Fatigue properties of a pseudoelastic NiTi alloy: Strain ratcheting and hysteresis under cyclic tensile loading

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1. Introduction

NiTi shape memory alloy has become, in the last years, increasingly important in different applications field, as a consequence of their peculiar properties [1], shape memory, pseudoelasticity, corrosion resistance—thus making it favorable to realize biomedical implants, dentistry, aerospace, engineering and sports equipment. However, due to the solid phase transformation mechanisms, involving this special alloy, unusual fracture and fatigue response has to be expected, therefore standard testing procedures to identify its fatigue and fracture response cannot be applied. Fatigue loads cause a big modification of the global response of NiTi alloys, due not only to the mechanical damage imposed by the cyclic load, but, especially, to the functional evolution related to the phase transition mechanisms.

As a consequence of these peculiar properties, both structural and functional fatigue behavior of NiTi alloys is still unknown. To this aim, starting from Melton’s pioneering work [2], some experimental studies were carried out in the last few years to analyze the fatigue behavior of NiTi alloys, by using non-standard specimens and testing procedures [3,4]. In particular, in most of these works the cyclic behavior of NiTi wires [5–16], subjected to rotating bending conditions were analyzed, and in one of them [12] an unusual behavior (“z-shape” response), in terms of applied strain-number of cycles to failure, is reported. Furthermore, NiTi tubes [17–23] were analyzed, in terms of both crack propagation rate and fatigue life estimation. In fact, stress induced phase transition mechanisms occurs in the crack tip region [24–27], which significantly affects the stress distribution and, consequently, the local values of the stress intensity factor [28,29]. Moreover, in order to better investigate the fatigue properties of such components, diamond-shaped samples were studied [30], with geometry very close to the unit cell of a stent. Furthermore, other studies [31,32] were carried out on single crystal specimens, cut along different crystallographic orientations, in order to investigate the functional behavior of NiTi alloys. In particular, fatigue resistance and functional evolution, for different orientations, were investigated in [31], while the influence of different heat treatments and of precipitates, were studied in [32]. In addition, the evolution of damping properties and the seismic damping capabilities of pseudoelastic SMAs was analyzed in [33,34], while the modification of the shape memory properties of thin wire for actuators was analyzed in [35,36].

Within this context, a low cycle fatigue study of a pseudoelastic NiTi sheet in the stress-induced transformation regime was undertaken. Each test was carried out in two subsequent steps: (i) material stabilization and (ii) fatigue life estimation. In the first step, to avoid compression stresses during unloading, a variable strain...
ratio was adopted until the mechanical stabilization of the alloy. Subsequently, the stabilized specimens were subjected to strain controlled fatigue tests, under a fixed strain ratio, up to complete failure. In this paper, based on experimental tests carried out in a previous study [37], where investigations on the structural fatigue properties of the alloy were carried out (second step), the stress–strain response was accurately monitored in the first step, in order to analyze the evolution of the functional properties of the alloy in terms of pseudoelastic recovery capabilities. In particular, this evolution was systematically analyzed by identifying several functional damage parameters, involving strain, energy, transformation stress, Young’s modulus and phase transition temperatures.

Results on functional fatigue, in terms of pseudoelastic evolution response, and on structural fatigue, in terms of cycles to failure, are here reported and discussed.

2. Materials and experimental methods

A commercial pseudoelastic Ni-rich NiTi sheet (50.8 at.% Ni–49.2 at.% Ti, Memry, Germany) with thickness \( t = 1.5 \text{ mm} \), was analyzed. Dog bone shaped specimens, with gauge length of 10 mm, were cut from as received sheets by wire electro discharge machining. A polishing of the machined surfaces was subsequently carried out by sandpapers with progressively finer grits (#400–#1200) and finally by diamond paste (5 \( \mu \text{m} \)).

Fig. 1a illustrates stress–strain curve of the as received material obtained from an isothermal (\( T = 298 \text{ K} \)) loading–unloading cycle, with a strain rate \( \dot{\varepsilon} = 2.5 \times 10^{-2} \text{ s}^{-1} \), up to complete stress-induced martensitic transformation corresponding to a maximum strain of about 6.2%. Deformations were measured by means of an extensometer with a gauge length of 10 mm. The figure also shows the values of the main thermo-mechanical parameters of the alloy, in terms of Young's moduli \( (E_A,E_M) \), transformation stresses \( (\sigma_M^{\text{EM}}, \sigma_M^{\text{AM}}, \sigma_M^{\text{LM}}, \sigma_M^{\text{LM}}) \), and transformation strain \( (\varepsilon_t) \). Fig. 1b illustrates a Differential Scanning Calorimetry (DSC) curve of the as received material which was performed over a temperature range between –100°C and 100°C using a heating/cooling rate of 10°C/min (DSC Seiko 220C). The graph clearly shows a two-stage direct transformation from high temperature parent phase (\( R2 \)) to rhombohedral phase (\( R \)) to low temperature stable phase (\( B19 \)). In contrast, a one-stage inverse transformation \( B19 \rightarrow R2 \) characterizes the heating branch of the curve. This is a typical curve of NiTi after aging, indeed the formation of \( Ti_Ni_4 \) precipitates are responsible of the change of the transformation path from \( B2 \rightarrow B19 \) to \( B2 \rightarrow R \rightarrow B19 \) [1].

Fatigue tests were carried out, under isothermal condition \( (T = 298 \text{ K}) \) by using a universal servo-hydraulic testing machine (Instron 8500) equipped with a climatic chamber (MTS 651).

Due to the cyclic creep-like behavior of NiTi alloys, which causes the accumulation of residual deformations in the first mechanical cycles \( (\delta_{\text{res}}) \), as illustrated in Fig. 2, fatigue tests were carried out in two subsequent steps, as described in [37]: (1) Material stabilization and (2) Fatigue life estimation. In particular, in the first step a variable strain ratio was adopted, in order to avoid compression stresses during unloading, and the strain ratcheting mechanisms were analyzed up to a stable mechanical response of the alloy, corresponding to \( N_0 \) cycles. The transition evolution was monitored during the first few \( N_i \) cycles in order to investigate on the loss functional capability of the alloy. The number of cycles to stabilization, \( N_0 \), was defined based on the evolution of residual deformations, in particular when the increment of \( \varepsilon_{\text{res}} \) in the previous 10 cycles is lower than 0.005 \( \varepsilon_{\max} \) (at: \( \sum_{N_i=N_0}^{N_0+10} \delta_{\text{res}} \leq 0.005 \cdot \varepsilon_{\max} \)).

In the second step, the specimens were subjected to strain controlled fatigue cycles at a frequency of 0.5 Hz, under a fixed strain ratio and with a strain range \( \varepsilon = 2 \varepsilon_{\max} \), were carried out up to complete failure and the corresponding number of cycles \( N_f \) has been recorded.

Several tests were carried out for different values of the maximum strain, \( \varepsilon_{\max} \), within the pseudoelastic regime of the alloy, i.e. in the range between 0.7% and 4.5% and at least two specimen for each testing conditions were analyzed.

3. Results and discussions

In the following sections the evolution on the functional properties of the alloy mainly occurring in the first step of fatigue tests are illustrated. In addition, structural fatigue data, in terms of number of cycles to failure versus applied strain, are reported and analyzed by a modified Coffin–Manson approach [37], together SEM analysis of the fracture surfaces.

3.1. Functional fatigue

The modification of the hysteretic stress–strain response of the material obtained under repeated isothermal mechanical cycles involving stress induced transformations can be attributed to several microstructural mechanisms, such as the formation of stabilized martensite, detwinning, grain reorientation, slips deformations and the generation of lattice defects mainly in the form of
dislocations [38,39]. In particular, upon repeated loadings, many preferentially oriented martensite variants reach stress conditions that inhibit the possibility to recover their original configuration, and the dislocation density tends to increase, as a consequence of shear deformations at the martensite-austenite interfaces. These microstructural evolutions cause a gradual loss of functional properties, i.e. the capability to dissipate energy and to recover the applied deformation, with a consequent increase of residual strain and the dislocation density tends to increase, as a consequence of the plastic deformation related to the martensitic transformation and the mechanical loading. Moreover, lattice defects may lead to martensite stabilization [40–43]. Nevertheless, the material reaches a pseudoelastic steady state condition with increasing the number of cycles. These phenomena are more evident for the higher values of applied deformation by which an higher evolution rate has been registered; on the contrary the number of cycles to stabilization $N_s$, which is always between 100 and 140, seems to be unaffected by the strain amplitude. Similar results have been obtained in previous researches [20,23] even in the case of single crystal alloys [32]. It is a unusual behavior if compared with common metals, where the stabilization of the stress–strain response of the material, due to repeated plastic deformations, is related to the cycles to failure and, consequently, to the strain amplitude [44]. In addition, Fig. 4a and Table 1 also show that pseudoelastic strain recovery capabilities of the SMA are mainly preserved, with stabilized values of $\epsilon_{\text{rec}}$ ranging from 72% to 97% of $\epsilon_{\text{max}}$, at $\epsilon_{\text{max}}= 4.5\%$ and 0.7% respectively.

Fig. 5 reports the stabilized values of $\epsilon_{\text{rec}}$ and $\epsilon_{\text{res}}$ as a function of the maximum applied strain, $\epsilon_{\text{max}}$, in a log–log diagram and a linear trend of both parameters is observed. In particular, $\epsilon_{\text{rec}}$ ranges from about 0.01% at $\epsilon_{\text{max}} = 0.70$–1.30% at $\epsilon_{\text{max}} = 4.50\%$ and, as a consequence, $\epsilon_{\text{rec}}$ ranges from about 0.69% to about 3.20%. Complete are reported in Table 1.

### 3.1.2. Recovered and dissipated energy

As described in the previous sections and schematically depicted in Fig. 3, repeated mechanical cycles cause a modification of the whole stress–strain hysteretic behavior of the alloy, i.e. they affect not only the pseudoelastic strain recovery capability but also the shape of the stress–strain hysteretic loop. As a consequence, a marked modification of the recovered and dissipated energy, $E_{\text{rec}}$ and $E_{\text{diss}}$ (see Fig. 3), has been observed and the knowledge of this trend is of major concern, especially when dealing with the design of energy absorber devices, such as seismic absorbers [33]. Fig. 6 reports the evolution of $E_{\text{rec}}$ (Fig. 6a) and $E_{\text{diss}}$ (Fig. 6b) as a function of the number of mechanical cycles and for different values of the maximum strain, $\epsilon_{\text{max}}$.
residual deformations (see Fig. 4b), and this effect becomes more evident as $\epsilon_{\text{max}}$ increases. However, a higher reduction rate of the dissipated energy has been observed, which can be attributed to plastic deformation and to an increase of dislocation density. Dislocations may lead to the formation of stress fields into the lattice and then to the formation of stabilized martensite induced by stress [40–43]. In fact, $E_{\text{dis}}$ is strictly related to the hysteresis in the stress-induced phase transition mechanisms. In particular, Fig. 6b and Table 1 show that stabilized values of $E_{\text{dis}}$ are between 30% and 40% of the values of the first cycles for $\epsilon_{\text{max}} > 1.30\%$, while even more marked reductions are observed for the lower values of $\epsilon_{\text{max}}$, because these latter are very close to the elastic limit of the material ($\sigma_{\text{AM}}^{0.04}$) and, consequently, the hysteretic behavior tends to vanish. This trend should be accurately taken into account in the design of energy absorbers and seismic devices operating under low cycle regime, as it implies a marked degradation of their functional response. Alternatively, proper training processes of the material should be carried out in order to obtain a stable functional response.

Fig. 7 reports the stabilized values of $E_{\text{rec}}$ and $E_{\text{dis}}$ as a function of the maximum applied strain, $\epsilon_{\text{max}}$, in a semi-log diagram. The figure show that $E_{\text{rec}}$ increases from about 1.22 MJ/m$^3$ at $\epsilon_{\text{max}} = 0.7\%$ to 7.64 MJ/m$^3$ at $\epsilon_{\text{max}} = 4.5\%$, while $E_{\text{dis}}$ ranges from about 0.03 MJ/m$^3$ to about 2.38 MJ/m$^3$. Complete data for the other values of maximum strain are reported in Table 1.

### Table 1

<table>
<thead>
<tr>
<th>Cycle #</th>
<th>$\epsilon_{\text{rec}}$ (%)</th>
<th>$\epsilon_{\text{dis}}$ (%)</th>
<th>$E_{\text{rec}}$ (MJ/m$^3$)</th>
<th>$E_{\text{dis}}$ (MJ/m$^3$)</th>
<th>$E_r$ (GPa)</th>
<th>$\sigma_{\text{AM}}^{0.04}$ (MPa)</th>
</tr>
</thead>
<tbody>
<tr>
<td>#1</td>
<td>Cycle #1</td>
<td>Cycle #1</td>
<td>Cycle #1</td>
<td>Cycle #1</td>
<td>Cycle #1</td>
<td>Cycle #1</td>
</tr>
<tr>
<td>0.70%</td>
<td>0.01</td>
<td>0.02</td>
<td>0.69</td>
<td>0.68</td>
<td>0.45</td>
<td>0.03</td>
</tr>
<tr>
<td>1.00%</td>
<td>0.01</td>
<td>0.04</td>
<td>0.99</td>
<td>0.96</td>
<td>0.80</td>
<td>0.09</td>
</tr>
<tr>
<td>1.30%</td>
<td>0.01</td>
<td>0.06</td>
<td>1.29</td>
<td>1.24</td>
<td>1.15</td>
<td>0.23</td>
</tr>
<tr>
<td>1.45%</td>
<td>0.01</td>
<td>0.09</td>
<td>1.44</td>
<td>1.36</td>
<td>1.40</td>
<td>0.42</td>
</tr>
<tr>
<td>1.70%</td>
<td>0.02</td>
<td>0.14</td>
<td>1.68</td>
<td>1.56</td>
<td>1.72</td>
<td>0.60</td>
</tr>
<tr>
<td>2.00%</td>
<td>0.03</td>
<td>0.16</td>
<td>1.97</td>
<td>1.84</td>
<td>2.10</td>
<td>0.81</td>
</tr>
<tr>
<td>2.40%</td>
<td>0.06</td>
<td>0.29</td>
<td>2.33</td>
<td>2.11</td>
<td>2.66</td>
<td>1.02</td>
</tr>
<tr>
<td>3.00%</td>
<td>0.07</td>
<td>0.59</td>
<td>2.92</td>
<td>2.41</td>
<td>3.29</td>
<td>1.21</td>
</tr>
<tr>
<td>3.50%</td>
<td>0.08</td>
<td>0.84</td>
<td>3.42</td>
<td>2.66</td>
<td>4.89</td>
<td>1.42</td>
</tr>
<tr>
<td>4.00%</td>
<td>0.16</td>
<td>0.95</td>
<td>3.83</td>
<td>3.05</td>
<td>5.87</td>
<td>1.81</td>
</tr>
<tr>
<td>4.50%</td>
<td>0.20</td>
<td>1.24</td>
<td>4.30</td>
<td>3.26</td>
<td>7.37</td>
<td>2.33</td>
</tr>
</tbody>
</table>

3.1.4. Transformation temperatures

Calorimetry tests were carried out on samples subjected to mechanical cycling. The DSC thermograms revealed to be similar to that of as received material (see Fig. 1b). In particular, a two-stage transformation is observed during cooling ($B2$-$B19'$), while a one-stage transformation ($B19'$-$B2$) characterizes the heating branch of the curve. The results, in terms of peak temperatures, are summarized in Fig. 9. Increasing the maximum strain ($\epsilon_{\text{max}}$), the $B19'$ peak shifts toward lower temperature (from $-67\,^\circ\text{C}$ to $-60\,^\circ\text{C}$), while the effect of $\epsilon_{\text{max}}$ on the other two peaks temperatures is less pronounced. The irreversible plastic strain induced on the specimens by deformation and by transformation cycling promotes the stabilization of the R-martensite. Indeed, likewise Ti$_3$Ni$_4$ precipitates, higher density of dislocations acts as a resistance to lattice distortion due to the transformation from austenite to martensite, and the resistance is much more significant for transformation involving large lattice distortion like $B19'$ transformation, while the effect becomes less considerable for transformation involving small lattice distortion like R-transformation [1]. Therefore, the introduction of dislocations by fatigue cycles leads to a decrease of the $R$-$B19'$ characteristic temperatures. It is worth to note that mechanical cycling and formation of lattice defects are also likely responsible for the stabilization of martensite regions [40–43]. Deeper structural investigations are needed for an utter understanding of the microstructural alterations owing to mechanical cycling which lead to a resulting modification of the functional and mechanical properties characteristic of the material.

3.2. Structural fatigue

In the following subsection fatigue data are analyzed by a modified Coffin–Manson approach [37]. Furthermore, scanning electron microscopic observations of the fracture surface are reported and analyzed to better understand the failure mode under different values of the applied strain.
3.2.1. Modified Coffin–Manson approach

A summary description of the modified Coffin Manson approach, which was proposed by the authors [37], is reported in the following for the sake of completeness. The strain amplitude, $\varepsilon_a = \varepsilon / 2$ (see Fig. 2), can be decomposed in the elastic strain amplitude, $\varepsilon_{ae} = \varepsilon_e / 2$, and inelastic strain, $\varepsilon_{ai} = \varepsilon_i / 2$, which can be regarded as the pseudoelastic recovery:

$$\varepsilon_a = \varepsilon_{ae} + \varepsilon_{ai}$$

where the elastic strain is calculated based on the assumption of linear evolution of the martensite fraction, $\xi_{M}$, along the stress–strain transformation plateau and on the use of the Reuss’s formula to estimate the Young’s modulus, $E(\xi_{M})$ (see Refs. [45, 46]):

$$\Delta \varepsilon_e = \frac{\sigma}{E(\xi_{M})}$$

Fig. 10 illustrates the elastic, inelastic and total strain amplitude ($\varepsilon_{ae}, \varepsilon_{ai}$ and $\varepsilon_a$) as a function of the number of cycle reversals to failure ($2N_f$) in a log–log diagram.
Furthermore, the figure shows that both elastic and inelastic strain amplitude (\(e_{ae}\) and \(e_{ai}\)) are well approximated by straight lines in the log–log diagram and, consequently, the two strain components can be expressed by a power law relations in the \(e_{a}/C_{0}^{2}N_{f}\) diagram, likewise to Coffin–Manson approach in common engineering metals. In particular, the total strain amplitude, \(e_{a}\), can be related to the cycle reversals to failure, \(2N_{f}\), based on a modified Coffin–Manson approach:

\[
e_{a} = e_{ae} + e_{ai} = C(2N_{f})^{c} + D(2N_{f})^{d}
\]

where the coefficients \(C\) and \(D\) and the exponents \(c\) and \(d\) obtained from the experiments are reported in Fig. 10. It is worth noting that these values have been obtained from a fitting of the experimental data, i.e. they are related to specific specimen geometry and loading conditions and, consequently, they should be considered as testing parameters. However, the transferability of the proposed model to the engineering community, i.e. to predict fatigue life under generic loading conditions, requires further systematic experimental tests. Furthermore, the results presented in this paper have been obtained with maximum deformation within the stress-induced transformation regime and, consequently, the fatigue response of the material

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**Fig. 7.** Stabilized values of the recovery and dissipated energies, \(E_{rec}\) and \(E_{diss}\), as a function of the maximum applied strain \(e_{max}\).

**Fig. 8.** Evolution of Young’s modulus, \(E\) (a) and of the direct transformation stress, \(\sigma_{AM}^{d}\), (b) as a function of the number of mechanical cycles and for different values of the maximum applied strain \(e_{max}\).

**Fig. 9.** Evolution of the peak transformation temperatures \((R_{p}, M_{p}\) and \(A_{p}\)) versus the maximum applied strain \(e_{max}\).

**Fig. 10.** Fatigue data analysis by the modified Coffin–Manson approach [37].
in the full austenitic and martensitic regions has not been investigated.

3.2.2. SEM analyses of the fracture surfaces

In Fig. 11, SEM micrographs of the fracture surfaces obtained by testing the samples at different values of maximum deformation (a. 0.7%, b. 1.3%, c. 1.45%, d. 1.7%) are reported. The analysis revealed that crack initiation occurs at the lateral surface of the specimens, as a consequence of the surface defects produced by the cutting process. In fact, these irregularities lead to local stress concentrations and act as preferable nucleation sites. Furthermore, fracture surfaces show two distinct regions characterized by different morphologies. In particular, the right part of the surfaces in the SEM micrographs of Fig. 11 are characterized by fatigue striations, which are attributed to the stable crack growth resulting from fatigue loads, while the left sides show dimples structures typical of ductile overload fractures. In addition, as expected, the stable crack penetration area decreases with increasing of the maximum applied deformation, ranging from about 2.8 mm at $\varepsilon_{\text{max}} = 0.7\%$ to 0.8 mm at $\varepsilon_{\text{max}} = 1.7\%$.

4. Conclusion

Strain controlled fatigue tests of a commercial pseudoelastic NiTi alloy were carried out within the stress-induced transformation regime. Both functional and structural fatigue were analyzed,
i.e. the evolution of the pseudoelastic capability and the cycles to failure. The results revealed a degradation of the pseudoelastic recovery, during the first mechanical cycles, and this effect becomes more evident when increasing the strain amplitude. However, a stable functional response is always observed after the first stabilization cycles, which occurs between 100 and 150 cycles. Furthermore, structural fatigue data have been analyzed by a novel strain-life model, based on a modified Coffin–Manson approach. Finally, fracture surfaces have been analyzed by SEM observation in order to study the stable and unstable crack growth mechanisms. However, future experimental tests should be carried out to validate the model and, consequently, to allow a direct transferability of the fatigue data to the engineering community.

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References