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# THEMIS: Tracking the health of the environment and missions in space

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6<sup>th</sup> European Space Debris modelling and Remediation workshop, Milano, 18-20 May 2022

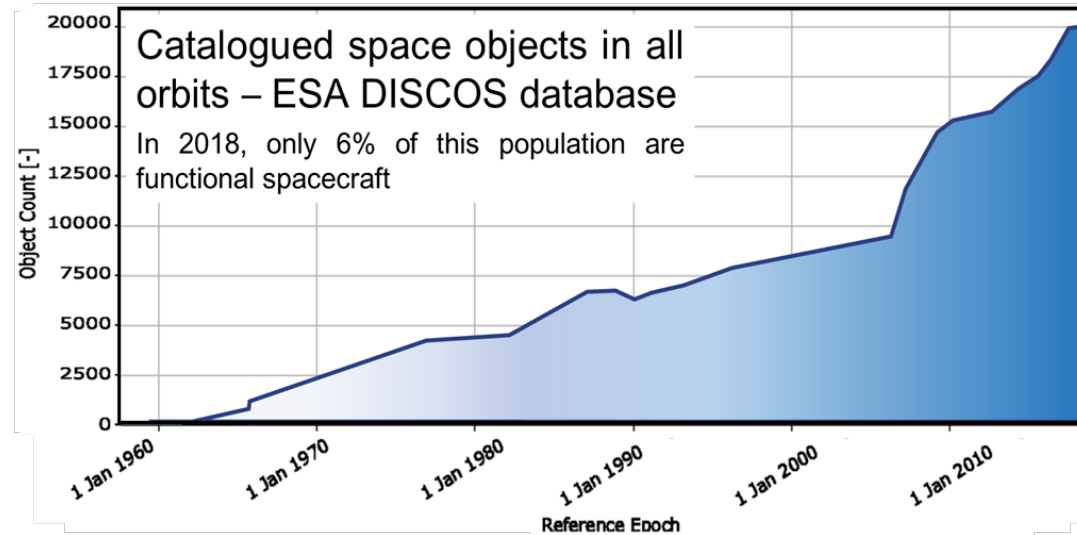


Apollo mission 2019. Simulation COMPASS Virtual Reality game. Actual space debris orbits, artistic representation of objects

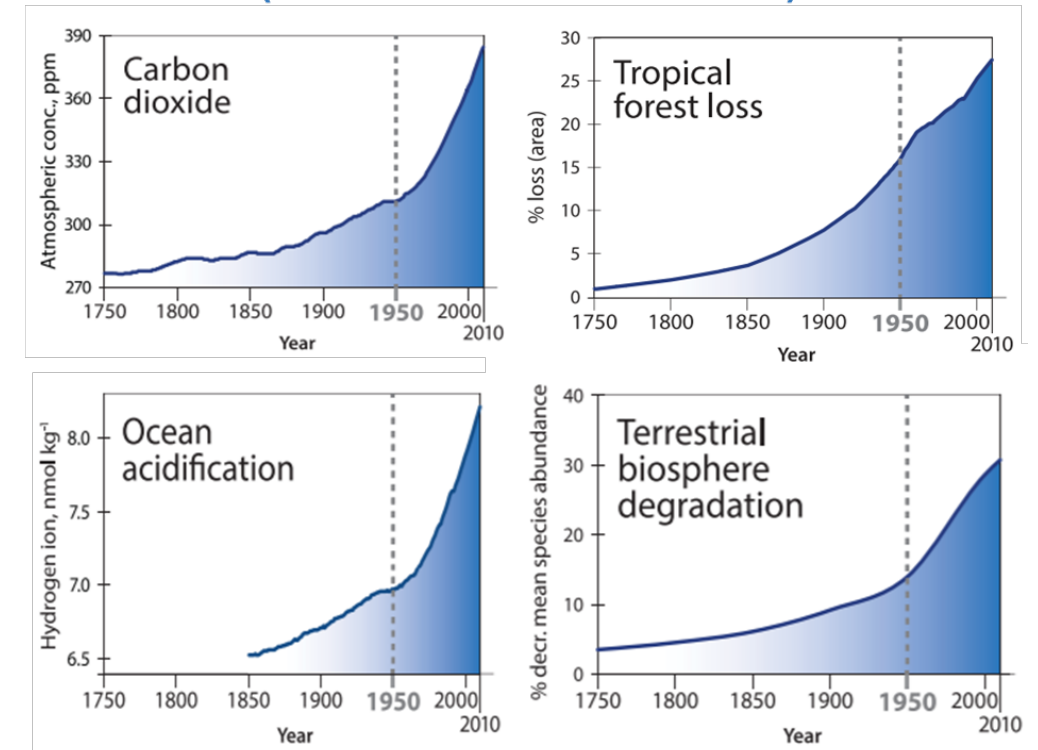


## Space debris like other environmental issues

### Orbital environment trend (space debris growth)



### Earth system trends (environmental stressors)



- Maury T., Loubet P., Trisolini M., Gallice A., Sonnemann G., Colombo C., "Assessing the impact of space debris on orbital resource in Life Cycle Assessment: a proposed method and case study", *Science of the Total Environment*, 2019. Earth system trend original image by Steffen, W., Broadgate, W., Deutsch, L., Gaffney, O., & Ludwig, C. (2015). The trajectory of the anthropocene: The great acceleration. *Anthropocene Review*, 2(1), 81–98. <https://doi.org/10.1177/2053019614564785>

## Goals and novelties

### Goals:

- To assess the **impact of a space mission on the space environment**
- To assess the **overall Space capacity** and the contribution of each mission to it

### Scientific development:

- A statistical **density-based approach** used for propagating explosion and collision fragments
- Definition and extension of **space debris index to all orbital regions**, including LEO, GEO, MEO, GTO, HEO
- Analysis of possible **capacity proxy** and **capacity threshold**

### Software development:

- Integration with **existing ESA tools** such as DISCOS, MASTER, DRAMA, OSCAR
- Single score output of the environmental analysis in the **ESA database DISCOS** for reporting analyses and for integration into a life cycle assessment procedure
- Develop a **web-based interface** for the submission and evaluation of the space by several users

# THEMIS SOFTWARE TOOL

## Tracking the Health of the Environment and Missions In Space

### Space debris mode

- to allow different users to assess the impact of a space mission on the space debris environment based on mission information such as orbit, mass, cross-section, and risk of fragmentation due to accidental collisions or break-up
- to determine the share of the capacity of space used by that mission under analysis

### Space capacity mode

- to allow the computation of the overall space capacity used by orbiting spacecraft
- to analyse possible definitions and proxy of the capacity threshold

## Software design

### THEMIS frontend

Interface for external users:

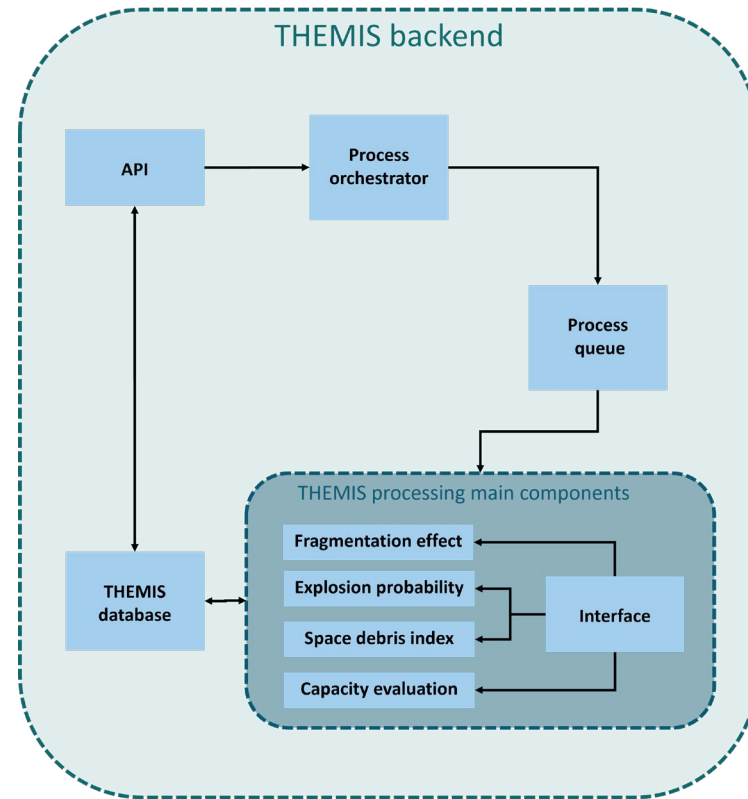
- to analyse missions and their impact
- to have an overview of the overall status of the space environment
- for registered users to submit user-defined mission for evaluation of its environmental impact both in terms of index and capacity consumption
- for operators to declare new missions profiles

### THEMIS backend

- Computation of the environmental index:
  - Create and propagate a mission profile
  - Compute the collision probability
  - Compute the explosion probability
  - Determine the collision effect
  - Determine the explosion effects
  - Interface with ESA tools
- Computation of the space capacity:
  - Long-term propagation using ESA DELTA
  - Compute the available capacity of the space environment

# THEMIS software design

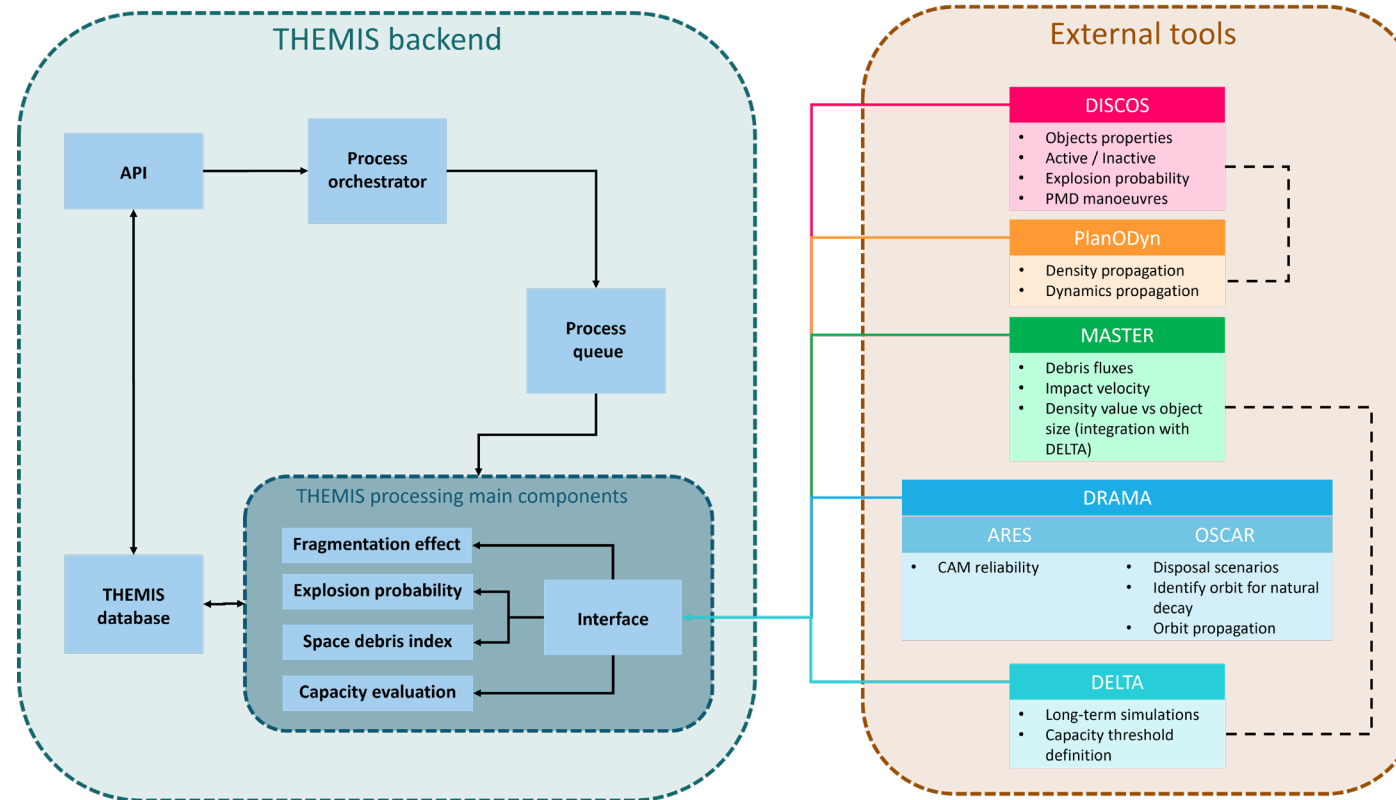
## Overall software design and flow





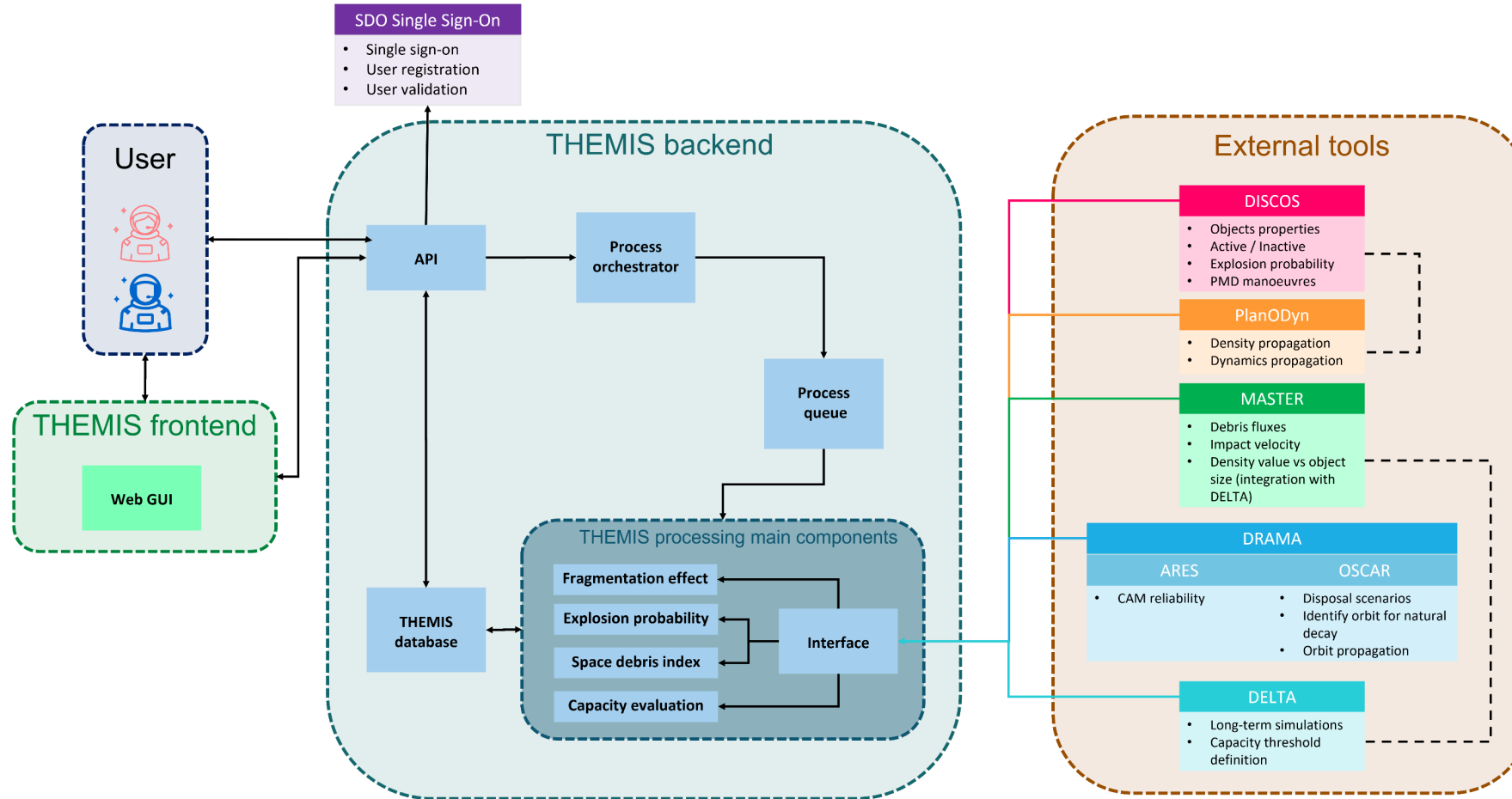
# THEMIS software design

## Overall software design and flow

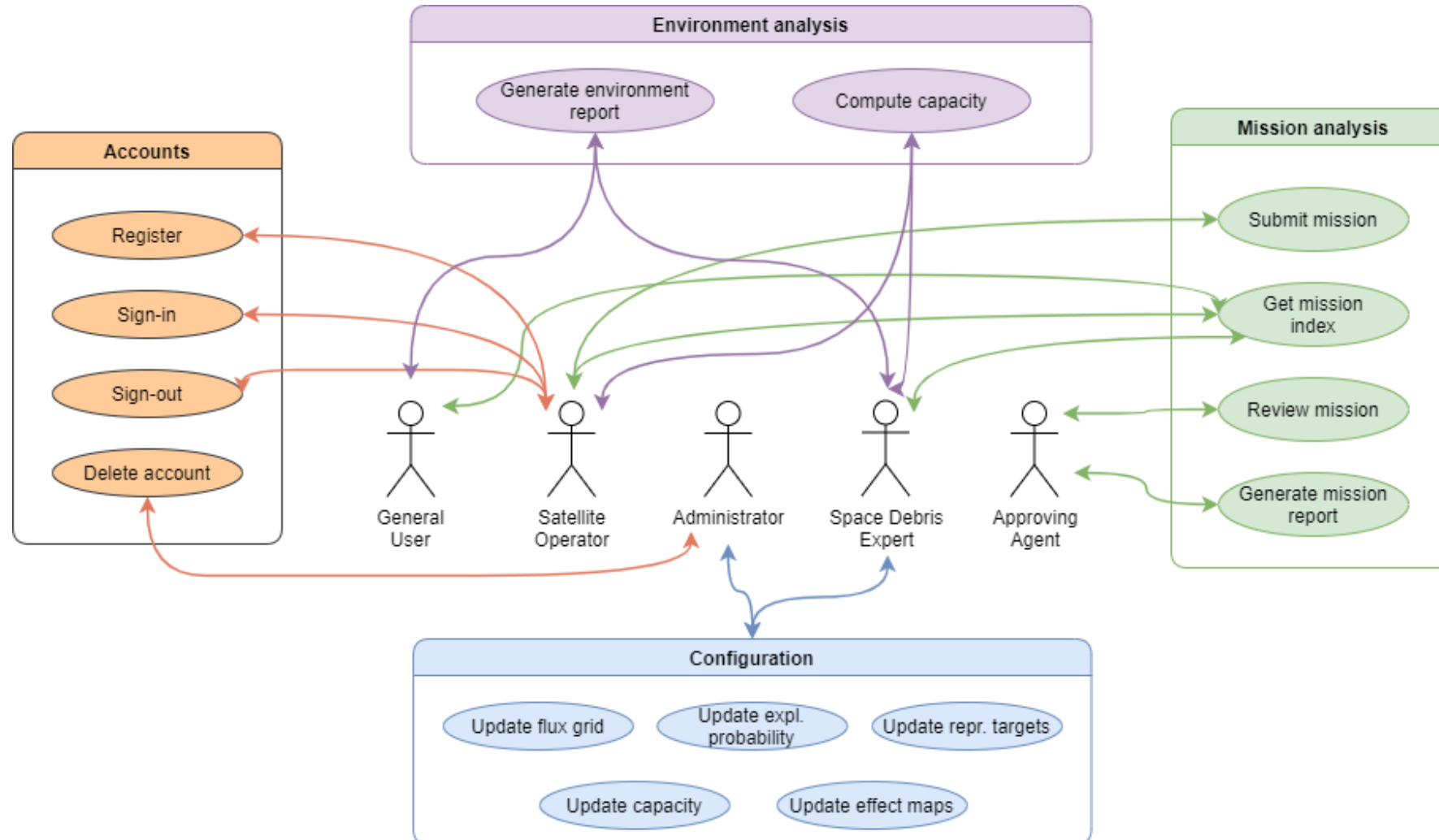


# THEMIS software design

## Overall software design and flow



## Basic functional analysis of the system subdivided by sections



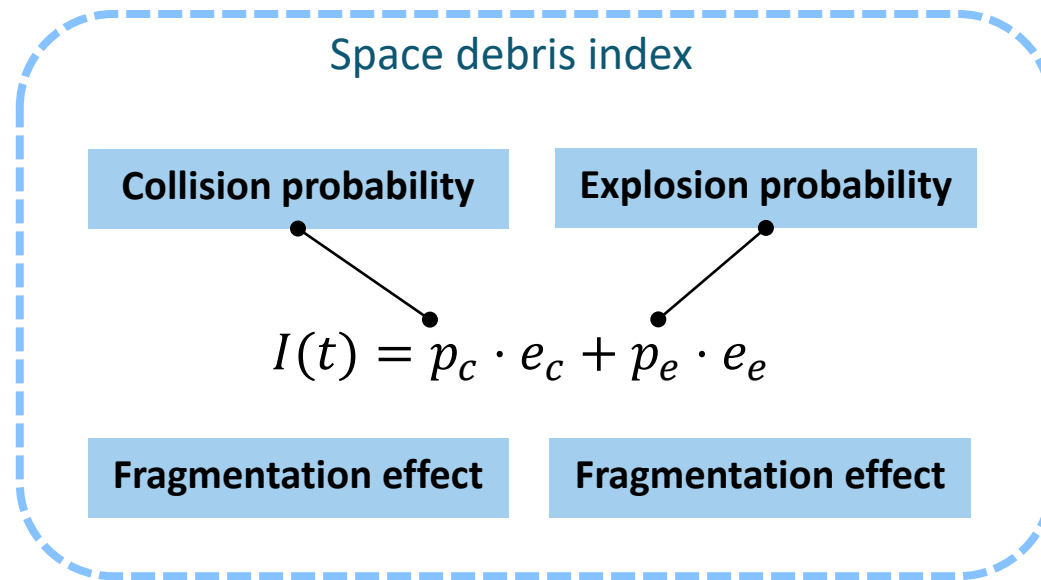
# SPACE DEBRIS INDEX

# Space debris index

## Index formulation

- ECOB formulation index to assess the **risk = probability x severity**

$p$  = probability  
 $e$  = effects (severity)

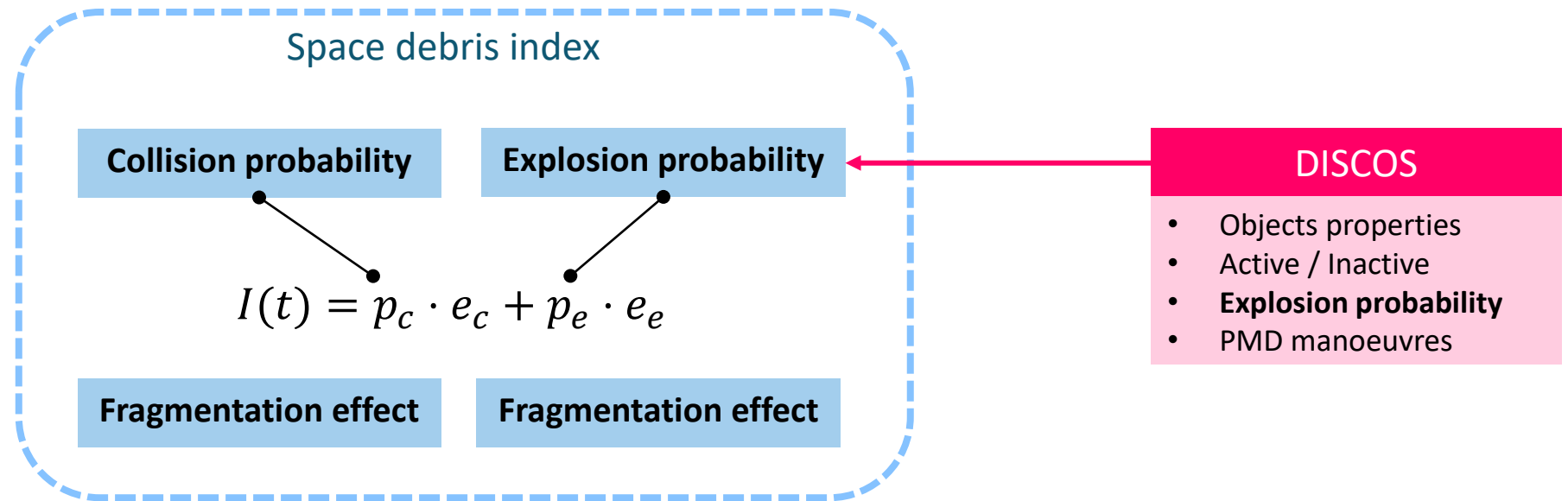


➤ Letizia, F., Colombo, C., Lewis, H. G., & Krag, H. (2016). Assessment of breakup severity on operational satellites. *Advances in Space Research*, 58(7), 1255-1274.



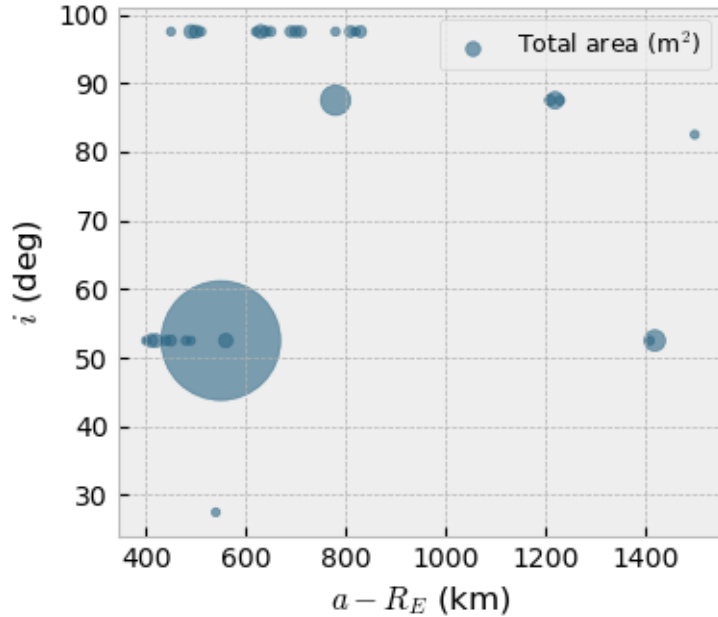
# Space debris index

## Explosion probability

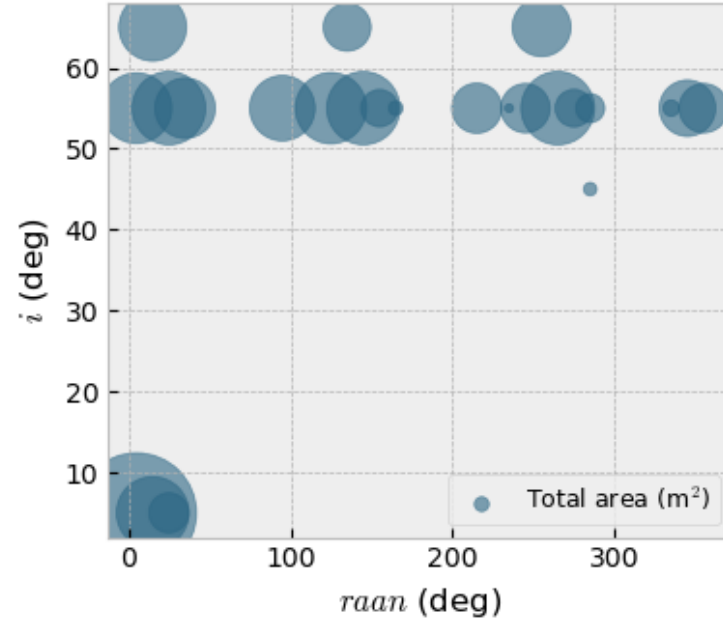


# Space debris index

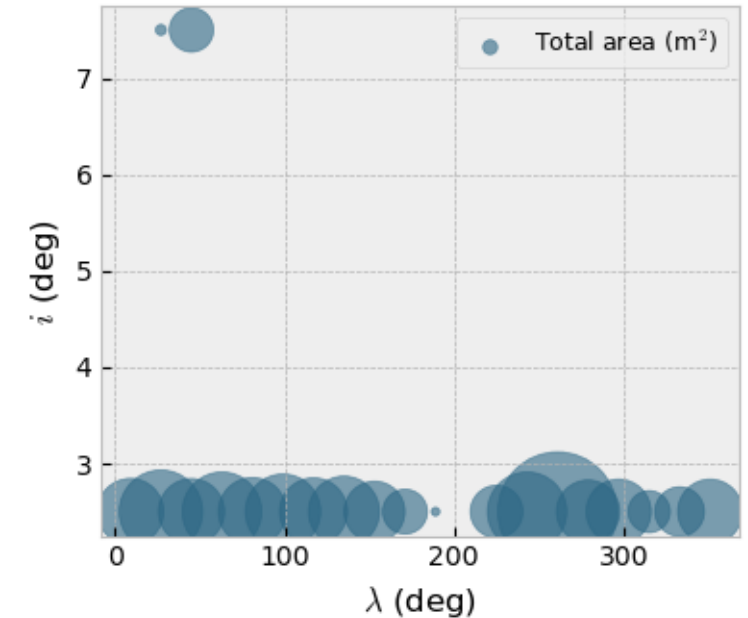
## Representative targets



LEO region representative targets in a semi-major axis and inclination grid



MEO region representative targets in a right ascension of ascending node and inclination grid



GEO region representative targets in a longitude and inclination grid

# Space debris index

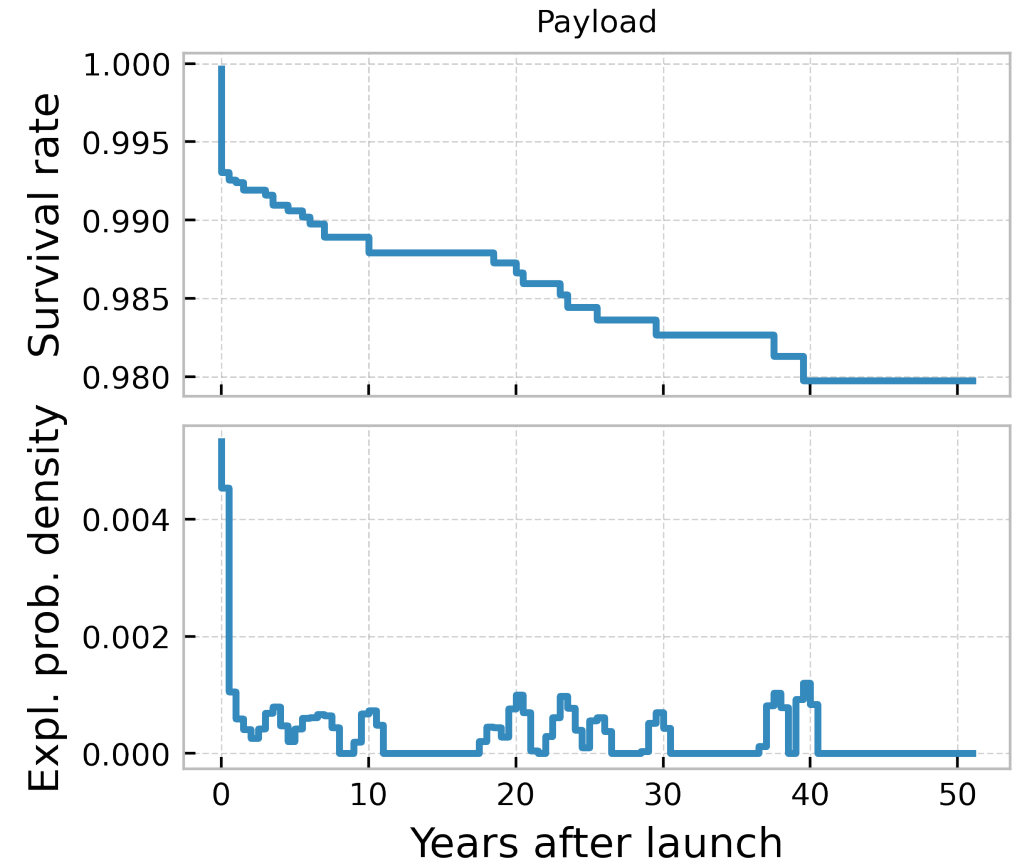
## Explosion probability

**Survival rate** evaluated using the **Kaplan-Meyer** estimator

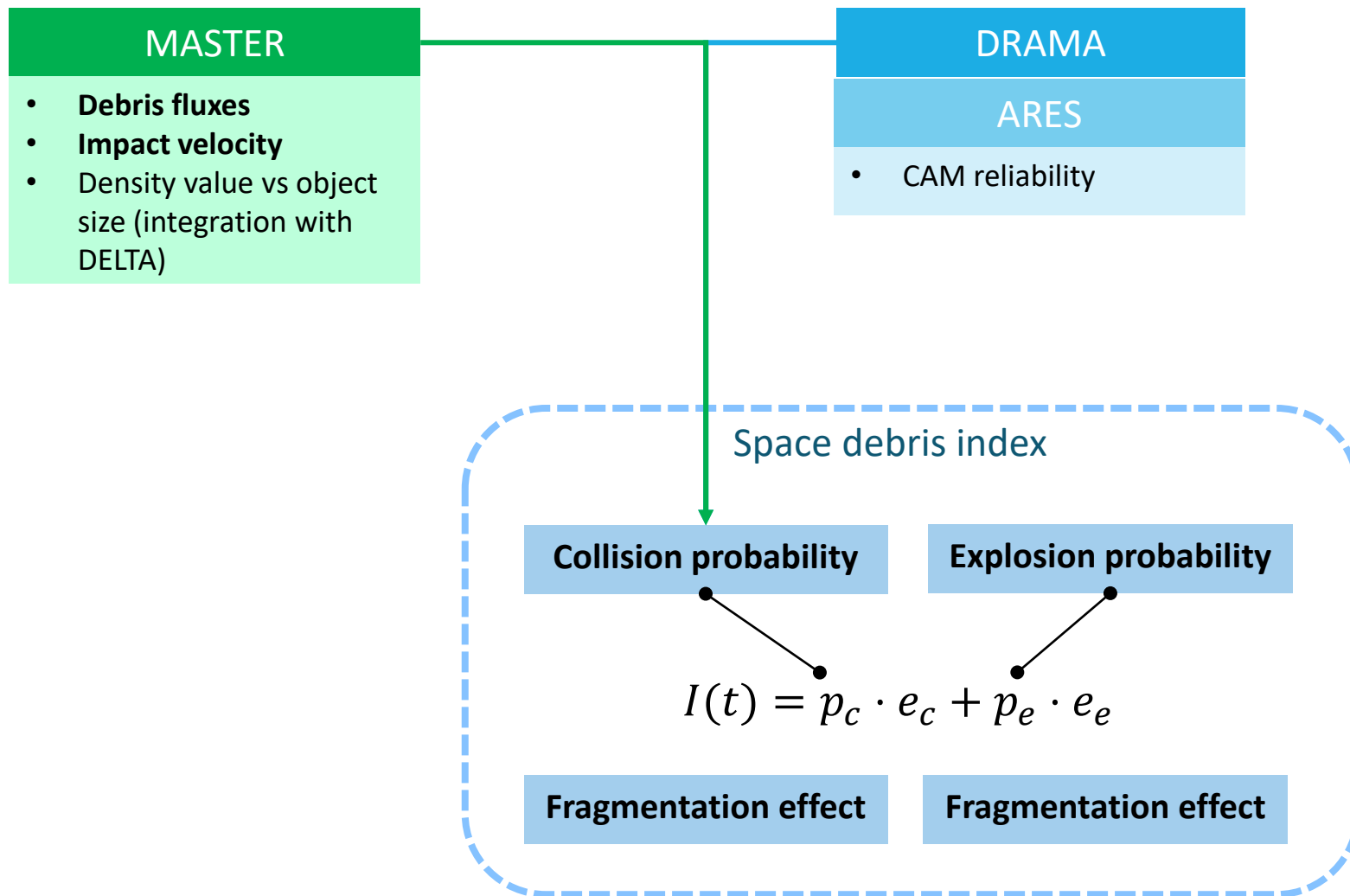
$$S(t) = \prod_{t_i < t} \left(1 - \frac{d_i}{n_i}\right)$$

**Explosion probability** evaluated using the **Nelson-Aalen** estimator

$$H(t) = \sum_{t_i < t} \frac{d_i}{n_i}$$

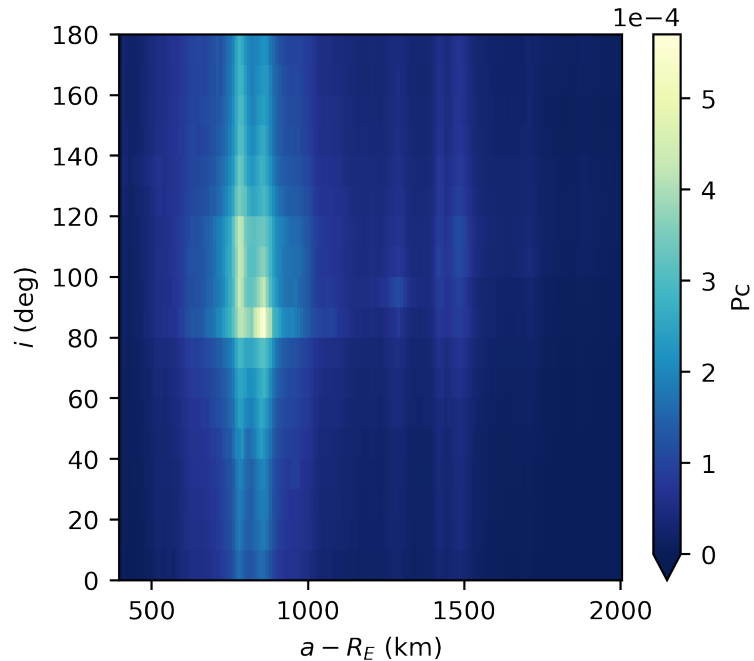


- Kaplan, E. L., Meier, P. (1958), Nonparametric Estimation from Incomplete Observations. Acta Astronautica, 53(282), 457-481.
- O. Aalen, (1978), Nonparametric Inference for a Family of Counting Processes. The annals of statistics, 6(4), 701-726.

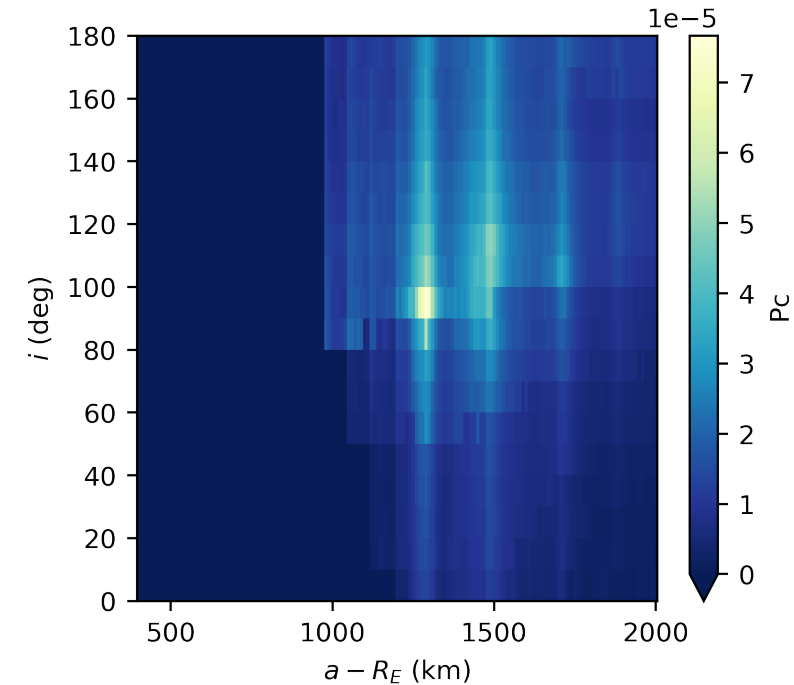


## Subcomponent: index evaluation – collision probability

### Collision probability without CAM capability



### Collision probability considering CAM capability



Collision probability evaluation as function of the semi-major axis and inclination considering:

- Cross-section =  $10 \text{ m}^2$
- Time discretisation = 1 year



## Space debris index

Collision probability

Explosion probability

$$I(t) = p_c \cdot e_c + p_e \cdot e_e$$

Fragmentation effect

## DISCOS

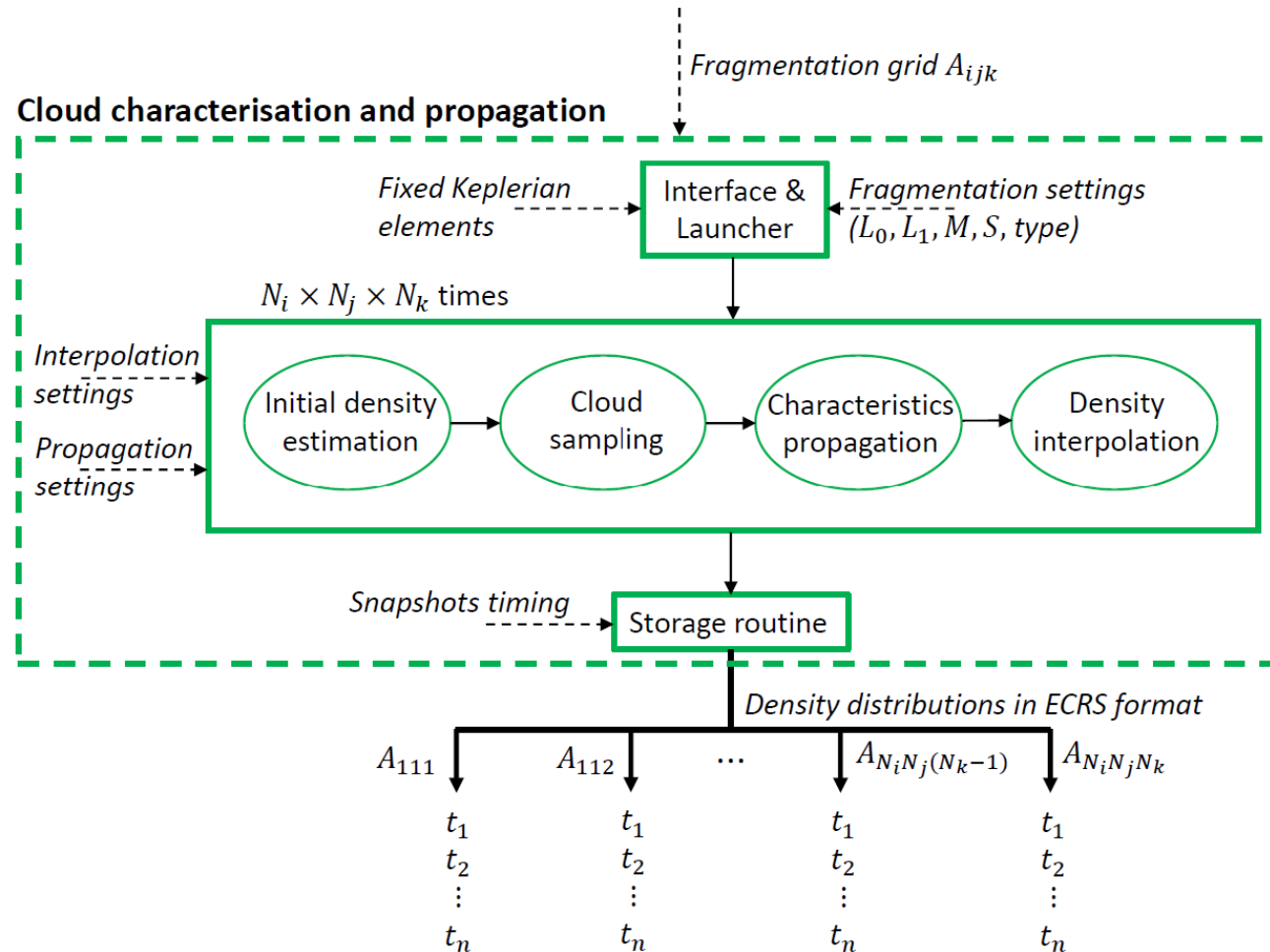
- **Objects properties**
- **Active / Inactive**
- Explosion probability
- PMD manoeuvres

## STARLING

### PlanODyn

- Density propagation
- Dynamics propagation

## Cloud characterisation and propagation



### Input:

- **Fragmentation grid:** coordinates of the subset of characteristic Keplerian elements of the orbital region under analysis

### Output:

- **Density distributions:** density values stored in ECRS\* format, for each fragmentation at each time snapshot

\* Compressed row storage applied to extended Karnaugh map representation of the density array

## Subcomponent: initial density estimation and sampling

### Inputs:

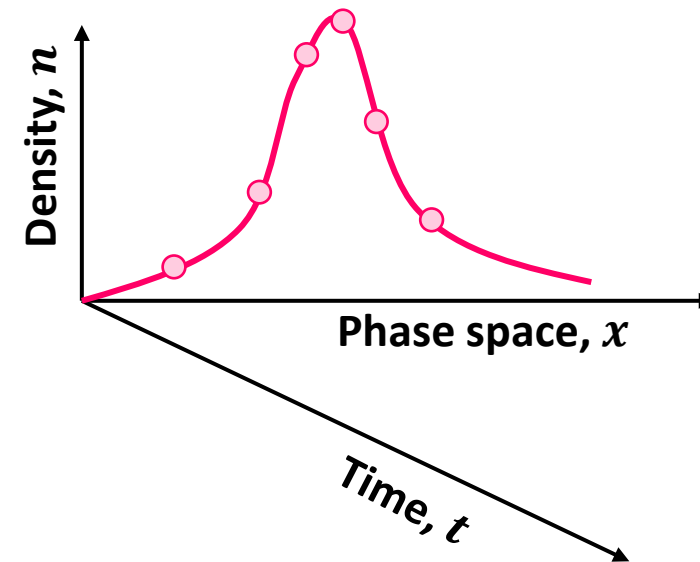
- **Fragmentation settings** specifying:
  - Parent orbit
  - Fragmentation type
  - Parameters (mass, fragments' size, scaling factor)
- **Interpolation settings** specifying:
  - Interpolation variables
  - Step-sizes for binning
  - Method (Monte Carlo or Weighted Monte Carlo)
  - Re-entry altitude

### Process:

- **Probabilistic definition** of the phase space domain
- Estimation of the density distribution through a **binning approach**
- **Characteristics' sampling** according to bins' size and (possibly) expected dynamical behaviour of the cloud

### Output:

- **Initial characteristics:** coordinates ( $a, e, i, \Omega, \omega, M, A/M_d, A/M_{srp}$ ) and density value of each characteristic to be propagated



## Subcomponent: characteristics' propagation

### Inputs:

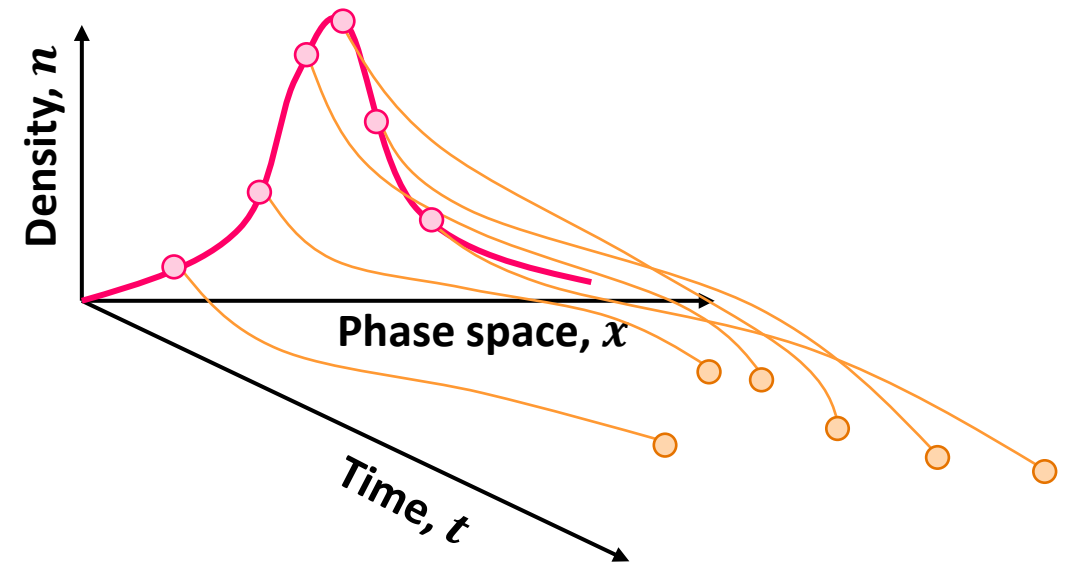
- **Initial characteristics:** coordinates ( $a, e, i, \Omega, \omega, M, A/M_d, A/M_{srp}$ ) and density value of each characteristic to be propagated
- **Propagation settings** specifying:
  - Snapshots' times (start, end, step-size)
  - Integration settings (tolerances, solver)
  - Dynamical model (parameters and flags, Jacobian, density model, ephemerides)

### Process:

- Propagation of characteristics using PlanODyn (semi-analytical tool) with set perturbations
- Storing in at some specified epochs

### Output:

- **Propagated characteristics:** coordinates and density values at each snapshot time



## Subcomponent: density interpolation

### Inputs:

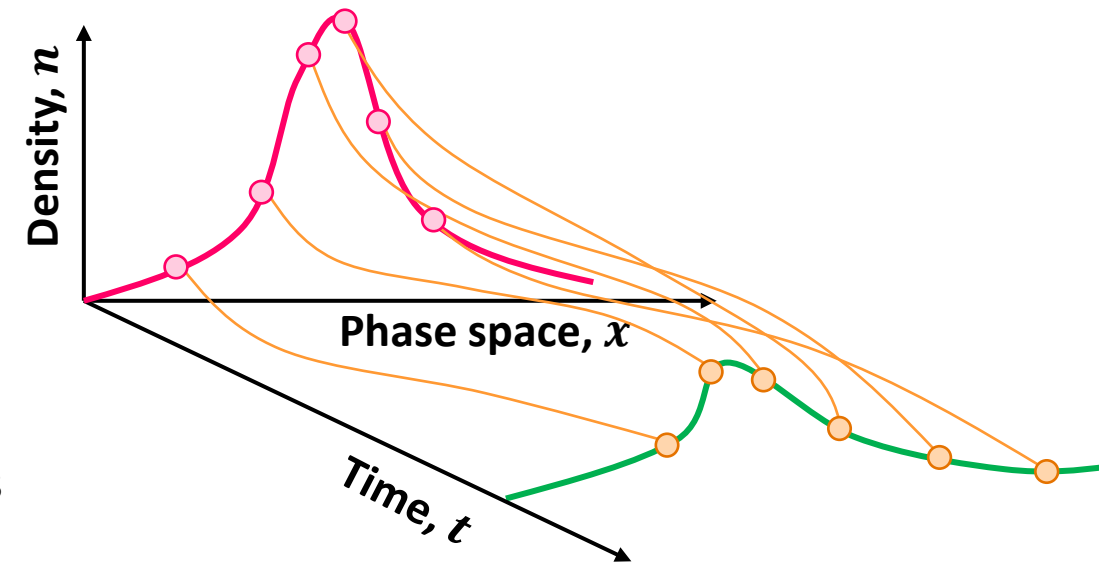
- **Interpolation settings** specifying:
  - Interpolation variables
  - Step-sizes for binning
  - Method (Monte Carlo or Weighted Monte Carlo)
  - Re-entry altitude
- **Propagated characteristics:** coordinates and density values at each snapshot time

### Process:

- Density distributions are recovered from the propagated characteristics through **binning in an (up to) 6D phase space**
- Nearest-neighbour – like **interpolation among neighbouring bins** is implemented to avoid missing data in the distribution

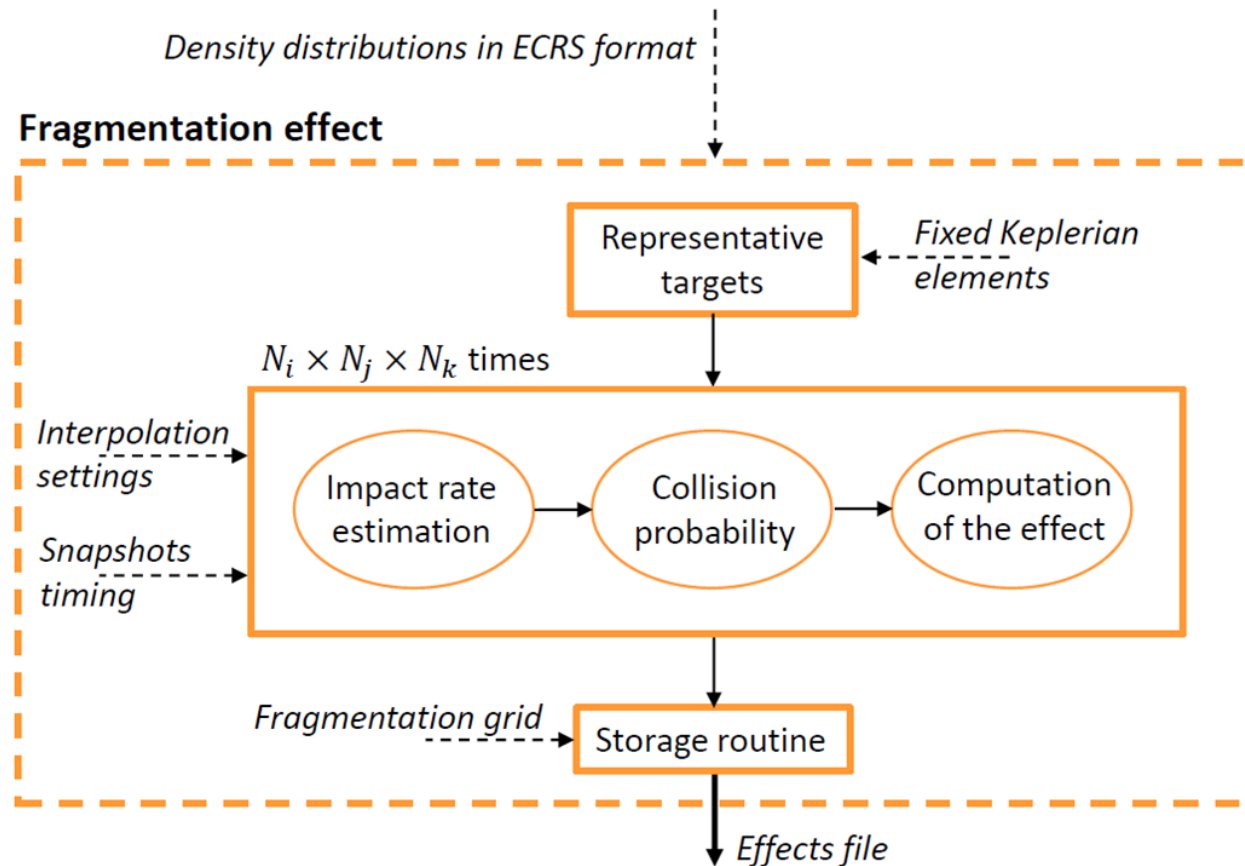
### Output:

- **Density distributions** at each specified snapshot time stored in ECRS format





## Main block: fragmentation effect



### Input:

- **Density distributions** at each specified snapshot time stored in ECRS format

### Output:

- **Effects:** coordinates of one fragmentation defined in the fragmentation grid and the relative effect on the representative targets

## Subcomponent: representative targets

### Inputs:

- **DISCOS active objects**
- **Grid** parameters:
  - Keplerian elements ranges and steps
  - Orbit type
- **Target settings** specifying the fixed Keplerian elements

### Output:

- **Representative targets:** Keplerian elements, area, and total area of each representative target

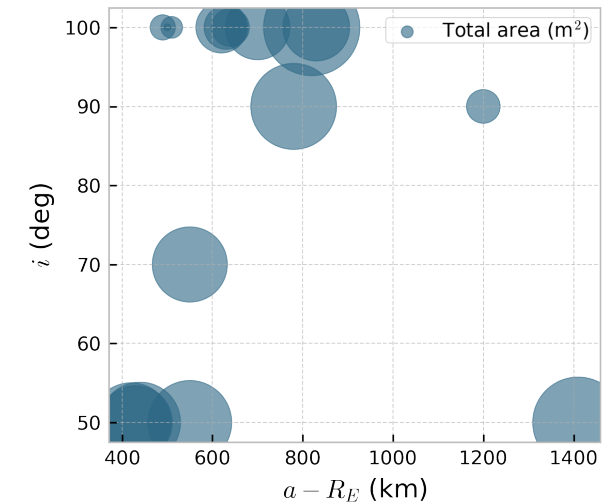
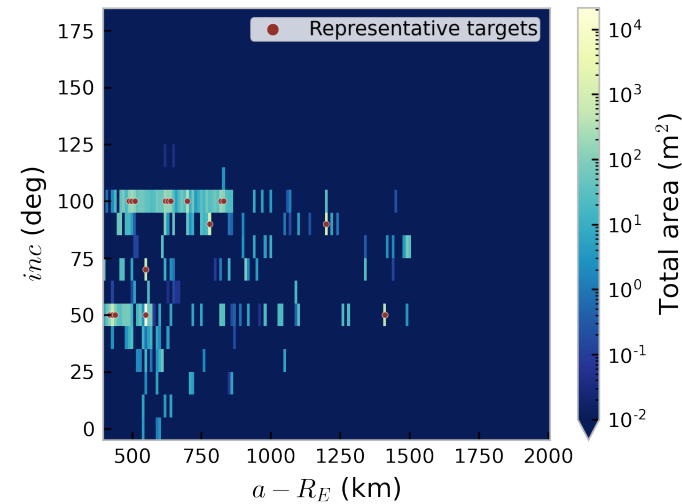
### Process:

- Reading DISCOS file with active objects
- Generation of the grid in Keplerian elements (according to the orbital region) and computation of the total and average areas in each cell of the grid
- **Identification** of the **representative targets** considering the cells containing the 90% of the cumulative cross-sectional area

## Subcomponent: representative targets

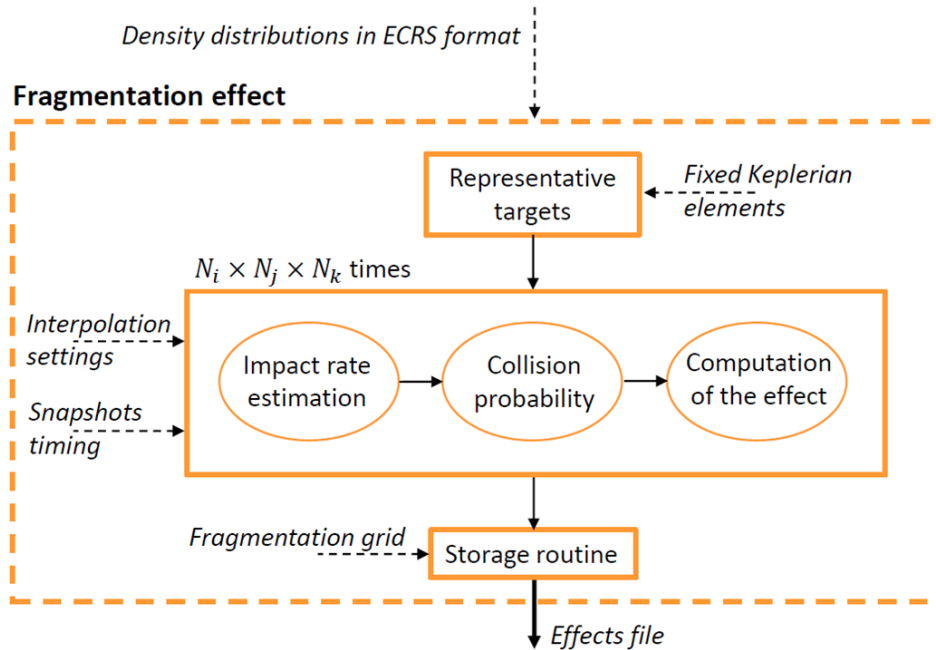
### Grid parameters:

- Semi-major axis range: [6778 – 8378] km
- Semi-major axis step: 10 km
- Inclination range: [0 – 180] deg
- Inclination step: 10 deg



Representative targets in LEO region - 14/02/2022

## Main block: fragmentation effect



## Impact rates:

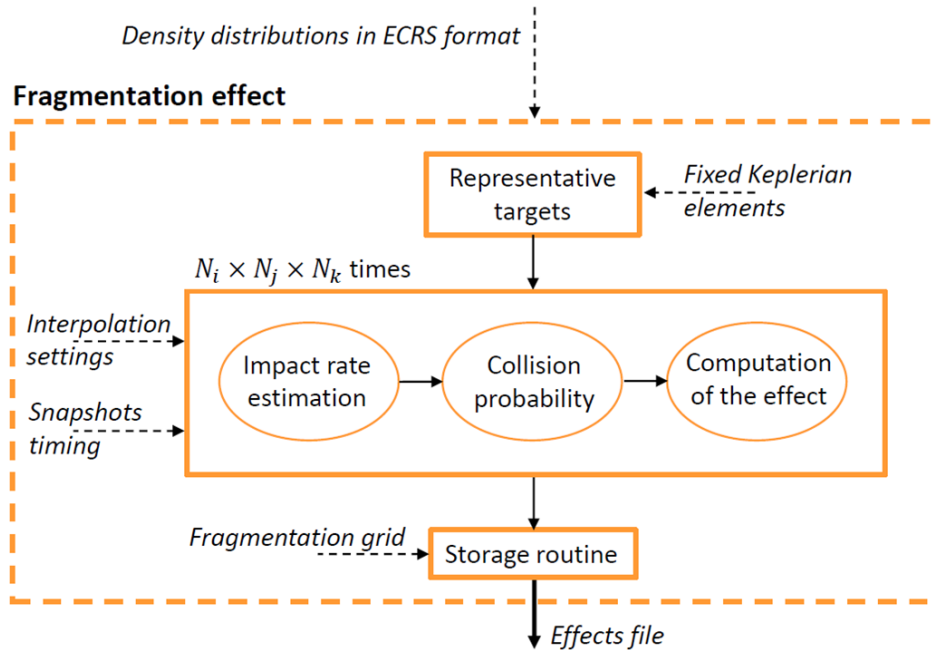
$\dot{\eta}$  for different target positions (according to an equally-spaced grid in mean anomaly) at each specified snapshot time

$$\dot{\eta} = A_c \int_{\mathbb{R}^3} \sum_{k=1}^4 \frac{n_\alpha(\alpha_{13}, \alpha_{46}^k)}{|\det J^k|} \|\mathbf{v}(\alpha_{13}, \alpha_{46}^k) - \mathbf{v}^*\| d\alpha_{13}$$

## Process:

- The **density distribution is sampled** in the subset of Keplerian elements  $(a, e, i)$
- By imposing **intersection with target position**, the full set of samples' coordinates is retrieved
- The density values in correspondence of the samples' coordinates is computed
- The impact rate is evaluated by **integrating the flux of fragments** over the target area

## Main block: fragmentation effect



## Cumulative collision probability:

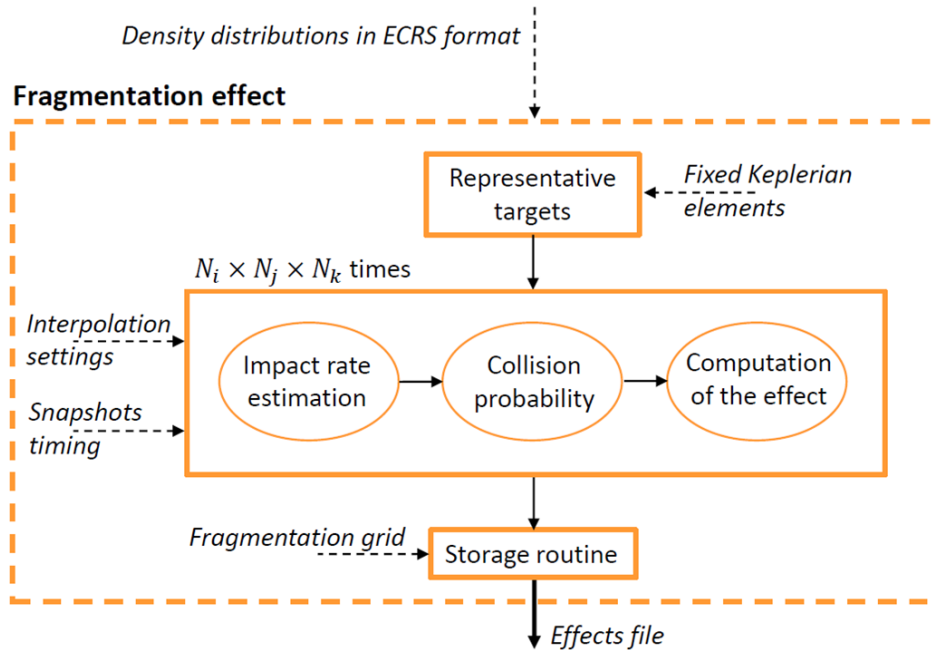
$p_c(t)$  at each specified snapshot time

$$p_c(t) = 1 - \exp(\eta(t)) = 1 - \exp\left(\int_{t_0}^t \dot{\eta}(\mathbf{r}^*, \mathbf{v}^*) ds\right)$$

## Process:

- The **number of impacts** with the target is estimated through midpoint integration
- The probability of collision is computed from the **cumulative number of impacts at final time**, through an analogy with kinetic gas theory

## Main block: fragmentation effect



## Fragmentation effect:

$e$ : weighted (according to shared area) cumulative collision probability of one fragmentation with the representative targets

$$e = \sum_{k=1}^{N_t} \frac{A_c^k}{A_c^{\text{tot}}} p_c^k(t_f), \quad A_c^{\text{tot}} = \sum_{k=1}^{N_t} A_c^k$$

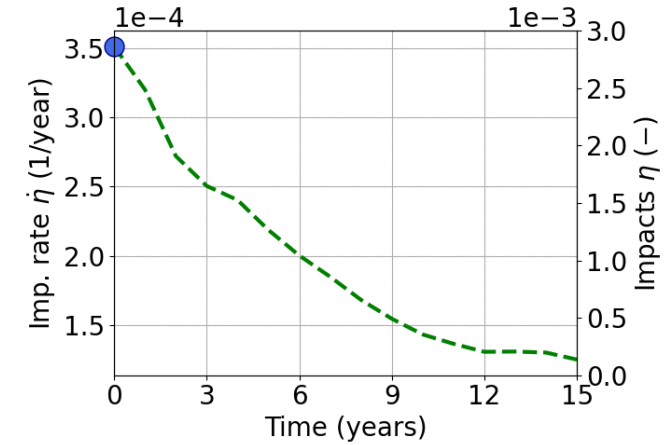
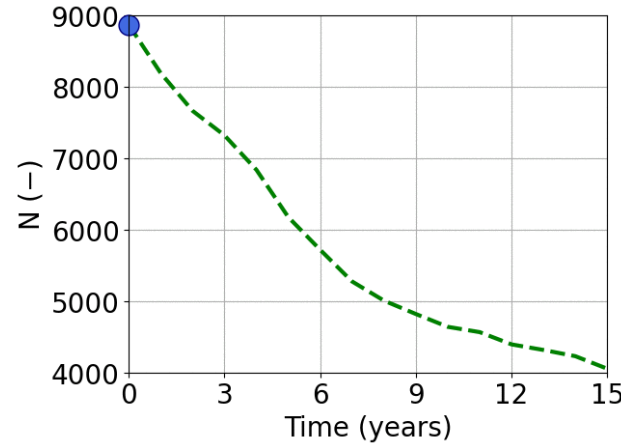
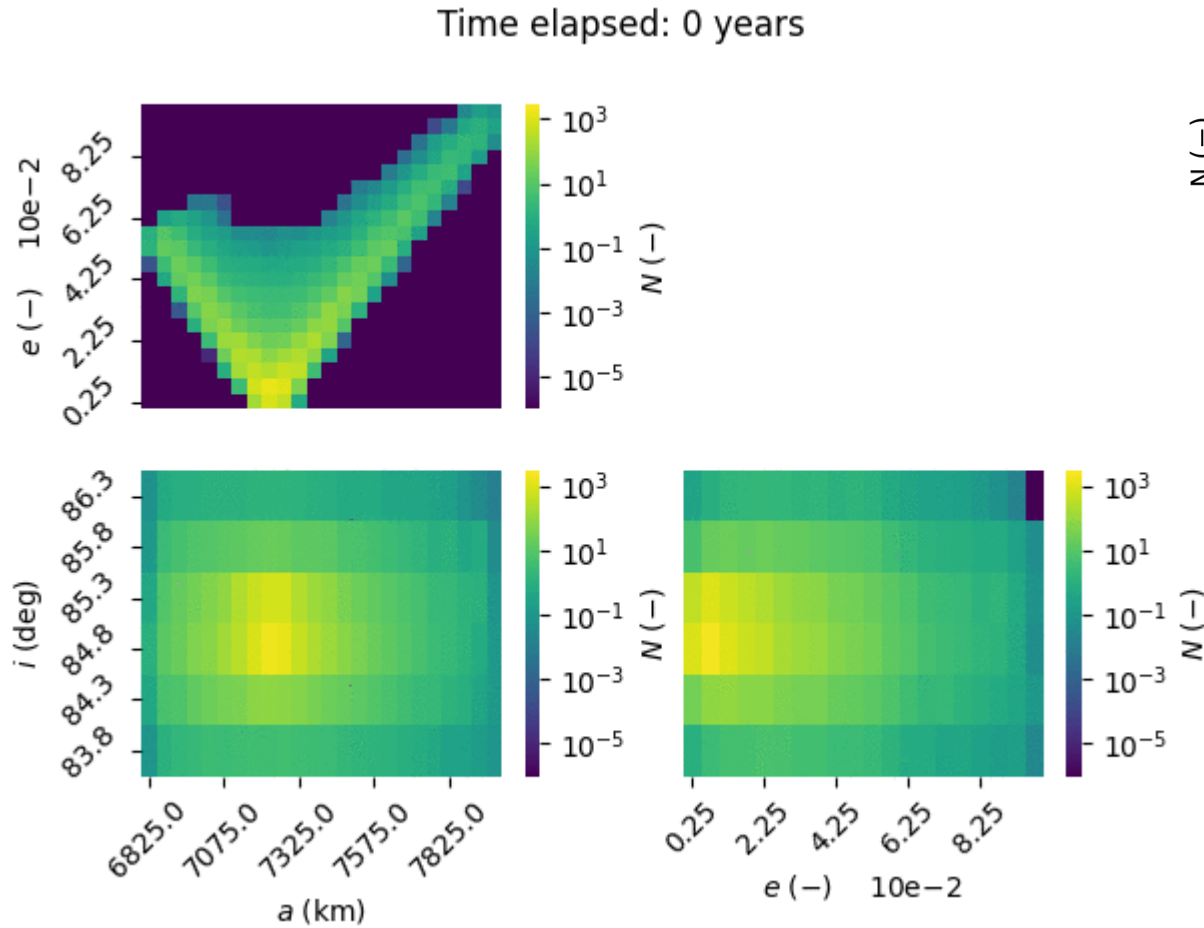
## Process:

The effect of a fragmentation is computed as the **weighted sum of the collision probabilities** according to the share of overall cross-sectional area of each target

# Fragmentation example

## Payload explosion in low-Earth orbit

Fragments number ( $N$ ), impact rate ( $\dot{\eta}$ ) and number of impacts ( $\eta$ ) over time

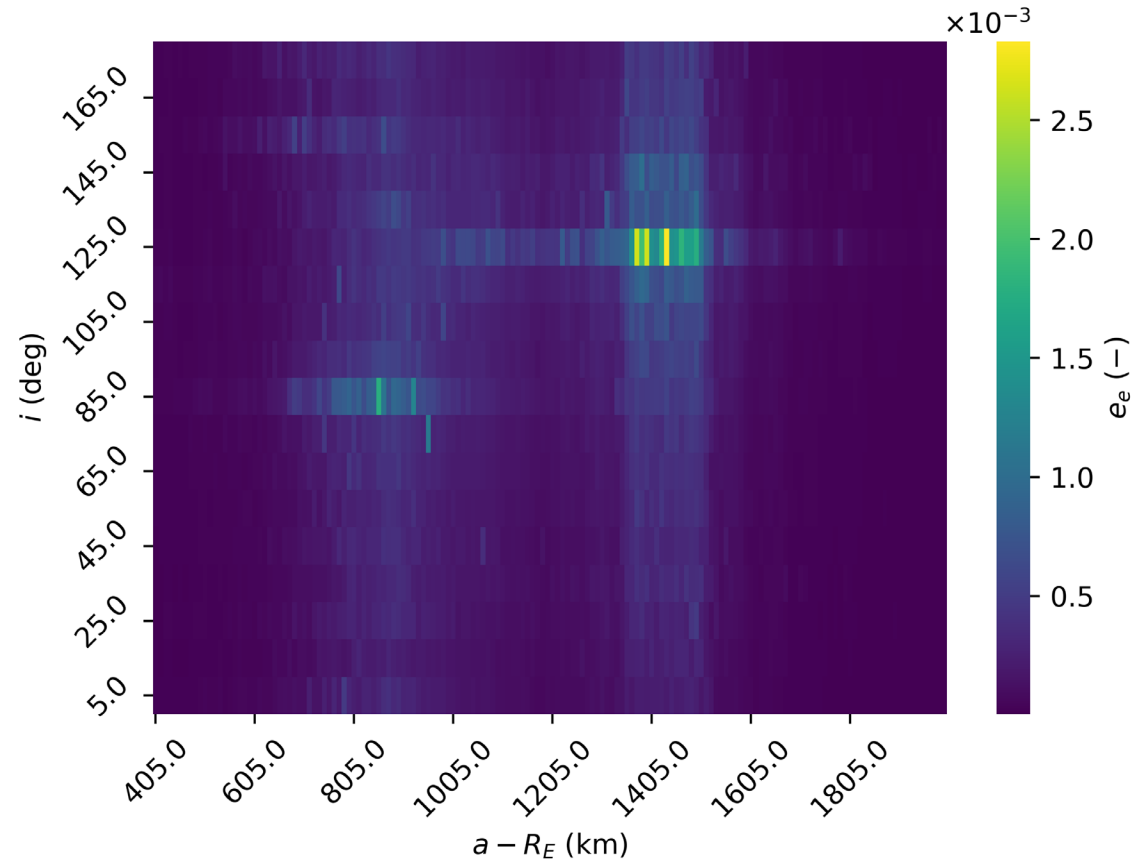


- **Fragmentation orbit:**  $a = 7236$  km,  $e = 0.001$ ,  $i = 85$  deg
- **Target orbit:**  $a = 7226$  km,  $e = 0.001$ ,  $i = 75$  deg
- **Perturbation model:**  $J_2$  and drag
- **Collision probability:** randomisation in  $\omega$ ,  $\Omega$ ,  $M$  assumed

Fragments' number ( $N$ ) distribution over time – heatmaps in  $a$ ,  $e$  and  $i$

# Effects map

## Payload explosions in low-Earth orbit



Cumulative collision probability at 15 years from fragmentation on 48 representative targets



## ECOB formulation overview

- The index assessed over time to get its evolution and cumulative value for the mission lifetime

$$I = \int ECOB dt$$

- Each mission profile is divided in mission phases: e.g. launch, injection, orbit raising, operational orbit, deorbiting etc.
- The basic formulation expanded to include the reliability of post-mission disposal (PMD) manoeuvres with a coefficient ( $\alpha$ )

$$I = \int_{t_0}^{t_{EOL}} ECOB dt + \underbrace{\alpha \cdot \int_{t_{EOL}}^{t_f} ECOB dt}_{\text{disposal}} + \underbrace{(1 - \alpha) \cdot \int_{t_{EOL}}^{t_f} ECOB dt}_{\text{no disposal}}$$

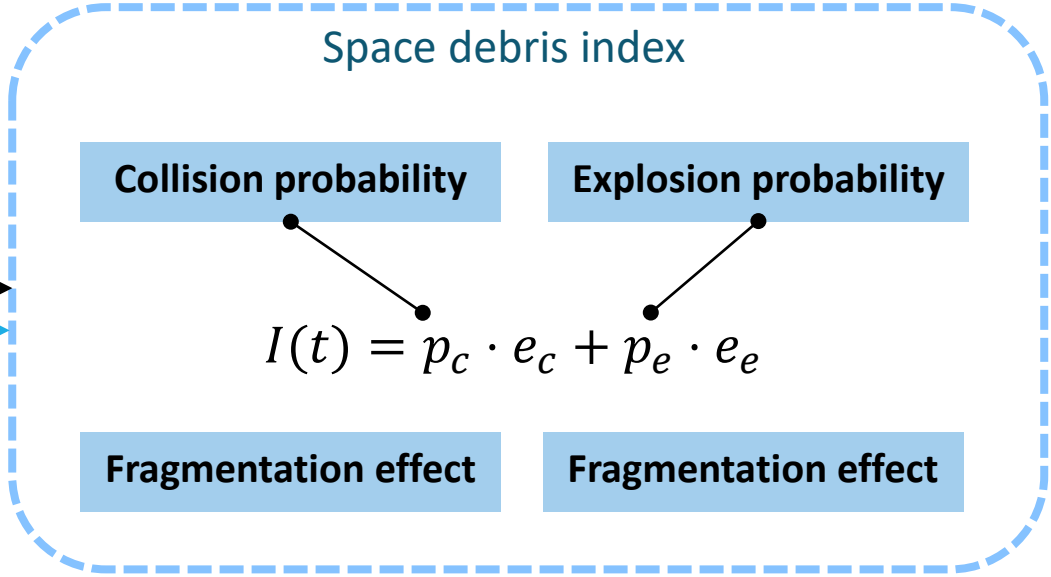
➤ Letizia, F., Colombo, C., Lewis, H. G., & Krag, H. (2016). Assessment of breakup severity on operational satellites. *Advances in Space Research*, 58(7), 1255-1274.



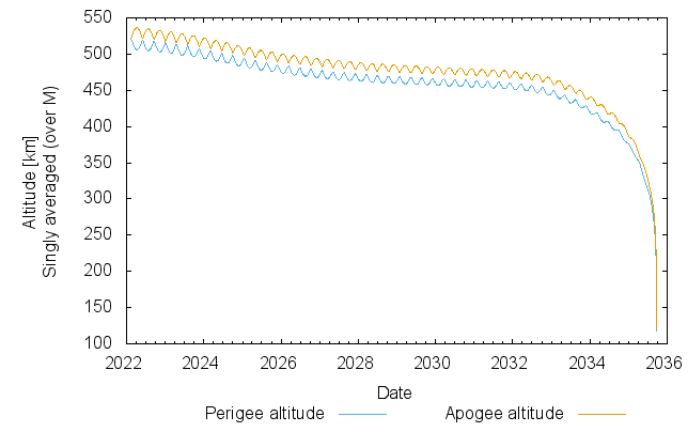
- Disposal scenarios
- Mission phases
- Spacecraft parameters

- DRAMA**
- OSCAR**
- Disposal scenarios
  - Identify orbit for natural decay
  - Orbit propagation

- Integrate along the trajectory
- Collision probability
  - Explosion probability
  - Fragmentation effects



DRAMA  
OSCAR - Orbital Spacecraft Active Removal  
Altitude vs. Time



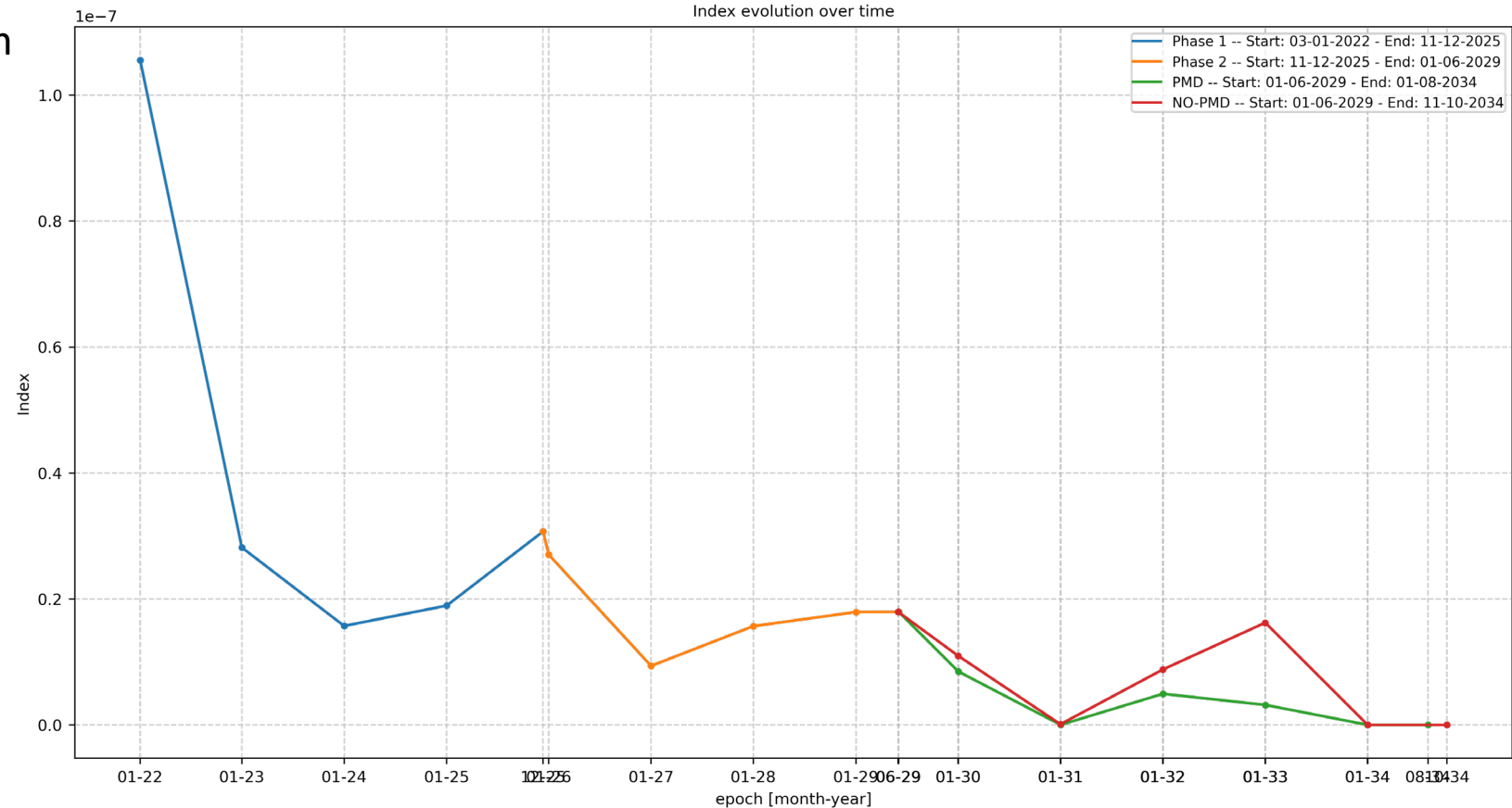
PMD reliability

$$I = \int_{t_0}^{t_{EOL}} ECOB dt + \alpha \cdot \int_{t_{EOL}}^{t_f} ECOB dt + (1 - \alpha) \cdot \int_{t_{EOL}}^{t_f} ECOB dt$$

➤ Letizia, F., Colombo, C., Lewis, H. G., & Krag, H. (2016). Assessment of breakup severity on operational satellites. *Advances in Space Research*, 58(7), 1255-1274.

## Index evolution – dummy mission

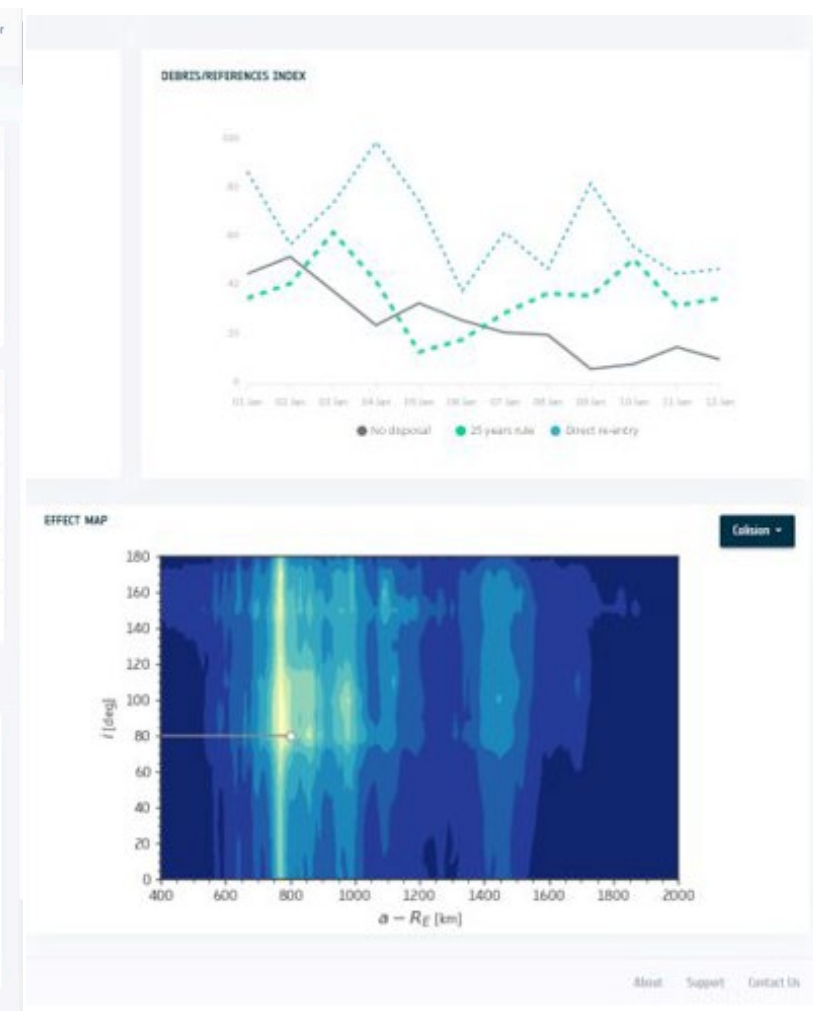
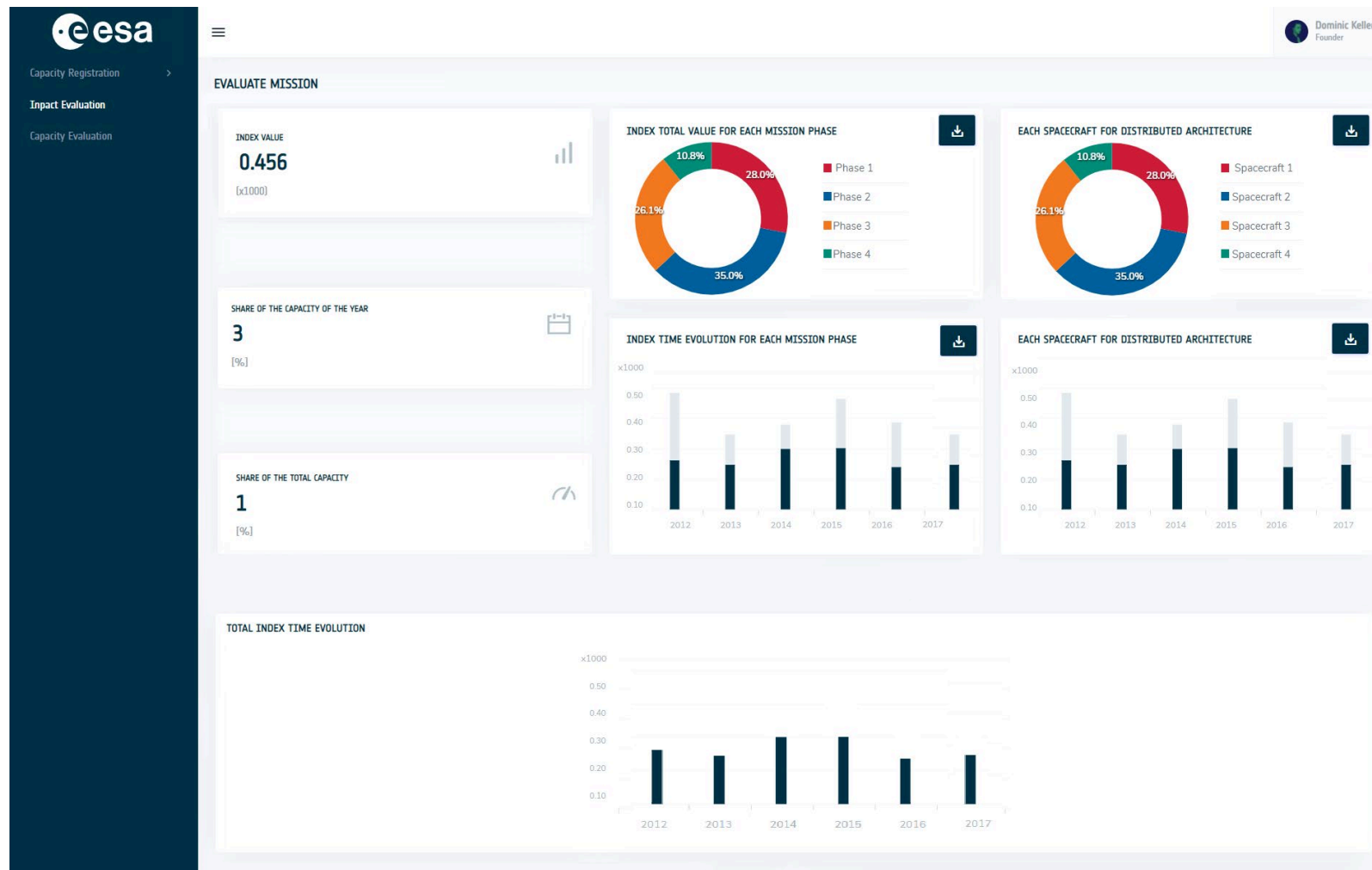
- **Phase 1:** Keplerian elements from an .oem file
- **Phase 2:** constant Keplerian elements
- **PMD/NO-PMD:** OSCAR propagation, considering a Re-orbit at 500 km using chemical propulsion



Index evolution over time – each color represents a single phase of the mission, and the index is computed at each time epoch

# THEMIS software design

## Frontend – Evaluation Output View



# CONCLUSIONS

## Steps completed

- Staling 2.0 tool applied to computation of the space debris index
- Space matrix approach for efficient binning
- Development of space debris ingredients **for any orbital region**
- Interfaces with ESA tools: DISCOS, MASTER, DRAMA

## Next steps

- Space debris implementation and validation
- Capacity formulation and definition of capacity threshold
- Engaging with the space community...stay tuned





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This project has received funding from the European Space Agency contract 4000133981/21/D/KS



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[www.compass.polimi.it](http://www.compass.polimi.it)

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6<sup>th</sup> European Space Debris modelling and Remediation workshop, Milano, 18-20 May 2022





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