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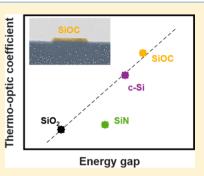
Letter

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## High Thermo-Optic Coefficient of Silicon Oxycarbide Photonic Waveguides

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**ABSTRACT:** In this Letter, we report on the observation of a high thermo-optic coefficient (TOC) of silicon oxycarbide (SiOC) films deposited by reactive RF magnetron sputtering for integrated photonic waveguides. In the 1550 nm wavelength range, the measured TOC of SiOC is as large as  $2.5 \times 10^{-4}$  RIU  $^{\circ}$ C<sup>-1</sup>, which is about 30 times larger than that of silica and almost twice that of silicon. Thin films of SiOC have been integrated in germanium-doped silica and silicon oxynitride conventional waveguide technology, achieving a  $10\times$  and  $3\times$  enhancement of the waveguide effective TOC, respectively. These results demonstrate the potential of SiOC for the realization of highly efficient phase actuators and low-power-consumption thermally tunable photonic integrated platforms.



KEYWORDS: integrated photonics, thermo-optic effect, silicon oxycarbide, optical waveguides

mong the currently available integrated photonics platforms, dielectric technologies are the most consolidated, preliable, and widely exploited to realize commercial photonic integrated circuits (PICs). Conventional dielectric waveguide technologies include germanium-doped silica glass (Ge:SiO<sub>2</sub>), silicon oxynitride (SiON), and silicon nitride (Si<sub>3</sub>N<sub>4</sub>). These technologies have long been used to fulfill the requirements of photonic industries and enabled the fabrication of low-loss, low-cost, polarization-independent, efficient fiber-coupled, and relatively compact complex devices.

The tuning and reconfiguration of PICs is typically achieved 28 through heaters that induce a phase shift in the propagating 29 light by the thermo-optic effect. In dielectrics the thermo-optic 30 coefficient dn/dT (TOC) is quite low, on the order of  $10^{-5}$ 31 °C<sup>-1</sup>. On one hand, it can be seen as an advantage because it 32 guarantees a weak dependence of PIC behavior on temperature 33 variations; on the other hand, the efficiency of the heaters is 34 rather low, as large electrical dissipation and large operational 35 temperatures are required for control operations. Devices 36 based on SiO<sub>2</sub>, SiON, and Si<sub>3</sub>N<sub>4</sub> show a spectral shift of about 37 1 GHz/°C, heaters are typically a few millimeters long, and the 38 electrical power dissipated to induce a  $\pi$  phase shift is some 39 hundreds of milliwatts. The high control temperatures 40 introduce stringent requirements on the packaging and on 41 the need of power-hungry Peltier cells to sink the heat. Further, 42 the high temperatures on chip impact the reliability of the 43 heaters, which deteriorate with time.

In order to realize energy-efficient and reliable reconfigurable PICs, materials with a large TOC could be integrated in 46 conventional dielectric platforms. Examples of high-TOC materials employed in optical waveguides include silicon (1.8  $\times$  10<sup>-4</sup> °C<sup>-1</sup>) and ultrarich silicon nitride (2.66  $\times$  10<sup>-4</sup> °C<sup>-1</sup>). 49 High negative TOC values have been reported in polymers and 50 TiO<sub>2</sub>, 4 which are mainly related to the thermal expansion.

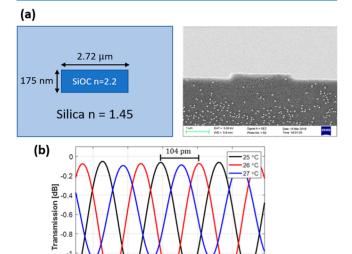
Silicon oxycarbide (SiOC) is a novel class of glass 51 compounds that has gained momentum in the scientific 52 community and adopted in technologically important 53 applications such as interlayer dielectrics, anode material in 54 lithium-ion batteries, and photoluminescence. 5-7 Recently, we 55 have introduced SiOC as a potential platform in integrated 56 photonics.<sup>8,9</sup> The refractive index of SiOC can be tailored from 57 n = 1.45, corresponding to SiO<sub>2</sub>, to about 3.2, for amorphous 58  $SiC.^{10-12}$  SiOC has the advantage of a low absorption 59 coefficient in the near-infrared region, and low-loss waveguides 60 on silica realized by sputtering have been demonstrated for the 61 first time with a core index of 1.578 and 2.2.8,9 Waveguide 62 attenuation of 2 to 4 dB/cm in the telecom window of 1550 63 nm has been measured. In comparison with SiON, exhibiting a 64 pronounced absorption peak around 1505 nm due to N-H 65 bonds, SiOC absorption is spectrally flat across the full (S, C, 66 L) telecom bands, offering a tremendous advantage for 67 broadband applications.

In this Letter, we report on silica-buried SiOC channel 69 waveguides where we observed a record TOC about 30 times 70 larger than that of silica-based waveguides and even higher 71 than that of silicon waveguides. Further, we propose and 72 demonstrate the integration of SiOC films with classical 73 dielectric waveguide technologies to enhance the efficiency of 74 thermo-optic phase actuators. Results suggest that the high 75 TOC of SiOC can be effectively exploited to achieve an 76 energy-efficient reconfiguration of integrated photonic circuits 77 based on conventional technologies such as Ge:SiO<sub>2</sub>, SiON, 78 SiN, and others.

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80 The cross section of the silica-buried SiOC channel 81 waveguide is shown in Figure 1a together with a scanning

f1



**Figure 1.** (a) Schematic and SEM photograph of the cross section of the SiOC channel waveguide. (b) Spectral response of a straight waveguide for three different temperatures.

1.5354

1.5355

1.5353

Wavelength [um]

1.5351

1.5352

82 electron microscopy (SEM) microphotograph of an uncovered 83 waveguide. The SiOC core of the waveguide has a rectangular s4 shape  $(2.72 \times 0.175 \ \mu\text{m}^2)$  and a refractive index of 2.2. The 85 SiOC film was deposited on a silicon wafer with a 6  $\mu$ m thick 86 silica substrate by using reactive radio frequency (RF) 87 magnetron sputtering from a SiC target in an oxygen and 88 argon atmosphere. Details on the SiOC sputtering procedure 89 can be found in previous publications. 8,9 X-ray photoelectron 90 spectroscopy (XPS) measurements revealed that the deposited 91 material con 45% silicon, 27% oxygen, and 27% carbon, so 92 that the actual chemical composition is Si<sub>0.45</sub>O<sub>0.27</sub>C<sub>0.27</sub> (for 93 brevity, in the remaining of the paper it will be simply referred 94 to as SiOC omitting the subscripts). Good adhesion of the 95 SiOC film on the silica substrate was observed, with no 96 evidence of either pin holes or porosity. The SiOC surface 97 roughness, as estimated with atomic force microscopy (AFM), 98 is as low as 0.24 nm rms, which is comparable to the silica 99 substrate. The optical constants of the SiOC film were 100 measured with a variable-angle spectroscopic ellipsometer over 101 a broad spectral range from the UV to near-infrared regions. 102 Around a wavelength of 1550 nm the measured refractive 103 index of the SiOC layer is about 2.2 and the extinction coefficient is less than 10<sup>-4</sup> above 600 nm.

The waveguide cross section was defined by direct-laser106 writing lithography using an AZ 5214E photoresist and etching
107 with a reactive ion etching (RIE) machine. The RIE process of
108 mixed gases CHF<sub>3</sub> (100 sccm) and O<sub>2</sub> (5 sccm) was run
109 applying an RF power of 50 W and inductively coupled plasma
110 (ICP) power of 250 W for 20 min. The etch rate was 9 nm/
111 min. After the SiOC core patterning, plasma enhanced
112 chemical vapor deposition (PECVD) silica with n = 1.45 was
113 deposited as the upper cladding material. The strip-shaped
114 waveguide was selected in order to have good transverse
115 electric (TE) mode properties, with a small contribution of the
116 sidewall roughness to the waveguide attenuation. Several

waveguides with different widths, ranging from 2 to 4  $\mu$ m, were 117 fabricated and tested. The waveguide propagation losses 118 measured by cut-back technique are about 2 dB/cm.

The TOC of SiOC was estimated by optical transmission 120 measurement of the fabricated waveguides at different 121 temperatures. The photonic sample was mounted on a holder 122 whose temperature was controlled by a thermoelectric Peltier 123 module with a temperature accuracy within 0.1 °C. Lensed 124 optical fibers were used to launch the light from a tunable laser, 125 and the polarization state of light was controlled with a 126 polarization controller guaranteeing at least -30 dB crosstalk 127 between TE and transverse magnetic (TM) polarizations. TE- 128 polarized light was coupled to the SiOC waveguides from a 129 tunable laser operating in the broad spectral range from 1520 130 to 1580 nm.

Figure 1b shows the measured transmission spectrum of a 132 SiOC waveguide around a wavelength  $\lambda=1535.3$  nm at three 133 different temperatures. The Fabry–Pérot fringes due to the 134 glass–air reflections at the waveguide input/output facets have 135 a period  $\Delta\lambda=172$  pm. The waveguide length is L=3.5 mm 136 and the effective group index results  $n_{\rm g}=\lambda^2/2L\Delta\lambda=1.95.$  137 When the temperature is increased by 1 °C, for instance from 138 25 °C (black curve) to 26 °C (red curve), a wavelength shift of 139 the waveguide transmission spectrum by  $d\lambda/dT=104$  pm/°C 140 is observed. The same wavelength shift was measured also 141 from 26 to 27 °C (blue curve) and for any additional 142 temperature degree. The effective thermo-optic coefficient of 143 the waveguide, hereinafter referred to as  $K_{\rm eff}$ , is given by

$$K_{\text{eff}} = \frac{n_g d\lambda}{\lambda dT} \tag{1}_{145}$$

and results to be  $K_{\rm eff} = 1.34 \times 10^{-4} \, {}^{\circ}{\rm C}^{-1}$ , a factor 10 larger <sup>146</sup> than that of Si<sub>3</sub>N<sub>4</sub> waveguides and 15 with respect to SiO<sub>2</sub>- <sup>147</sup> based waveguides.

The thermo-optic coefficient of the SiOC material can be 149 evaluated by considering the overlap of the optical mode with 150 all the materials the waveguide is made of. With a variational 151 approach the perturbation of the phase propagation constant  $\beta$  152 due to a variation  $\Delta\varepsilon(x,y)$  of the dielectric constant of the 153 waveguide is given by 13,14

$$P\Delta\beta = \omega \iint_A \Delta\varepsilon(x, y) \mathbf{E} \mathbf{E}^* \, \mathrm{d}x \, \mathrm{d}y$$
 (2) <sub>155</sub>

where **E** is the electric field of the guided mode, P is the power 156 carried by the mode, and the integral is over the entire 157 waveguide cross section A. Assuming that the perturbation is 158 induced by a change of temperature dT,  $\Delta\beta = \omega K_{\rm eff} \, dT/c$  and, 159 for each material,  $\Delta\varepsilon = 2nK \, dT$ , where K is the material TOC. 160

The effective thermo-optic coefficient  $K_{\rm eff}$  can hence be 161 written as a combination of the contribution of the various 162 materials,

$$K_{\text{eff}} = \sum_{i} K_{i} \Gamma_{i} \tag{3}$$

where  $K_i$  is the thermo-optic coefficient of the *i*th material and 165

$$\Gamma_{i} = \frac{c \iint_{A_{i}} [\varepsilon o \vec{E} \cdot \vec{E}^{*}] \, dx \, dy}{\iint_{A} [\varepsilon o \vec{E}_{t} \times \vec{H}_{t}^{*}] \cdot \hat{z} \, dx \, dy}$$

$$(4)_{166}$$

is the confinement factor of the mode in the considered 167 material, which is evaluated across a cross-sectional area  $A_{\rm i}$ . 168 From eq 3 and the measured value of  $K_{\rm eff}$  of the waveguide, the 169

ACS Photonics Letter

170 thermo-optic coefficient of the SiOC material is  $K_{\rm SiOC} = 2.5 \times 171~10^{-4}~{\rm ^{\circ}C^{-1}}$ , one of the largest values ever reported for dielectric 172 materials. Table 1 reports the values of the confinement factor

Table 1. Materials and Waveguide Parameters

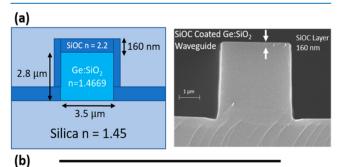


		SiOC coat SiO <sub>2</sub>	SiOC c iON
technology	SiOC wg	wg	ring
group index $n_{\rm g}$	1.95	1.93	1.574
index contrast	34%	1.5%	5.7%
size $[\mu m^2]$	$2.72 \times 0.175$	$3.5 \times 2.8$	$2.5\times1.8\times0.4$
$\Delta \lambda \ [pm]/^{\circ}C$	104	130	31.3
$\Gamma_{ ext{SiO2}}$	0.59	0.59	0.26
$\Gamma_{ ext{SiOC}}$	0.53	0.46	0.049
$\Gamma_{\text{SiON}}$			0.72
$K_{\rm eff} \times 10^{-4}$	1.34	1.62	0.32
(expt)			

173 in the SiOC ( $\Gamma_{\text{SiOC}}$  = 0.53) and SiO<sub>2</sub> ( $\Gamma_{\text{SiO2}}$  = 0.589) layers of 174 the waveguide, as evaluated from electromagnetic simulations. 175 The thermo-optic coefficient of silica is  $K_{\text{SiO2}}$  = 0.9 × 10<sup>-5</sup> 176 °C<sup>-1</sup>.

The high TOC of SiOC, together with the transparency at telecom wavelengths and the high refractive index, suggests its use as a potential candidate for high integration scale and low control power integrated optics. Here, we propose and demonstrate the exploitation of SiOC for realizing highly efficient thermo-optic phase shifters in classical and well-source consolidated photonic technologies, such as Ge-doped  ${\rm SiO_2}$  and  ${\rm SiON}$  waveguides.

A thin layer of SiOC was deposited on the core of the optical 186 waveguides, which was then buried under a PECVD silica 187 upper cladding. The cross sections and micrographs of the 188 SiOC-coated Ge:SiO<sub>2</sub> waveguide and SiON ring resonator are 189 shown in Figure 2. The index contrast of the Ge:SiO<sub>2</sub> 190 waveguide is 1.5%, and the core size is 3.5 × 2.8  $\mu$ m<sup>2</sup>; for 191 the SiON waveguide, a rib shape with a size of 2.5 × 1.8  $\mu$ m<sup>2</sup> 192 (slab height of 0.4  $\mu$ m) is used, the index contrast being equal 193 to 5.7%. Waveguide data are summarized in Table 1, and



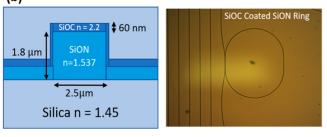
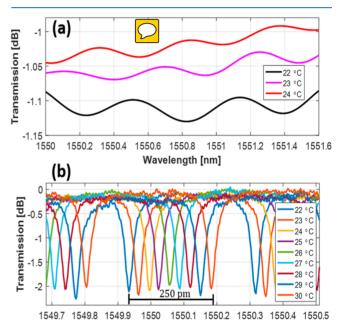


Figure 2. Cross section and microphotograph of (a) a  $Ge:SiO_2$  waveguide coated with a SiOC layer; (b) a SiOC-coated SiON waveguide and ring resonator.

details of their respective fabrication and optical character- 194 ization can be found in specific contributions. 15,16 Electro- 195 magnetic simulations were performed to optimize the overlap 196 of the guided mode with the SiOC layer and limit the 197 perturbation on the waveguides. The thickness of the 198 deposited SiOC layers is 160 and 60 nm for Ge:SiO<sub>2</sub> and 199 SiON waveguiding structures, respectively. The thickness of 200 the deposited SiOC films on the waveguide sidewalls is about 201 40% of the top SiOC layer thickness, as estimated from the 202 SEM image given in Figure 2a.

Experiments were performed on Ge:SiO<sub>2</sub> straight wave- 204 guides and SiON ring resonators coated with the SiOC film. 205 The radius of the ring resonator is 555.3  $\mu$ m, the coupler 206 length is 260  $\mu$ m, and the physical length of the cavity is 4.009 207 mm. As in the case of the SiOC-core waveguide discussed in 208 Figure 1,  $K_{\rm eff}$  was estimated by optical transmission measure- 209 ments of the fabricated structures at different temperatures. 210 Figure 3a shows the measured optical transmission spectrum of 211 f3



**Figure 3.** Spectral response of (a) a SiOC-coated Ge:SiO<sub>2</sub> straight waveguide for three different temperatures; (b) a SiOC-coated SiON ring resonator for nine different temperatures.

Wavelength [nm]

a SiOC-coated Ge:SiO<sub>2</sub> straight waveguide around  $\lambda=1550$  212 nm. The Fabry–Pérot fringes, which are less pronounced than 213 in Figure 1(c) because of the lower effective index of the 214 waveguide, reveal  $n_{\rm g}=1.93$ . When the temperature is increased 215 by  ${\rm d}T=1$  °C, a wavelength shift of the waveguide transmission 216 spectrum  ${\rm d}\lambda/{\rm d}T=130$  pm/°C is observed. According to eq 1, 217 this shift corresponds to an effective thermo-optic coefficient 218  $K_{\rm eff}=1.62\times10^{-4}$  °C<sup>-1</sup>, which is more than 1 order of 219 magnitude higher than that of SiO<sub>2</sub> waveguides.

The enhancement of the waveguide effective TOC is 221 confirmed by results achieved on SiOC-coated SiON wave- 222 guides. Figure 3b shows the thermally induced wavelength shift 223 of the transmission spectrum of a microring resonator around a 224 wavelength of 1550 nm. When the temperature increases from 225  $^{\circ}$ C to 30  $^{\circ}$ C, the resonance of the microring is shifted by 226 250 pm. From eq 1, the resulting  $K_{\rm eff}$  is  $3.2 \times 10^{-5}$   $^{\circ}$ C<sup>-1</sup>. 227 Remarkably, a thin layer of SiOC of only 60 nm thickness and 228

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229 with a confinement factor  $\Gamma_{\text{SiOC}}$  of less than 5% increases by 3 230 times the  $K_{\rm eff}$  of the ring original SiON waveguides ( $K_{\rm SiON}$  = 231  $1.1 \times 10^{-5}$  °C<sup>-1</sup>). These results confirm that SiOC seems an 232 enabling platform to develop highly efficient reconfigurable 233 photonic systems.

The origin of the large TOC of SiOC is related to the 235 volume change in polarizability and, in a minor part, on the 236 thermal expansion. This is the typical situation for high melting 237 point, high hardness, and high elastic moduli materials. Also, 238 near the transparency edge, the polarizability (and dn/dT) 239 rises. <sup>17</sup> Figure 4 reports the TOC of various materials plotted

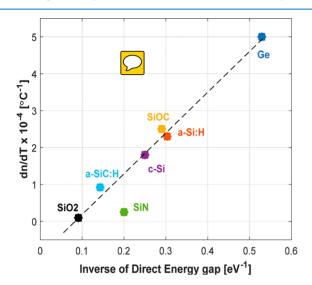


Figure 4. Thermo-optic coefficient dependence on the inverse of the direct band gap energy.

240 against their direct band gap energy  $E_{\rm g}$  at telecom wavelengths. 241 Reported data are obtained from the literature. 18,19 The 242 thermo-optic coefficient is nearly dependent on the inverse of  $E_g$  and increases approaching the band gap. Silica is transparent 244 until the deep UV and has a very small TOC, while germanium 245 has the highest coefficient but it is not transparent at telecom 246 wavelengths. The direct band gap of the SiOC film has been 247 determined by using absorption spectra measured with 248 spectroscopic ellipsometry and applying the Tauc relation 249  $(\alpha h\omega)^2 = h\omega - E_g$  where  $\alpha$  is the absorption coefficient and 250  $h\omega$  is the photon energy. The direct band gap of the SiOC 251 film with n = 2.2 is calculated as  $E_g = 3.5$  eV, which is lower 252 than that of Si and is responsible for its higher thermo-optic 253 coefficient. As can be seen in Figure 4, SiOC is aligned with the 254 trend of increasing TOC value with decreasing energy band 255 gap.

In conclusion, we investigated the thermo-optic effect in 257 optical waveguides integrating high refractive index (n = 2.2)258 SiOC films. Experiments on three different waveguiding 259 structures (channel SiOC waveguide, SiOC-coated SiO<sub>2</sub> waveguide, and SiOC-coated SiON waveguide) show that 261 the thermo-optic coefficient of SiOC, amounting to  $2.5 \times 10^{-4}$ 262 °C<sup>-1</sup>, is 1 order of magnitude larger than that of dielectric 263 materials conventionally employed in integrated optics and 264 almost twice that of silicon. The high TOC of SiOC was also 265 exploited to achieve a significant enhancement of the TOC of 266 conventional glass waveguides (10× in SiO<sub>2</sub>, 3× in SiON 267 waveguides) by coating the waveguide core with a thin film of 268 SiOC. These results demonstrate the potential of SiOC for the realization of highly efficient thermally tunable photonic 269 integrated platforms.

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**Author Contributions** 277

F.A.M. fabricated the waveguides and performed experiments 278 for the characterization of the thermo-optic coefficient of 279 SiOC. Results were discussed by all authors. The manuscript 280 was written and approved by all authors.

**Notes** 282

The authors declare no competing financial interest.

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