

# Torsional MEMS Magnetometer Operated off-Resonance for in-Plane Magnetic Field Detection

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## Abstract

The work presents a microelectromechanical system (MEMS) based magnetometer, targeting compass applications performance, which measures magnetic fields along an in-plane direction. The magnetometer is fabricated with the surface micromachining process used for consumer gyroscopes, accelerometers, and recently proposed out-of-plane magnetometers. The magnetometer is based on the Lorentz force principle, so to avoid the need for magnetic materials integration. It features an area of  $282 \times 1095 \mu\text{m}^2$ , and it is wafer-wafer packaged at a nominal pressure (0.35 mbar) similar to the one used for gyroscopes. In agreement with theoretical predictions, operation is demonstrated both at-resonance and off-resonance: in both situations the measured resolution, normalized to unit bandwidth and applied Lorentz current, is about  $120 \text{ nT}\cdot\text{mA}/\sqrt{\text{Hz}}$ , but the maximum sensing bandwidth is extended from 4 Hz (at resonance) to 42 Hz in off-resonance mode, which copes with consumer specifications. Within magnetic fields of  $\pm 5 \text{ mT}$ , the device shows measured linearity errors  $< 0.5\%$  of the full-scale-range (demonstrating a large linearity) and a cross-axis rejection of  $\sim 50 \text{ dB}$ . **The bias stability in off-resonance operation mode (80 nT·mA at 100 s) improves by a factor 100 with respect to resonance operation.**

*Keywords:* MEMS, magnetometers, inertial measurement units, digital compass

## 1. Introduction

The increasing interest towards multi-axis, multi-parameter measurement units [1], where different devices are integrated on the same die, drives the research on miniaturized magnetometers compatible with industrial MEMS processes. Magnetometers can be used to determine the absolute orientation, so for heading purposes, and to improve navigation capabilities when coupled to gyroscopes and accelerometers. Though some works propose the integration of magnetic thin layers on top of suspended MEMS structures [2], most of the literature about MEMS magnetometers rely on the Lorentz force principle, as this concept allows avoiding magnetic materials and the corresponding need for relatively low temperature during the fabrication steps (some magnetic materials begin losing their properties above about 300 °C). Early works [3] and several thereafter [4, 5, 6] mostly focused on Lorentz-force devices to measure out-of-plane magnetic fields. Few examples of in-plane (either differential or non-differential) MEMS magnetometers were also described in the literature [7, 8, 9, 10, 11, 12, 13]. The performances of all these devices, from a system point of view, are limited by a critical trade-off between resolution and bandwidth when operated at resonance: the former improves, the latter worsens with decreasing damping coefficients (obtainable e.g. by lowering the package pressure down to values compatible with high-quality-factor gyroscope operation). Among the strategies to overcome this limitation, a way to improve the resolution was proposed in [4]: the use of multiple loops for current re-circulation directly increases the sensitivity (and in turn the resolution) by the number of added loops. This technique is however not directly compatible with industrial surface micromachining, as it requires the deposition of metals on suspended springs. A second proposed strategy is the use of parametric amplification [14], where the device stiffness is modulated at twice the device resonance frequency. The intrinsic need for added circuitry to generate and control this added sine

30 wave implies added power consumption, and it is therefore not in the direction  
of low-power solutions. Another solution to extend the bandwidth is the use  
of frequency modulated (FM) operation [15]. Recently, off-resonance opera-  
tion was also proposed [16] as an effective alternative to solve the mentioned  
trade-off, still using an amplitude modulated (AM) approach.

This off-resonance technique is here applied to a novel single-axis, differen-  
35 tial, torsional magnetometer, sensitive to an in-plane direction of the magnetic  
field. The device preliminary characterization was presented in [17]. Capacitive  
sensing can be performed through differential parallel plates designed beneath  
the suspended, tilting mass. The device description is given in details in Sec-  
tion II. The structure geometry is designed in order to have a pronounced form  
40 factor, (i) to exploit long current paths, which directly determine the Lorentz  
force, and (ii) to cope with the possible integration of two of such devices in a  
single die together with 3-axis gyroscopes, 3-axis accelerometers, and the Z-axis  
magnetometer [16]. Fig. 1 is a possible arrangement of such devices in a 9-axis  
inertial measurement unit (IMU), which is derived from a typical floorplan of a  
45 6-axis unit: a single-mass, 3-axis gyroscope is designed (as a single drive stage  
saves power consumption), and the accelerometers are placed in a separate cav-  
ity to operate at a different pressure. The overall IMU area taken up by this  
solution may be smaller than in situations where a single 3-axis magnetometer  
is designed (see e.g. the implementation in [7]).

50 The device of this work is coupled to a custom readout electronic board and  
tested both at resonance and with driving frequencies slightly below resonance  
(according to [16]), under AC and DC varying magnetic fields. As expected,  
the overall analog sensitivity (output voltage per unit magnetic field change)  
decreases linearly with the frequency mismatch, according to the theory dis-  
cussed in Section III. With proper electronic filtering however (see Section IV),  
55 thermomechanical noise also decreases by the same amount, so that the resolu-  
tion per unit bandwidth and unit current consumption (as defined in [18]) does  
not worsen ( $\approx 120 \text{ nT} \cdot \text{mA}/\sqrt{\text{Hz}}$  is measured in both cases), as experimentally  
demonstrated in Section V. Long-term acquisitions (10 minutes) reveal a much

60 larger stability in off-resonance operation mode (about  $1.6 \mu\text{T}$  at  $50 \mu\text{A}$  drive  
current) than for resonant operation, thanks to the insensitivity to bias fluc-  
tuations.. Furthermore, the measured  $\pm 3$  dB bandwidth under AC magnetic  
fields, increases by a factor 10, from the quality-factor-limited value of 4 Hz at  
resonance to more than 40 Hz in off-resonance mode. Such a bandwidth value,  
65 together with the good linearity and cross-axis rejection measurements, make  
the device compatible with consumer-grade specifications.

## 2. Devices description and finite element model (FEM) simulation

A sketch of the device working principle with a detail captured at the scan-  
ning electron microscope (SEM) is shown in Fig. 2.

### 70 2.1. Process and mechanical design

The device is fabricated with the ThELMA (thick epitaxial layer for micro-  
actuators and accelerometers) technology from ST-Microelectronics, which con-  
sists of an epitaxial growth of a  $22\text{-}\mu\text{m}$ -thick layer of heavily doped polycrys-  
talline silicon that, once etching and release are performed, forms the suspended  
75 frame of the device. Suspension is obtained through suitable torsional springs.  
Beneath the suspended structure, and electrically isolated from the substrate  
through an oxide layer, a thin polysilicon layer is used as a bottom electrode  
for differential parallel-plate capacitive sensing ( $C_1$ ,  $C_2$ ). In order to minimize  
the Brownian noise, the device is packaged at a relatively low pressure (nomi-  
nally  $0.35$  mbar), through the use of getter materials and glassfrit bonding. The  
80 reader can find more details on the process e.g. in [19].

In details, the structure consists of four torsional springs sustaining a  $1095\mu\text{m}\cdot$   
 $282\mu\text{m}$  suspended plate, as represented in Fig. 2b. The springs are all designed  
along the rotational axis of the device, and their optimization considers both  
85 the mechanical and electrical aspects involved in the device working principle:  
on one side, they are designed with a relatively short length ( $51 \mu\text{m}$  each fold),  
to shift the in-plane translational mode to high frequencies; their layout width

(3.7  $\mu\text{m}$ ) is chosen in such a way that the total electrical resistance (seen by the current generator) is in the order of 1.4 k $\Omega$ . Two springs are indeed used  
90 as current inlets, and two are used as current outlets. In this way, by injecting a current through the springs, which then flows along opposite x-directions, in presence of an external magnetic field along the y-axis, a Lorentz forces pair arises, which determines a torque on the suspended plate along its longitudinal axis.

95 Suitable cuts in the geometry direct the injected current along the most lateral part of the frame, so to maximize the generated torque. If the lumped coefficient  $\alpha$  is defined to take into account the effectiveness of the applied force ( $\alpha = 1$  for a force applied at the plate lateral ends,  $\alpha = 0.5$  for a force evenly distributed on the plate area), from finite element (FE) electrical simulations such cuts allow  
100 to have an  $\alpha$  coefficient in the order of 0.8.

The device is designed in order to have the first mechanical mode (Fig. 3) at a nominal frequency of 20 kHz, just out of the acoustic bandwidth and above the typical vibration bandwidth, to avoid related disturbances (a very common approach also in other inertial sensors [20]). The motion is detected by  
105 the parallel-plate capacitors (Fig. 2c), with an area of  $7.9 \cdot 10^4 \mu\text{m}^2$ , suitably designed 2  $\mu\text{m}$  below the frame (the corresponding buried electrical interconnections can be seen in the SEM detail of Fig. 2a).

The first mode corresponds to a differential capacitance variation that is read-out by a suitable electronics. Parametric FE simulations were also performed  
110 to check the stability of the frequency against process nonuniformities. The relatively wide springs make the device well immune to typical over- or under-etching values. Apart from etching nonuniformities, the process height may vary as a result of a non perfect planarization. The results of the FE simulations indicate a relative variation in the first mode frequency of  $\pm 0.7 \%$  only, for a  
115 maximum relative thickness variation of  $\pm 4.6 \%$  ( $\pm 1 \mu\text{m}$  around a nominal height of 22  $\mu\text{m}$ ).

It is also important that high-order modes occur at frequencies much larger than the mode of interest, to help rejecting possible effects of in-plane or out-of-plane

accelerations. In the proposed design, the structure second mechanical mode is  
120 an in-plane translation which occurs at high frequency (about 78 kHz) thanks  
to the width of the designed springs, and ideally produces no variations in both  
the capacitors. The third mode (at about 92 kHz) is an out-of-plane mode that  
produces the same nominal capacitance variation on the two capacitors: it is  
therefore rejected by the electronics because it is seen as a common-mode signal.  
125 These high-order modes are shown in Fig. 4.

## 2.2. Capacitance variation per unit displacement

As the sensing capacitor is here not an ideal capacitor, but rather a perforated torsional plate, FE electrical simulations were performed to evaluate the variation of the sensing capacitance per unit displacement of the structure. The  
130 results will be later used to predict the overall device sensitivity (output voltage variation per unit magnetic field change) and compare it to experimental data. The simulation includes the relevant parameters for the capacitance calculation, like the nominal distance between the suspended plate and the readout electrodes (1.8  $\mu\text{m}$ ), the thickness of the oxide between the readout electrodes  
135 and the substrate (2.6  $\mu\text{m}$ ), and the distance between the package and the top face of the suspended mass (5  $\mu\text{m}$ ). The dielectric constant of the gas inside the package volume is reasonably assumed as that of vacuum.

The results are reported in Fig.5a, showing the absolute value of the two single-ended capacitances as a function of the maximum vertical displacement (i.e. of  
140 one lateral end of the plate). A deviation with respect to the best linear fitting is visible. However in differential mode (Fig.5b),  $C_1 - C_2$ , the linearity error is lower than 0.4% for displacements as large as 150 nm, with a fully differential sensitivity  $\frac{dC}{dZ} = 0.225 \text{ fF/nm}$ . Note that such displacement values are lower than the maximum displacement to which the structure is subject in the oper-  
145 ating conditions described in the following of this work.

Table 1 summarizes the design parameters of the torsional magnetometer [in-  
serire tabella].

### 3. Theory for off-resonance operation

Off-resonance or mode-split operation is defined as the operation of a sensor with an excitation force slightly below the resonance frequency. It is a well-known technique to extend the sensing bandwidth in gyroscopes, by designing on purpose the drive mode at a frequency below the sense mode [21]. It was first proposed for magnetometers in [18], using a frequency of the Lorentz current below the resonance frequency. The split between driving and resonance frequencies is meant to be much lower than the resonance frequency itself and at the same time much larger than the mechanical bandwidth, determined by the -3 dB width of the resonance peak.

In the case of the considered magnetometer, when a sinusoidal current  $i(t) = i_0 \cos(\omega \cdot t)$  is injected through the structure as described above, in presence of an external magnetic field  $B_{ext}$  along the shown direction, a pair of Lorentz forces arises, each with a modulus

$$F_L(t) = i(t) \cdot B_{ext} \cdot L \quad (1)$$

$$\frac{dF_L(t)}{dB_{ext}} = i(t) \cdot L \quad (2)$$

where  $L$  is the effective length of the current path. The current flows distributed in the outer part of the frame: assuming therefore the coefficient  $\alpha$  described in Section 2, and regardless of the operation mode of the device (either at or off-resonance), the displacement  $z(t)$  experimented by each of the plate lateral ends can be expressed as:

$$z(t) = \frac{Q_{eff}}{k} \cdot \alpha \cdot i(t) \cdot B_{ext} \cdot L \quad (3)$$

$$\frac{dz(t)}{dF_L(t)} = \frac{Q_{eff}}{k} \alpha \quad (4)$$

where  $k$  is the device stiffness (a small displacement approximation is used, so that  $k = 33 \text{ N/m}$  is here intended as the ratio between a DC or quasi-stationary

force applied at each plate lateral end, and its corresponding displacement).

$Q_{eff}$  represents the displacement amplification with respect to DC operation, and is a direct consequence of the equation describing the modulus of the maximum vertical displacement as a function of the force in the Fourier domain ( $\omega$  being the angular frequency and  $\omega_0 = 2 \cdot \pi \cdot f_0$ ):

$$\left| \frac{z(j\omega)}{F_L(j\omega)} \right| = \frac{1}{m} \frac{1}{\sqrt{\omega_0^4 + \omega^4 - 2\omega_0^2\omega^2 + \left(\frac{\omega_0\omega}{Q}\right)^2}} \quad (5)$$

For the device operated at the angular resonance frequency  $\omega_0$ ,  $Q_{eff}$  exactly corresponds to the quality factor  $Q$ , which depends on the damping coefficient  $b$  at the typical operating pressures. For the device operated off-resonance (e.g. by a split  $\Delta f$  in the order of 50-100 Hz below a resonance of 20 kHz),  $Q_{eff}$  represents an effective amplification factor.  $Q_{eff}$ , within a suitable range of mismatches  $\Delta f$ , is independent on the damping coefficient and only depends on  $f_0$  and  $\Delta f$ [18]:

$$Q_{eff} = \frac{\omega_0}{2\Delta\omega} = \frac{f_0}{2\Delta f} \quad (6)$$

For more details on off-resonance operation, the reader can refer to [18].

Assuming that the system is limited by the Brownian noise of the device, the expression of the intrinsic signal-to-noise ratio (SNR) and of the minimum measurable magnetic field per unit bandwidth and current consumption  $\sigma_B$  (e.g. in units of nT·mA/ $\sqrt{\text{Hz}}$ ) turns out to be identical for both the operation modes [16]:

$$SNR = \frac{i \cdot B \cdot L}{\sqrt{4 \cdot k_b \cdot T \cdot b \cdot BW}} \quad \sigma_B = \frac{B_{min} \cdot i_0}{\sqrt{BW}} = \frac{2}{L} \sqrt{k_b \cdot T \cdot b} \quad (7)$$

For the expressions above, the remarkable difference between resonance and off-resonance operation is in the meaning of the system bandwidth  $BW$ : for resonance operation,  $BW$  is limited by the narrow -3 dB mechanical bandwidth of the device  $BW_{mech} = f_0/(2Q) = b/(4\pi m)$ ; for off-resonance operation,  $BW$  represents an electronic filtering at a frequency typically chosen in the order of  $\Delta f$ . Therefore, for resonance operation, a trade-off between the minimum measurable field  $\sigma_B$  and the system bandwidth  $BW$  arises: it is e.g. possible



to improve  $\sigma_B$  decreasing the damping coefficient  $b$ , yet this determines an unavoidable reduction of the bandwidth. As both required noise and bandwidth are usually determined by the application (e.g. a few hundred nT and simultaneously at least a few tens Hz in the consumer field), the conclusion is that it is difficult to match the target specifications using AM resonance-operated Lorentz force magnetoemeters.

On the contrary, off-resonance operation allows the bandwidth to be independent on the damping coefficient: it is therefore possible to improve the resolution by decreasing  $b$ , without affecting the system bandwidth; or it is possible to keep the same resolution (the same damping coefficient) with an extended bandwidth.

As anticipated above, this discussion is valid if the system is limited by the MEMS thermomechanical noise. If we include the electronic noise  $\sigma_{eln}^2$  (in  $[V^2/Hz]$ ), Eq. (7) becomes:

$$\sigma_B = \frac{2}{L} \sqrt{k_b \cdot T \cdot b + \sigma_{eln}^2 \frac{k^2}{4 \cdot Q_{eff}^2 \cdot \frac{dC}{dz} \frac{dV}{dC}}} \quad (8)$$

where the electronic gain  $\frac{dV}{dC}$  is introduced in the next section. The equation clearly shows that a large  $Q_{eff}$  is advantageous to make the electronic noise negligible. Off-resonance operation therefore requires a lower noise readout electronics than resonant operation to effectively hold the same SNR.

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#### 4. Measurement setup

With the purpose of obtaining a low-noise readout, the front-end of this work is implemented using the circuit presented in Fig. 6, based on board-level charge amplifiers (Fig. 6), a lock-in amplifier that provides the reference current and performs the demodulation and a LabVIEW acquisition interface [16] (in the future perspective of a miniaturized system, the lock-in reference signal can be substituted by a signal generated by a MEMS resonator, and the demodulation can be performed with custom circuits).

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As explained in Section II, if the device is subject to a magnetic field that has  
225 a component in the sensing direction, a Lorentz-force pair arises, causing a dif-  
ferential capacitance variation between the tilting mass and the sensing plates  
on the substrate. The two sensing plates are held at a fixed potential (6 V)  
thanks to the virtual ground of the two charge amplifier stages to which they  
are directly connected. These charge amplifiers, implemented through *AD8065*  
230 operational amplifiers,  $C_F = 0.6$  pF feedback capacitances and  $R_F = 600$  M $\Omega$   
feedback resistances, are used to convert the current flowing out of the MEMS  
stators to voltage signals at their outputs. These signals (nominally with the  
same amplitude and a relative phase shift of  $\pi$ ) are further amplified through  
an instrumentation amplifier (*INA 129*), in order to reject any common mode  
235 component. At this output there is a sinusoidal signal, whose amplitude is pro-  
portional to the external magnetic field. In order to obtain a DC voltage at the  
end of the readout chain, a demodulation is performed with a lock-in ampli-  
fier, with a low-pass bandwidth that can be selected according to the needs of  
the specific measurement. Regarding the electronic noise of the whole readout  
240 chain, it turns out to be limited by the thermal noise of the feedback resistances  
( $R_F$ ) of the charge amplifier stages.

For the generation of the driving current through the magnetometer, a bal-  
anced, differential Howland current pump circuit is used, as shown in Fig. 6,  
which converts the sinusoidal voltage coming from the lock-in amplifier into a  
245 sinusoidal current signal, which is injected into the sensor.

Apart from the useful signal, an offset contribution arises at the output, likely  
due to simultaneous resistivity unbalance of the current paths, and a mechanical  
offset at rest for the suspended mass. The offset origin is currently under deeper  
investigation. Though the driving circuit is set in order to minimize this offset,  
250 a residual contribution in the order of 1 mT is observed (both at resonance and  
off-resonance) and compensated through a post-acquisition subtraction (hard-  
ware offset compensation techniques were discussed in [22]). The stability of  
this offset will be analyzed in the next subsection.

The board with the magnetometer is mounted within a three-axial Helmholtz-

255 coils magnetic field generator, that is capable, through suitable LabVIEW interfaces, to generate arbitrary-shape fields, with a maximum frequency of  $\sim 200$  Hz and a maximum intensity of 5 mT.

The described electronics gives an overall capacitive sensitive gain described by the equation below:

$$\frac{dV_{out}(t)}{dC(t)} = \frac{V_{bias}}{C_F} * G_{INA} * G_{LIA} = 2.9V/fF \quad (9)$$

260 where  $V_{bias} = 6$  V is the biasing voltage of the stators, and  $G_{INA} * G_{LIA}$  is the product of the Instrumentation Amplifier and Lock-in Amplifier gains. It is now possible to put together equations (2), (4), (8) and the results of FE simulations of Section 2b to derive the theoretical expression of the sensitivity in both operation modes:

$$S = \frac{dV_{out}}{dC} \cdot \frac{dC}{dZ} \cdot \frac{dz}{dF_L} \cdot \frac{dF_L}{dB_{ext}} \quad (10)$$

265 which turn out to be  $S_{res} = 1.15$  V/mT and  $S_{mis,50Hz} = 0.09$  V/mT at a driving current of 50  $\mu$ A and assuming  $\alpha = 1$ . The sensitivity difference in the two operation modes is still given by the 12.5-fold ratio between the quality factor  $Q$  and the effective quality factor  $Q_{eff}$  when operating 50 Hz off-resonance.

## 270 5. Experimental results

### 5.1. Sensitivity and linearity

In order to characterize the device and to validate the proposed theory, a sensitivity analysis is first performed by injecting the current at the measured resonance frequency  $f_0 = 19953$  Hz, and generating a quasi-static ramp of magnetic fields from -5 mT to +5 mT, consecutively along the three Cartesian axes. The measured output voltage values at the end of the acquisition chain are shown in Fig. 7. A sensitivity of 0.85 V/mT is obtained for the sensitive axis, which is compatible with a full-scale range of a few mT at reasonably low voltages. This value matches the predictions made at the end of Section IV,

280 provided that the coefficient  $\alpha$  is assumed to be  $\approx 0.75$ . Cross-axis rejection ratios of  $\sim 47$  dB and  $\sim 50$  dB are obtained for the other two axes (likely limited by unavoidable manual alignment errors), confirming the goodness of the mechanical design to reject cross-axis effects, as discussed in Section 2.

Starting from the sensitivity measurement, a linearity analysis is also performed  
285 by comparing the acquired voltage values with their best linear fitting. In Fig. 7 it is shown the very good linearity of the device, that turns out to be lower than  $\approx 0.5\%$ , up to magnetic fields comparable with the target full-scale of consumer applications (a few mT). Note that the maximum vertical displacement at 5 mT,  $50 \mu\text{A}$ ,  $Q \approx 2500$  is in the order of 20 nm only. The linearity results are  
290 therefore in agreement with the simulation predictions of Section 2.

The device is then operated off-resonance by changing the frequency of the drive signal: further sensitivity measurements are performed for several values of the frequency split, as shown in Fig. 8. The theory according to which the sensitivity is inversely proportional to the frequency split (see Eq. 6 above) is thus  
295 validated. As the ratio between the sensitivities in different operation modes is equal to the  $Q_{eff}$  ratio, it is also possible to extract the value of the quality factor of the device at resonance, that results to be approximately 2500, theoretically indicating a -3 dB mechanical bandwidth of 4 Hz for the device. This value is an intrinsic limit to the system BW for resonance operation.

300 For off-resonance operation, at a mismatch of 50 Hz, a sensitivity of 0.068 V/mT is obtained, which is again in agreement with the predictions of Section 4 using the same coefficient  $\alpha$  considered for resonant operation.

### 5.2. Noise and long-term stability

305 A noise analysis is then performed, by holding the device inside a zero-gauss-chamber and by varying the demodulation frequency from around resonance to  $\sim 500$  Hz of mismatch, with a very narrow lock-in low-pass-filter (LPF) bandwidth. Fig. 9a shows the measured results, where one can note that at frequency mismatches higher than  $\approx 100$  Hz the noise becomes significantly limited by the

310 electronics: this is the point after which, increasing the frequency split, the SNR  
begins to worsen with respect to resonance operation. As shown in Fig. 9b, in-  
deed, the minimum measurable magnetic field per unit current and bandwidth  
is the same both for resonance and for off-resonance operation up to  $\sim 50$  Hz  
of frequency mismatch. The measured value of  $\approx 120$  nT·mA/ $\sqrt{\text{Hz}}$  begins to  
315 worsen only when the electronics noise starts to overcome the intrinsic MEMS  
thermomechanical noise.

The long-term stability of the output, which is inherently related to the offset  
stability, is then measured in both operation modes through the Allan vari-  
ance method, this time out of the zero-gauss chamber. In this case, the lock-in  
320 bandwidth is set to 53 Hz. The 50  $\mu\text{A}$  driving current is kept on during the  
measurements. Fig.10a reports the output signal captured consecutively for 10  
minutes in three different operating conditions: (i) resonance operation with a  
control of the stators bias voltage of 300 ppm; (ii) resonance operation with a  
control of the stators bias voltage better than 100 ppm; (iii) off-resonance oper-  
325 ation with a control of the stators bias voltage of 300 ppm. In the first situation,  
a drift is clearly visible as a consequence of the small changes in the resonance,  
caused by the variable biasing voltage, and the corresponding frequency tuning.  
In the second situation, the results are slightly better, confirming the voltage  
variation to be responsible of the observed drifts. Finally, in the third situa-  
330 tion, no visible drift appears even under poor stability of the biasing voltage,  
confirming the off-resonance operation immunity to small variations in the re-  
sonance frequency. Fig.10b reports the same data, now elaborated in terms of  
Allan variance, indicating a white noise of  $\approx 220$  nT·mA/ $\sqrt{\text{Hz}}$  (slightly deteri-  
orated with respect to the situation inside the zero-gauss chamber, likely due  
335 to real magnetic field disturbance) and a stability of about 1.6  $\mu\text{T}$  at 100 s  
observation times, 50  $\mu\text{A}$  of driving current (i.e. 80 nT·mA). On the contrary,  
for resonance operation, (i) the effect of the narrow bandwidth is clearly visible  
at small observation times, and (ii) huge drifts occur after a few s of observation.

340 *5.3. Bandwidth*

Finally a bandwidth analysis is performed, generating sinusoidal magnetic fields at increasing AC frequencies and measuring the corresponding output sine wave amplitude: a 3 dB bandwidth of about 4 Hz is obtained for resonance operation, in perfect agreement with the value estimated above. Operating the device with a frequency split  $\Delta f = 50$  Hz, with a lock-in 2-pole low pass filtering of 50 Hz, a  $\pm 3$  dB bandwidth of 42 Hz is obtained, as shown in Fig. 11. The data are normalized to the DC value of the response in resonant mode. The small increase (still within  $\approx \pm 4$ dB) of the response appearing in off-resonance mode is due to the MEMS transfer function peak, which occurs 50 Hz from the resonance frequency in the selected mode-split operation.

### Conclusion

The work demonstrated a more than 10x bandwidth extension technique applied to Lorentz-force MEMS magnetometers for in-plane field detection. Such an improvement is obtained by exploiting off-resonance operation, and does not imply any loss in terms of minimum measurable field performance. With excellent linearity and cross-axis rejection performance, the magnetometer is compatible with consumer-grade specifications. Further, thanks to the much better immunity to small changes of the resonance frequency, which may be induced by poor stability of the biasing voltages or by temperature changes, off-resonance operation demonstrates a 100-fold better long-term stability at 100 s observation time.

The future perspectives include the combination of three magnetometers to sense all the fields directions, together with the development of suitable tunable resonators to provide the reference frequency for off-resonance operation within the same MEMS package.

The development of a suitable driving and readout ASIC to implement an autonomous magnetic field sensing system represents ongoing work. To be competitive with other technologies, an overall power consumption of less than 0.5

mW per axis is required. Assuming a voltage in the order of 1.7 V, the overall  
370 current consumption of  $294 \mu A_{rms}$  can be in a first approximation equally split  
between the device and the ASIC. This results in  $210 \mu A$  peak current available  
for the design of a low-noise ASIC.

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Table 1: Device parameters

<i>Parameter</i>	<i>Value</i>
Vertical gap at rest ( $z_0$ )	1.8 $\mu\text{m}$
Thickness ( $h$ )	22 $\mu\text{m}$
Linear stiffness ( $k$ )	33 N/m
Effective mass ( $m$ )	2.1 nkg
Resonance frequency ( $f_0$ )	19.95 kHz
Nominal package pressure ( $p$ )	0.35 mbar
Quality factor ( $Q$ )	2500
Electrical resistance ( $R$ )	1.405 k $\Omega$

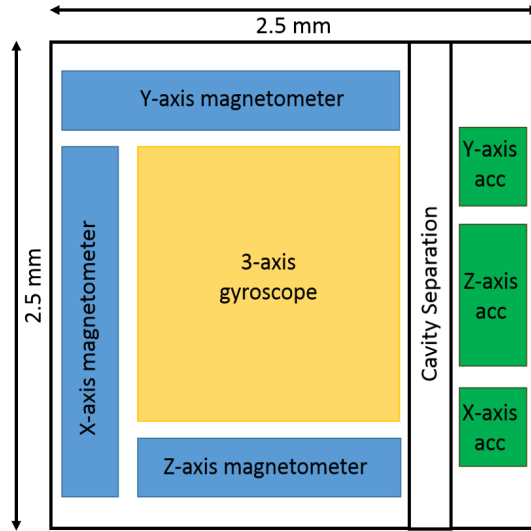


Figure 1: Schematic concept of an inertial measurement unit (IMU) integrating three single-axis accelerometers, a 3-axis gyroscope and three single-axis magnetometers. The implementation of the gyroscope as a highly symmetric monolithic 3-axis device is guided by power consumption and quadrature error issues. The magnetometers well fit on the gyroscope sides.

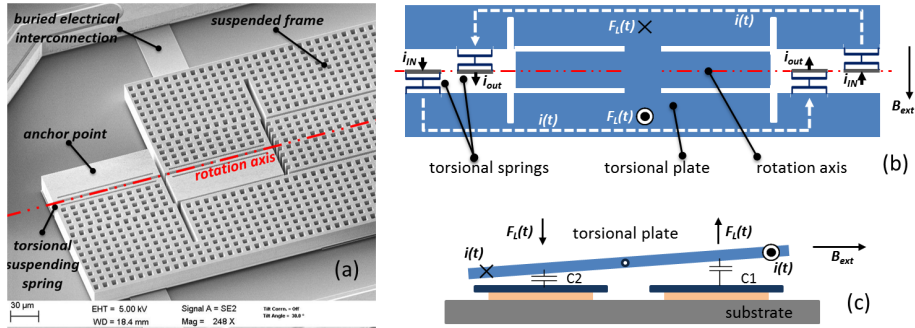


Figure 2: (a) scanning electron microscope (SEM) picture of the device proposed in this work, showing details of the torsional springs and the rotation axis. The operating principle is schematized by the top view (b) and the cross-section (c).

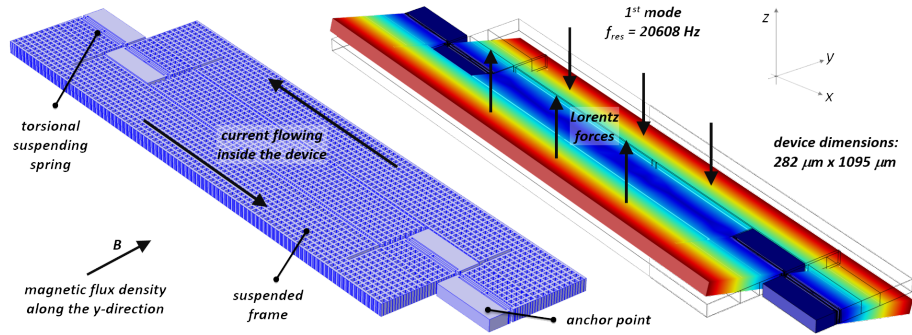


Figure 3: Device geometry and first resonant mode: the current, flowing as indicated by the arrows, causes a Lorentz torque in event of magnetic fields along the y-axis. The corresponding displacement is read by differential parallel plates designed beneath the seismic mass (not shown in the figure).

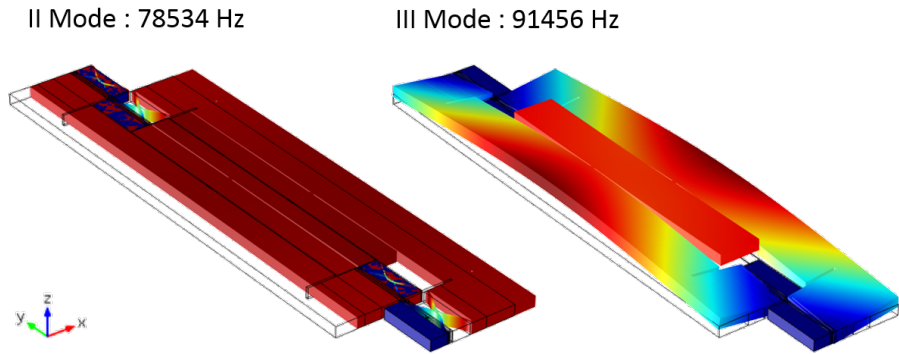


Figure 4: Second and third mechanical modes of the structure: ideally they produce no effect and a common mode effect (respectively) on the differential capacitance variation.

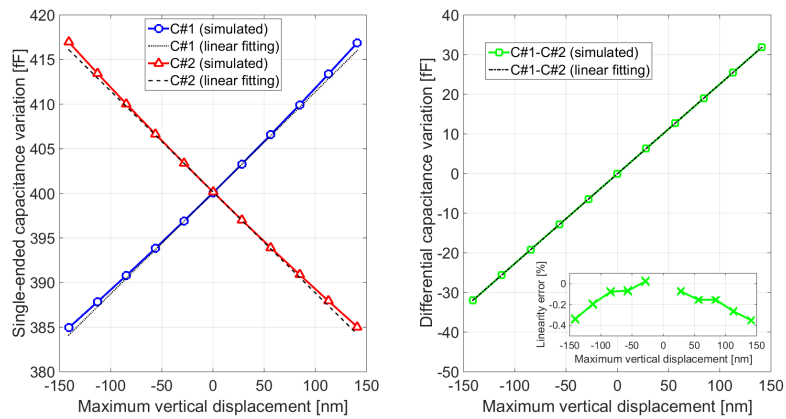


Figure 5: (a) results of FE simulations for the single-ended capacitance variation of the torsional magnetometer, and (b) results in terms of differential capacitance change (b). The inset shows the linearity error in the latter condition.

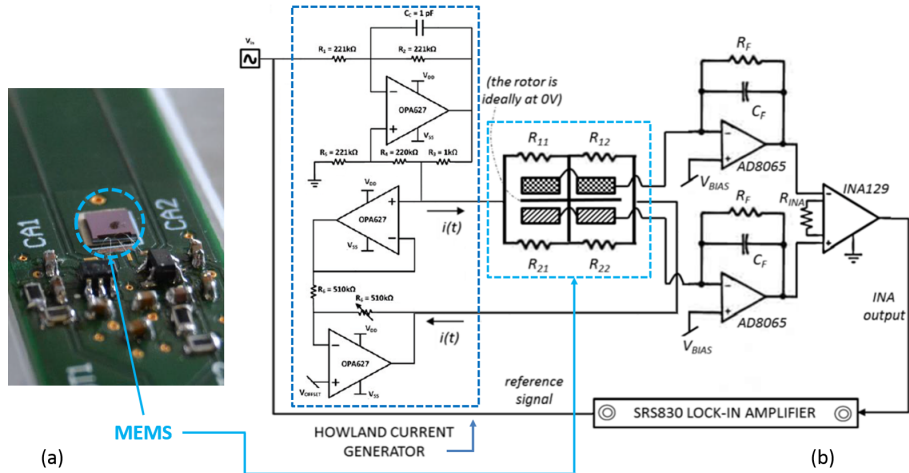


Figure 6: (a) Optical picture showing the MEMS package glued onto the printed circuit board, and the front-end of the readout electronics with the charge amplifiers; (b) complete schematic of the circuit used for the readout, where the Howland current generator, the charge amplifiers, the INA stage and the Lock-In amplifier can be identified.

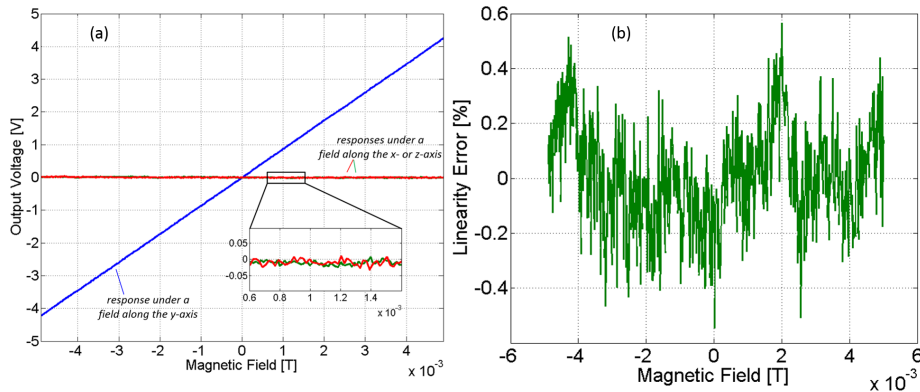


Figure 7: (a) Output voltage as a function of the magnetic field, applied subsequently along the three axes while the device is driven with a current at the resonance frequency; (b) linearity error between measured sensitivity and its best linear fitting demonstrates the very good linearity of the device.

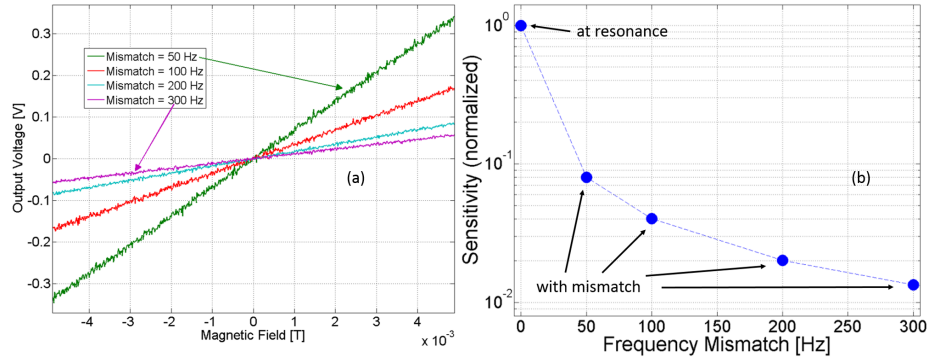


Figure 8: (a) Output voltage as a function of the magnetic field, for a current injected off-resonance for different frequency mismatches; (b) the resulting sensitivity goes linearly with the inverse of the mismatch, as predicted by the theory developed in Section III.

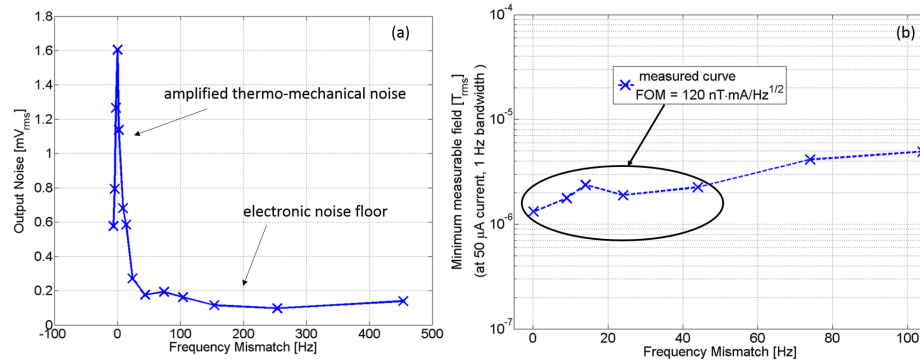


Figure 9: (a) Measured output noise as a function of the frequency mismatch. The thermo-mechanical contribution, amplified by the quality factor, is clearly visible at resonance. For large mismatches the noise floor is due to the electronics; (b) minimum measurable field per unit bandwidth and current consumption, from resonance to off-resonance operation: the value is almost constant up to mismatches of about 50 Hz.

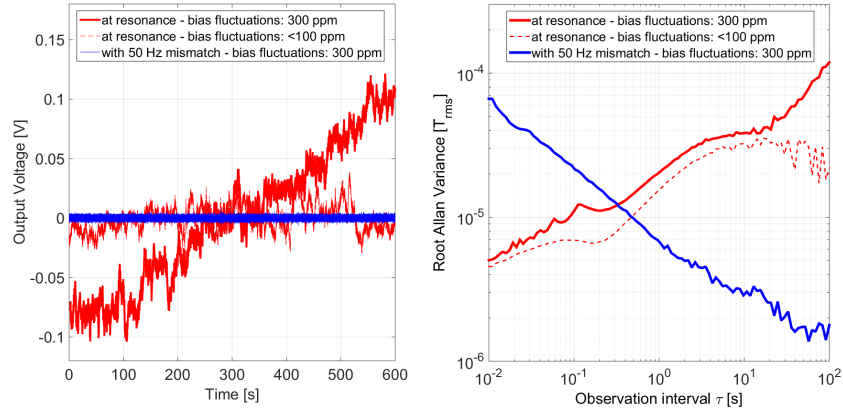


Figure 10: (a) measured output voltage vs time in different conditions of stator bias voltage stability in resonance mode, and in off-resonance operation; (b) Allan variance plots derived from the acquisition in (a).

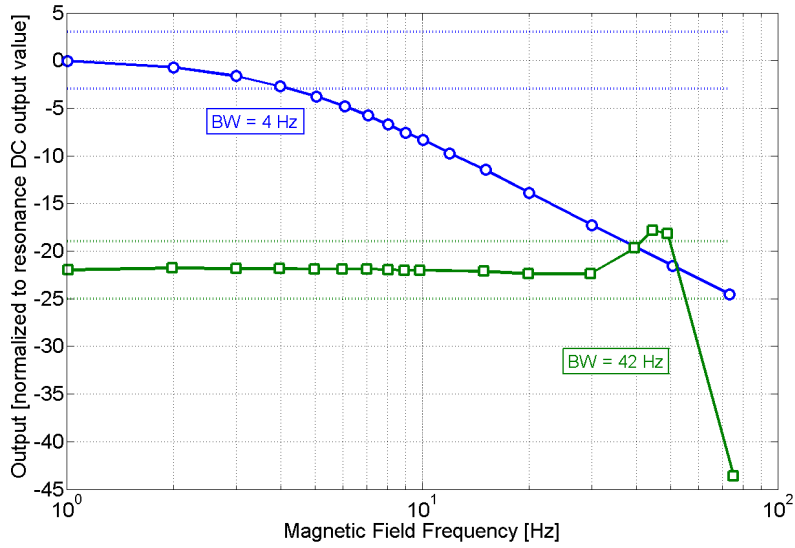


Figure 11: Sensing bandwidth measured under AC fields for resonance and off-resonance operation. The obtained bandwidth extension in off-resonance mode is larger than a factor of 10. The sensitivity-bandwidth trade-off is visible.