, \sigma_M^2) \tag{2}$$

As the direct maximization of the likelihood is intractable, the minimization of the negative log-likelihood  $(E(\psi))$  will instead be taken as the objective [24]:

$$E(\psi) = -\sum_{n=1}^{N} \log \sum_{m=1}^{M} \mathcal{P}(\mathbf{X}_{m}) \mathcal{P}(\mathbf{y}_{n} | \mathbf{X}_{m}(\theta; \sigma_{m}^{2}))$$
(3)

The minimization function can thus be transformed in:

$$E(\psi) = \frac{1}{2} \sum_{n=1}^{N} \sum_{m=1}^{M} \frac{p_{nm}}{\sigma_m} \left[ \left( ||\mathbf{y}_n - \mathbf{X}_m(\theta)||^2 \right) + 3\sigma_m^2 \log(\sigma_m^2) \right] + \frac{\rho}{2} ||L(\phi)||^2$$
 (4)

where  $||L(\phi)||^2$  is a regularization parameter over the transformation, and  $\rho$  weights its contribution to the minimization.

The ECM algorithm allows a simplification of the problem dividing the minimization in two steps (CM-step):

- minimization of eq. (3) over the registration parameters
- update of the variances using the newly estimated registration parameters

In the case of a rigid transformation, the parameter  $||L(\phi)||^2$  is equal to 0, and the solution of the problem is given by a least-squares fitting of two 3D point sets, as described in [28].

If the shape to be registered is a  $3DS_{SSM}$ , the parameters to be estimated are the shape coefficient vectors  $\beta_k$ , and the regularization term assumes the form of the Mahalanobis distance, with  $\lambda_k^2$  eigenvalues of the SSM:

$$||L(\phi)||^2 = \sum_{k=1}^{K'} \frac{\beta_k^2}{\lambda_k^2}$$
 (5)

All the shape coefficients are determined with a closed form solution as described in [23].

The algorithm converges to a minimum if the percentage difference between the likelihood of two consecutive frames is below a predefined threshold. Specifically:

 $\frac{\mathcal{L}^{(t)}(\mathcal{X} \mid \mathcal{Y}) - \mathcal{L}^{(t-1)}(\mathcal{X} \mid \mathcal{Y})}{\mathcal{L}^{(t-1)}(\mathcal{X} \mid \mathcal{Y})} < \epsilon \tag{6}$ 

where  $\mathcal{X}$  and  $\mathcal{Y}$  are respectively the GMM and the observations. The likelihood of the current step is defined as:

$$\mathcal{L}(\mathcal{X} \mid \mathcal{Y}) = \prod_{m=1}^{N} \sum_{m=1}^{M} \alpha_m \cdot \left( \sigma_m^{-2} e^{\frac{-||\mathbf{y}_m - \mathbf{x}_m||^2}{2\sigma_m^2}} \right)$$
 (7)

In (7),  $\alpha_m$  is the component prior of the specific model [29].

# Algorithm 1 GMM-based registration

```
1: procedure Initialization
       Extract contours from figure y_n
       Select landmarks on images L and find initialization matrix T
 4: procedure Registration
       procedure RIGID TRANSFORMATION
 5:
 6:
           loop
 7:
           procedure E-STEP
               Project silhouette points x_m \leftarrow X_m
 8:
               Calculate posterior probability p_{mn} = \mathcal{P}\left(Z(y_n = x_m(\theta, \sigma_m^2)) \mid y_n\right)
 9:
           procedure CM-STEP (3DS_{CT/MRI})
10:
11:
               Find virtual observations o_m
12:
               Backproject virtual observations O_m
13:
               Compute registration parameters \theta
14:
               \sigma \leftarrow update\ variance
           goto loop.
15:
       if Shape = SSM then
16:
17:
           procedure SSM ADAPTATION
18:
               loop:
19:
               procedure E-STEP
20:
               procedure CM-STEP (3DS_{SSM})
21:
                  Find virtual observations o_m
22:
                  Backproject virtual observations O_m
23:
                  Compute shape deformation parameters \beta
24:
                  \sigma \leftarrow update\ variance
25:
               goto loop.
26: for all images do
       procedure RIGID TRANSFORMATION
27:
```

#### 2.3 Validation protocol

Twenty-four healthy knees were imaged with MRI scans and manually segmented to find the 3D shape. Those shapes were used to define the SSM as described in A [27].

The subject dataset is the following (Table 1):

- one healthy subject  $S_0$  who underwent a CT scan (Sensation Cardiac 64, Siemens). The CT dataset is composed of 59 slices of  $512 \times 512$  pixels each (0.7890625 mm/pixel). The slice thickness is 2 mm and the space between slices is 1.7 mm. The CT dataset was used to generate the DRR for evaluation purposes.
- Seven osteoarthritic patients  $(S_i, i=1,\ldots,7)$  eligible for TKA with different grades of osteoarthritis. The patients underwent a preoperative CT scan from which the  $3\mathrm{D}S_{CT}$  of the femur was segmented [30]. The CT datasets were composed of DICOM images acquired with a SIEMENS Sensation 64 CT machine. Each slice is 512x512 pixel  $(0.3516 \mathrm{\ mm/pixel})$  with a slice thickness of 0.6 mm and a spacing between slices of 0.4 mm. All the patients were also imaged at seven fixed flexion angles using two sequential fluoroscopic projections with an AXIOM Luminos dRF flat-bed (Siemens; Berlin, Germany) [4]. The first image was taken with the projector placed horizontally (lateral image), while the second was taken with the source at  $10^\circ$  below horizontal. Both projections were calibrated using custom made calibration software [31]. The fixed flexion angles  $(0^\circ, 15^\circ, 30^\circ, 45^\circ, 60^\circ, 75^\circ, 90^\circ)$  were obtained using steps of different customized heights on which the subject could step up. Three subjects  $(S_1, S_2, S_3)$  with different grades of osteoarthritis were selected to generate the DRRs of diseased knees.

All the patients signed an informed consent and the institutional review board approved the study.

Subject	Age	Gender	Osteoarthritic grade	CT	$DRR_{0/10/90}$	${\it Fluoroscopies}_{0/10}$
$S_0$	47	F	none	х	$0^{\circ}:3^{\circ}:72^{\circ}$	
$S_1$	67	${ m M}$	severe	x	$0^{\circ}:8^{\circ}:80^{\circ}$	$0^{\circ}:15^{\circ}:90^{\circ}$
$S_2$	75	$\mathbf{M}$	$\operatorname{mild}$	x	$0^{\circ}:8^{\circ}:80^{\circ}$	$0^{\circ}:15^{\circ}:90^{\circ}$
$S_3$	82	$\mathbf{F}$	moderate	x	$0^{\circ}:8^{\circ}:80^{\circ}$	$0^{\circ}:15^{\circ}:90^{\circ}$
$S_4$	65	F	mild	x		$0^{\circ}:15^{\circ}:90^{\circ}$
$S_5$	75	$\mathbf{M}$	severe	X		$0^{\circ}:15^{\circ}:90^{\circ}$
$S_6$	71	$\mathbf{F}$	moderate	X		$0^{\circ}:15^{\circ}:90^{\circ}$
$S_7$	82	$\mathbf{M}$	mild	X		$0^{\circ}:15^{\circ}:90^{\circ}$

**Table 1:** For each subject, the age, gender and osteoarthritic grade are indicated. All the femurs analysed were right femurs. The  $DRR_{0/10/90}$  values indicate the angles for which we generated the DRRs. We specify the starting and ending angle, with the step used. The Fluoroscopies<sub>0/10</sub> values indicate the angles of the fluoroscopic images.

In order to assess the model reconstruction performances all the CT datasets were segmented using Amira<sup>®</sup> (VSG—FEI, France) and the anatomical reference frame was defined as in [32].

The DRR is built integrating the density of each voxel of the CT along the direction of each ray as in [33]. Three different sources and image planes were simulated for each patient, resulting in three sets for each patient: the

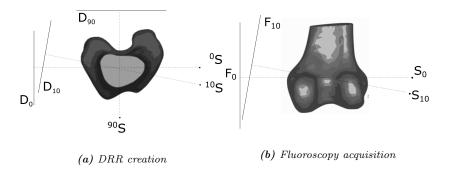


Fig. 2: Description of the virtual environment setup for the DRR creation and fluoroscopic acquisitions. The source  $S_0$  was established on the medio-lateral axis, as well as the center of  $D_0$  and  $F_0$ .

For the DRR,  $D_{10}$  is obtained rotating the source-plane axis of 10 degrees on the horizontal plane.  $D_{90}$  is obtained rotating the source-plane axis of 90 degrees, having it correspondent to the antero-posterior axis.

For the fluoroscopies,  $F_{10}$  is obtained rotating the source-plane axis of 10 degrees on the medio-lateral axis.

first image shows a lateral view of the femur  $(L_0)$ , the second and third images show a view rotated on the sagittal plane of  $10~(L_{10})$  and  $90~{\rm degrees}~(L_{90})$  (see Figure 2) [34]. For Subject  $S_0$  we rotated the femur from  $0^{\circ}$  to  $72^{\circ}$  with a step of  $3^{\circ}$  generating the ground truth pose  $(\mathbf{T}_{GT_0}^i, i = 0^{\circ}, 3^{\circ}, \dots, 72^{\circ})$ . The three pathological DRRs were instead created rotating the femur from  $0^{\circ}$  to  $80^{\circ}$  with a step of  $8^{\circ}$  generating the ground truth pose  $(\mathbf{T}_{GT_1,2,3}^i, i = 0^{\circ}, 8^{\circ}, \dots, 80^{\circ})$  [20].

#### 2.3.1 Tests

The initialization is done as described in paragraph 2.2.1. The tracking consists in finding the correct pose of the 3DS for all the images provided for a given flexion sequence. The tests were performed with six different conditions  $C_{1,...,7}$ :

- $C_1$ : 3DS pose initialization with  $D_0(0^\circ)$  and  $D_{90}(0^\circ)$  and tracking with  $D_0$  and  $D_{90}$  for all angles with  $S_0, \ldots, S_3$
- $C_2$ : 3DS pose initialization with  $D_0(0^\circ)$  and  $D_{90}(0^\circ)$  and tracking with  $D_0$  for all angles with  $S_0, \ldots, S_3$
- $C_3$ : 3DS pose initialization with  $D_0(0^\circ)$  and  $D_{10}(0^\circ)$  and tracking with  $D_0$  and  $D_{10}$  for all angles with  $S_0, \ldots, S_3$
- $C_4$ : 3DS pose initialization with  $D_0(0^\circ)$  and  $D_{10}(0^\circ)$  and tracking with  $D_0$  for all angles with  $S_0, \ldots, S_3$
- $C_5$ : 3DS pose initialization with  $F_0(0^\circ)$  and  $F_{10}(0^\circ)$  and tracking with  $F_0$  and  $F_{10}$  for all angles with  $S_1, \ldots, S_7$
- $C_6$ : 3DS pose initialization with  $F_0(0^\circ)$  and  $F_{10}(0^\circ)$  and tracking with  $F_0$  for all angles with  $S_1, \ldots, S_7$

For each trial, both the SSM  $(3DS_{SSM})$  and the CT segmented shape  $(3DS_{CT})$  were used.

#### 2.3.2 Results evaluation

The homogeneous matrix  $\mathbf{T}_{\theta}^{i}$  was constructed from the optimal parameters  $\theta$  returned by the ECM algorithm. In case of conditions  $C_{1}, \ldots, C_{4}$ , we computed  $\mathbf{T}_{residual}^{i} = \mathbf{T}_{GT}^{i-1} \cdot \mathbf{T}_{\theta}^{i}$ . The errors were presented as rotations (in terms of Euler angles) and translations of  $\mathbf{T}_{residual}^{i}$ .

For the conditions  $C_3, \ldots, C_6$ , Edge to Surface (E2S) distance was computed [21]. E2S is defined as the Euclidean distance between a point on the 3D shape and the closest point on the associated contour pixel back projection. In this way, E2S does not require the ground truth pose to evaluate the accuracy of the algorithm. Kruskal-Wallis test with p < 0.05 was used to asses if the results for  $C_3, \ldots, C_6$  using  $3DS_{CT}$  and  $3DS_{SSM}$  were statistically different.

#### 3 Results

Figure 3 represents the results of an optimization of a  $3DS_{CT}$  in  $C_1$  condition. As shown in the figure, the points of the projected silhouette tend to overlay the points of the contour, in order to minimize the distance between the two datasets.

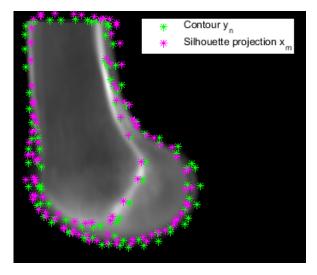


Fig. 3: Representation of the contour points and the silhouette points projected after the optimization of the algorithm

In order to better understand the results, the errors have been expressed in the anatomical axes of the subject.

Figure 4 shows the values of rotation and translation of  $\mathbf{T}_{residual}$  in the case of the healthy subject  $S_0$ . As can be seen, in case of single plane tracking or dual plane tracking with  $D_0$  and  $D_{10}$  the error in the medio-lateral axis

is increasing up to 3 cm with the flexion angle. The translation errors on the other axis, as well as the rotation errors on every axis is bounded between some mm and 1 cm in the case of  $3\mathrm{D}S_{SSM}$ . The results are more accurate using the  $3\mathrm{D}S_{CT}$ . In this case, the errors are below 1 cm also in the out-of-plane axis (medio-lateral).

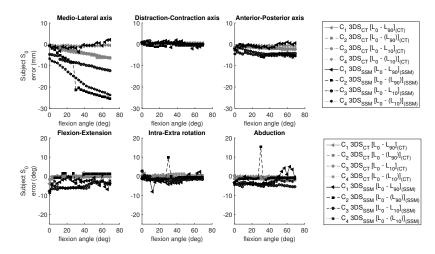


Fig. 4: Translation and rotation error of  $\mathbf{T}_{residual}$  for  $S_0$ 

Figure 5 shows the errors in terms of rotation and translation for conditions  $C_1, \ldots, C_4$  and using  $3DS_{CT}$  and  $3DS_{SSM}$ . In these figures it can be seen that the error is generally lower in the case of  $3DS_{CT}$ , a part from the medio-lateral axis of  $S_2$  when the error raises up to 6 cm. In  $S_3$  an angle dependent trend is clearly visible, similar to those shown in Figure 4.

The edge to surface index is represented in Figure 6 for the only tests with  $L_0$  and  $L_{10}$  images and for subject  $S_1, S_2, S_3$ . Results are presented as a populations of E2S Root Mean Square (RMS) for each pose of the trials. Results were grouped for type of images analysed (DRR or fluoroscopies). The parenthesis above the boxplot indicate that Kruskal-Wallis test returned differences in the distribution median.

In Figure 7 are shown the E2S results for the fluoroscopic acquired images. Patients  $S_1, \ldots, S_7$  proved to be statistically different only in a few cases, with  $S_2$  that has the highest differences.

#### 4 Discussion

This paper describes an innovative method to obtain the pose of the femur from single or biplane fluoroscopies to be used in knee tracking for accurate planning of orthopaedic surgery, starting from a patient specific model (obtained from volumetric dataset) or from a generic SSM. In the latter case,

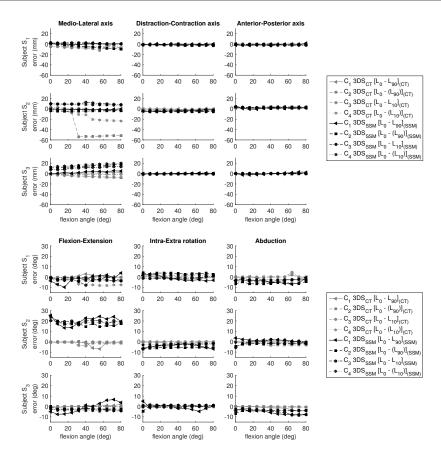
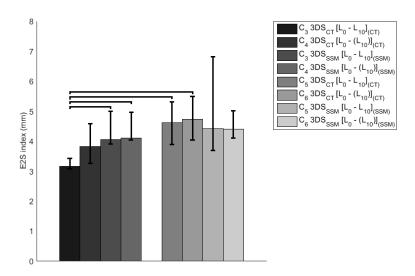


Fig. 5: Translation and rotation error of  $T_{residual}$  for  $S_1, S_2, S_3$ 

the radiation dose for the patient can be reduced. Knowing knee kinematics allows understanding pain zones associated with tensions of the ligaments and contact of the bones on each other, improving the outcome of the surgery.

Our registration method is based on GMMs and solves the Maximum Likelihood (ML) problem using an ECM approach, which allows significantly reducing the computational costs. Only a few seconds per image are enough to ensure the convergence of the system to the correct result, while for the previous methods [20,35] several hours were needed to reach convergence. Compared to previous works that used GMMs to register two different shapes on each other [22,23,36], our approach implements a 2D/3D registration, addressing the problem of a registration between two datasets with different dimensions. The method works in a semi-automatic way: it requires a rough initialization from the user and a threshold parameter to extract the contours with a Canny edge detector, saving time and augmenting the accuracy.



**Fig. 6:** Comparison of the Edge to Surface index for subjects  $S_1, S_2, S_3$  with DRR or fluoroscopic images

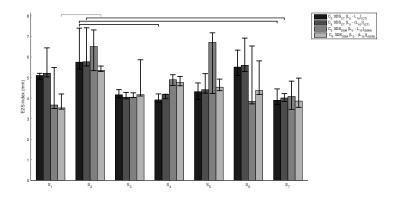


Fig. 7: Edge to Surface index for each subject with fluoroscopic images

The results presented in our analysis show that the difference between the SSM and the CT extracted shape is significant only in a few cases, especially with diseased shapes. This can be due to limited morphing capability of the statistical model given by the low number (24) of healthy knees used as datasets [20].

Overall, the implemented registration method proved to have results comparable to the literature. In [21] the authors found a translation error of a few mm (0.48-0.81 for the median accuracy, and approximately 2 mm for the

precision), that are comparable with the results we found in our experiments in the case of DRR tracking with  $S_0$  and  $C_1$ .

The fluoroscopic images projection angle influences the tracking accuracy of the depth dimension. The ML axis has bigger errors compared to the others axis, because reducing the angle between the two projections from  $90^{\circ}$  to  $10^{\circ}$  decreases the pose determination accuracy [37]. The same behaviour regarding out of plane errors, can be observed when the tracking is performed with single-plane fluoroscopy. The error in depth increases from frame to frame, as there are no constraints on this axis. In the case of diseased patients, the error in depth can reach up to 6 cm (Figure 5). In fact, the indetermination given by the single projection must be added to the non-perfect correspondence between the extracted contours and the statistical shape. The same considerations could be asserted relative to the rotation errors. A-part from Subject  $S_2$ , which has a very distal cut of the diaphysis (due to a tight joint intraoperatively) that compromises the reconstruction of the correct pose, the results are in line with those presented in [11,18], who found errors below 1 cm with a higher distance in the out-of-plane axis.

The evaluation of the accuracy with fluoroscopic images was performed using the E2S index to allow an evaluation of the accuracy without knowing the correct pose of the ground truth. The results show a statistical difference in the case of tracking with the  $3DS_{CT}$  (Figure 6). This is probably due to a different Canny threshold, which influenced the correct positioning of the shape. The same error is not visible in the case of  $3DS_{SSM}$  thanks to the lower deformation of the shape. These results are comparable with the one stated by [21] who found an error of approximately 2 mm. However, their dataset had a proximal cut of the diaphysis, augmenting the accuracy of the algorithm. Dealing with pathological subjects is more challenging, especially with a reduced set of shapes that created the SSM. Results are in the order of some mm (depending on the condition) and could be still acceptable to evaluate the kinematics of the knee. The method proved to be robust and efficient, especially when used with patient specific shapes. Future work will increase the number of shapes to construct the ssm and include also the tibia in the study, in order to have the joint angle value for a proper kinematic analysis. For single image tracking higher constraints on the depth axis must be implemented (e.g. a constrained motion of max 1 mm between frames).

#### 5 Conflict of Interest

The authors declare that they have no conflict of interest.

#### 6 Aknowledgements

The authors want to acknowledge the Natural Sciences and Engineering Research Council of Canada (NSERC) and the Canadian Institutes of Health Research (CIHR) for funding the acquisition of the validation images.

## Appendix A Statistical Shape Model

A SSM is a set of shapes on which the location of the landmarks is correspondent. From this set of shapes we can extract the mean model  $\bar{\mathbf{M}}$  and the covariance matrix, from which we can compute the eigenvectors (modes of variation) and the eigenvalues.

$$\mathbf{D} = \frac{1}{K-1} \sum_{k=1}^{K} (\mathbf{M}_k - \overline{\mathbf{M}}) (\mathbf{M}_k - \overline{\mathbf{M}})^T$$

$$\mathbf{D} \cdot \overrightarrow{\mathbf{M}}_k = \lambda_k^2 \cdot \overrightarrow{\mathbf{M}}_k$$

$$\sigma_1^2 \ge \lambda_2^2 \ge \dots \ge \lambda_{K-1}^2$$
(8)

where K is the number of shapes,  $\lambda_k^2$  are the descending-order eigenvalues of the covariance matrix  $\mathbf{D}$  and  $\mathbf{M}_k$  are the corresponding eigenvectors. To deform a SSM we can multiply specific weights to the modes, and add them to the mean model.

$$\mathbf{M}_{SSM} = \mathbf{\bar{M}} + \sum_{k=1}^{K'} \beta_k \mathbf{\overline{M}}_k \tag{9}$$

# Appendix B Expectation Conditional Maximization algorithm for GMMs

A femur model is represented by a set of 3D points  $\mathbf{X}_s$ ,  $s=1,\ldots,S$ . A set of fluoroscopic images  $I_j$ ,  $j=1,\ldots,J$  are simultaneously acquired with different sources  ${}^j\mathbf{S}$  and image planes. On each fluoroscopic image  $I_j$ , the contour of the femur  ${}^j\mathbf{y}_n$  is semi automatically segmented. The femur silhouette is defined by points  $\mathbf{X}_m$ , and their projection leads to  ${}^j\mathbf{x}_m$  where j indicates the image on which the points are projected. We also define a set of virtual observations  ${}^j\mathbf{o}_m$  that have a correspondent point in the 3D space  $\mathbf{O}_m$ . The registration problem is the estimation of the homogeneous matrix (expressed by the transformation parameters  $\theta$ ) which minimizes the distance between the virtual observation  $\mathbf{O}_m$  and the silhouette point  $\mathbf{X}_m$ .

The variables used in this description are:

- $-j\mathcal{Y}$  is the contour extracted from each image, whose pixels are  ${}^{j}\mathbf{y}_{n}, n = 1, \ldots, N$  (also called observations)
- $-\mathbf{X}_s, s=1,\ldots,S$  are the points of the 3D shape
- $-j\mathcal{X}$  is the set of points of the silhouette  $j\mathbf{X}_m, m=1,\ldots,M< S$
- $-j\mathbf{x}_m, m=1,\ldots,M$  are the pixel of the shape's silhouette projected on image j
- $-j\mathbf{o}_m, m=1,\ldots,M$  are the virtual observations on the image j
- $-\mathbf{O}_m, m=1,\ldots,M$  are the virtual points backprojected in the 3D space

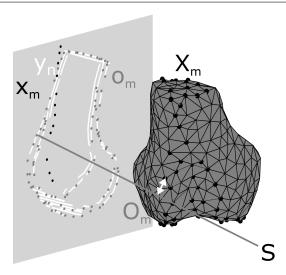


Fig. B.1: In the figure are represented the shape with the points  $\mathbf{X}_s$ , the extracted silhouette on the shape  $\mathbf{X}_m$  and their projection  $\mathbf{x}_m$  on the image plane. It also represented the source of the x-ray beam (S) and the points extracted from the contour of the image  $\mathbf{y}_n$ , from which we can calculate the virtual observation  $\mathbf{o}_m$  and its backprojection  $\mathbf{o}_m$ . The white arrow between the backprojected virtual observation  $\mathbf{o}_m$  and its associated silhouette point  $\mathbf{X}_m$  is the minimized distance at each iteration.

#### B.1 Gaussian Model and Likelihood

Each  $\mathbf{X}_s$  point of the model is defined as the centroid of a 3D Gaussian distribution with mean  $\mathbf{X}_s$  and covariance matrix  $\mathbf{\Sigma}_s$ , identifying in this way a Gaussian Mixture Model (GMM). Considering isotropic covariances, each  $\mathbf{\Sigma}_s$ ,  $s = 1, \ldots, S$  is defined as

$$\Sigma_s = \sigma_s \mathbf{I}_3 \tag{10}$$

where  $\mathbf{I}_3$  is the 3×3 identity matrix and  $\sigma_s$  is the scalar value of the covariance that varies for each  $\mathbf{X}_s$  point. The operator  $\mu: \mathbb{R}^3 \to \mathbb{R}^3$  transforms a point  $\mathbf{X}_s$  in another point  $\mu(\mathbf{X}_s, \theta)$  where  $\theta$  is the parametrization of the transformation.

The likelihood  $(\mathcal{L})$  that expresses the probability that the contour is coincident with the silhouette projection is a function of both the registration parameters  $\theta$  and the covariances.

$$\mathcal{L}(\theta, \sigma_1, \dots, \sigma_S \mid \mathcal{Y}) = \log \mathcal{P}(\mathcal{Y}; \theta, \sigma_1, \dots, \sigma_S)$$
(11)

where  $\mathcal{P}()$  is the probability that the set of observations  $\mathcal{Y}$  is extracted from the GMM with parameters  $(\theta, \sigma)$  and the likelihood indicates the probability that the set of observations  $\mathcal{Y}$  is coincident with the projection of the shape's silhouette  $\mathcal{X}$ .

This maximization can not be performed due to the presence of missing data, as the assignment of each observation to one of the Gaussian of the

GMM is unknown. The operator  $\{Z: \mathbf{y}_n \to \mathbf{x}_m\}, n=1,\ldots,N$  assigns an observation  $\mathbf{y}_n$  either to a silhouette model point  $\mathbf{x}_m$  or to an outlier class. If  $(Z: \mathbf{y}_n \to \mathbf{x}_m)$  then the observation  $\mathbf{y}_n$  is associated to the point  $\mathbf{x}_m$ , otherwise, if  $(Z: \mathbf{y}_n \to \mathbf{x}_{M+1})$  then the observation  $\mathbf{y}_n$  is an outlier.

The likelihood is replaced by the expected complete-data log-likelihood  $\mathcal{E}$  conditioned by the observed data, as suggested by Dempster [24].

$$\mathcal{E}(\theta, \sigma_1, \dots, \sigma_S \mid \mathcal{Y}, Z) = E_Z[\log \mathcal{P}(\mathcal{Y}, Z; \theta, \sigma_1, \dots, \sigma_S) \mid \mathcal{Y}]$$
 (12)

To evaluate eq (12) the probabilities of the observations must be expressed as a set of Probability Density Functions (PDFs).  $p_m = \mathcal{P}(Z: \mathbf{y}_n \to \mathbf{x}_m)$  is the prior probability that the observation  $\mathbf{y}_n$  belongs to the cluster m with centre  $\mu(\mathbf{x}_m; \theta)$  while  $p_{M+1} = \mathcal{P}(Z: \mathbf{y}_n \to \mathbf{x}_{M+1})$  expresses the prior probability of  $\mathbf{y}_n$  to be an outlier.

$$p_m = \begin{cases} \mathcal{P}\left(Z : \mathbf{y}_n \to \mathbf{x}_m\right) = \frac{a}{A} & \text{if } 1 \le m \le M \\ \mathcal{P}\left(Z : \mathbf{y}_n \to \mathbf{x}_{M+1}\right) = \frac{A - Ma}{A} & \text{if } m = M + 1 \end{cases}$$
(13)

In eq (13) the variable a indicates a small circular area  $(a = \pi r^2)$  around the centre of the projected GMM  $\mu(\mathbf{x}_m, \theta)$ , whereas A indicates the whole volume of work, so that  $a \ll A$ . The likelihood of an observation  $\mathbf{y}_n$  given its assignment to cluster m is drawn from a normal distribution:

$$\mathcal{P}\left(\mathbf{y}_n \mid Z : \mathbf{y}_n \to \mathbf{x}_m\right) = \mathcal{N}(\mathbf{y}_n \mid \mu(\mathbf{x}_m; \theta), \sigma_m) = \frac{1}{\sigma_m \sqrt{2\pi}} e^{-\frac{||\mathbf{y}_n - \mathbf{x}_m||^2}{2\sigma_m^2}}$$
(14)

and the same likelihood of the observation given its assignment to the outlier class is a uniform distribution over the area  ${\cal A}$ 

$$\mathcal{P}\left(\mathbf{y}_n \mid Z : \mathbf{y}_n \to \mathbf{x}_{M+1}\right) = \mathcal{U}(\mathbf{y}_n \mid A, 0) = \frac{1}{A}$$
 (15)

The marginal distribution of an observation is:

$$\mathcal{P}(\mathbf{y}_n) = \sum_{m=1}^{M+1} p_m \mathcal{P}(\mathbf{y}_n \mid Z : \mathbf{y}_n \to \mathbf{x}_m)$$
 (16)

Eq (11) then becomes

$$\log \mathcal{P}(\mathcal{Y}) = \sum_{m=1}^{M} \log \left( \sum_{n=1}^{N} p_n \mathcal{N}(\mathbf{y}_m \mid \mu(\mathbf{x}_n; \theta), \sigma_n) + \frac{p_{n+1}}{A} \right)$$
(17)

and eq. (12) becomes

$$\mathcal{E}(\theta, \sigma_1, \dots, \sigma_S \mid \mathcal{Y}, \mathcal{Z}) = \sum_{\mathcal{Z}} \mathcal{P}(\mathcal{Z} \mid \mathcal{Y}, \theta, \sigma_1, \dots, \sigma_S) \log \mathcal{P}(\mathcal{Y}, \mathcal{Z}; \theta, \sigma_1, \dots, \sigma_S)$$
(18)

#### B.2 Expectation Maximization

The Expectation Conditional Maximization method is an iterative way to solve the Maximum Likelihood problem of eq (12). Starting from an initial estimate of the parameters, the method computes the posterior probabilities given the current parameters and covariances and then maximizes the expectation in (12) with respect to the registration parameters (given the current covariances) and the covariances (given the newly estimated parameters).

# B.2.1 Expectation step

The expectation step is defined as the computation of the posterior probabilities given the current estimate of the registration parameters and the covariance matrix. In this case, the posterior probability is computed between the contour points  $({}^{j}\mathbf{y}_{n})$  and the projection of the silhouette on the 2D images  $({}^{j}\mathbf{x}_{m})$ . Recovering the equations (13), (14), (15) and (16) and using the Bayes' rule the expression for the posterior probability becomes:

$$p_{mn}^{q} = \mathcal{P}\left(Z : \mathbf{y}_{n} \to \mathbf{x}_{m} \mid \mathbf{y}_{n}; \theta^{q}, \sigma^{q}\right) =$$

$$= \frac{\mathcal{P}\left(\mathbf{y}_{n} \mid Z : \mathbf{y}_{n} \to \mathbf{x}_{m}\right) \mathcal{P}\left(Z : \mathbf{y}_{n} \to \mathbf{x}_{m}\right)}{\mathcal{P}\left(\mathbf{y}_{n}\right)} =$$

$$= \frac{\sigma_{m}^{-2} e^{\frac{-||\mathbf{y}_{n} - \mathbf{x}_{m}||^{2}}{2\sigma_{m}^{2}}}}{\sum_{i=1}^{M} \sigma_{i}^{-2} e^{\frac{-||\mathbf{y}_{n} - \mathbf{x}_{i}||^{2}}{2\sigma_{i}^{2}}} + c}$$

$$(19)$$

with c that is the outlier component:

$$c = 2r^{-2} \tag{20}$$

#### B.2.2 Conditional Maximization step

The conditional maximization step aims at maximizing the likelihood described in eq. (11) and (12). It uses the definition of virtual observation, that is a normalized sum over all the observations weighted by their posterior probability [22]. The virtual observation O and its weight  $\lambda$  are obtained for each model point  $x_n$  using the posterior probabilities  $p_{mn}^q$  and the observations  $y_m$ :

$$\nu_n = \sum_{m=1}^{M} p_{mn}$$

$$\mathbf{o}_n = \frac{1}{\nu_n} \sum_{m=1}^{M} p_{mn} \mathbf{y}_m$$
(21)

Eq. (12) can be rewritten replacing the conditional probabilities with the normal and uniform distribution as expressed in eq (22) (for the complete steps the reader can refer to [22])

$$\mathcal{E} = -\frac{1}{2} \sum_{m=1}^{M} \sum_{n=1}^{N} \frac{p_{mn}}{\sigma_n^2} (||\mathbf{y}_m - \mu(\mathbf{X}_n, \theta)||^2 + \log(\sigma_n^2))$$
 (22)

The minimization of eq (22) over  $\theta$  keeping constant the covariances  $\sigma$  lead to:

$$\theta^{q+1} = \arg\min_{\theta} \frac{p_{mn}}{\sigma_n^2} ||\mathbf{y}_m - \mu(\mathbf{X}_n, \theta)||^2 + \frac{\rho}{2} ||L(\mu)||^2$$
 (23)

where  $||L(\mu)||^2$  is a regularization term over the parameters. Eq (23) can be simplified using the definitions of eq (21):

$$\theta^{q+1} = \arg\min_{\theta} \nu_n ||\mathbf{O}_n - \mu(\mathbf{X}_n, \theta)||^2 + \frac{\rho}{2} ||L(\mu)||^2$$
 (24)

where  $\mathbf{O}_n$  is the 3D point nearest to  $\mathbf{X}_n$  on the ray backprojected from  $\mathbf{o}_n$ . A 2D/3D registration problem is now cast into a 3D/3D registration that can be solved using already addressed solutions [22, 23, 28, 38].

The second step of the conditional maximization is the update of the covariances, using the registration parameters newly computed:

$$\sigma_n^2 = \frac{\sum_{m=1}^{M} p_{mn} ||\mathbf{y}_m - \mu(\mathbf{x}_n, \theta)||^2}{2\sum_{m=1}^{M} p_{mn}}$$
(25)

In eq (25) the value  $\mu(\mathbf{x}_n, \theta)$  is the projection of the 3D point  $\mathbf{X}_n$  updated with the parameters  $\theta$ .

# 7 Authors



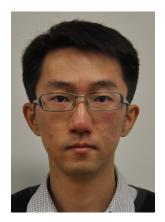
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