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Vortex Flow and Cavitation in Liquid Injection: a Comparison Between High-Fidelity CFD Simulations and Experimental Visualizations on Transparent Nozzle Replicas
International Journal of Multiphase Flow, In press - Published online 17/02/2021
doi:10.1016/j.ijmultiphaseflow.2021.103605

The final publication is available at <https://doi.org/10.1016/j.ijmultiphaseflow.2021.103605>

Access to the published version may require subscription.

When citing this work, cite the original published paper.

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Highlights

1. CFD simulation performed from a virtual model of the real injector directly built from XCT;
2. vortex strings generation in the injectors are related to the flow pattern in the sac;
3. a non-dimensional parameter is proposed to characterize the flow in the injector sac;
4. the non-axial kinetic energy in the nozzle is linked to the intensity of cavitation;
5. flow unsteadiness and vortex pair instabilities influence the flow topology.

Vortex Flow and Cavitation in Liquid Injection: a Comparison between High-Fidelity CFD Simulations and Experimental Visualizations on Transparent Nozzle Replicas

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Abstract

Experimental instantaneous shadowgraph visualizations on transparent glass nozzle replica of high-pressure fuel injectors have been used to validate a novel in-house developed high-fidelity LES-VOF multiphase solver, to study the evolution of vortex flow and fuel cavitation. Both experiments and simulations capture the formation of an unsteady vapor structure inside the nozzle volume, which is referred to as ‘string-cavitation’; strings are found at the core of the recirculation zones. High-fidelity simulations provide a very detailed insight into the vortex generation in the injector nozzle; strings appear within the time scales that are relevant for fast injection events (on the order of 0.1 milliseconds) and, for the problem under consideration, their generation seems mostly related to the flow pattern in the sac. It is also shown that vortexes interact, merge till they disrupt and favor the temporary inception of shear cavitation.

Key words: 3-phase LES-VOF solver, CFD of internal nozzle flows, cavitation, liquid injection, primary atomization, OpenFOAM, LibPoliMi/DAER

1. Introduction

The study of atomization in liquid injection is a rapidly developing field of broad importance. There are many interesting applications of spray theory related to aeronautics, power, propulsion, heat transfer and materials processing. The flow inside the nozzle, guided by the injector design, has a dominant effect on the generation of spray patterns and propellant-air mixing. Optimal design of the injector geometry enables one to control the spray patterns and hence

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6 ultimately control the combustion efficiency. This is especially true in the presence of cavitation, where the flow field
7 inside the nozzle must be regulated to maximize the available liquid surface area at the nozzle exit to facilitate mass,
8 momentum and heat transfer. Cavitation plays a pivotal role in achieving finer atomization of the spray, enabling
9 improved fuel economy and reduced emission levels during combustion [1, 2]; however, cavitation may limit the
10 stability of the spray [3] and potentially damage the injector components, leading to reduced reliability of the injector.
11 In injector nozzles, surface spots initially surrounded by a cavitating flow region tend to erode at an accelerated pace:
12 cavitation pits increase the turbulence of the flow and create crevices that act as nucleation sites for new cavitation
13 bubbles, thus leading to an avalanche effect. For the above mentioned reasons, the study of internal nozzle flows in
14 injectors is essential. However, characterization of the flow inside the nozzle is difficult, both experimentally and
15 numerically. Non-invasive experimental measurements are difficult on account of the high pressures and small sizes.
16 Experimental studies on scaled (enlarged) geometries and reduced pressures do not provide meaningful insights of
17 the flow characteristics and hence are of limited usefulness. Very few examples of detailed numerical studies with
18 validation against experiments on internal flows in actual nozzles under realistic operating conditions are available in
19 the literature [4, 5, 6]. Numerical simulations of such flows are difficult not only because they require robust numerical
20 schemes and models to accurately capture the turbulent, multiphase nature of the flows (liquid fuel, gaseous fuel
21 and air) but also large computational resources to compute the long transients with high-resolution grids capable of
22 capturing the sharp liquid/vapor interfaces. Despite these challenges, various researchers have sought to study injector
23 flows using experimental and numerical methods. Given the micron-sized dimensions of these nozzles, Particle Image
24 Velocimetry (PIV) and Laser Doppler Velocimetry (LDV) are rarely available in the nozzle orifice and in the primary
25 breakup region [7, 8, 9, 10, 11, 12, 13]. Typically, flow visualization is done using shadowgraph techniques with modern
26 high speed cameras on transparent replicas [14, 15, 16, 17]. Andriotis et. al [16] reported studies on large injector
27 from propulsion systems for marine applications, being the construction of replicas easier. Standard shadowgraphy
28 (illumination from above) on an internal nozzle flow of an asymmetric prototype of a glass nozzle has been published
29 in [17]. Studies of fully transparent replicas of high-pressure injector nozzles under actual operating conditions (100 -
30 2000 bars) have been reported [14, 15, 18, 19]. In [18], the influence of the relative position of the holes and the hole-
31 to-hole interactions on string cavitation was investigated in a real-scale nozzle for pressures up to 2000 bar. There are
32 a relatively fewer simulations of flows in nozzle injectors under realistic operating conditions and geometries [20, 21].
33 In [20], enlarged replicas of Valve Covered Orifice-type (VCO) injectors incorporating tapered converging holes were
34 simulated; a similar study has been published in [21], where the solver handled the presence of multiple phases using
35 the homogeneous equilibrium model [22], to calculate the compressibility of the liquid/vapor mixture. Most of the
36 experimental tests to investigate cavitation in high-pressure liquid injection were done by observing the similarity
37 laws. Nozzles were built as large as possible (geometrical similarity); also, same Reynolds numbers (dynamical similarity),
38 same cavitation numbers (cavitation similarity) and same Weber number were preserved. Unfortunately, being
39 cavitation a multi-scale effect due to bubble growth from nuclei sizes, it cannot be scaled up [23]. The first realization
40 of real size nozzles was a great step toward a more representative transparent nozzle which compares good to real
41 parts. Simplified realistic size two-dimensional holes were initially considered in [24] and are still useful for basic
42 simulation model validation or well-controlled optical measurements [25]. In [26], it was found that visualizations are
43 more sensitive than mass flow rate measurement: cavitation inception occurs prior to the change in mass flow rate, and
44 bubbles are observed in the spray area even in absence of choked flow. The hole inlet radius was identified to strongly
45 influence the cavitation inception and the flow detachment at the hole inlet edge as the flow's direction turns toward
46 the hole. Finally, in [8] it is shown that the cavitation length increases with the injection pressure and that cavitation
47 collapse at the vicinity of the hole exit improves atomization. At higher cavitation numbers, when the cavitation zone
48 is reaching the hole exit, the air can propagate back in the nozzle; air fills part of the volume that would be taken
49 by the vapor, reducing the amount of cavitation and stabilizing the gaseous flow area. This so-called hydraulic flip
50 limits the intensity of the atomization and stabilizes the flow [8, 24]. The limit of two-dimensional holes is driven by
51 the two-dimensional cavity depth. If too small, the influence of the boundary will not be negligible; if too deep, the
52 shadowgraph visualization will be integrated along the whole optical path and it is the result of a superimposition of
53 multiple bubbles developing at different depths. The signal absorption saturates even with low density of cavitation
54 and in moderate regimes. It is then almost impossible to distinguish different vapor density levels. It is thus useful
55 to use more complex X-Ray measurements. Another aspect which cannot be fulfilled by two-dimensional nozzles is the
56 fluid velocity at needle seat and towards the sac geometry as found in real nozzles. The reason is that the flow area
57 along the flow line is usually becoming smaller due to the conical geometry around the seat and the sac, that cannot be
58 represented in two dimensions. Many authors investigated central axisymmetric holes that are more realistic in terms
59 of geometry scale. However, visualization of axisymmetric holes is also difficult. Finally, in central two-dimensional
60 channel or axisymmetric holes, the fluid is cavitating uniformly with a stable behavior, whereas the observed regimes

61 of asymmetrical nozzles with non divergent holes (like supercavitation) are mostly unstable. Therefore, asymmetrical
62 inlet conditions and inclined holes were then studied [11]. Recent publications report building and measurements of
63 a realistic shape of transparent nozzles using one simple rectangular insert with the flow hole inside. Some authors
64 succeeded to integrate it in a real metal nozzle [18], or to produce an even more complex shape fully transparent
65 [27]. However, keeping the nominal geometry or managing a complex shape when considering real-size nozzles and
66 high-pressure conditions becomes very difficult. No real proof of concept of realistic nozzles that are exhibiting the
67 former qualities while being at the same time compatible with rapid prototyping approach has been demonstrated until
68 now to our knowledge. A proof of concept of a real-size, real-shape, real-pressure, representative surface roughness,
69 transparent nozzles for Design of Experiments, is used to validate a LES-VOF solver developed by the authors in [28].

70 The aim of this work is to conduct a systematic study, both experimentally and numerically, of the flow charac-
71 teristics in high pressure liquid injectors working under typical operating conditions. Two different configurations of
72 real-size transparent glass-nozzle replicas of injectors were built by Vitesco Technologies for this study [29]. Nozzle
73 replicas have been realized using a novel rapid prototyping technique using laser-etched manufacturing and presented
74 in [29]. The aim of the experiments was to provide a detailed visualization of the in-nozzle flow and of the extent
75 primary jet breakup. Tests have been carried out sequentially by using a camera to produce shadowgraph images for
76 two different viewing, namely the front view and the lateral view, in order to obtain well resolved three-dimensional
77 visualization of the flow characteristics. High-resolution simulations of the injector flows were conducted using an
78 in-house Finite Volume (FV) variable-density multiphase VOF solver developed by the authors. The solver used in
79 this study [28] is developed in the OpenFOAM Technology and it is included in a in-house C++ library developed by
80 the authors. Validated results from the simulations were post-processed to investigate the physical mechanism leading
81 to the flow instability inside the nozzle. The experiments (and simulations) were conducted using n-Heptane as the
82 injected liquid fuel at a pressure of 100 bar.

83 The paper is organized as follows: Sec. 2 discusses the phenomenological process of flow and cavitation in real
84 world injectors operating at high pressures. A discussion of the experimental and measurement procedure is included
85 in Sec. 3. The simulation methodologies used in multiphase (liquid and gas), multi-component (fuel and air in
86 gaseous phase) flows as it pertains to injector and the main equations of the variable-density flow solver implemented
87 and verified in [28] are discussed in Sec. 4. Simulation results using the solver of [28] are validated against the
88 instantaneous shadowgraph pictures from experiments in Sec. 5, to prove the reliability of the solver to describe the
89 cavitating structures occurring in the real glass nozzle injectors. Sections 6-7 discuss the simulation results. The main
90 phenomena influencing the primary break-up mechanisms, generated inside the nozzle orifices, are identified into two
91 sources: cavitation and flow dynamics, which are the subjects of the present work. Primary breakup mechanism is not
92 analyzed in this work and it will be the topic of further publications. Conclusions are drawn in Sec. 10.

93 **2. Phenomenological process of flow and cavitation in high pressure injectors**

94 Two different forms of cavitation have been distinguished [30, 31] and they are known as “geometry-induced”
95 (or shear) and “string” (or vortex) cavitation respectively. Shear cavitation is initiated at sharp corners where the
96 pressure falls below the saturation value [32, 33, 34] because of a sudden flow detachment and the accompanying
97 recirculation region. For a given injector geometry, as the injection pressure increases, the region of cavitation grows
98 and extends to the outlet until supercavitation occurs. The growth of the cavitation region increases the turbulence and
99 spray angle of the jet [8, 35]. During this process, the liquid jet atomization is enhanced [35]. Increasing the injection
100 pressure beyond a critical value leads to a “hydraulic flip”, wherein the air surrounding the nozzle outlet is sucked
101 into the nozzle orifice to fill the cavitation area which makes the cavitation disappear immediately as a thin layer of
102 gas is attached to the wall [36]. This occurrence is not beneficial for the atomization and can badly affect the fuel
103 injector performance as a decrease of the spray cone angle is usually observed in this situation [36]. However, real
104 nozzles are not completely smooth and symmetrical on account of the manufacturing process and hence maintaining
105 a stable hydraulic flip is difficult. Thus, the phenomenon of local reattachment will occur periodically. String (or
106 vortex) cavitation, conversely, develops by the evolution of the vorticity which allows the formation of geometry-
107 scale vortices and is significantly influenced by the walls and the interaction with other vortices [15]; additionally,
108 low pressure regions in the centers of the vortexes in the nozzle can generate a phase-change or entrap and stabilize
109 bubbles that were entrained in their proximity, similarly to what is observed in hydro-machines [37, 38]. Vortex
110 cavitation in the injector nozzles was first observed by Kim [39] and since then it has been described in further studies
111 performed in enlarged nozzle replicas and was termed also as “string cavitation” [16, 40]. The main differences
112 between vortex cavitation in propellers and turbines and those in fuel injectors arise from the geometric size and
113 operating conditions. Nozzle flows develop in very confined volumes (nozzle geometries are on the order of a few

114 hundred microns) and at high pressures (> 100 atm) whereas turbines and propellers have much larger geometrical
 115 sizes and lower operating pressures. In nozzle flows, the high operating pressures and small geometrical size may
 116 allow formation of vortices whose sizes are large relative to the nozzle geometry and where each cavitating vortex
 117 may interfere with other vortices. In these small sized nozzles the proximity of the walls can also significantly impact
 118 the formation and structure of these vortices. Additionally, large pressure drops in fuel injectors are encountered
 119 within very short distances (few hundreds of micrometers) while the lifetime of the formed vortical structure is usually
 120 only a fraction of the injection period. Cavitation strings are usually formed during fuel injection in areas where large-
 121 scale vortical structures develop: this happens when local pressure level is lower than the vapor pressure of the fuel.
 122 In a typical nozzle geometry, cavitation vortices are located between the separation point on the needle surface and
 123 the separation point at the hole inlet corner, and where there is sharp flow turning inside the sac volume of the injector.
 124 Unlike geometrical cavitation, string cavitation is present in any nozzle geometry: with sac-type and VCO nozzles
 125 and with either cylindrical or tapered holes, whose inlet can be either sharp or rounded. This has raised questions
 126 about the existence of vaporized liquid inside large-scale vortical structures; more recent studies [16, 41] suggest that
 127 string cavitation represents a transport process of vapor carried by the vortex flow rather than a phase-change process.
 128 Formation of string cavitation would originate from pre-existing (shear) cavitation sites, forming a continuous vapor
 129 column that extends into the flow region between adjacent holes. This can explain the presence of vapor where the
 130 pressure is quite high, for instance in the sac volume between holes. The underlying physics of confined vortex
 131 cavitation and of its onset in high pressure injectors still remains unclear and not yet fully understood. In this sense,
 132 the combination of shadowgraph visualizations on real-size transparent nozzle replicas and high-fidelity simulations
 133 can help to improve the understanding about this complex flow physics.

134 3. Experimental setup

135 *Ad-hoc* prototypes of real-sized glass nozzle injectors used for this study are capable of operating under realis-
 136 tic nozzle pressures; they were designed and built by Vitesco Technologies to contribute to the nozzle design and
 137 cavitation control efforts aimed at improving high-pressure fuel injectors [29]. The geometrical features of the proto-
 138 type have been thought to reproduce a single-hole injector, representing a 60° sector of a real multi-hole injector, as
 139 reported in Fig. 2. This includes the needle, the sac geometry, the hole geometry and the external nozzle shape.

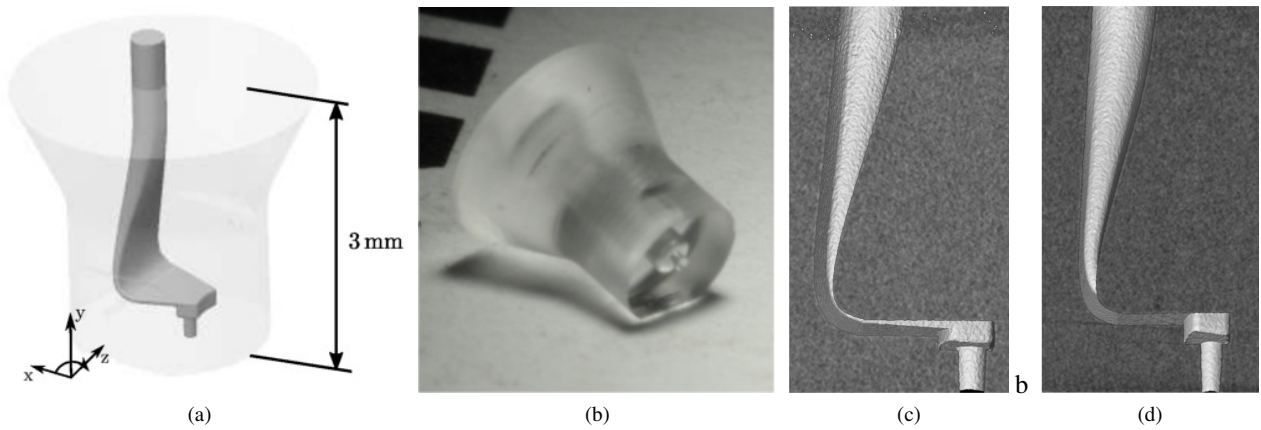


Figure 1: Sample of transparent glass nozzle replica: a) external view; b) sample of a central-nozzle hole; c) XCT visualization of glass nozzle side of ID-3; d) XCT visualization of glass nozzle side of ID-10

140 The injector prototype has been built in quartz glass (fused silica) by a laser-etched manufacturing process [29]
 141 that is able to achieve an average surface roughness of $1 - 3 \mu m$. This surface roughness is typical of micro-EDM
 142 (Electrical Discharge Machining) processes used for manufacturing real injectors (A sample is shown in Fig. 1b).
 143 The nozzle can withstand pressure up to 350 bar and is compatible with any working fluid. The sector angle is
 144 slightly enlarged to allow the 60° flow, while the side wall and the single hole are modifications when compared to
 145 real injectors. The injector geometry has been measured by a multisensor coordinate measuring machine based on
 146 a X-ray computed tomography (see Fig. 1c and Fig. 1d), to ensure the quality of the manufacturing process and

147 the correspondence between simulated and experimental geometry. The XCT is a V Tome XS 240 kV from General
 148 Electric. The nano-focus, 180 kV X-Ray tubes at 18 W (maximum power) has been used together with a tungsten-
 149 synthetic diamond target. XCT measurements are shown in Fig. 1 and the design values confirmed by XCT are
 150 presented in the table of Fig. 2.

Table 1: Thermodynamic properties for n – Heptane_(liq), n – Heptane_(vap) at T=25° C, and non-condensable gas (air) at T=15° C.

Parameter	Fluid		
	n – Heptane _(liq)	n – Heptane _(vap)	air
density ρ_l [kgm ⁻³]	684	4.25	1.225
dynamic viscosity μ_l [kg m ⁻¹ s ⁻¹]	4.0835×10^{-4}	7.0125×10^{-6}	1.7885×10^{-5}
surface tension [Nm ⁻¹]	0.019517	-	-
saturation pressure [Pa]	7000	-	-

151 Experiments have been carried out at Vitesco Technologies at the facility in Toulouse (France). The aim of
 152 the experiments was to provide a detailed visualization of the flow within the nozzle and the extent of the primary
 153 jet breakup. Experimental tests of liquid-into-air injection have been carried out at a needle lift of 79 μm , that is
 154 representative of a fully opened nozzle using n-Heptane as the working fluid, (both the numerical solver and the test
 155 bench can work with real fuels and are not limited to n-Heptane). The thermophysical and transport properties of n-
 156 Heptane are listed in Tab. 1. Tests have been carried out using a camera for two different viewing angles, $\theta_1 = 0^\circ$ (front
 157 view) and $\theta_2 = 90^\circ$ (lateral view), θ being the azimuthal angle. The flow solver described in [28] has been validated
 158 on two glass-nozzle configurations based on their individual jet penetrations. The average jet penetration over twenty
 159 experiments of ten different geometrical configurations (ID-1 to ID-10) was measured. Configurations ID-3 and ID-10
 160 (see Fig. 2) showed respectively the maximum and minimum penetrations in the injection time interval (1400 μs)
 161 tested; these configurations were hence chosen for numerical validation and analysis. They have identical lift and
 162 similar values of nozzle inlet and outlet diameters. They are designed to deliver similar mass flow rate, but with
 163 different: a) nozzle sac geometry, through the height of the step H, the hole offset (off-H) and the length of the dead
 164 space; b) nozzle length. They operate at the conditions reported in Tab. 2.

Parameter	ID-10	ID-3	Unit
p_{inlet}	100	100	bar
p_{amb}	1	1	bar
Mean liquid Velocity U_l	155.07	149.43	m s ⁻¹
Re at plane N_6	36110	35104	-
Re at plane S_1	14499	13020	-
K	1.0095	1.0095	-
C	104.9422	104.9422	-
We	110049	104712	-

Table 2: Operating conditions of the experimental tests applied to nozzle configurations ID-3 and ID-10 on plane N_6 of Fig. 6.

165 The fuel supply system consists of a low-pressure electrical pump, a heat exchanger, a high pressure pump, a
 166 common rail to damp oscillations, a fuel supply line with a pressure sensor to the injector valve along with the
 167 transparent testing nozzle. In the present work, the inlet fuel pressure has been set to 100 bar. The outlet of the nozzle
 168 is ambient temperature and pressure. While the solver assumes isothermal conditions of the working fluid, Tab. 1
 169 reports the fluid properties computed at two different temperatures. In experiments usually n-Heptane and air have
 170 different temperatures: n-Heptane is usually warmer, at $\approx 25^\circ\text{C}$, while air in the injection chamber stays at $\approx 15^\circ\text{C}$.
 171 Under the isothermal approximation, the sensible heat exchange that would have been occurred during fuel-air mixing
 172 is neglected.

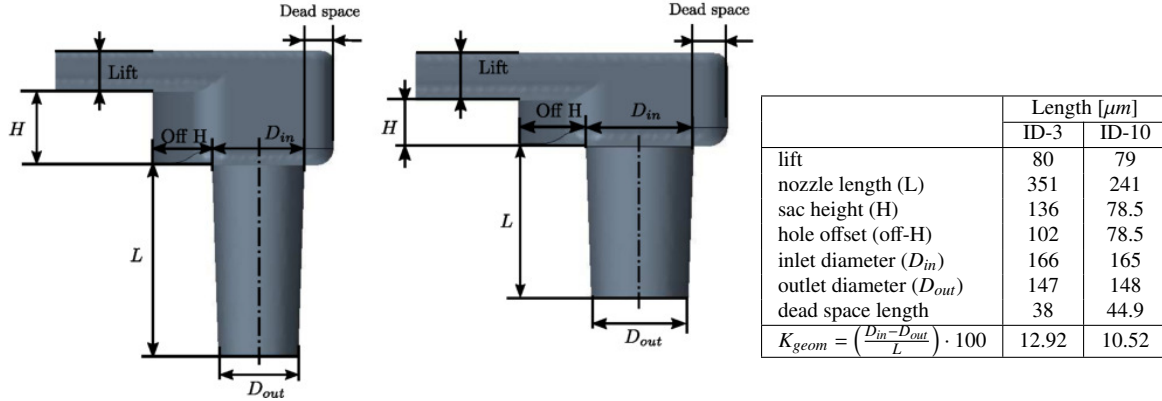


Figure 2: The nozzle geometries studied, named as configuration ID-3 (left), ID-10 (right). Dimensions are specified in the Table.

173 Operating conditions for the flow were characterized on the basis of the following parameters:

- the cavitation number K , according to the definition of Nurick [27]:

$$K = \frac{p_{inj} - p_{sat}}{p_{inj} - p_{back}} \quad (1)$$

- the cavitation number C , according to the definition of Bergwerk [42]:

$$C = \frac{p_{inj} - p_{back}}{p_{back} - p_{sat}} \quad (2)$$

- the liquid Reynolds number (Re_l):

$$Re_l = \frac{\rho_l U_l D}{\mu_l} \quad (3)$$

with p_{inj} being the fuel injection pressure, p_{back} the pressure of the chamber, p_{sat} the saturation pressure of the liquid, ρ_l the density of liquid n-Heptane, D is the hydraulic diameter; U_l the mean liquid velocity, defined as:

$$\mathbf{U}_l = \frac{\langle \dot{m} \rangle}{\rho_l A_{N_6}} \quad (4)$$

174 In Eq. (4), A_{N_6} is the cross-sectional area of plane N_6 in the nozzle hole (see Fig. 6), ρ_l is the density of liquid
175 n-Heptane and $\langle \dot{m} \rangle$ is the time-averaged mass flow rate (MFR) from experiments.

176 4. Computational Methodology for the Simulation of Cavitation in High-Pressure Injectors

177 CFD simulations have been performed on the XCT-based virtual model of the real component, rather than on the
178 ideal CAD geometry. The workflow of the combined XCT–CFD procedure is summarized in Fig. 3. It is important
179 to mention that the effect of the surface roughness is not accounted in the CFD simulations: despite the grid used is
180 quite fine (80 M cells), it is still not fine enough to account for the influence of the roughness on the evolution of
181 the boundary layers on the walls at the Reynolds numbers studied. It is worth mentioning that high resolution XCT
182 cannot properly capture sharp edges; this may be a serious limit when dealing with injectors, because sharpness of
183 the edges strongly influences the development of cavitation at the nozzle entrance. To correct this bias, measurements
184 using a microscope were therefore used to quantify the hole edge rounding and to verify the average wall roughness
185 (that were both found to be about $1 \mu\text{m}$). Manual corrections were therefore applied to the CAD file in proximity of
186 the sharp corners at the nozzle entrance, where information from the microscope were available.

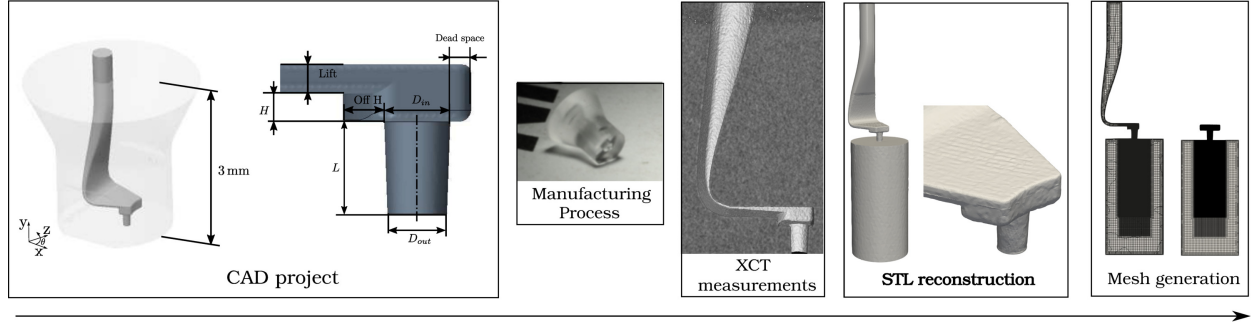


Figure 3: Sketch of the workflow for the generation XCT-based virtual model of the injectors studied. Since high resolution XCT cannot properly capture sharp edges, measurements from the microscope were used to quantify the hole edge rounding at the nozzle entrance. Manual corrections in the STL file, before the automatic generation of the polyhedral mesh.

187 The grid consists of 80 million of polyhedral cells, that allow different refinement levels in the different regions of
 188 the injector geometry, as shown in Fig. 3. The nozzle region is followed by an open cylindrical reservoir (a portion
 189 of the ambient volume where injection takes place) with different cell refinement levels. The finest refinement region
 190 in the grid has an average cell size of about $3\ \mu\text{m}$ and it covers the sac, the nozzle and part of the reservoir, where
 191 primary atomization takes place. The selected cell size in this region is assumed to be sufficient to capture the finest
 192 ligament structures in the primary breakup region, that from experimental visualization was found to be in between 10
 193 and $15\ \mu\text{m}$ for the injectors studied. A region with average cell size of $8\ \mu\text{m}$ is used in between the fine and the coarse
 194 regions of the grid and it is located in the reservoir, near the outlet of the domain. Finally, the coarse cell region has
 195 an average cell size of $40\ \mu\text{m}$ and it is used where the flow is fully liquid (nozzle inlet) and in the buffer regions.

A three-phase variable-density multiphase VOF solver developed by the authors [28] for three fluids, two of which are miscible is used in this work. The three fluids are liquid fuel, fuel vapor and air (non-condensable gas). Fuel vapor and air are considered to be miscible fluids. The solver includes support for phase-change (fuel cavitation/condensation) by the implementation of the model by Schnerr and Sauer [43] with the extensions proposed by Yuan [44]. The cavitating fluid, the vapor and the non-condensable gas in the three-phase flow are represented in a single-fluid approximation as a mixture of phases, in which the phase-fraction distribution includes a sharp yet resolved transition between the phases. An algebraic-type VOF method belonging to the family of the interface-capturing methods [45] is used to capture the interface. Specifically, the interface is visualized by the contour of a scalar function, that is assumed to be the iso-value (set to 0.5 in this work) of the void fraction of the phase considered. Each phase i has a partial volume V_i , that is a fraction of the volume V of the cell element ($V_i \subseteq V$) and it is defined by its local volume fraction $\alpha_i \in [0;1]$:

$$\alpha_i = \frac{V_i}{V} \quad (5)$$

196 with:

$$\sum_{i=1}^3 \alpha_i = 1 \quad (6)$$

a “mixture” density:

$$\rho = \sum_i \alpha_i \rho_i \quad (7)$$

and a “mixture” viscosity:

$$\mu = \sum_i \alpha_i \mu_i \quad (8)$$

197 It is important to note that density in the solver varies with pressure, through the phase transport equations. The flow
 198 is assumed to be isothermal. The effect of the heat transfer on the temperature, that can be accounted by solving the
 199 energy equation, is not considered in the present work. As mentioned earlier, the difference in the liquid fuel and air
 200 temperature is about 10 K justifying the isothermal assumption. The complete system of equations for three-phase
 201 flow with phase change are the phase-fraction equations, that are written as:

$$\begin{cases} \frac{\partial \alpha_l}{\partial t} + \nabla \cdot (\mathbf{U} \alpha_l) = -\frac{S_\alpha}{\rho_l} \\ \frac{\partial \alpha_v}{\partial t} + \nabla \cdot (\mathbf{U} \alpha_v) = \frac{S_\alpha}{\rho_v} \\ \frac{\partial \alpha_{nc}}{\partial t} + \nabla \cdot (\mathbf{U} \alpha_{nc}) = 0 \end{cases} \quad (9)$$

In the system of equations (9), S_α is a source term to model the phase-change (cavitation or condensation) at the liquid interface through the cavitation model and couples the effects of the cavitation with the evolution of the interface directly:

$$S_\alpha = \frac{\rho_v \rho_l}{\rho + \alpha_{nc}(\rho_l - \rho_{nc})} \frac{D\alpha_v}{Dt} \quad (10)$$

202 In Eq. (10) the subscripts l and v denote the liquid and vapor (that are involved in the phase change) respectively, while
 203 the subscript nc denotes the non-condensable gases (air). It is important to note that the closure of the system of equa-
 204 tions (9) in presence of a cavitation/condensation source term S_α requires the explicit solution of a transport equation
 205 describing the third phase fraction (non-condensable phase). The solution of the transport equation describing the
 206 third fraction enables the inclusion of the cavitation model and the coupling of the equations with the compatibility
 207 condition (6). This procedure ensures that the system is closed and implicitly bounded on account of (6). In absence of
 208 source terms, 3-phase VOF solvers usually calculate the void fraction of non-condensable gases directly from Eq. (6),
 209 that is sufficient for closure only in that case. These aspects of the solution procedure are discussed in detail in [28],
 210 where the derivation of the full system of equations is shown and the formulation of the source terms for the phase
 211 change is also described. The discretization of the governing equations in the solver is based on the Finite-Volume
 212 (FV) approach as implemented in OpenFOAM [46]. Mass and momentum are solved using the pressure-implicit split-
 213 operator (PISO) algorithm [47]. Source terms for phase-change have been included in a semi-implicit formulation of
 214 the phase-fraction equations, where a flux corrected transport technique [48] is used to preserve boundedness of the
 215 solution. Detailed information about the solver is reported in [28].

216 LES turbulence modeling is used for the simulations, despite of its high computational cost, because of its better
 217 ability to characterize the different flow scales and therefore to capture the cavitation onset in the nozzle [49, 50,
 218 51, 52, 53, 54, 55]. Unsteady Reynolds Averaged Navier-Stokes (URANS) methods can significantly underestimate
 219 the formation and the extent of cavitation, because they usually overestimate the turbulent viscosity in the cavitating
 220 regions [56, 57, 58, 59, 60]; a possible solution to overcome the limitations of URANS to model cavitation consists
 221 of reduce the eddy-viscosity predicted by the turbulence model [56]. Synthetic turbulence fluctuations were applied
 222 to initialize the internal flow field and replicate the initial conditions of the stagnant air in the reservoir, according
 223 to the method implemented in [61].

224 In [62], several numerical results of primary breakup using an Adaptive Mesh Refinement (AMR) technique
 225 show fairly good agreement with experimental data. The multiphase solver used in this work is able to support
 226 dynamically load-balanced Adaptive Mesh Refinement (AMR), but the authors chose to use a static polyhedral grid
 227 because: a) dynamic refinement/coarsening being a topological change, it has a negative impact on the accuracy of the
 228 calculation of the temporal derivatives (see Appendix A of [63]); b) the operation of the LES filtering would change
 229 with the dynamic topological change of the mesh due to the AMR [63, 64]; c) in the LES simulations presented in
 230 this work, the initial grid is very fine: even with load balancing, AMR would have a non-negligible impact on the
 231 simulation time, because it requires the mesh connectivity to be updated with each mesh refinement. Furthermore,
 232 even though the solver supports dynamic load balancing with AMR, one has to set practical limits of load unbalance
 233 among processors (usually 25% imbalance) to avoid excessive wall time spent in attaining the optimal load balance,
 234 especially for simulations with large grid sizes. Due to these considerations, the use of fine static grids is chosen in
 235 this work. Full detail about the numerical setup used for the simulations is described and discussed in [28].

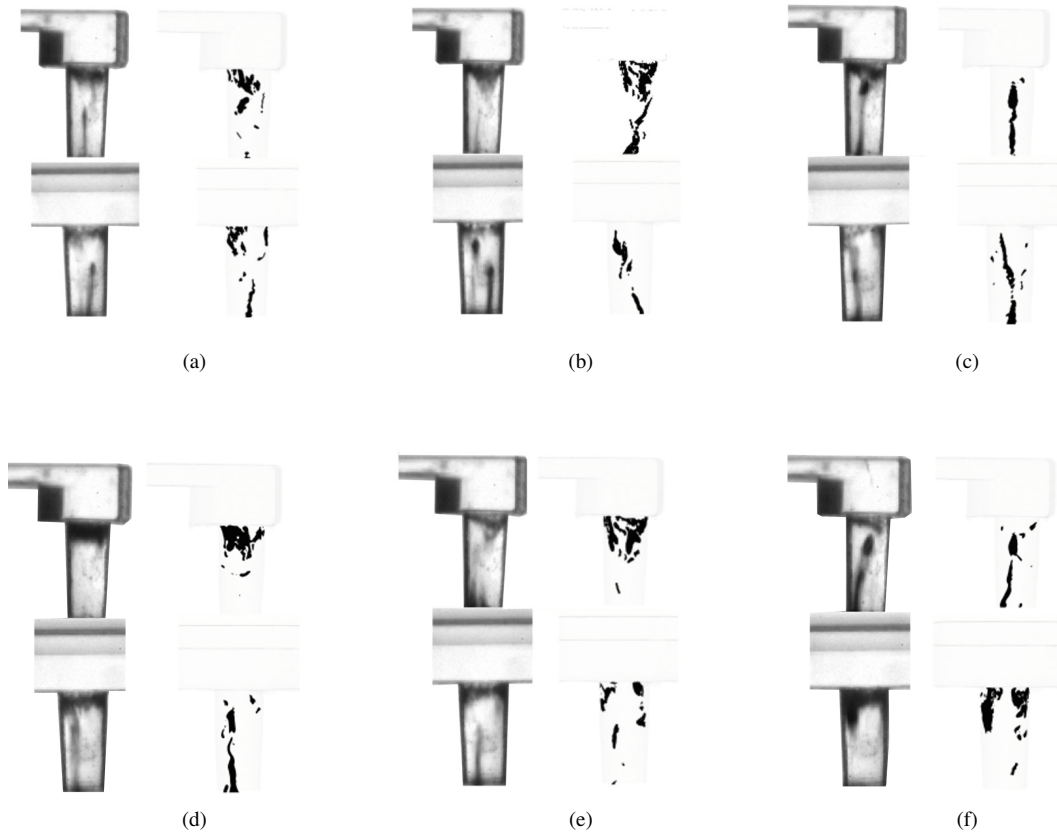


Figure 4: Configuration ID-3. Comparison of detected cavitation structures from experimental instantaneous shadowgraphies (left) and numerical simulations (right). Rows 1, 3: lateral view ($\theta = 90^\circ$). Rows 2, 4: front view ($\theta = 0^\circ$).

236 5. Validation

237 A validation by the comparison with experiments is presented, to prove the reliability of the solver to describe the
 238 cavitating structures occurring in the real glass nozzle injector. Experimental shadowgraph pictures of the cavitating
 239 areas have been realized using a long-range microscope (Navitar with home-made tubes from RDvision company) on
 240 the glass nozzle. A half-inch flexible fiber optic light guide mated with a powerful LED illuminator (white steady
 241 light). The camera is typically used with a exposure time of 2μ seconds, but it is also possible to use a non coherent
 242 light with a very short duration of the illumination (about 10 ns). Bubbles appear dark in the image, while liquid
 243 regions appear bright. The experimental setup and the measurements are described in [29].

244 Simulations results are generated as projected views of the three-dimensional iso-surfaces ($\alpha_v = 0.3$) of the fuel-
 245 vapor.

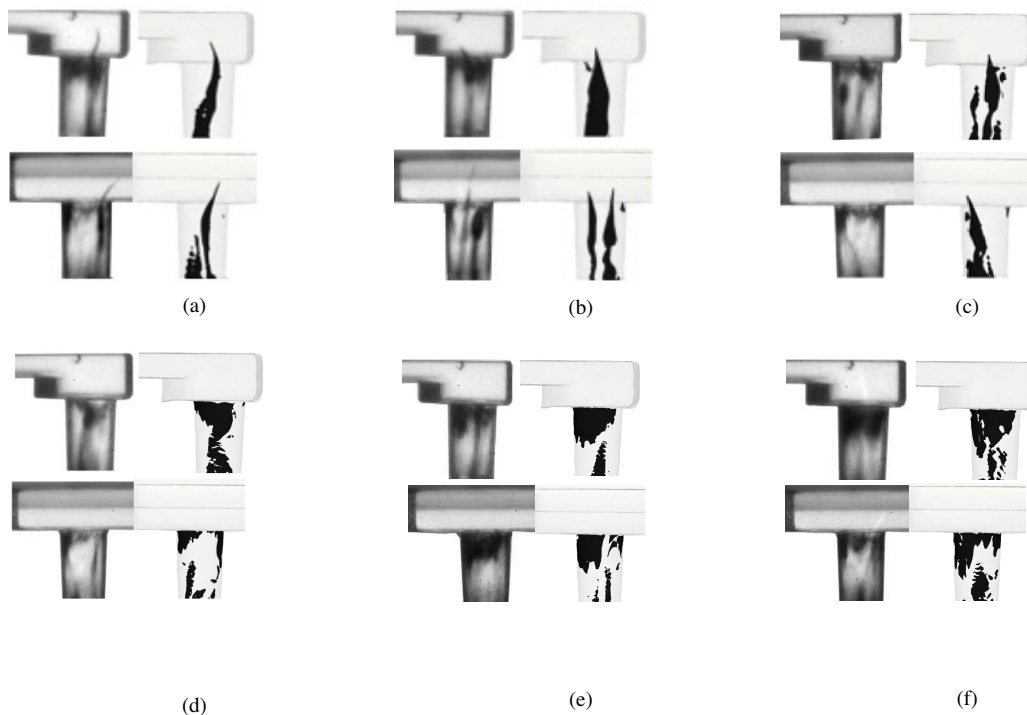


Figure 5: Configuration ID-10. Comparison of detected cavitation structures from experimental instantaneous shadowgraphies (left) and numerical simulations (right). Rows 1, 3: lateral view ($\theta = 90^\circ$). Rows 2, 4: front view ($\theta = 0^\circ$).

246 We report a comparison of numerical and experimental results on the front ($\theta = 0^\circ$) and lateral (side) view
 247 ($\theta = 90^\circ$) for the two injector configurations studied in this work. This kind of analysis can give a measure of
 248 reliability of the solver in describing the cavitating structures occurring inside the nozzle. In Figs. 4 and 5, a selection
 249 of instantaneous events from simulations and experiments are compared. The experimental visualizations using the
 250 front and lateral view are helpful to understand the contribution of each type of cavitation and the multiphase flow
 251 topology of each zone. Two different sets of images, namely a front ($\theta = 0^\circ$) and a lateral view ($\theta = 90^\circ$) have
 252 been realized by turning the injector sample around its axis. The flow through the two nozzles exhibits a moderate
 253 amount of cavitation, rarely noticed in the literature at the Cavitation and Reynolds numbers at which the injectors
 254 are operating (see Tab. 2). Central holes typically exhibit a circular, axisymmetric shear cavitation that develop over
 255 the section [29]; turning holes typically exhibit a large asymmetric single-side cavitation area [17, 65, 66]. In the
 256 cases studied, a moderate shear cavitation appears quite rarely, randomly, and it often involves a small portion of the
 257 nozzle area. Shear cavitation is directly driven by the low pressure area in the detached flow region in proximity of the
 258 hole entrance. Being the sharpness of the edge at the hole entrance directly linked to the intensity of the cavitation,
 259 the sharp edges at the hole entrance in the XCT-based virtual model have been manipulated by a CAD software; this
 260 ensures to be coherent with the measurements at the microscope and to cancel out the possible errors coming from
 261 the XCT-based reconstruction of the virtual model on those regions. The geometry has also been directly measured to
 262 generate the CAD, capturing some discrepancy in the asymmetry of the hole entrance. Few aspects help to explain this
 263 moderate shear cavitation in the two injector configurations. The geometry is a sector of a complex real nozzle: the
 264 shape includes a confined, non-negligible sac area. The role of the initial steep transition from the intake pipe to the
 265 sac volume causes a strong flow recirculation in the sac. Lastly, shear cavitation cannot develop along the complete
 266 hole due to its conicity and it vanishes at almost one third of the hole. Injectors ID-3 and ID-10 show very similar
 267 behavior in terms of shear cavitation. With such a moderate development of shear cavitation, the position of the strings
 268 of fuel-vapor can be quite easily distinguished by the shadowgraph pictures. This is especially useful because a large
 269 amount of string cavitation develops in the nozzle. String cavitation appears visually as vertical filaments. They can
 270 appear as a single full ligament, covering all the hole length. They can also appear partly at the hole entrance, at the
 271 hole end or in both (see Fig. 4 and 5). Ligaments mostly appear as vertical strings but some slight bending can be
 272 visible. String cavitation is more visible than shear cavitation in the geometries studied. This is a surprising result that

273 will be discussed in detail in the next sections. Additionally, in configuration ID-10, string cavitation is more intense
 274 than in ID-3. This is a consequence of the flow conditions at the hole entrance (due to the sac geometry) and of the
 275 hole geometry and it will be also discussed in the next sections.

276 It can be stated that simulations are reproducing with a very satisfying agreement the typical appearance either
 277 of shear and string cavitation. The LES-VOF solver [28] is able to capture the large, coherent eddies to reproduce
 278 accurately the complex features of the two phase flow, at least for the two studied cases. The fine-mesh is adapted
 279 to reproduce the asymmetry and small details of the shear cavitation zone and the cavitating vortex core. Despite the
 280 large grid used, space filtering used certainly cannot properly describe the thinnest vortex cavitating cores.

281 6. Flow Analysis

282 The agreement achieved between simulations and experimental visualizations allows us to consider the simulation
 283 reliable enough to be used for the in-nozzle multiphase flow analysis. The main features of the flow pattern in the
 284 geometries studied are summarized in the sketch of Fig. 7: the flow pattern presents two secondary vortices on the
 285 sides, that turn into two three-dimensional counter-rotating vortical structures centered in the nozzle axis. Only after
 286 entering into the nozzle, the rotation axis of these vortical structures tends to align with the nozzle axis.

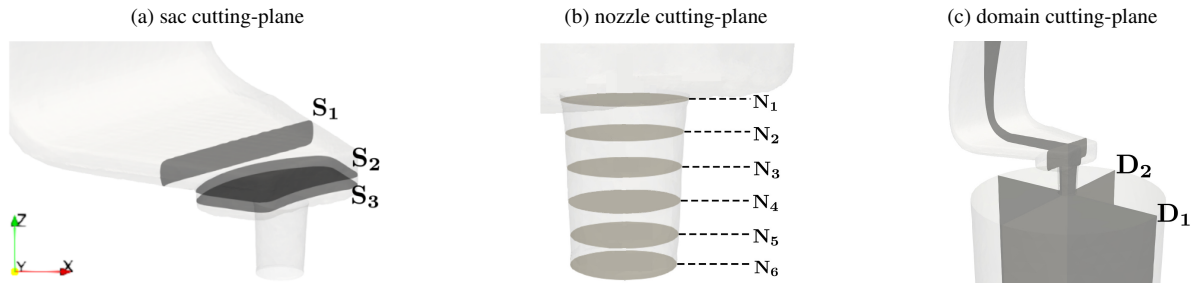


Figure 6: The flow analysis is based on time- and space- averaged flow quantities over: a) the three cross sections S_1 , S_2 and S_3 located in the sac; b) cross-planes N_i , $i \in [1; 6]$ along the nozzle; c) two cutting planes, D_1 (lateral) and D_2 (frontal), parallel to the nozzle axis are defined by the $\theta_1=0^\circ$ and $\theta_2=90^\circ$ respectively.

287 The study presented in this paper aims at providing a detailed characterization of the in-nozzle flow field, to
 288 study the influence of the sac geometry on the formation of shear and vortex cavitation. A qualitative comparison of
 289 numerical and experimental visualizations for the two configurations, is used for validation and it is shown first. Then,
 290 a deep analysis of the in-nozzle flow features is presented and it is organized as follows:

- 291 1) *study of the influence of the feeding system/nozzle sac on the flow field at the nozzle entrance.* Flow features in
 292 the sac volume are studied; additionally, the fuel distribution at the nozzle inlet section for the two configurations
 293 investigated are studied, to identify the regions where the flow detachment and the largest recirculation occurs
 294 (Sec. 6.1);
- 295 2) *study of the internal nozzle flow field and evolution of the shear and string cavitation.* Time-averaged velocity
 296 magnitude, static pressure, liquid volume fraction and nozzle-streamwise vorticity are plotted in the nozzle to
 297 identify the cavitating regions of the flow; they are used to visualize the counter-rotating vortical structures and
 298 secondary vortices in the nozzle, their intensity and direction of rotation and how they radially expand (see Sec.
 299 7).
- 300 3) computation of the *time-averaged values of nozzle coefficients* (Sec. 8) and an unsteady flow analysis is pre-
 301 sented in Sec. 9.

302 The flow analysis is based on time- and space- averaged flow quantities over several cross planes, namely: a) the
 303 three cross sections S_1 , S_2 and S_3 located in the sac, Fig. 6a; b) six cross-planes in the nozzle, referred as to $N_1 - N_6$
 304 (Fig. 6b); c) two cutting planes, that will be referred in the following as to D_1 and D_2 (see Fig. 6c).

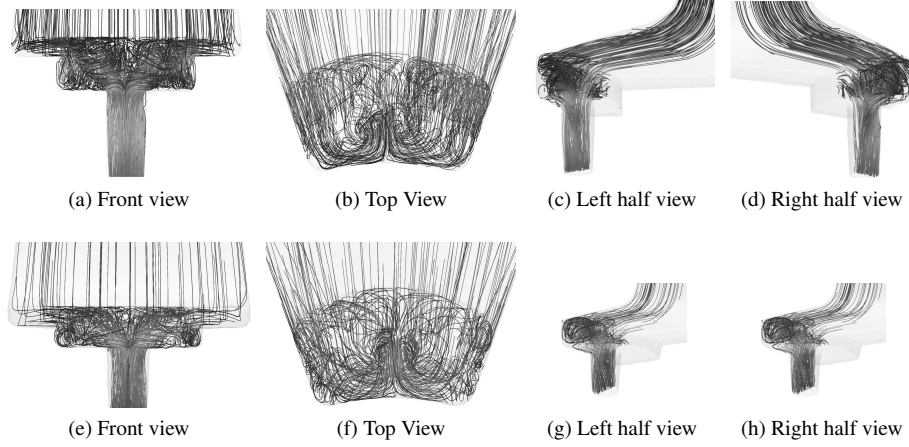


Figure 7: Three-dimensional representation of the average streamlines for injector configuration ID-3 (a-d) and ID-10 (e-h).

6.1. Influence of the feeding system/nozzle sac on the flow field at the nozzle entrance

Fig. 8 and Fig. 9 show the contour plots describing the main features of the flow field on planes S_1 , S_2 and S_3 of Fig. 6c for injectors ID-3 and ID-10 respectively. Differences in the velocity field between the two configurations, in terms of mean value and fluctuations, are a consequence of the different geometry of the feeding system and in the lift (see Fig. 1). While entering into the sac, the flow then separates and a recirculating region forms, as apparent by plane S_2 (Figs. 8 and 9, d-f). This region is wider for configuration ID-10 and becomes larger at the nozzle inlet section (plane S_3 , Figs. 8 and 9, g-i), where the velocity profile is almost symmetric. Differences in the average flow velocity and in the flow-symmetry in section S_1 are responsible of the different vortical structures evidenced on planes S_2 and S_3 for the two injector configurations. Flow separation is visible on plane S_2 (Fig. 8 and 9, d-f): two small vortices appear on the side walls and they are also present in both configurations on plane S_3 . The intensity of the flow separation can qualitatively be estimated by observing the different extension of the side vortices. In both cases, the largest average flow velocity is located near the nozzle entrance, as also evidenced by the two-dimensional streamlines in Fig. 8g-i and 9g-i. It is interesting to observe that in configuration ID-3, the average flow velocity and fluctuations are spread over a larger area on sections S_2 and S_3 ; this is most probably due to the shorter volume of the dead space and of the nozzle, that favors a reverse flow that interacts with the central counter rotating vortices. Fig. 10 and 11 show the contour plots of the velocity flow field on planes D_1 (a-c) and D_2 (d-f); for both injectors, the reverse flow generated from the recirculation in the dead zone of the sac limits the extension of the recirculating zone from the step, as clearly confirmed by contour plots on plane D_1 . The visualizations show that flow features are similar for the two injectors in the flow sac and at the nozzle entrance; on the other hand the flow field for the two injectors is very different in the nozzle, as apparent in Figs. 10 and 11.

Config.	Plane S_1		Plane S_2		Plane S_3	
	ID-10	ID-3	ID-10	ID-3	ID-10	ID-3
$\langle \bar{U} \rangle$ [m/s]	56.64	43.05	27.53	15.34	19.29	15.45

Table 3: area-weighted average of $\langle U \rangle$ for plane S_1 , S_2 and S_3 .

To summarize, different sac geometries of the two injectors provide very similar flow distributions at the nozzle entrance and comparable average velocity in sections S_2 and S_3 , as shown in Tab. 3. On the other hand, the flow atomization of the two injector configurations at the nozzle outlets is very different: a possible reason for this might be a different amount of cavitation for the two nozzle configurations. The following analysis is focused to a more quantitative estimation of these statements.

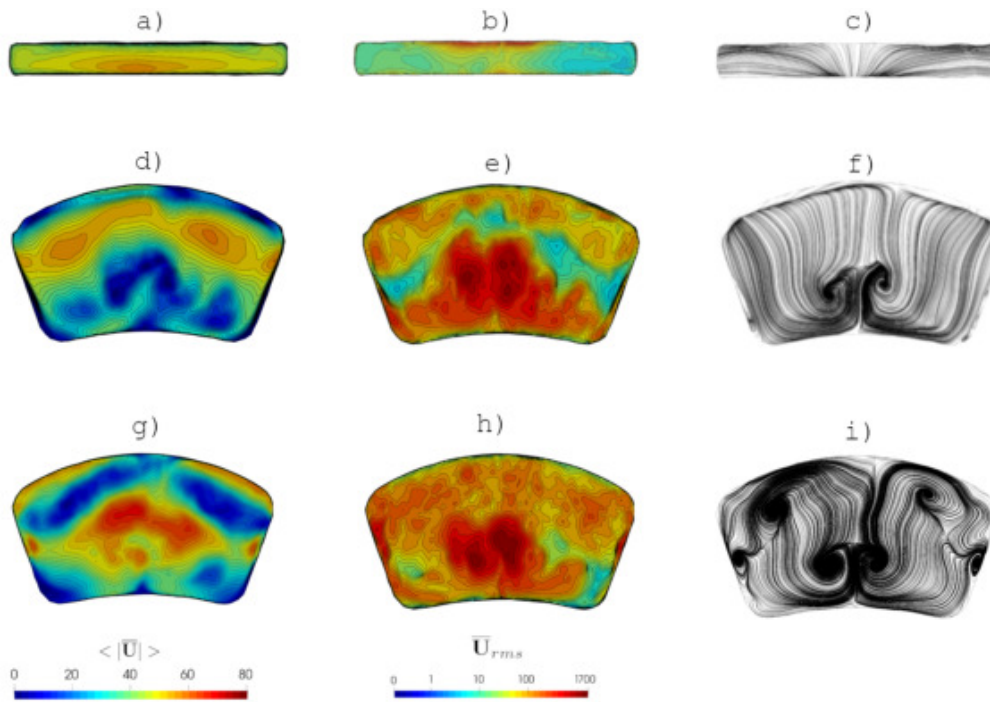


Figure 8: flow analysis on planes S_i ($i=1, \dots, 3$) of Fig. 6 for injector ID-3: plane S_1 (a-c), plane S_2 (d-f) and plane S_3 (g-i). Time-averaged mean flow velocity (a,d,g); time-average velocity fluctuations (b,e,h); velocity streamlines (c,f,i).

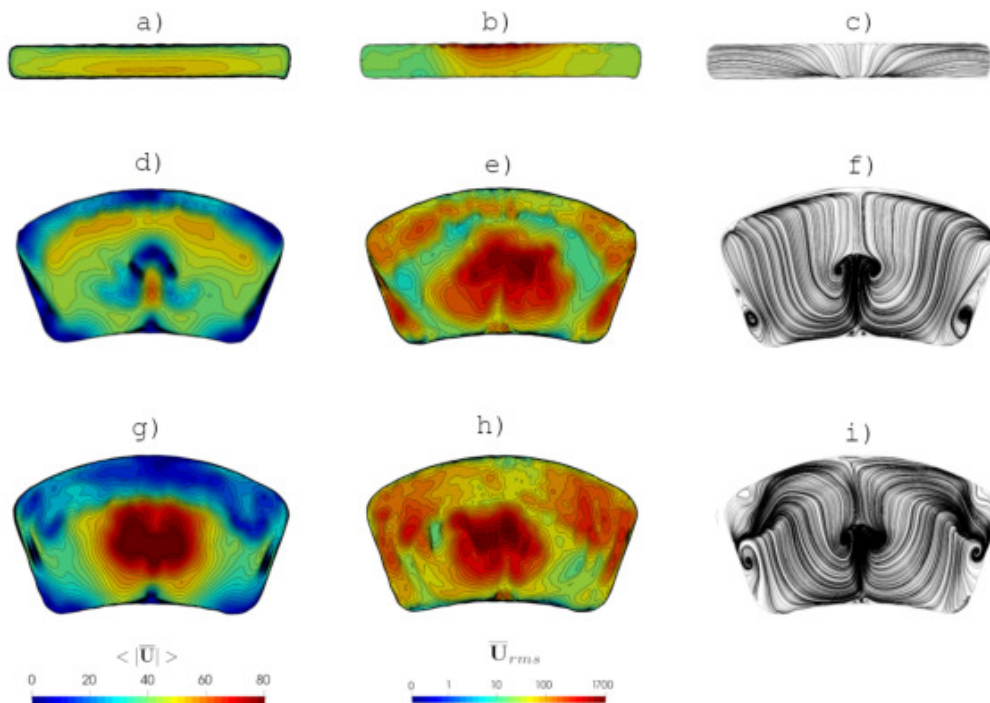


Figure 9: flow analysis on planes S_i ($i=1, \dots, 3$) of Fig. 6 for injector ID-10: plane S_1 (a-c), plane S_2 (d-f) and plane S_3 (g-i). Time-averaged mean flow velocity (a,d,g); time-average velocity fluctuations (b,e,h); velocity streamlines (c,f,i).

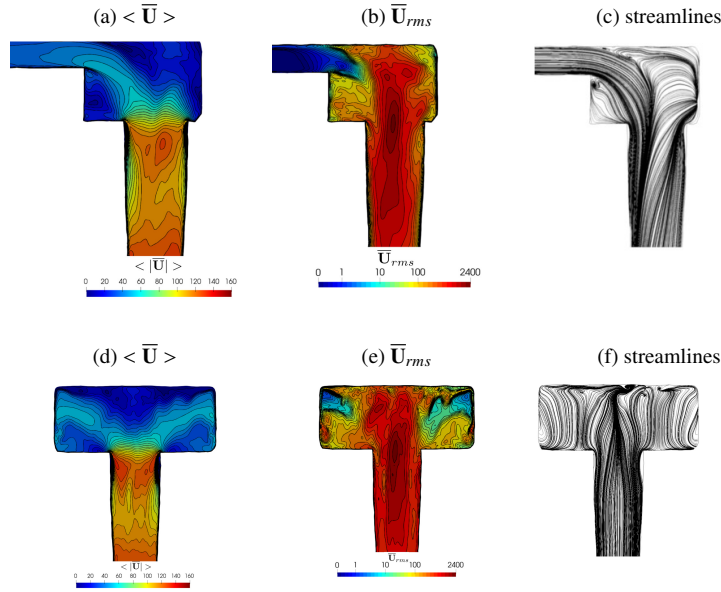


Figure 10: Configuration ID-3: velocity flow field on planes D_1 (a-c) and D_2 (d-f).

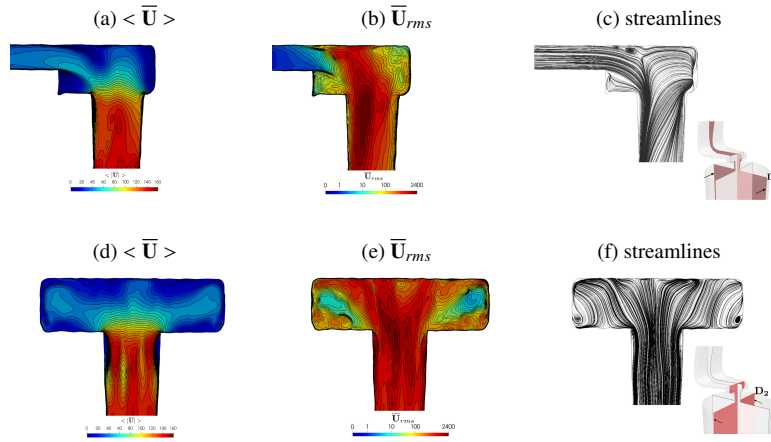


Figure 11: Configuration ID-10: velocity flow field on planes D_1 (a-c) and D_2 (d-f).

330 7. In-nozzle flow field

A main goal of this research is to identify the mechanisms driving to very different flow atomization in the two injector nozzles. The two injectors studied operate at the same injection pressure and very similar Mass Flow Rate (MFR), see Fig. 20. The volume of the region where flow recirculation occurs is not very different among the two geometries. Also the sector angle is the same. They present different sac heights and hole-to-step distances (named here offs-H) though, while the fuel pattern in the injector sac volume does now show relevant differences in the flow features, as seen in Figs. 7, 8, 9, 10 and 11. Also the flow pattern at the hole entrance is very similar. The pattern of the primary flow coming from the inlet channel separates while it encounters a step and it immediately turns to enter into the hole. Similarly to the Backward Facing Step (BFS), where the flow characteristics can be linked to its aspect ratio, it is here proposed a ratio r to characterize the separating flow in the sac of the injector, defined as:

$$r = \frac{\text{lift} + H}{\text{off-H}} \quad (11)$$

331 The discrepancy between the values of r calculated for ID-3 and ID-10 lies in a range of 5%: from (11), $r= 2.12$ for
 332 ID-3, while $r= 2$ for ID-10.

333 We focus then our attention: a) on the study of the formation of vortices at the hole entrance (plane \mathbf{N}_1); b) on the
 334 analysis of the evolution of the in-nozzle flow, by the information provided by the validated high-fidelity simulations.
 335 Two parameters are identified as possible promoters for the formation of string vortices at the hole entrance: the
 336 development of the streamwise vorticity and the amount of the tangential flow velocity on plane \mathbf{N}_1 , as shown in Fig.
 337 12. For each cell of plane \mathbf{N}_1 with reference to Fig. 12, the flow is labelled as *side flow* ($|\overline{U}_z| > |\overline{U}_x|$), *direct flow*
 338 ($|\overline{U}_x| > |\overline{U}_z| \cap \overline{U}_x > 0$) and *reverse flow* ($|\overline{U}_x| > |\overline{U}_z| \cap \overline{U}_x < 0$).

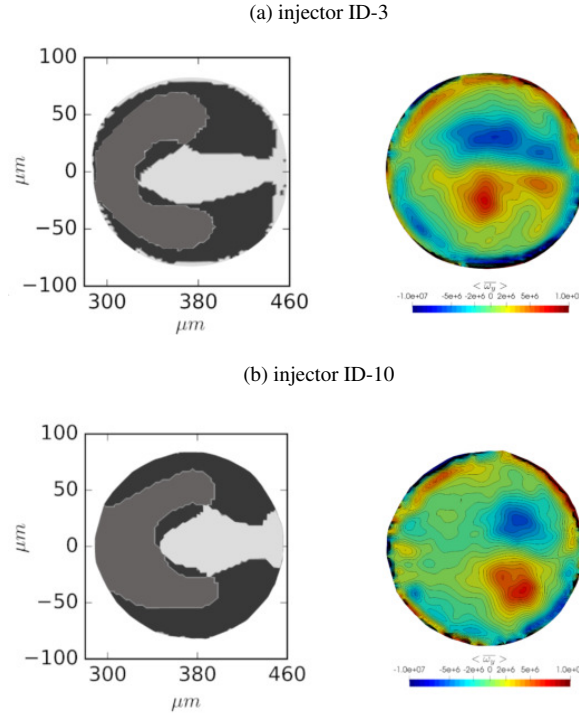


Figure 12: flow features on plane \mathbf{N}_1 for injector configurations ID-3 and ID-10. Left: ■ direct flow ■ side flow ■ reverse flow. Right: time-averaged flow vorticity.

339 Results for the two injector configurations studied are reported in Fig. 12 and in Tab. 4. For both injectors, the
 340 percentage of cells where the side, reverse and direct flow on section N_1 is very similar. Also, the area magnitude, the
 341 average mass-flow rate (MFR) and the average velocity on the plane N_1 for the two injectors do not differ significantly.

	ID-3			ID-10		
	side	direct	reverse	side	direct	reverse
Area [%]	44.5	35.8	19.7	43.9	33.3	23.8
MFR [g/s]	0.66	0.6	0.3	0.682	0.59	0.31
$\langle \overline{U} \rangle$ [m/s]	99.5	113.3	103.9	100.3	118.5	84.8

Table 4: percentage of the area of plane \mathbf{N}_1 , velocity magnitude and mass-flow rate (MFR) of different types of flows: side/direct/reverse.

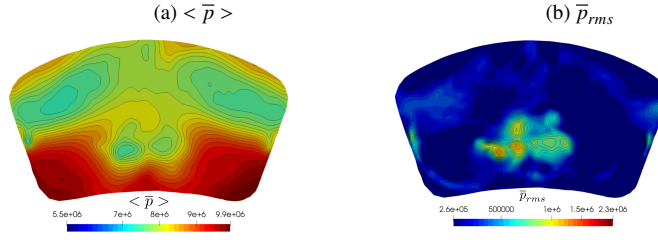


Figure 13: injector ID-3, plane S_3 of Fig. 6. Pressure field (a) and pressure RMS (b). Quantities are time-averaged.

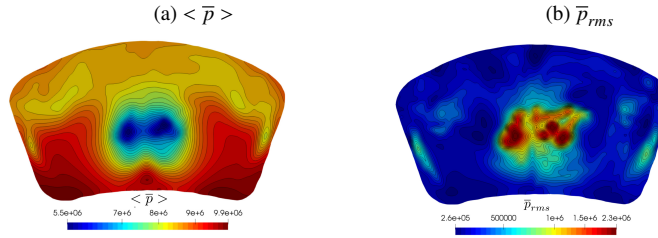


Figure 14: injector ID-10, plane S_3 of Fig. 6. Pressure field (a) and pressure RMS (b). Quantities are time-averaged.

342 Besides, the contour plot of the time-averaged vorticity on plane N_1 evidences some difference in the vortex
 343 structures at the entrance of the hole; these differences are not sufficiently large to identify the sac geometry as a main
 344 driver of the different flow cavitation along the nozzle and, eventually, of the different spray atomization at the nozzle
 345 outlet. The same holds for the average pressure level in the sac, as reported in Figs. 13, Fig. 14 and in Tab. 5).

346 It can be therefore concluded that the different geometry of the sac in the two injectors is not the main driver for
 347 the flow atomization at the nozzle exit.

	plane S_1		plane S_2		plane S_3	
	ID-10	ID-3	ID-10	ID-3	ID-10	ID-3
$\langle \bar{p} \rangle$ [bar]	91.31	91.16	87.53	87.18	85.69	83.27

Table 5: area-weighted average of $\langle \bar{p} \rangle$ for plane S_1 , S_2 and S_3

348 Since the nozzle inlet and outlet diameters are the same for the two injectors, it is reasonable to think that different
 349 flow features in the injectors are driven by the nozzle length and this, in turn, has an impact on the pressure field inside
 350 the nozzles. The pressure drop over the nozzle is the same for the two injectors, since it is forced by the boundary
 351 conditions: liquid pressure is 100 bar at the inlet and the reservoir where the fuel is injected is at ambient pressure.
 352 This is apparent from Figs. 15 and 16, where the average pressure field and the fluctuations in pressure are reported
 353 for planes D_1 and D_2 of Fig. 6. Besides, different nozzle lengths affect the capability of the flow to reorganize.

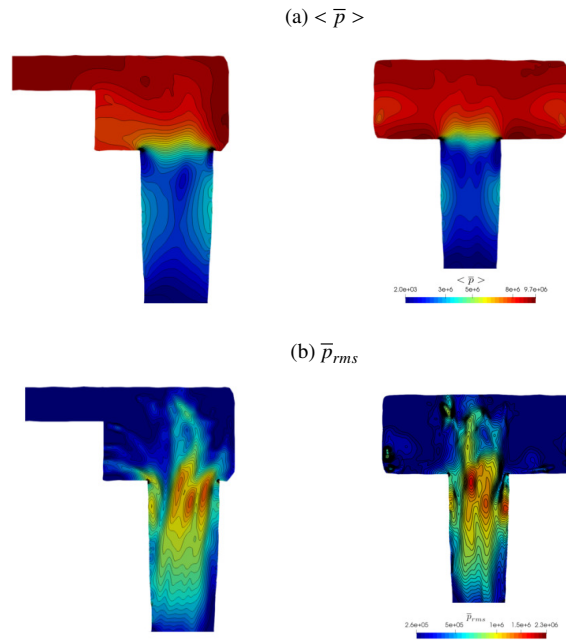


Figure 15: injector ID-3: a) time-averaged pressure field $\langle \bar{p} \rangle$; b) time-averaged pressure rms \bar{p}_{rms} on sections **D1** (left) and **D2** (right) of Fig. 6.

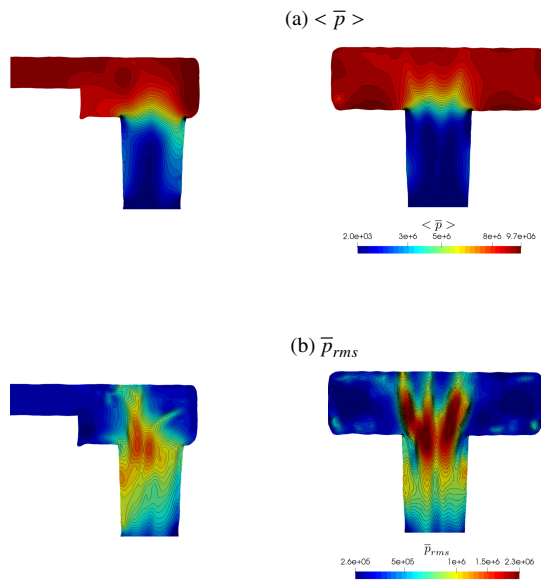


Figure 16: injector ID-10: a) time-averaged pressure field $\langle \bar{p} \rangle$; b) time-averaged pressure rms \bar{p}_{rms} on sections **D1** (left) and **D2** (right) of Fig. 6.

354 Pressure losses occur at the nozzle entrance; there, a recirculating region forms and shear cavitation is observed
 355 while a vortex core also generates. From the time-averaged pressure field in Figs. 13, 14, 15a and 16a, it is not
 356 possible to detect the appearance of cavitating strings in the nozzle. Being the string cavitation a very seldom and
 357 random phenomenon, it might be canceled by the time-averaging procedure. Therefore, the appearance of cavitating
 358 strings is detected by looking at high pressure fluctuations in the nozzle, Figs. 15b and 16b. In regions where the
 359 intensity of pressure fluctuations is of the same order of magnitude of the mean flow pressure, string cavitation might
 360 occur. In Figs. 13 and 14, the flow pressure significantly deviates from the average condition; since vortices are not

361 stable within the sac but they periodically grow and disrupt, those strings represent spots where string cavitation is
362 likely to occur (see also Figs. 4 and 5 for comparison). Being strings stretched over the nozzle, the L/D ratio and the
363 conicity factor K_g are of foremost importance to influence the evolution of the pressure field in the nozzle.

364 It is important to mention that the three-phase solver does not detect any presence of air in the hole at the mentioned
365 operating conditions for the two injector configuration, as also confirmed in [29].

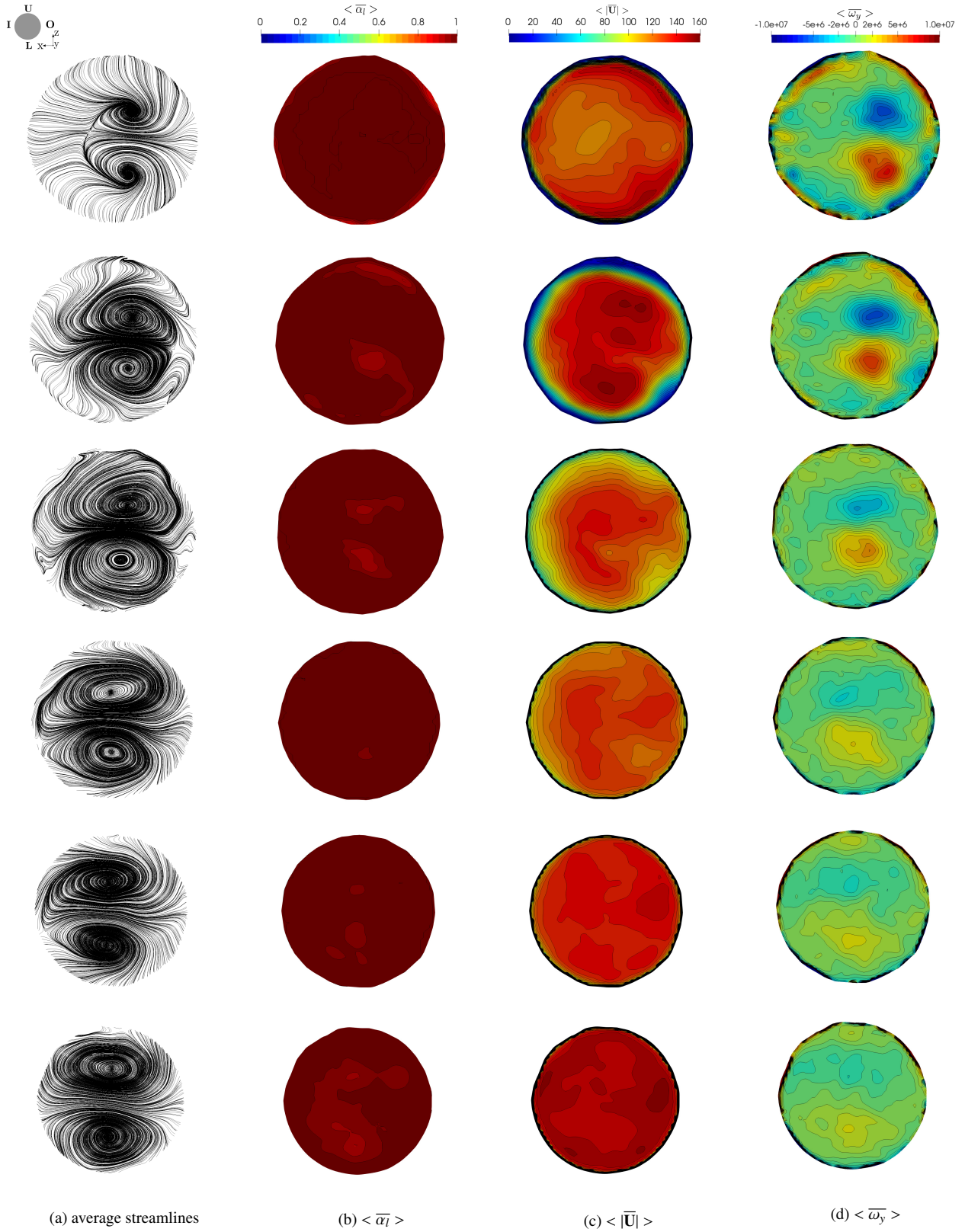


Figure 17: injector ID-3: average quantities on nozzle cutting planes $N_1, N_2, N_3, N_4, N_5, N_6$ (from top to bottom).

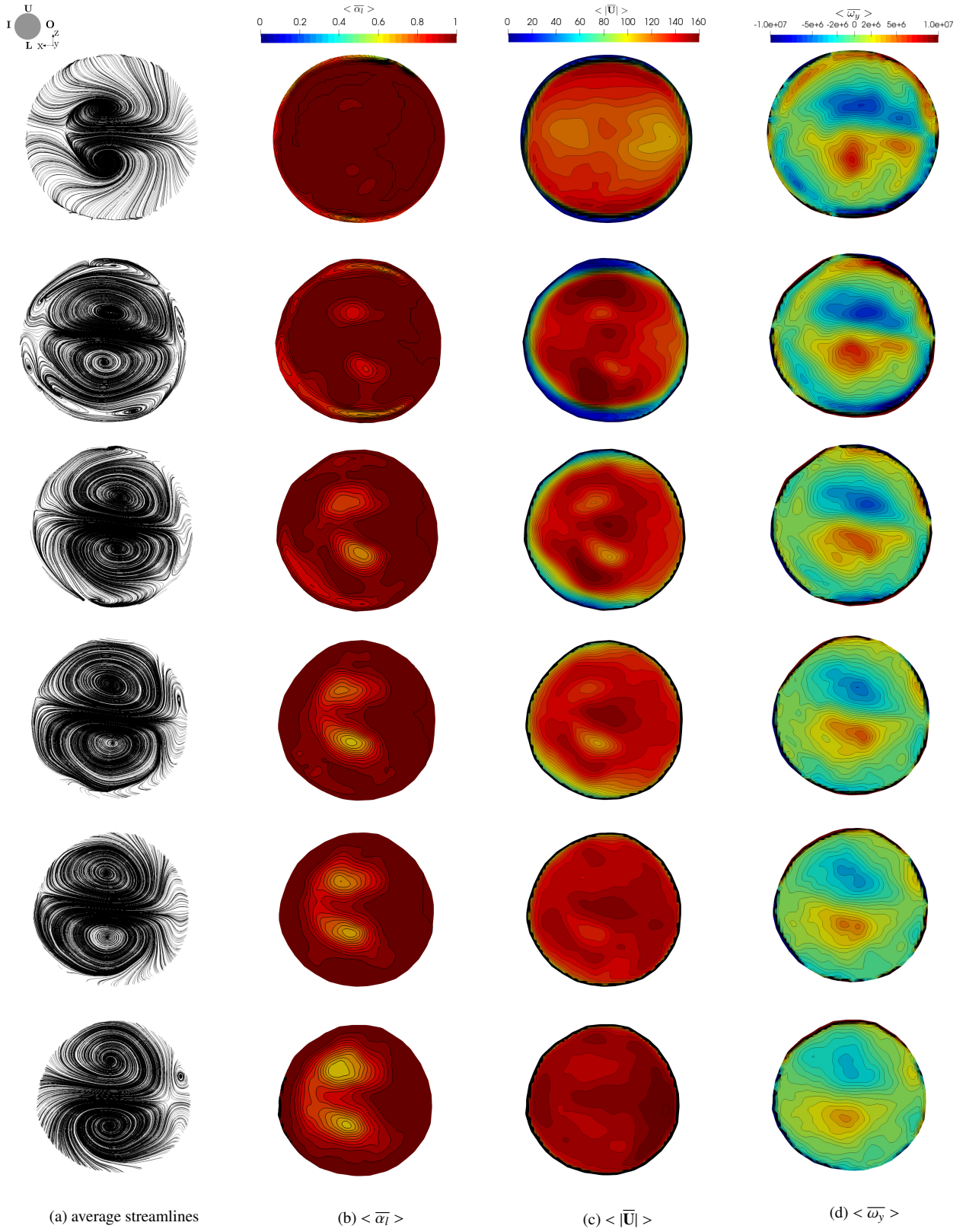


Figure 18: injector ID-10: average quantities on nozzle cutting planes $N_1, N_2, N_3, N_4, N_5, N_6$ (from top to bottom).

366 In Fig. 17b and 18b, the time-averaged liquid fraction over planes N_1 to N_6 is shown. Near the nozzle wall of
 367 injector ID-3 (Fig. 17b), the flow from the sac detaches and shear cavitation appears in a recirculating low-pressure
 368 region. On plane N_4 , the flow is fully reattached, as evidenced by the streamlines (Fig. 17a). At the center of the
 369 nozzle hole, the contour plots of the vorticity (Fig. 17d), of the streamlines (Fig. 17a) and of the flow velocity (Fig.
 370 17c) highlight the formation of a small amount of fuel vapor at the hole center on plane N_3 , where two counter-rotating
 371 vortices appear. The large average flow pressure, maintained in ID-3 over the short length of the nozzle (Fig. 19d),
 372 avoids a strong vortex cavitation and, consequently, a strong atomization of the flow.

373 Also in injector ID-10 (Fig. 17), shear cavitation is triggered by the flow detachment near the nozzle walls on
 374 planes N_2 and N_3 (Fig. 18b). On planes N_4 , N_5 and N_6 string cavitation progressively becomes stronger; besides,
 375 cavitating vortices favors a faster flow reattachment at the walls. As a consequence, the flow velocity in injector ID-10
 376 is larger and the average pressure is lower (Fig. 18c), if compared to injector ID-3. The resulting stronger amount of
 377 cavitation causes the stronger atomization of the flow.

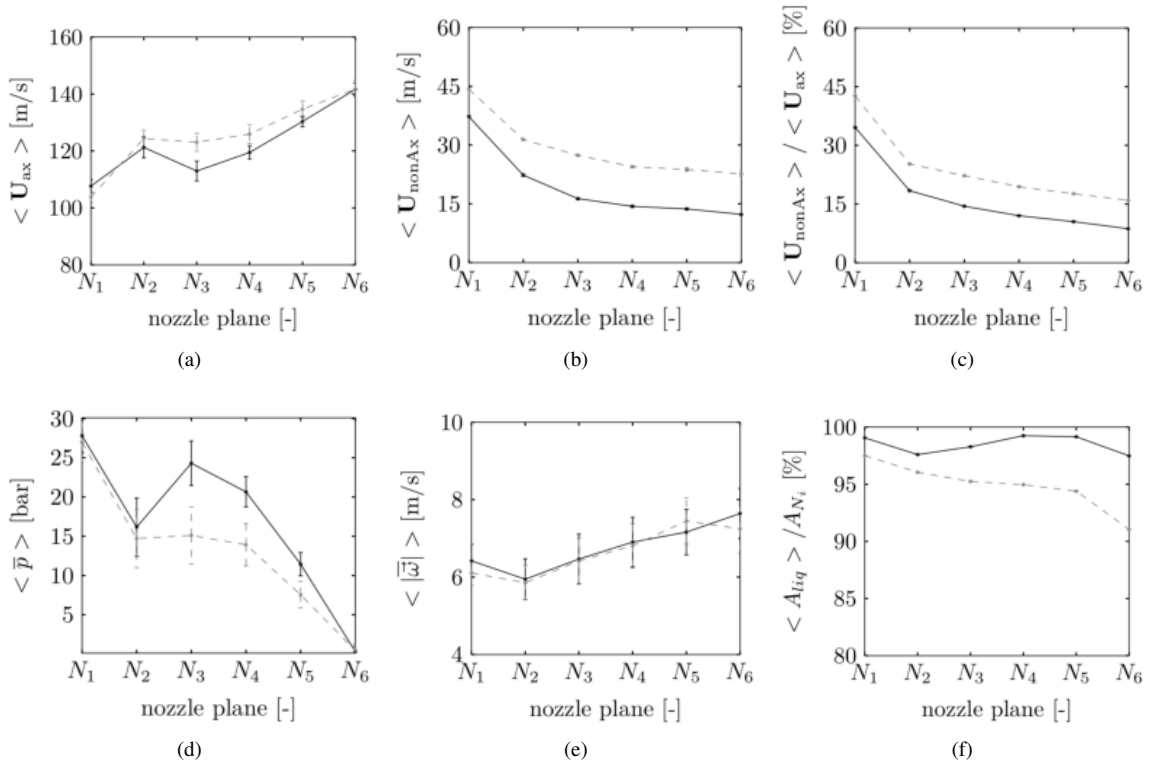


Figure 19: Mean values over the nozzle axis, on planes N_1 to N_6 , of time-averaged quantities: 1) MFR-weighted average axial velocity; b) magnitude of the MFR-weighted average non-axial velocity; c) radial/axial velocity ratio; d) average pressure; e) MFR-weighted vorticity magnitude; f) liquid area over cross sectional area. Legend: — ID-3; - - ID-10.

378 In Fig. 19a, a comparison between the two injectors is carried out by looking at the main features of the flow
 379 in the nozzle holes. Quantities over six equispaced parallel planes in the nozzle holes (N_1 - N_6 of Fig. 6) are plotted.
 380 The position of each plane is normalized by the length of the nozzle. From Figs. 19a, it is apparent that the axial
 381 component of the flow velocity is progressively increasing over the injector nozzles. This is a direct consequence of
 382 the combined effect of the nozzle conicity K_g and of the cavitation. Swirling vortices generated at the nozzle entrance
 383 expand and progressively disappear in proximity of the nozzle end (planes N_4 – N_6); the magnitude of the non-axial
 384 velocity therefore reduces (Fig. 19b) and the axial velocity progressively increases (Fig. 19a), so that the ratio among
 385 the two quantities is decreasing (Fig. 19c). Because of the acceleration of the flow in the hole (Fig. 19a), shear
 386 cavitation tends to disappear. The larger non-axial velocity in injector ID-10 (see Fig. 19b) favors a stronger string
 387 cavitation. This is also confirmed by Fig. 19f. The corresponding time-averaged mean pressure over planes N_1 - N_6
 388 is shown in Fig. 19d. As expected, time-averaged pressures on planes N_1 and N_6 are the same, being forced by the
 389 boundary conditions. A stronger pressure recovery to the atmospheric pressure is noticed for ID-10 near the nozzle

390 exit, between planes \mathbf{N}_5 and \mathbf{N}_6 . The larger conicity factor k_{geom} of injector ID-3 favors a pressure recovery of almost
 391 the 85% of the nozzle average inlet pressure, with a local maximum at plane N_3 . The longer hole of injector ID-3
 392 allows for the formation of larger detachment regions at the nozzle entrance and favors a different intensity of swirl
 393 cavitation. The vorticity magnitude (Fig. 19e) has a similar trend in the two configurations, but ID-3 shows a stronger
 394 decay while the flow is reaching the nozzle end. Also, the liquid area of the flow on the different nozzle sections
 395 $\mathbf{N}_1 - \mathbf{N}_6$ (Fig. 19f) is larger for injector ID-3, as a consequence of a weaker cavitation of the liquid along the nozzle.
 396 The higher conicity of injector ID-3 results in a lower atomization of the liquid, that fills most of the nozzle area on
 397 sections $\mathbf{N}_3 - \mathbf{N}_6$.

398 8. Discharge coefficient

Fig. 20 shows the variation in time of some relevant parameters for the injectors ID-3 and ID-10 at the nozzle outlet (plane N_6), namely: the discharge coefficient C_d , the velocity coefficient C_v , the area coefficient C_a and the liquid void fraction α_l . The discharge coefficient C_d of the injectors is computed as:

$$C_d = \frac{\langle \dot{m} \rangle}{\dot{m}_{th}} = \frac{A_{eff} U_{eff} \rho_l}{A_{th} U_{th} \rho_l} = C_a C_v \quad (12)$$

where A_{th} and A_{eff} is the real geometric cross sectional area of plane N_6 , ρ_l is the density of the liquid fuel and $\langle \dot{m} \rangle$ is the average mass flow rate from the simulation, \dot{m}_{th} is the mass flow rate calculated using the velocity from the Bernoulli theorem:

$$U_{th} = \sqrt{\frac{2(p_{inj} - p_{back})}{\rho_l}} \quad (13)$$

399 From Eq. (12), C_d is calculated as the product of two coefficients:

- the velocity coefficient C_v , defined as the ratio between the actual and the ideal velocity, calculated by the Bernoulli's theorem (see Eq. 13):

$$C_v = \frac{U_{eff}}{U_{th}} \quad (14)$$

where U_{eff} is computed using the normal area average:

$$\frac{\sum_{j=1}^k \langle \bar{\mathbf{U}}_j \rangle \cdot \mathbf{S}_{f,j}}{\sum_{j=1}^k |\mathbf{S}_{f,j}|} \quad (15)$$

400 In Eq. (15), k is the number of cell faces that are used for the discretization of the plane where the spatial
 401 average is computed; $\langle \bar{\mathbf{U}}_j \rangle$ is the time-averaged velocity on the j -th face, $\mathbf{S}_{f,j}$ is the surface area vector of the
 402 j -th face computed as $|\mathbf{S}_{f,j}| \cdot \hat{\mathbf{n}}_j$ where $\hat{\mathbf{n}}_j$ is the unity normal vector to the j -th face of the surface;

- the area coefficient C_a :

$$C_a = \frac{A_{eff}}{A_{th}} \quad (16)$$

is defined as the ratio between effective area to the geometrical area, measured by XCT, being:

$$A_{eff} = \sum_{j=1}^k |\mathbf{S}_{f,j}|_{(\langle \bar{\mathbf{U}} \rangle_j \cdot \hat{\mathbf{n}}_j > 0) \cap (\langle \bar{\alpha}_l \rangle_j = 1)} \quad (17)$$

403 In Eq. (17), the condition $(\langle \bar{\mathbf{U}} \rangle_j \cdot \hat{\mathbf{n}}_j) > 0$ ensures to compute the effective area on the basis of the liquid
 404 leaving the nozzle ($\langle \bar{\alpha}_l \rangle_j = 1$).

405 Density variations in the nozzle due to phase-change are taken into account by C_d and C_v (together with C_a , they
 406 are listed in Tab. 8). Oscillations in the C_a are mostly linked to changes of α_l (Fig. 20): the presence of vapor at the
 407 outlet reduces the available area to inject liquid fuel, Figs. 10 and 11; additionally, it is also responsible for oscillations
 408 in the mass flow rate.

	ID-3	ID-10
C_d	0.79048	0.74705
C_a	0.93162	0.9077
C_v	0.84847	0.823

Table 6: Values of the coefficients C_d , C_a and C_v from the numerical simulations for injector ID-3 and ID-10. Time averaging starts after $t = 110 \mu\text{s}$, when the influence of the initial conditions on the solution is assumed to be negligible.

409 The discharge coefficient is therefore influenced by the ratio between the fuel-vapor and the liquid. Pressure losses
 410 in the sac and at nozzle entrance (plane N_1) also influence the discharge coefficient, but those are not linked to the
 411 amount of phase change. The shorter nozzle length of injector ID-3 favors a higher recovery of the initial kinetic
 412 energy, as apparent from its values of C_d and C_v . The flow detachment for this configuration does not extend to the
 413 outlet section (plane N_6), while the convergent nozzle geometry contributes to recover a part of initial kinetic energy.
 414 The rate of the kinetic energy between planes N_3 and N_6 is the larger for ID-3 than for ID-10, as reported in Fig. 19a.

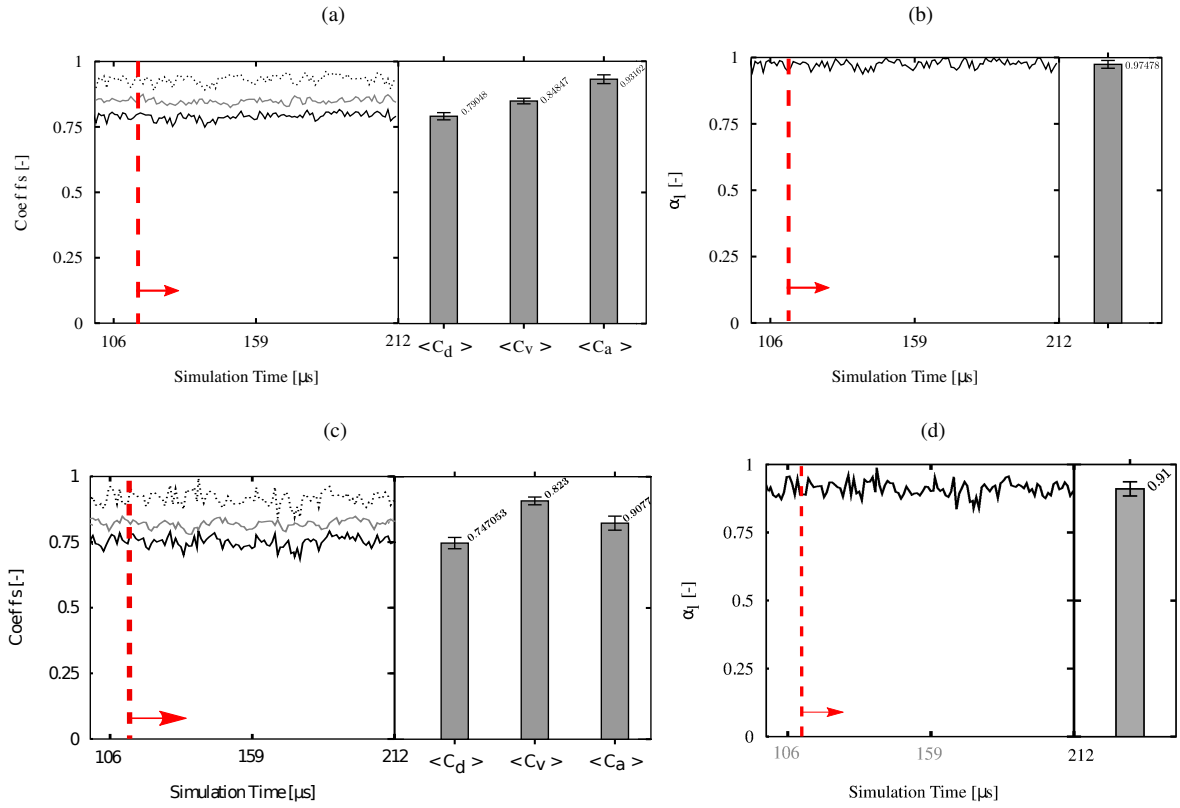


Figure 20: Evolution in time and time-averaged of C_d , C_v , C_a and of the area-weighted liquid fraction on plane N_6 for ID-3 (a, b) and ID-10 (c, d). Time averaging is performed on a time interval of $80 \mu\text{s}$ of the simulation, starting from $t = 132 \mu\text{s}$. Legend: a, c) — C_d ; - - - C_v ; — C_a ; b, d) — area-weighted liquid fraction.

415 9. Unsteady vortex flow physics and behavior

416 An analysis of the unsteady vortex flow physics in the nozzle is presented for configuration ID-10, because it
 417 exhibits a stronger cavitation with respect to configuration ID-3. Starting from $t = 117 \mu\text{s}$ (red dashed line, Fig. 20),
 418 forty-one snapshots (Figs. 23 and Fig. 22) in a time interval of $90 \mu\text{s}$ of the simulation were analyzed, corresponding
 419 to two flow-through times of the hole. For each snapshot, the nature of the newly generated amount of fuel vapor in the
 420 volume was observed and it was classified as follows: a) if the fuel vapor was found near the walls, in a recirculating
 421 region or along the nozzle axis, then its origin was attributed to the shear cavitation; b) if the new fuel-vapor was

422 found far from the walls and it was included in a swirling vortex, then its origin was attributed to string cavitation.
 423 The criterion mentioned above has been applied to each snapshot to characterize the cavitation in the nozzle and
 424 populate the plots of Fig. 21.

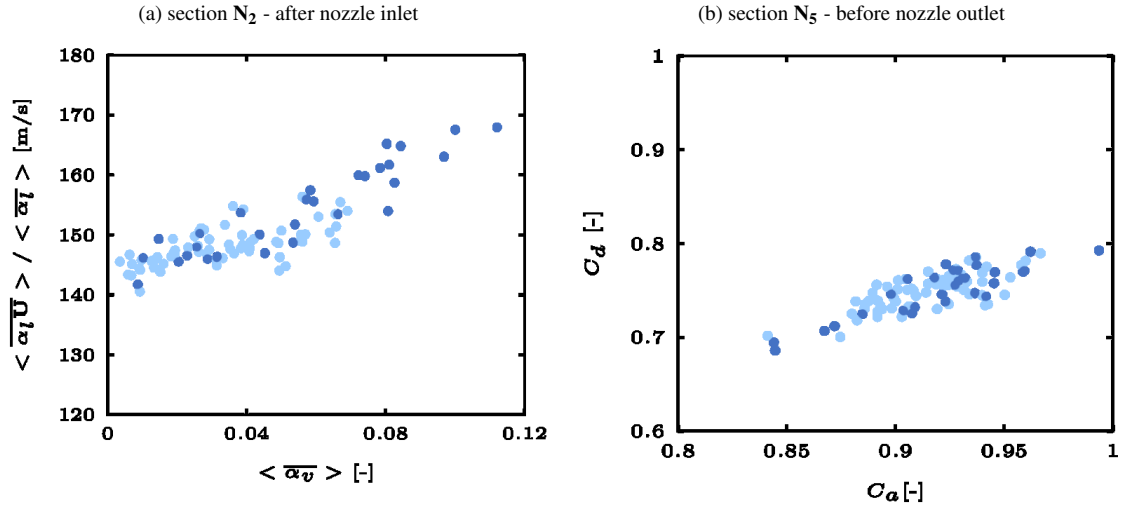


Figure 21: global characterization of the unsteady behavior of the flow at planes N_2 and N_5 of Fig. 6a; a) conditional liquid average velocity versus vapor fraction; b) area coefficient versus flow coefficient. ● events with shear; ● events without shear.

425 Shear cavitation is produced at the liquid shear layer forming at the hole entrance; the rate of vaporization can
 426 be controlled by the modification of the orifice design, which influences the pressure recovery. An alternative way
 427 to study this effect is to link the instantaneous flow velocity in the nozzle at a certain plane with the fuel-vapor void
 428 fraction α_v , that is proportional to the rate of vaporization. It is important to note that with a single-fluid solver [28],
 429 the liquid velocity $\langle \alpha_l \bar{U} \rangle / \langle \bar{\alpha}_l \rangle$ can only be estimated; this is done by weighting the time-averaged flow velocity
 430 by the liquid void fraction (see y-axis, Fig. 21a). The liquid velocity increases with the amount of vapor, since the
 431 effective flow area on the nozzle cross plane of the liquid reduces. Fig. 21a confirms that string cavitation appears
 432 when a large amount of fuel vapor in the hole is combined with large velocity of the liquid. In Fig. 21b, the correlation
 433 of the flow coefficient C_d with the effective flow area (through the C_a coefficient) is shown. The spreading of the points
 434 around a theoretical linear relationship between C_a and C_d suggests that the value of C_v in Eq. (12) varies from time
 435 to time. This is assumed to be a consequence of the flow detachment at the nozzle entrance, of the chaotic behavior of
 436 the flow and to the presence of a secondary flow that can cavitate. It is finally important to note that the relationship
 437 between C_a and C_d is independent on the type of cavitation.

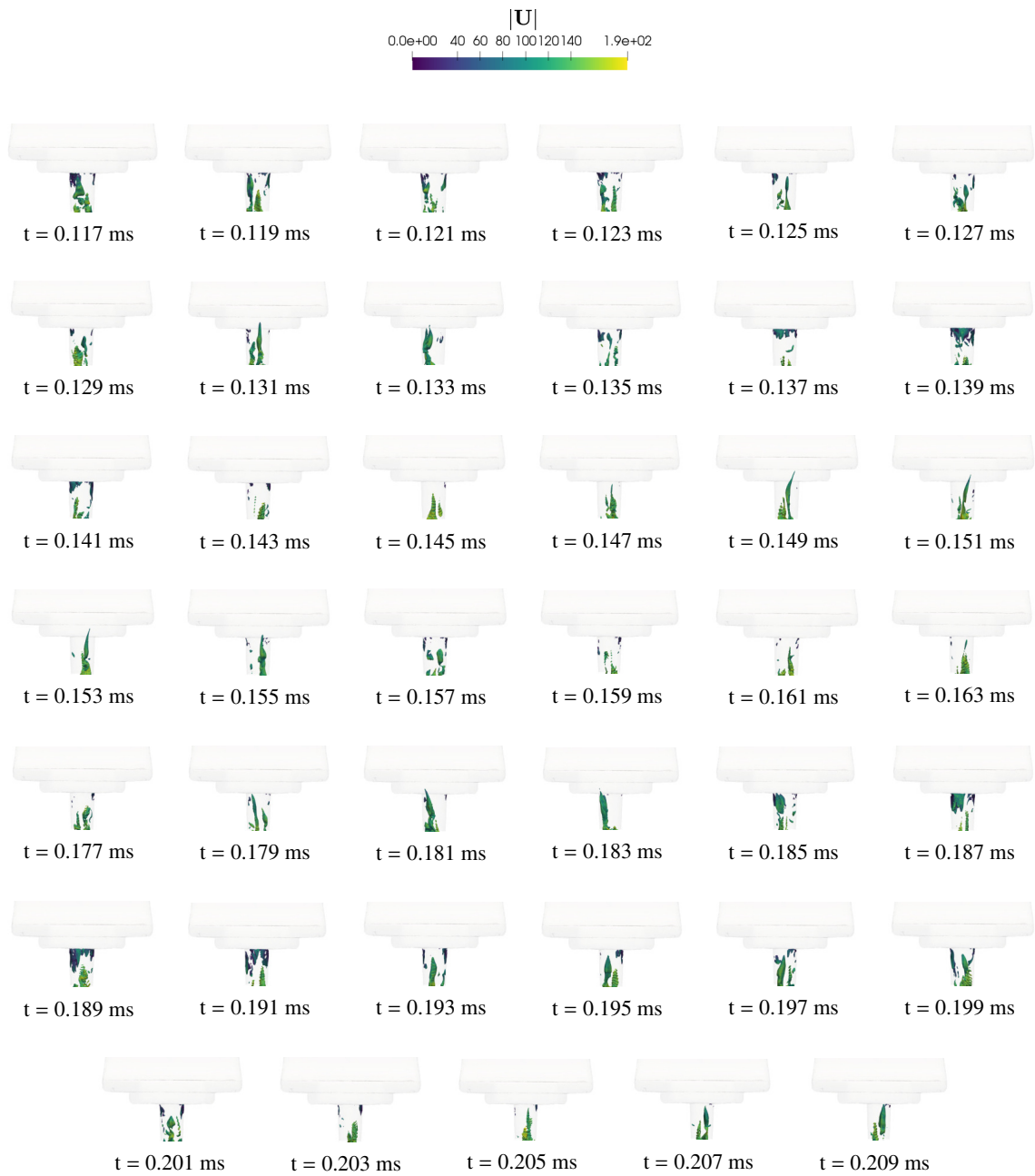


Figure 22: Instantaneous isosurfaces $\alpha_v=0.3$ showing the evolution of the vapor pockets generated by string and shear cavitation into the nozzle of injector configuration ID-10 during the injection event.



Figure 23: Isosurfaces of the second invariant of the rate of deformation tensor (Q-criterion), showing the evolution of the vortex strings into the nozzle of injector configuration ID-10 during cavitation.

438 Figures 22 and 23 are representative of the evolution of the cavitation in the nozzle (enlarged pictures are provided
439 in additional online material).. A counter-rotating vortex pair associated with the jet cross-section evolves along the
440 convergent nozzle, the flow accelerates, the pressure decreases (see Fig. 19d) and the liquid progressively cavitates.
441 Cavitating pockets of fluid expands radially in the vortexes. This is also observed experimentally. At the Reynolds
442 numbers considered, a counter-rotating vortex pair is typically unstable. Flow unsteadiness and vortex pair instabilities
443 make the vortex pair merge or brake in multiple eddies. The counter-rotating vortex pair may appear with a symmetric
444 or asymmetric shape. Finally, during its evolution, the vortex pair can move towards the nozzle walls. Then, shear
445 cavitation appears, see $t \in [169, 175] \mu s$. Shear-cavitation can stabilize in a specific region at the hole entrance, where
446 the side flow is intense (see Fig. 12). Typically, shear cavitation is weak and localized in small volumes; more rarely,
447 shear cavitation can uniformly develop at the hole inlet edge (see $t \in [137, 139] \mu s$) or on a part of it. As the recirculating
448 vortex pair reappears, $t \in [199, 207] \mu s$, shear cavitation is no longer observed. The primary flow coming from the
449 inlet channel and turning inside the sac volume adapts to the injector geometry, favoring a progressive deviation before
450 the hole entrance (see Figs 9 and 14). The primary flow strongly interacts in the sac with the flow labelled in Fig. 12
451 as “reverse“. As a result, a swirling vortex pair is generated and most of the mass flow in the nozzle axial direction is
452 found on the side (see side flow in Fig. 12), that is also the preferred location of shear cavitation spots. To summarize,
453 the string cavitation regime is dominant during the injection event of the injector studied. When string cavitation
454 appears by a counter-rotating vortex pair centered at the hole entrance, no shear-cavitation is usually observed. The
455 reduction or the collapse of the vortex pair favors the direct flow from the inlet to turn, separate and a shear-cavitation
456 regime can temporarily develop. As the vortex pair is observed again, shear-cavitation disappears. String and shear
457 cavitation rarely appear together: this happens only if a single cavitating vortex is present ($t \in [189, 191] \mu s$) or rarely
458 in short time intervals ($t \in [157, 159] \mu s$). At $t = 197 \mu s$, shear cavitation is followed by a string that will cavitate at
459 the nozzle hole end; then, this small vortex will merge with the main strings at time $t = 199 \mu s$.

460 A remark about the visual classification of cavitation is finally due, with specific reference to the time interval [119,
461 129] μs . Cavitating vortices can move freely while shear cavitation is geometric-driven. A cavitating vortex can move
462 toward the wall of the nozzle hole, can reach the proximity of the wall ($t \in [119, 121]$), then shear and string cavitation
463 disappear. The process restarts in the time interval [127, 129]. From the observations, cavitation seems always to
464 originate from shear cavitation; then, it is driven by a vortex and it does not exhibit the same kinematic features of the
465 classical shear cavitation. High-fidelity simulations suggest that additional care is required when classifying the type
466 of cavitation (shear vs string) from the analysis of the images.

467 10. Conclusion

468 A three-phase LES solver [28] has been used to carry out a study about the evolution of string cavitation on two
469 transparent nozzle replicas of real high pressure injectors, namely configurations ID-3 and ID-10. Both geometries
470 represent one sixth of a sector with a multi-hole injector. The different performance of ID-10 and ID-3 is due to their
471 geometrical features (e.g nozzle diameters, height, dead spaces) and to the inlet flow conditions developing from the
472 small details in the sac. The agreement between simulations and experimental visualizations of the cavitating flow
473 observed by two views (frontal and side) is satisfying. Validated results have been then used to analyze the nozzle
474 flow fields. Results are somehow unexpected. The flow pattern in both injectors is almost symmetric and presents a
475 large recirculating region in the sac generating a pair of counter-rotating eddies in the region between the upper wall
476 of the sac and the hole entrance. Despite the different sac geometry of the two samples, flow features at the nozzle
477 entrance are similar, as evidenced by the values of the parameter r of Eq. (11).. While r is used to characterize the flow
478 behavior in the sac, the conicity is used for the hole only. Injector ID-10 presents a shorter hole and a lower conicity;
479 its mean pressure level and the intensity of the flow recirculation (identified by the ratio between the non-axial and
480 the axial kinetic energy), as well as the amount of vapor produced at the nozzle outlet, are the largest for this injector
481 geometry. From the present study it is shown that non-axial kinetic energy in the nozzle seems to be a more relevant
482 parameter with respect to vorticity to characterize the motion of large structures and the intensity of the in-nozzle
483 cavitation. On the other hand, no conclusive remarks to optimize the injector design can be still drawn: the size and
484 distribution of the maximum ligaments out of the nozzle exit and the spatial dispersion/homogeneity of the spray in
485 the outer region are some of the additional relevant parameters that must also be taken into account. These parameter
486 are related to the study of the primary atomization, that will be the topic of upcoming publications.

487 Finally, a pseudo-periodic appearance of string and shear cavitation has been observed from the simulations. It
488 has been shown that string and shear cavitation can coexist. The occurrence of shear and string cavitation is the result
489 of different superimposing types of flow motions. In the sac, a secondary motion is superposed on the primary flow
490 with the fluid coming from the inlet channel and the fluid deviated inside the sac volume being swept towards the

491 nozzle hole entrance. This kind of flow promotes string cavitation, but in principle it does not generate enough flow
492 detachment for shear cavitation to develop. On the other hand, flow unsteadiness and vortex pair instabilities make
493 string vortices in the nozzle hole merge or move towards the walls and brake. As a consequence, the flow topology
494 may change and the rate of cavitation of the fuel is temporarily dominated by the classical shear cavitation in the
495 liquid shear layer forming at the hole entrance. In between of these two extreme conditions, a wide range of complex
496 interaction between string and shear cavitation has been observed.

11. Acknowledgments

Authors gratefully acknowledge the Laboratory Computing Resource Center (LCRC) at Argonne National Laboratory for the computing resources provided through the KNL-OpenFOAM-VOF project. Authors would like to thank also Mr. Louis-Philippe Elie, Dr. Stefan Schuster and Dr. Eberhard Kull for the support received on the transparent nozzle manufacturing. The code used for the simulations, including automatic pre- and post-processing, is part of the LibPoliMi/DAER code, an open-source C++ library developed by the authors at the Dept. of Aerospace Science and Technology, Politecnico di Milano (DAER-PoliMi) based on the OpenFOAM Technology (OpenFOAM-8 and OpenFOAM-dev, commit 4c08b463f). Argonne National Laboratory's work was supported in part by the U.S. Department of Energy Office of Science, under contract DE-AC02-06CH11357.

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