



POLITECNICO
MILANO 1863

RE.PUBLIC@POLIMI

Research Publications at Politecnico di Milano

Post-Print

This is the accepted version of:

J. Yin, K. Rossignol, M. Barbarino, D. Bianco, C. Testa, H. Brouwer, S.R. Janssen, G. Reboul, L. Vigevano, G. Bernardini, M. Gennaretti, J. Serafini, C. Poggi
GARTEUR Activities on Acoustical Methods and Experiments for Studying on Acoustic Scattering
CEAS Aeronautical Journal, Vol. 10, 2019, p. 531-551
doi:10.1007/s13272-018-0333-0

This is a post-peer-review, pre-copyedit version of an article published in CEAS Aeronautical Journal. The final authenticated version is available online at:

<https://doi.org/10.1007/s13272-018-0333-0>

Access to the published version may require subscription.

When citing this work, cite the original published paper.

Permanent link to this version

<http://hdl.handle.net/11311/1079517>

GARTEUR ACTIVITIES ON ACOUSTICAL METHODS AND EXPERIMENTS FOR STUDYING ON
ACOUSTIC SCATTERING

Jianping Yin	Karl-Stéphane Rossignol	Mattia Barbarino
Research Scientist	Research Scientist	Research Scientist
DLR	DLR	CIRA
Braunschweig, Germany	Braunschweig, Germany	Capua, Italy
Davide Bianco	Claudio Testa	Harry Brouwer
Research Scientist	Research Scientist	Research Scientist
CIRA	CNR-INSEAN	NLR
Capua, Italy	Rome, Italy	Amsterdam, Netherlands
Stevie Ray Janssen	Gabriel Reboul	Luigi Vigevano
Research Scientist	Research Scientist	Associate Professor
NLR	ONERA	Politecnico di Milano
Amsterdam, Netherlands	Paris, France	Milano, Italy
Giovanni Bernardini	Massimo Gennaretti	Jacopo Serafini
Professor	Professor	Professor
Roma TRE University	Roma TRE University	Roma TRE University
Rome, Italy	Rome, Italy	Rome, Italy
	Caterina Poggi	
	PhD Student	
	Roma TRE University	
	Rome, Italy	

ABSTRACT

This paper deals the activities conducted in the GARTEUR Action Group HC/AG-24 to address the noise scattering of helicopter rotors in presence of the fuselage. The focus of the Action Group is on the development and the validation of numerical prediction methods and establishing an experimental data base for numerical validations. The numerical methods include Boundary Element Method (BEM) for solving the Helmholtz

equation and Computational AeroAcoustic method (CAA) for solving linearized Euler equations. The test activities are conducted in the DLR Acoustic Wind Tunnel in Braunschweig (AWB). In the current paper, the results from the numerical simulations, the wind tunnel tests as well as numerical and test comparisons are addressed. The test configurations include the sphere, the sphere with sting support and a finite NACA0012 wing (thanks to share data with a NATO STO group). The acoustic predictions of the scattering by spheres will be compared with the analytic solution to address the influence of the sphere support systems at different wind speeds. The acoustic predictions of the scattering by NACA0012 wing will be analyzed and compared to available test results for different source locations and frequencies.

NOTATION

D Diameter of the sphere

f Frequency

p_{tot} Total acoustic pressure perturbation

p_i Incident acoustic pressure perturbation

p_s Scattered acoustic pressure perturbation

γ_T Shielding factor $\gamma_T = p_{tot}/p_i$ or $\langle p_{tot} \rangle / \langle p_i \rangle$ for numerical or test results, respectively

r Observer position

r_0 Magnitude of the vector from source to observer

r_s Source position

R Radius of the sphere

V Flow speed

ψ Azimuth angle

θ Polar angle

AG Action Group

AWB Acoustic Wind tunnel in Braunschweig

BEM Boundary Element Method

$GARTEUR$ Group for Aeronautic Research and

	Technology in Europe
HC	Helicopter
<i>PPW</i>	Point Per Wave length
SPARC	Source-imPulsionnelle AeRoacoustique
STO	Science and Technology Organization

1. INTRODUCTION

Helicopter noise reduction is a long term objective of the helicopter industry in view of extending the market to new civil applications, as well as getting prepared to comply with the new and increasingly stringent noise regulation. Both the main and the tail rotors (including Fenestron) of a helicopter are major sources of the noise and contribute significantly to its ground noise footprint. The research efforts in the past were mainly concentrated on the helicopter rotor noise generation and reduction. Even though the scattering of noise generated by helicopter rotors has been recognized as having a significant influence on the noise spectra and directivity generated by isolated rotating blades, there has not been an extensive research effort towards the comprehension of the phenomenon. This is particularly important when dealing with the tail rotor noise, for which the wavelength of the harmonics is comparable or smaller than the characteristic dimension of the fuselage. In order to boost research activities on the noise propagation in presence of the fuselage a specific Action Group (AG) 24 [1][2][3][4] has been constituted in the Group for Aeronautical Research and Technology in EUROpe (GARTEUR). The focus has been put on the development and the validation of numerical prediction methods, addressed within the first Work Package (WP) of the AG. The experimental activities are carried out in the second WP of the AG. The objectives of this AG are (1) to expand the limits of current noise prediction tools, so that the shielding effects and controlled surface impedance can be exploited for the development of new vehicles with less environmental impact and more public acceptance and (2) to generate a unique noise scattering database through wind tunnel test using generic configurations, such as spheres of different materials (wood or aluminium), wings and a GARTEUR helicopter model composed of an ellipsoid fuselage, cylinder tail boom and a simple empennage.

In the current paper, the results from the numerical simulations, the wind tunnel tests as well as the numerical and test comparisons are addressed. The test configurations include the spheres, the sphere with sting support and a finite NACA0012 wing (thanks to share data with a NATO STO group). One purpose of choosing spheres in the test is to verify the accuracy of the complete test system, such as support systems and noise sources, microphones as well as the

reliability of the test results. By comparing with analytic solutions, the influence of the sphere support systems and different wind speeds can be addressed.

This paper is organized as follows: the methodologies applied in the numerical simulations by GARTEUR AG24 partners will be first described and advantages and disadvantages are then summarized; the introduction of the experimental approach used in the acoustic scattering test, including noise sources, wind tunnel models, acoustic instrumentation and data reduction will then be presented; the acoustic scattering predictions from the sphere and from the NACA0012 wing will be analyzed and compared with available test results for different source positions and frequencies. In addition a comparison with analytic or numerical results is also presented to assess the accuracy of the test system.

2. DESCRIPTION OF METHODOLOGIES APPLIED IN NUMERICAL SIMULATIONS BY THE PARTNERS

In this section, a brief description of the scattering formulations used by the AG partners is presented. Figure 1 summarizes the computational methodology used when a Boundary Element Method (BEM) code is employed for a point source scattering problem.

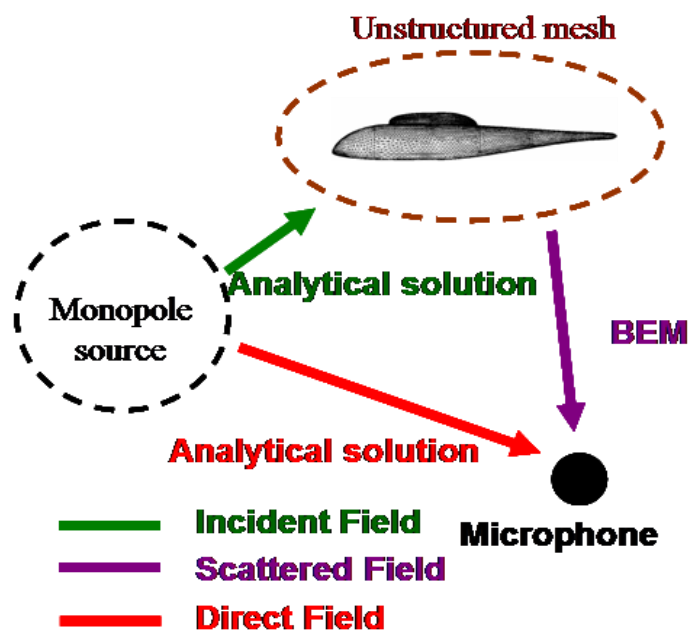


Figure 1. Computational methodology using BEM

As shown in Figure 1, the incident field from the source is indicated by the green arrow and can be obtained by either analytical solution or numerical one. For a conventional BEM code, the required inputs are the incident pressure field and the normal pressure gradient on the scattering surface and BEM code then provides scattered radiation indicated by the purple arrow. Both the direct field (the red arrow) and the scattered field (the purple arrow) add in the microphone position to construct an overall sound pressure. The BEM codes used by all partners are the frequency domain codes. The unstructured mesh is used by all partners, except the University of RomaTRE and CNR-INSEAN.

The CIRA BEM code, OptydB-BEM [5][6], has the possibility to include the effect of the fluid velocity, solving the convected Helmholtz equation formulated either in pressure (Lighthill's analogy) or in terms of the velocity scalar potential (Howe/Pierce analogy). The uniform mean flow effect is treated by means of the convected free-field Green functions. The integral equations are treated using the collocation approach and the Combined Helmholtz Integral Equation Formulation (CHIEF) for removing the spurious frequencies. The discrete set of equations associated then with the boundary problem is solved with an iterative approach. The code can manage unstructured grids with triangular and quadrilateral elements and different types of boundary conditions. At last a black-box directional, Fast Multipole Method (FMM) is implemented for dealing with large scattering problems.

DLR is using the Fast Multipole Boundary Element Method (FMBEM) code [7] which solves the exterior Helmholtz problem for the scattered pressure field. It is a BEM method which employs the Fast Multipole Method (FMM) for triangulated surfaces. FMBEM uses an iterative solver from PETSc library as well as OpenMP/MPI parallelization for the fast evaluation of matrix-vector products so that no storage of the matrix is required. In addition, the Burton-Miller approach [12] is used to guarantee the uniqueness of the solution. Based on the assumption of low Mach number potential flow, a Taylor transformation of the convected wave equation into the Helmholtz equation is used to take into account the mean flow effect [14]. Similar to ONERA method, a post-processing is used following [13] to deal with potential flow effect.

NLR uses its in-house finite-volume CFD/CAA code ENFLOW [8]. It solves the linearized Euler equations for a given non-uniform steady flow-field on a block-structured, boundary-conforming grid. The code utilizes a 4th order accurate low dispersion & dissipation scheme to be able to propagate acoustic disturbances over large distances. Generation of spurious waves is avoided by implementation of 6th order artificial diffusion, and the use of non-reflecting boundaries. The code uses an explicit 4th order Runge-Kutta scheme to advance the solution in time.

ONERA is using two different acoustic scattering codes. The goal is to identify the limitation of the first using the later as a reference. The simplest method is based on the Kirchhoff integral with the assumption of a locally flat surface approach (FSA) with single reflections. This methodology is implemented in ONERA FW-H code named KIM [9]. Compare to BEM, this approach has the advantage to be fast and to be implemented in the time-domain which could be interesting when dealing with multi-frequency application and impulsive phenomenon such as BVI for example. The second approach used at ONERA is the BEM code named BEMUSE[10]. The Onera's in-house BEMUSE code solves this system using either a Brakhage Werner [11] or Burton-Miller integral formulations[12]. Sommerfeld radiation condition is applied at infinity and the scattering surface defines the boundary conditions which can be for instance Neumann, Dirichlet or Robin ones. These elements are coupled with an algebraic approach of the kernel approximation (inverse matrix) based on the Adaptive Cross Approximation (ACA) method. The implemented method is following the works of Grasedyck [13] on asymptotically smooth kernel operators. It computes a low-rank approximation of appropriate matrix blocks, independent on the kernel operator. Even if convection effects are not taken into account in BEMUSE, a post-processing is used following [14] to deal with potential flow effect. The following equation is used to compute the total acoustic pressure ($p(x,t)$) thanks to the solution of the Helmholtz equation (Φ_h) and the mean flow velocity potential (φ):

$$p(x,t) = -\rho(-i\omega\Phi_h + \nabla\varphi \cdot \nabla\Phi_h) \cdot \exp\left\{i\omega[\varphi(x_o) - \varphi(x)]/a_o^2\right\} \exp(-i\omega t)$$

where ρ is the free-stream mean density and x and x_o are the field and source location, respectively.

For validation purpose ONERA has also performed a CAA computation on the NACA0012 test case. sAbrinA-v0 is a structured grid, time-accurate code that solves either the full or the linear Euler equations, in a conservative and perturbed form (with a splitting of the complete variables into a "frozen" mean flow and a "fluctuating" perturbation). The solver employs high-order, finite difference operators, involving a 3rd-order, multi-stage, Runge-Kutta time-marching scheme. The code deals with multi-block structured grids with one-to-one interfaces, and is fully parallelized using the Message Passing Interface (MPI) standard. More detailed information about the sAbrinA-v0 solver and its underlying methodology can be found in reference [15]. In this application a newly developed Immersed Boundary Condition has been applied [16].

Differently, the University of RomaTRE and CNR-INSEAN have developed a nonstandard tool, in the frequency domain, based on the boundary integral solution of the Ffowcs-Williams and Hawkings (FWH) Equation for the scattering analysis of moving/elastic bodies [17]. Beside this pressure-based approach, the Helmholtz equation for the velocity potential is also proposed to compute the scattered pressure field [17]. Both formulations use the CHIEF method to remove spurious frequencies effects (if present). Recently, the potential-based formulation has been extended to include nonlinear effects due to the steady-state aerodynamic mean flow: a first-order formulation based on the linearization of nonlinearity about the steady-state aerodynamic condition has been proposed in [18][19].

	CAA	BEM
<i>Features</i>		
	• Derivative-based on Linearized Euler • Domain mesh:3D • Mesh generation: expensive • Optimal at low frequencies • Gradients of velocity of sound and flow in the medium: YES and no limitation • Time domain • Noise sources: included in simulations • Complex source:Yes • Near field : Yes • Diffraction: Yes • Boundary layer: Yes • Flow effect: No limits • Computation time: Much intensive and expensive	• Integral-based on Helmholtz equation • Boundary mesh:2D, • Mesh generation : FAST • Optimal at low frequencies • Gradients of velocity of sound and flow in the medium: NO • Frequency domain: Problem with non-periodic • Noise sources: prescribed • Complex source:Yes • Near field : Yes • Diffraction: Yes • Boundary layer: No • Flow effect: only low Mach • Computation time: fast

Table 1: A comparison of the CAA and BEM

The comparison of CAA and BEM method applied in the AG is summarized in Table 1, regarding their main features as well as advantages and disadvantages. The BEM requires only 2D mesh and is therefore computationally more efficient than CAA method where 3D mesh is required. The gradients of velocity of sound and the flow in the medium can be treated by CAA method without limitation, which is not the case for the BEM. Seven codes of varying complexity have been used in producing the numerical results. The main characteristics of the codes are summarized in Table 2. All codes formulated within the context of BEM are suitable for the far field. In case of no mean flow, all BEM codes should provide the same level of the accuracy. Due to different treatment on the mean flow effect, the difference may occur when the flow effect is introduced in the simulation using BEM. The simulation with CAA can provide most accuracy results and capture most of physics, especially when the flow effect is considered. However the computation time using CAA prohibit its application for the far field. FSA method is much simpler and faster than traditional BEM, but only reflections are considered.

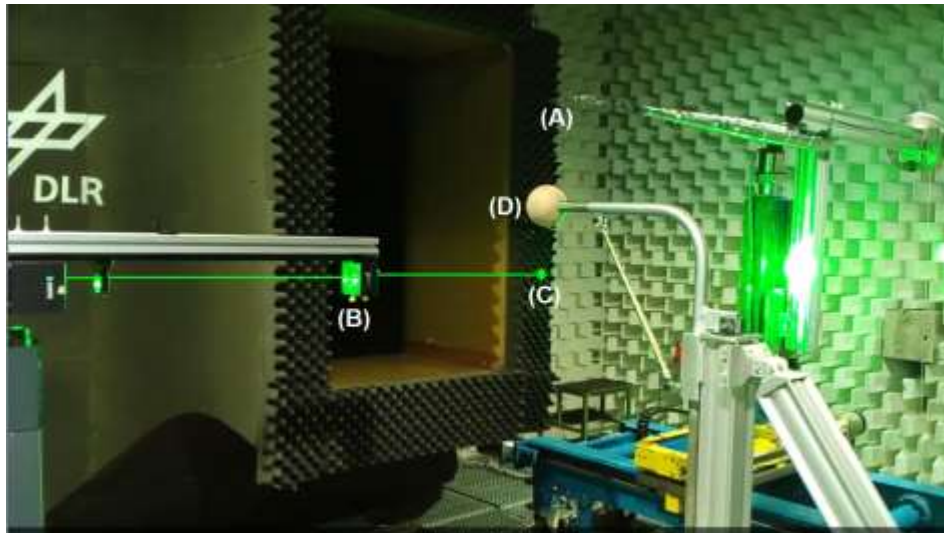
	CIRA	DLR	NLR	ONERA (1)	ONERA (2)	ONERA (3)	RomaTRE /CNR-INSEAN
Formulation	BEM	BEM	CAA	BEM	CAA	FSA	BEM
Treatment singularity	CHIEF	Burton-Miller		Burton-Miller			CHIEF
Flow effect	Taylor transform	Taylor transform	Included	Taylor transform	Included	No	Convective Green's function or nonlinear effect
Mesh	2D unstructured	2D unstructured	3D structured	2D unstructured	3D structured	2D unstructured	2D structured
Acceleration	Fast multiple	Fast multiple		Fast multiple			No
Diffraction	yes	yes	yes	yes	yes	No	yes
Domain	Frequency	Frequency	Time	Frequency	Time	Time	Frequency

Table 2. Main Characteristics of the codes

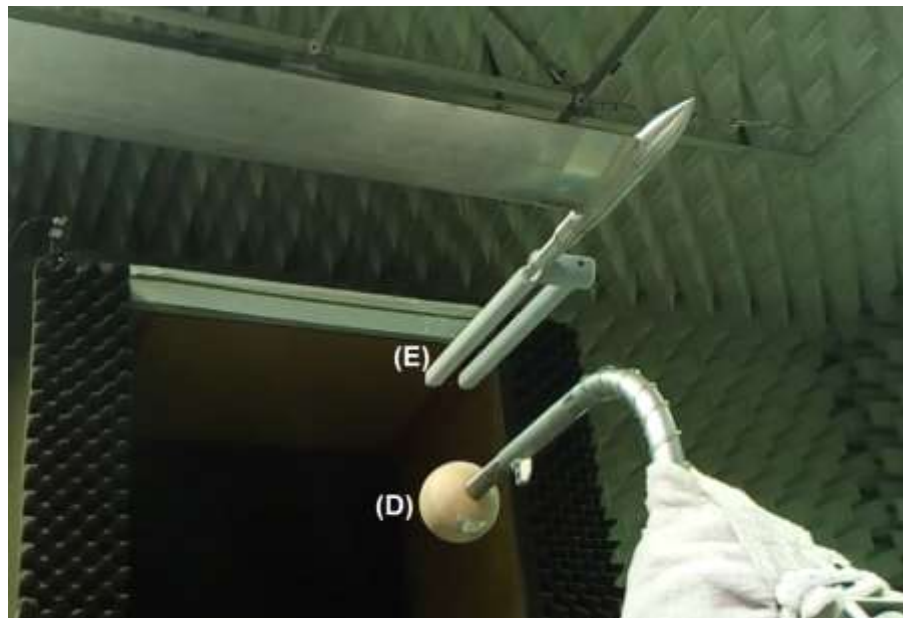
3. DESCRIPTION OF THE TEST SETUP

GARTEUR AG24 shielding experiments are performed in the DLR Acoustic Wind tunnel in Braunschweig (AWB), as shown in Figure 2 for a sphere test with a sting support configuration. The AWB has a cross section of $(1.2 \times 0.8)m^2$. The open jet test section is known for its excellent flow quality and anechoic properties as well as its low background noise. For the sphere test, two sphere sizes, a small one with $D1=0.12m$ diameter and a big one with $D2=0.34m$ diameter are used. The sizes of the spheres are derived according to the largest dimension of 1/12.5 scaled BO105 fuselage in lateral or streamwise directions. To quantify the influence of the sting support on the scattering results, the wire support (Figure 3), where the sphere is hanged with three 0.002m diameter wires, is also used. In addition, spheres of different materials (wood or aluminum) are also tested.

The shielding setup for a 2D wing with NACA0012 profile is shown in Figure 4. The wing is mounted vertically in the test section with a $dx=0.2$ m shift away from the tunnel centerline. This is done to provide enough room for the inflow microphone to be placed in the geometric far-field of the model. The whole laser was tilted 3° towards the model, to avoid collision of the optical components with the wing's support when moving the source. A detailed description of the NACA0012 wing test can be found in [20].



(a) Test set-up with laser point source: (A) microphone, (B) convex lens, (C) laser source, (D) sphere



(b) Test setup with SPARC: (D) sphere, (E) SPARC

Figure 2. Complete test set-up for two different noise sources

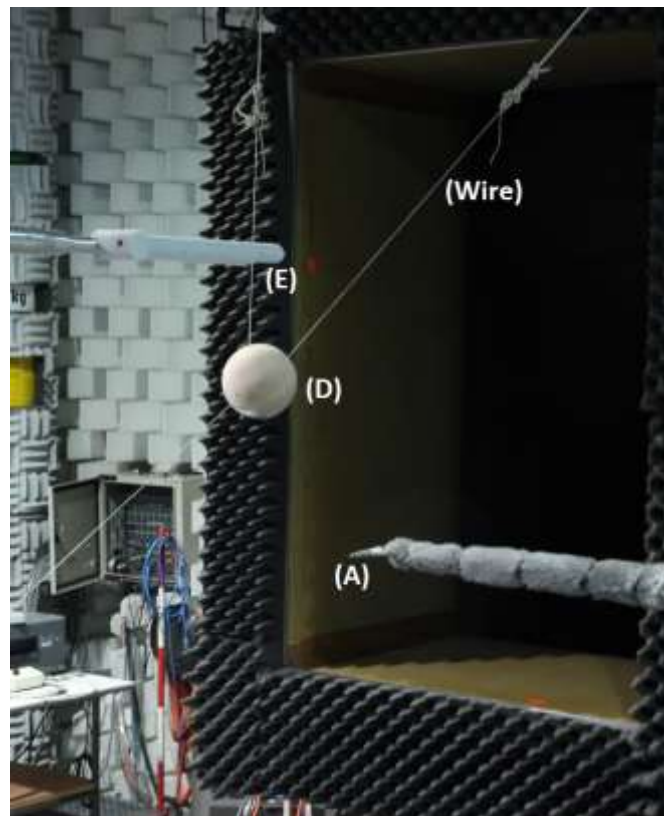


Figure 3. Sphere hanged by wires: (A) microphone, (D) sphere, (E) SPARC

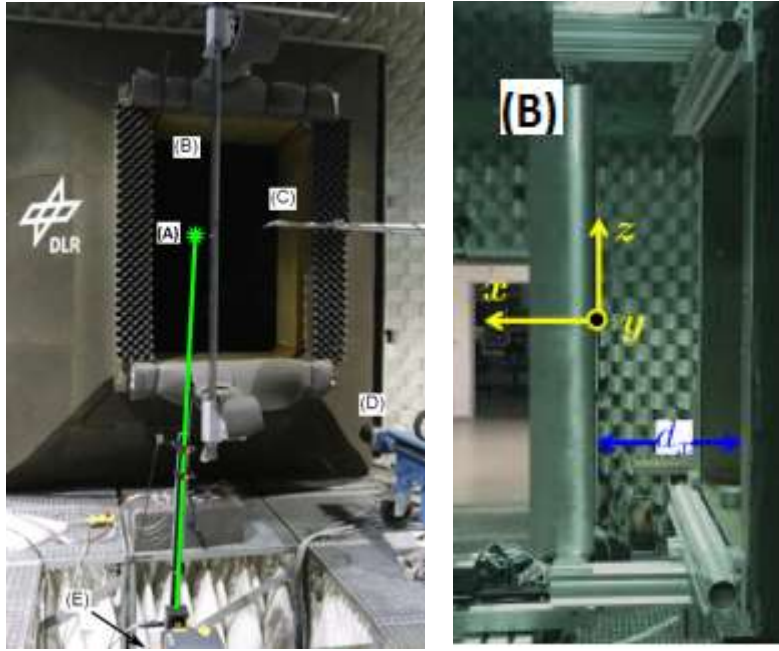


Figure 4. Shielding setup for 2D wing: (A) laser source, (B) NACA0012 2D wing, (C) microphone, (D) microphone positioning system, (E) laser source positioning system

3.1 Description of the noise sources

The choice of the noise sources is based on the criterion of non- or minimum-intrusiveness for both the mean flow and the acoustic field. As shown in Figure 2, two point-source systems are used. The first one is a laser plasma pulse system from DLR [21] indicated as (C) in Figure 2a, and the other noise source is SPARC system of ONERA [22] indicated as (E) in Figure 2b. The peak frequency for the DLR laser source is located at about 30 kHz and the useful frequency range extends from 1 kHz to 80 kHz, while the peak frequency for ONERA SPARC is located at about 10 KHz with useful frequency range from 1 KHZ to 30 kHz.

3.1.1 DLR Laser Generated Sound

By focusing a high energy laser beam on a point, it is possible to initiate the formation of a small plasma which rapidly expands [23][24], thus forming a pressure wave about its boundary which propagates through the surrounding medium. The optical setup for the DLR laser sound source is shown in Figure 5, where the combination of one concave length and two convex lenses is applied to ensure the plasma creation at about 500mm from last convex lens.

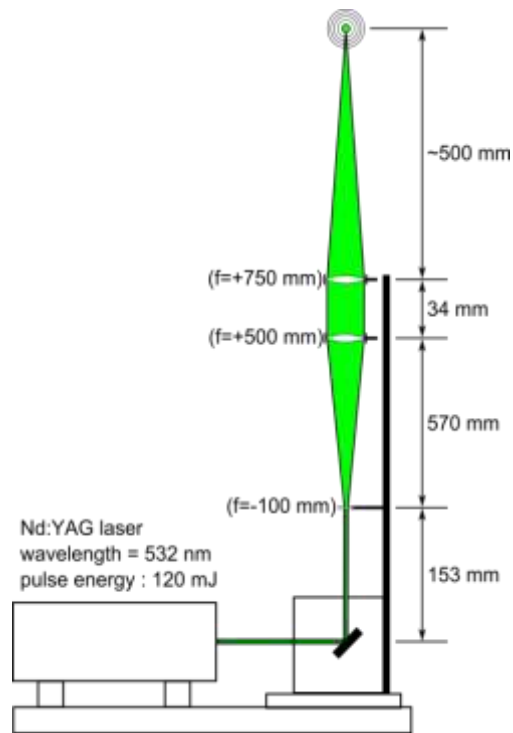


Figure 5. Optical setup for the laser sound source

The DLR laser sound source has the advantage of being non-intrusive for both mean flow and the acoustic field. Because of its small size and uniform directivity, it can be represented as a point monopole source.

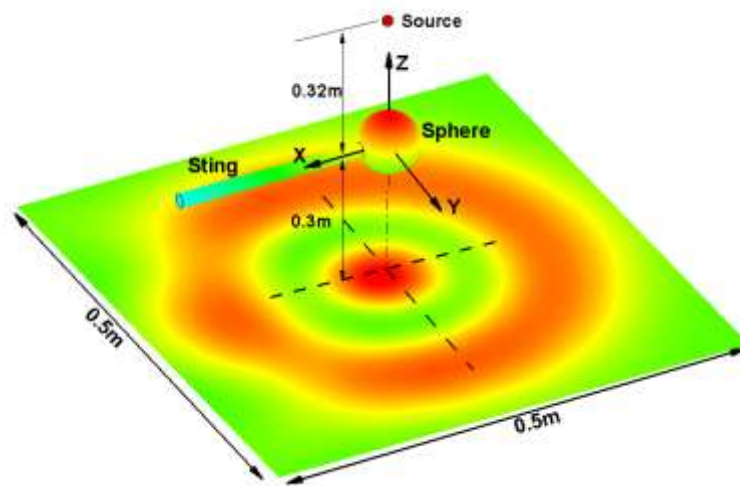


Figure 6. A detailed setup of the sharp probes from SPARC

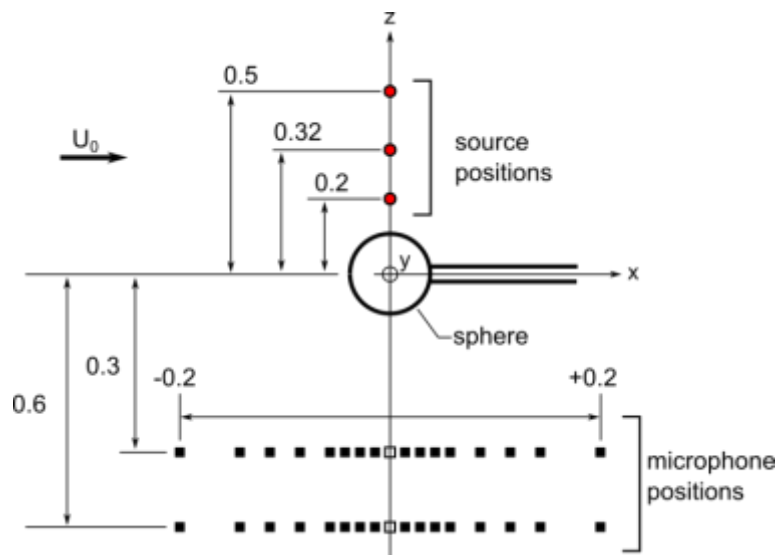
3.1.2 ONERA SPARC (Source im Pulsionnelle AeRoAcoustique)

Above a given threshold, a strong electric field ionizes the air between two sharp probes [22]. In this way, an electrical channel is created and an abrupt current discharge occurs. A part of the released energy is then converted into the heat in the small region between the probes. This intense heat induces a local expansion of the air which generates an acoustic pressure wave. A detailed setup of the sharp probes is shown in Figure 6.

3.1.3 Acoustic Instrumentation



a) Axis system and traverse directions (dashed line)



b) Source and microphone positions. Same microphone traverse for the y direction

Figure 7. The configuration with the sting support

In-flow measurements are performed using 1/8" inch Bruel & Kjaer pressure field microphones equipped with a standard nose cone. The in-flow microphone is mounted on a traversing system and can be moved in both x direction and y direction, as shown in Figure 7a. As shown in Figure 7b, the measurement positions of the in-flow microphone in x direction are marked as the solid squares. The same measurement positions in y direction are also used in order to define the influence of the support system, such as the sting. In addition, one microphone is installed at a fixed position near the ground and serves as a reference measurement. The coordinate center is chosen as the center of the sphere.

4. RESULTS AND DISCUSSION

In the following sections, only a comparison of the shielding factor or attenuation factor γ_T from the tests or numerical results is conducted. The shielding factor is defined as the ratio of total pressure $p_{tot} = p_i + p_s$, and incident pressure p_i ,

$$GT = \gamma_T(f) = \frac{p_{tot}(f)}{p_i(f)}$$

where p_s is the scattered acoustic pressure. The shielding factor deviation from value 1 can be considered as the effect of the scattering by the obstacles. When evaluating the shielding factor for the test result, the ensemble averaged total and incident pressure fluctuations are used to reduce the measurement errors. The advantage of using the shielding factor to evaluate the scattering effect is that no corrections on the signal amplitude are required. In addition, when the microphone is equipped with a nose cone during the measurement, corrections on microphone directivity are not required.

4.1 Test results of the sphere scattering for two noise sources

In this section, the test results of the sphere scattering by two different noise sources, DLR laser pulse and ONERA SPARC, are compared. The test results are also compared with the analytical solution, to verify the accuracy of the complete test system, such as support systems and noise sources, microphones as well as the reliability of the test results. The analytical solution is derived using a rigid sphere and a point monopole source.

The measured shielding factors γ_T at $f=3000\text{Hz}$ from the wood sphere hanged with wires (Figure 3) are shown in Figure 8 for the two different noise sources. The diameter of the sphere is 0.12m. The test results with DLR noise source using Laser fit well with the analytic solution (blue line) in both x- and y-traversing directions, except in the shadow region around $x=0$ or $y=0$ m below the sphere where some small deviations are noticed. One possible reason for

the small deviations in the shadow region is that due to the longer propagation paths of the sound waves about the shielding object, the time series taken in post processing isn't longer enough to capture all of the relevant sound intensity, which causes the reduction of the signal to noise ratio. Therefore, when a shielding object is present between the sound source and a remote receiver, one has to be more careful to make sure that all the meaningful part of the measured signal is kept for further processing. Similar observations are made for the ONERA SPARC source, but the error using SPARC source is larger than that using DLR source, as the additional errors are caused by the intrusiveness of the SPARC setup on the sound field. In general, the measured shielding factors from both noise sources capture the characteristics of the troughs and peaks of an interference pattern around the shadow region. The matching with the analytical results indicates that the wood sphere can be considered as acoustic hard sphere, as the solid wall condition is used in deriving the analytical solution.

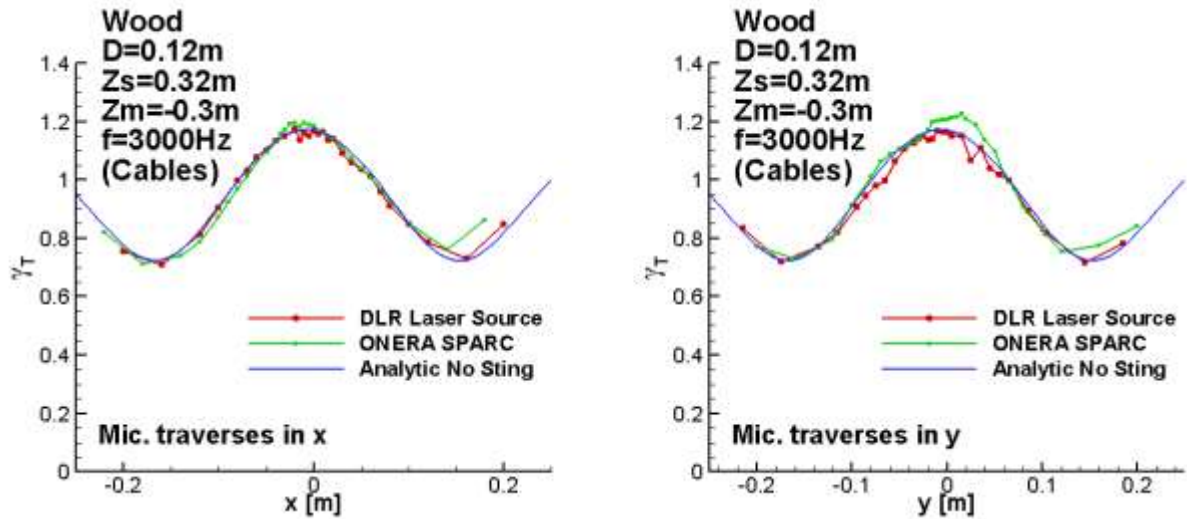
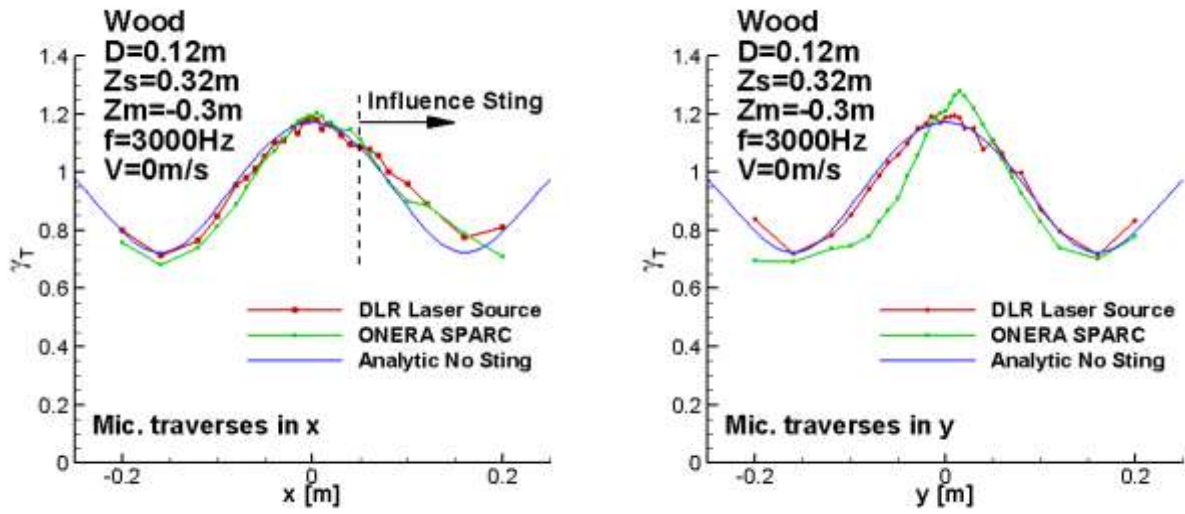


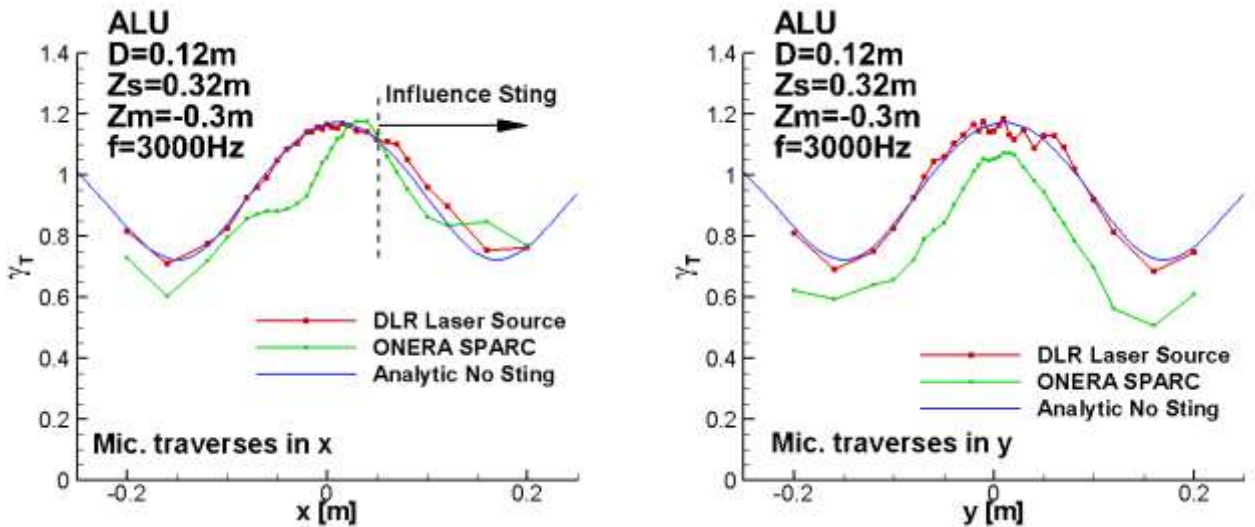
Figure 8. Measured shielding factor γ_T for the wood sphere $D=0.12\text{m}$ with the cable support at 3000Hz

Figure 9 (a) and (b) show the comparisons of measured shielding factor γ_T for both the aluminum and the wood sphere with the sting support (Figure 2). For the DLR laser source, the comparisons with the analytical results show that the general characteristics of the local peak and troughs from two types of spheres are well matching the analytical one. As the analytical solution was obtained for a solid surface without the sting support, the deviations from the analytic solution, especially for the microphone positions in the positive x direction (Figure 9 left) indicate the interference from the sting support. The deviations are similar for both the wood and the aluminum spheres. The difference caused by the different material cannot be identified since the results are almost independent of the materials. For the ONERA SPARC source, the comparisons with both the analytical results and DLR results indicate large deviation for the

aluminum sphere, especially for the microphone position in the y direction (Figure 9 right) where a clear offset is observed. For the wood sphere, the deviation caused by the sting support fitted relative well with the results from DLR source for the microphone positions in the x direction (Figure 9 (a) left). There are several possible reasons that might contribute to the difference. The possible reasons for the large deviation observed in using SPARC source are (1) the interferences of the support structure from the source probes (Figure 6) on the sound propagation, (2) the disruption of the metal sphere on ionized electric field which caused the signal deviation from the point source, and (3) relative lower signal to noise ratio at 3000Hz for the ONERA SPARC source.



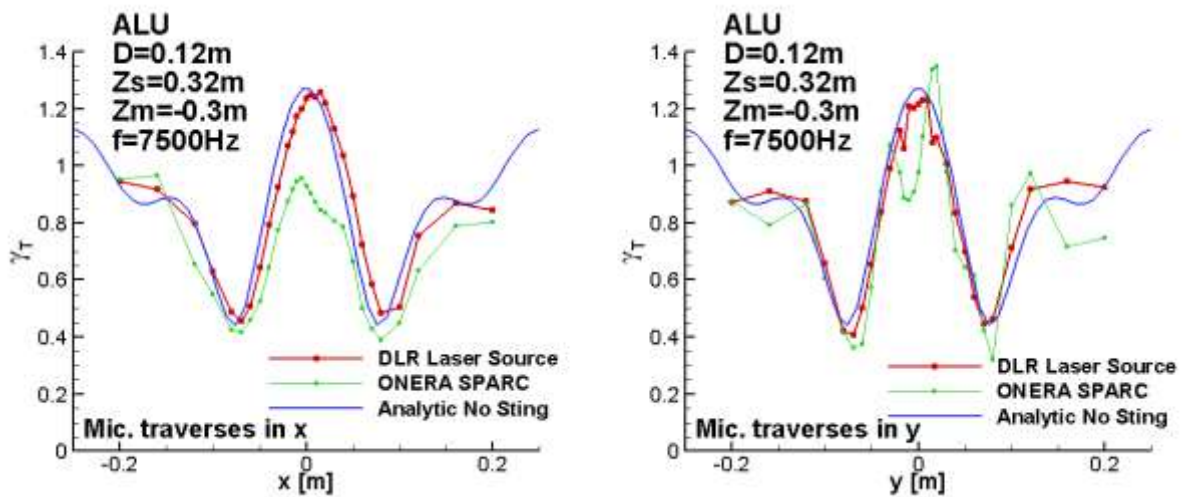
(a) Measured shielding factor for the wood sphere, Left: X-traverse, Right: Y-traverse



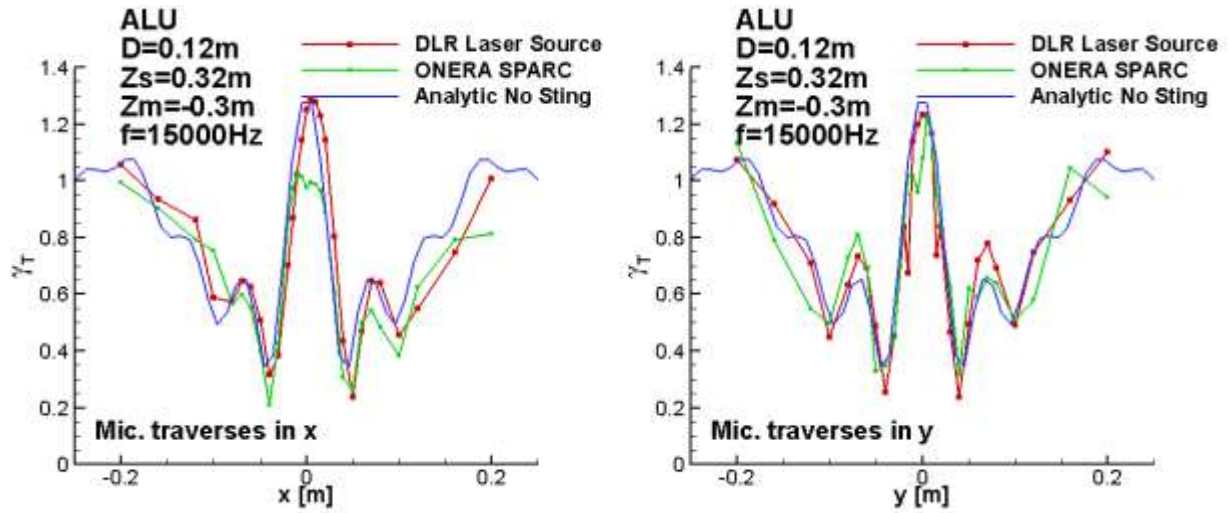
(b) Measured shielding factor for the aluminum sphere, Left: X-traverse, Right: Y-traverse

Figure 9. Shielding factor γ_T for the aluminum (a) and the wood sphere (b), with sting support at 3000Hz

Figure 10 (a) and (b) show the comparisons of the measured shielding factor γ_T for the aluminum sphere at 7500Hz and 15000Hz respectively. The wave lengths at both 7500Hz and 15000Hz are smaller than the characteristic length of the small sphere diameter $D=0.12\text{m}$. The strong scattering is expected in comparing with 3000Hz. The interference patterns, as shown in Figure 10, indicate an increasing number of side lobes around the shadow area when increasing the frequency. The width of both the side lobes and peak in the shadow region becomes narrower when increasing the frequency. In general, the test results using both DLR laser source and ONERA SPARC have captured all the characteristics of the interference pattern in space, except large deviation occurring in the shadow region around $x=0$ or $y=0$ m for the results using ONERA SPARC, which may be caused by disruption of metal sphere on ionized electric field as mentioned before. In addition, the good correlation for ONERA source for these two frequencies in comparing with 3000Hz indicates also the higher signal to noise ratio in the high frequency range. As the acoustic signal at 15000Hz has a wave length close to the diameter of the sting ($D=0.028\text{m}$), a relative large influences of the sting support on the shielding factor are expected for the microphones beneath the sting (positive x).



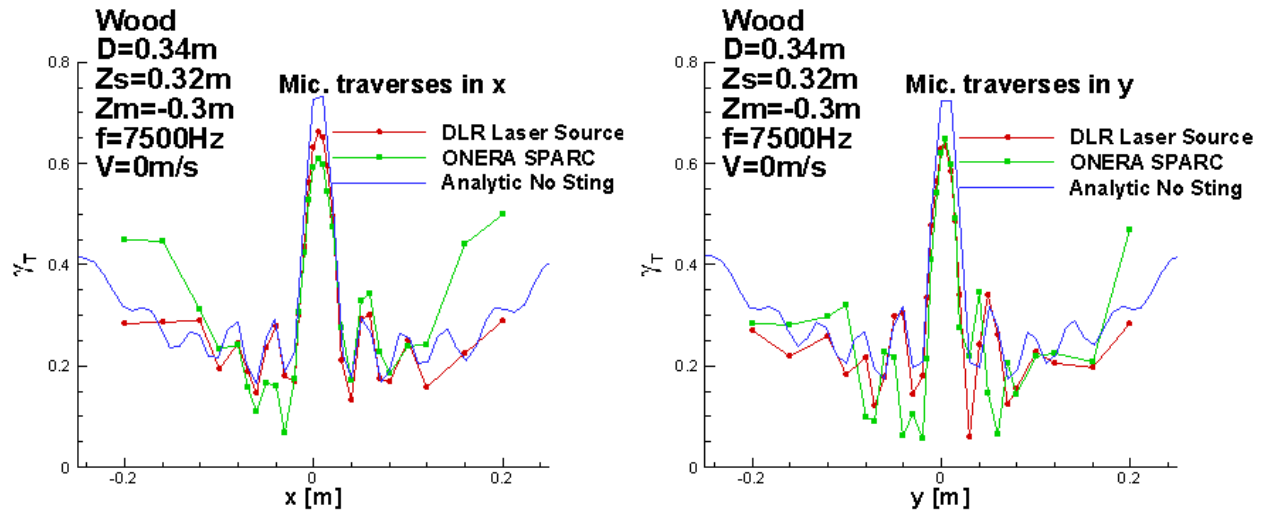
(a) Measured shielding factor at 7500Hz, Left: X-traverse, Right: Y-traverse



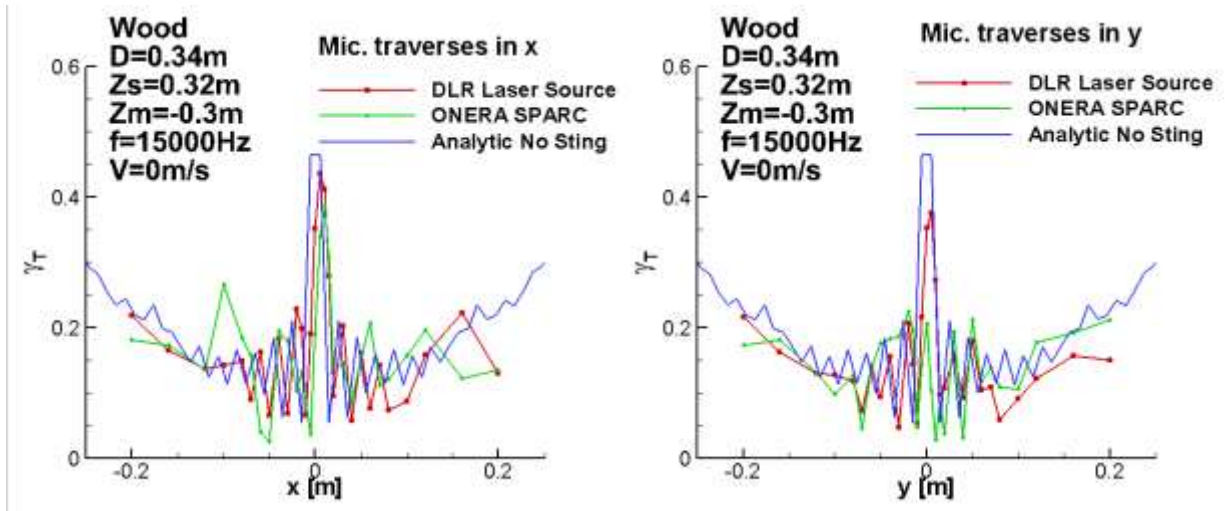
(b) Measured shielding factor at 15000Hz, Left: X-traverse, Right: Y-traverse

Figure 10. Shielding factor for the aluminum sphere $D=0.12\text{m}$ with sting support at 7500 and 15000Hz

The measured shielding factors for a large wood sphere ($D=0.34\text{m}$) at $f=7500\text{Hz}$ and 1500Hz are given in Figure 11. For the large sphere the interference patterns become more complicated, showing more side lobes. The shielding factors exhibit a narrow shadow region and lower value of the shielding factor in comparison with the small sphere for these two frequencies. For the large sphere, strong reflections of the acoustic energy at the sphere surfaces causes a large shadow region ($\gamma_T \ll 1$) in all measurement area. The experimental results for two noise sources at 7500Hz show a behavior similar to the analytic solution and therefore demonstrate the small effect of the sting in the measurement results. In addition, the test has captured at least the first two side lobes. For noise source at $f=15000\text{Hz}$, the test results using DLR source still demonstrate satisfactory comparison in terms of the troughs and peaks of an interference pattern around the shadow region, while ONERA SPARC misses the main interference peak directly underneath the sphere for the y traversing. In general, for the considered frequency range, notwithstanding some level of disagreement in representing the side lobes, the experimental results are comparable with the analytical ones with acceptable accuracy.



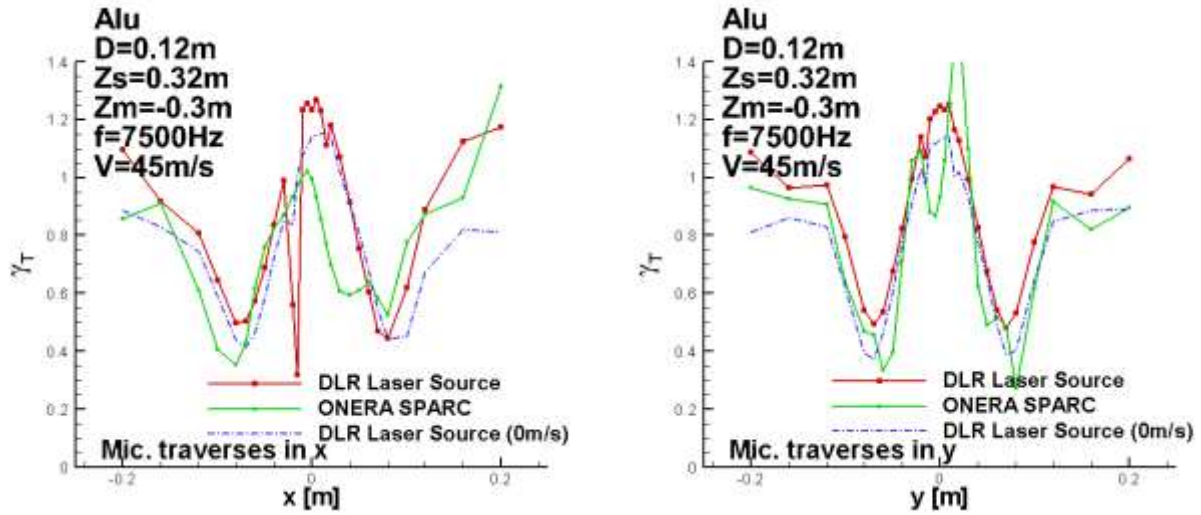
(a) Measured shielding factor at 7500Hz, Left: X-traverse, Right: Y-traverse



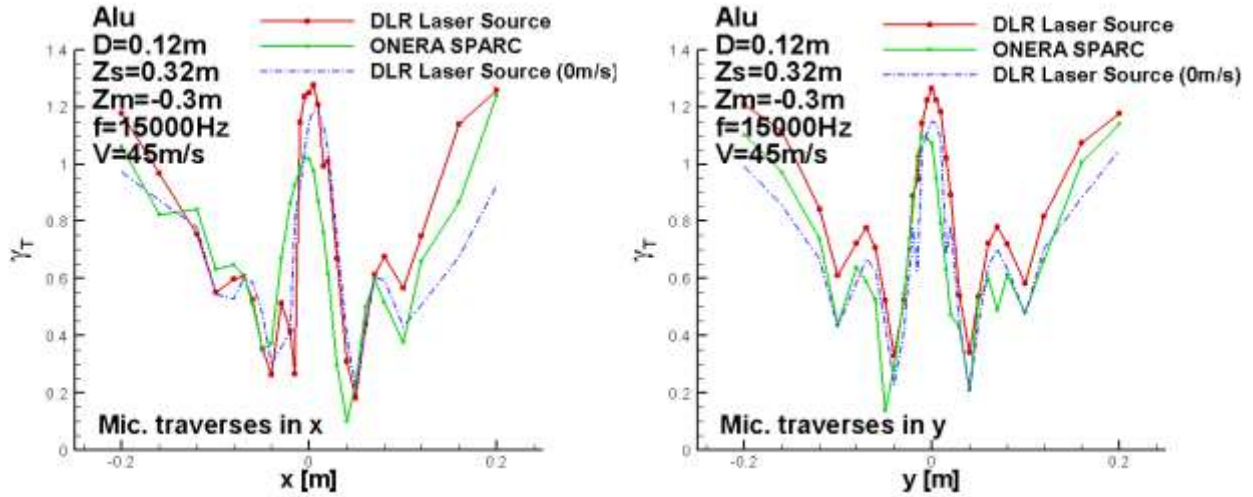
(b) Measured shielding factor at 15000Hz, Left: X-traverse, Right: Y-traverse

Figure 11. Shielding factor for the wood sphere D=0.34m with sting support at 7500Hz

Figure 12 shows the comparisons of the shielding factor at two frequencies under the influence of a mean flow ($V=45\text{m/s}$). For the comparison, the test results from DLR laser source at $V=0\text{ m/s}$ are also included, as there is no analytical solution including a mean flow available for the case.



(a) Measured shielding factor at 7500Hz, Left: X-traverse, Right: Y-traverse



(b) Measured shielding factor at 15000Hz, Left: X-traverse, Right: Y-traverse

Figure 12. Effect of the mean flow with 45m/s on shielding factor for the sphere D1=0.12m with sting support

Direct comparisons of the results from two noise sources indicate that, with the exception of the large deviation occurring in the shadow region around $x=0$ or $y=0$ m, both sources demonstrate the same trends for upstream (the microphone with the negative x value) and downstream (the microphone with the positive x value) as well as in lateral direction in y . When comparing DLR laser source results with the results (blue dashed line) without the mean flow for the streamwise microphones (Figure 12a and Figure 12b, Left), the large deviations occur in the downstream of the sphere (positive x value) for both frequencies. The flow in the downstream of the sphere can be complicated and

contains large flow gradient due to possible separation of the flow field behind the sphere. The influence of mean flow gradients and separation flow on the directivity and strength of sound waves propagating can contribute to the large deviations. In addition, the DLR source shows a sharp drop in shielding factor occurs in the upstream part of the x-traversing, just before the main peak: the reason of this drop still needs to be further investigated. The ONERA source in general has relative low level, especially in shadow peak region, in comparing with DLR results. The effect of the presence of the mean flow is in general to increase the level of the shielding factor for both array traverse directions.

In general, the measurement error comes from the uncertainty in the measured shielding factors. The estimated value of the uncertainty on the measured shielding factors is in the range $\pm 8\%$ for the case without the mean flow. For the case with mean flow, at $V=45\text{m/s}$, a slightly larger uncertainty of about $\pm 10\%$ is obtained. This slightly larger value is related to the fewer number of valid data blocks available for the Fourier analysis. In addition, the accuracy of the measurement results in comparing with the analytical one also depends on following factors: (1) the accuracy on the microphone- and source-position measurement; (2) the deviation of the test sphere (the radius, surface curvature and the smoothness, etc.) from the analytical one; (3) interference of the microphone itself on the sound field and the flow field; (4) the pulse signal post processing, including the definition on the meaningful length of the signal, identification on the reflection from the sphere and wind tunnel setup.

4.2 Numerical simulation results

4.2.1 Scattering from sphere

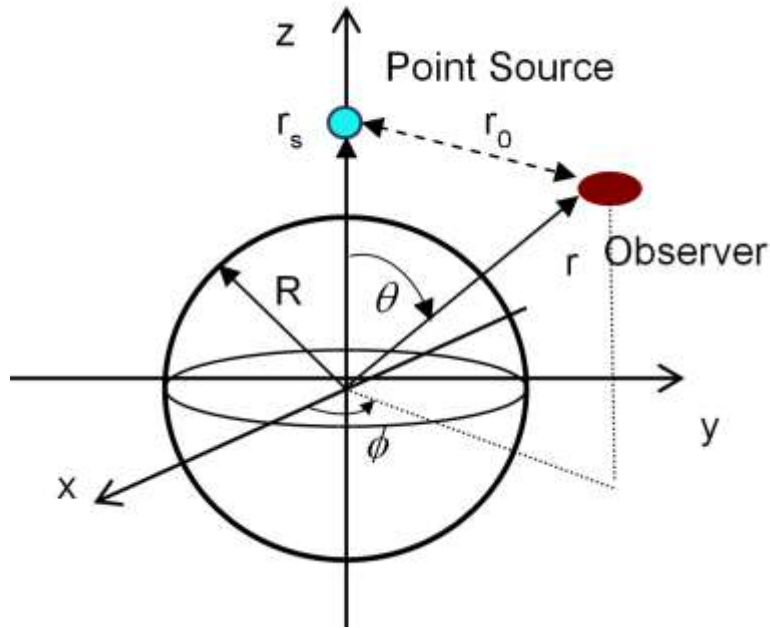


Figure 13. Scheme of acoustic scattering of a point monopole source by a sphere

One of the main objectives of the GARTEUR AG24 is the assessment through validation of the acoustic scattering prediction capabilities available within the group and the possible improvement of the existing tools. The numerical simulations were first conducted for the sphere scattering from a point source with two sphere sizes ($D1=0.12\text{m}$ and $D2=0.34\text{m}$), and various source positions and frequencies. The simulations were first validated with the analytical solution. The schematic relation of the source and observer or microphone in these first simulations is given in Figure 13.

The effect of the geometry discretization can be classified representing the grid size in terms of Points Per Wavelength (PPW). The code-to-code comparisons were conducted using, when possible, the same number of PPW. The grid size ΔX can be defined according to a given PPW; for example for a given PPW, the actual size ΔX of the grid cells is:

$$\Delta X(m) = 340\left(\frac{m}{s}\right)/f(\text{Hz})/PPW$$

PPW	F=2500(Hz)	5000(Hz)	7500(Hz)
7	$\Delta X=0.01943\text{m}$	0.00971m	0.00648m

14	0.00971m	0.00486m	0.00324m
28	0.00486m	0.00243m	0.00162m

Table 3. grid size ΔX as function of frequency and PPW

The large values of PPW correspond to a fine surface grid and therefore lead to large computation times. The grid size for three different PPW values is given in Table 3.

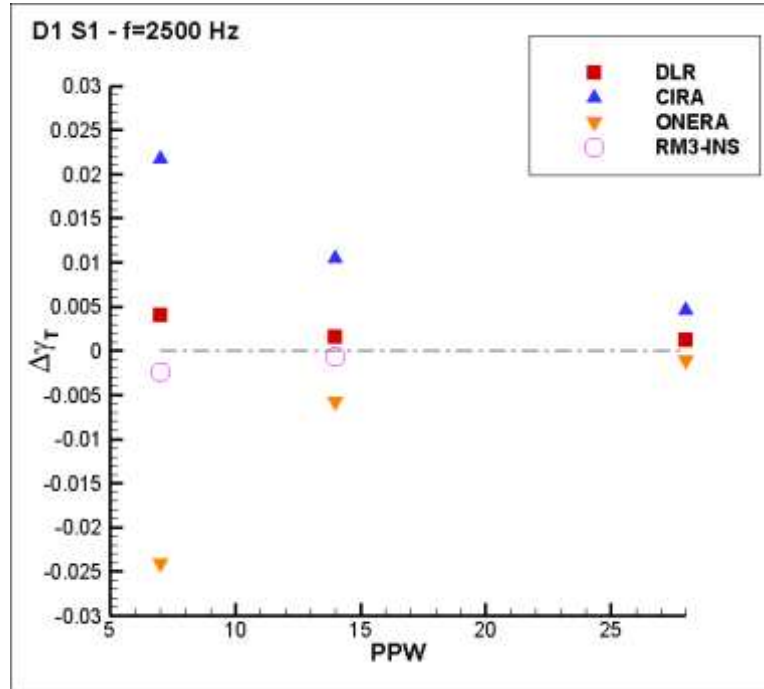
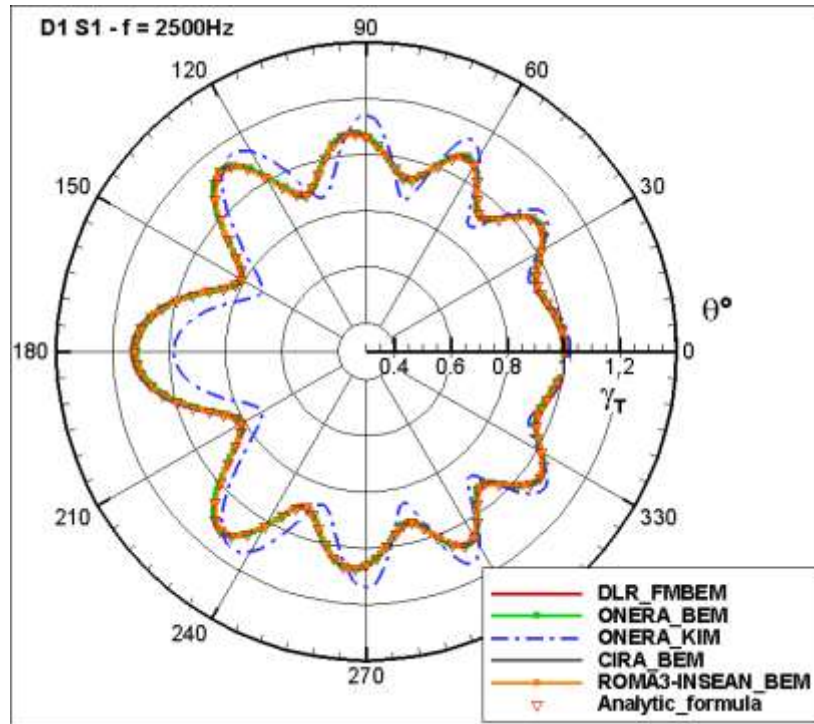


Figure 14. Influences of the numerical discretization error at 2500Hz

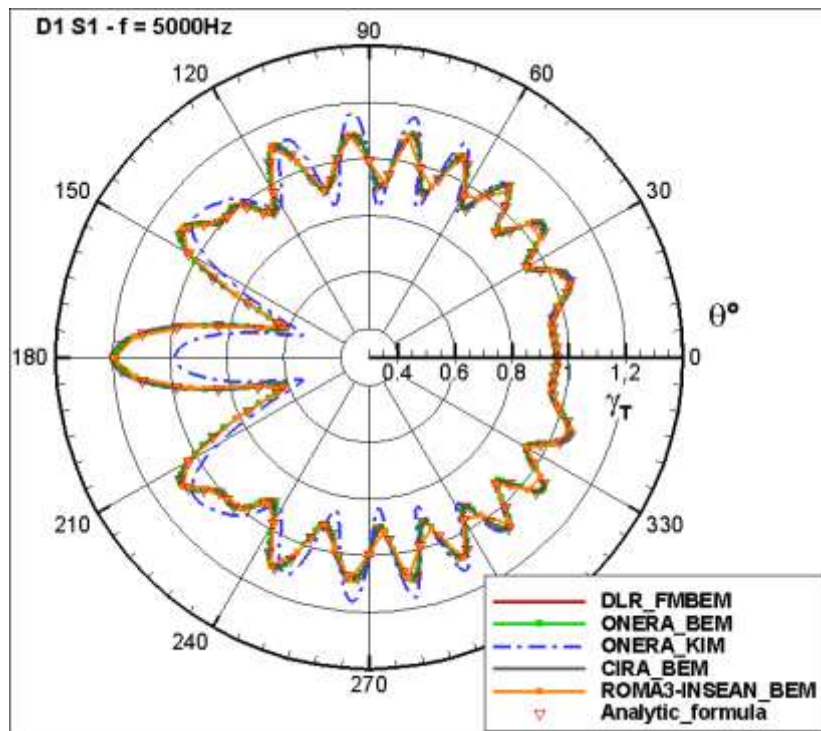
The influences of the numerical discretization as a function of PPW at 2500Hz are summarized in Figure 14. The Results refer to a point source placed at $r_s = 0.32\text{m}$ from the center of the sphere. The sphere has a diameter $D1 = 0.12\text{m}$ and considers as a rigid surface. The results indicate absolute errors defined by the difference between the simulation and the analytical solution, taken from a point in the shadow region at $r = 0.6\text{m}$ and $\theta = 180^\circ$ as shown in Figure 13, where the microphones are located direct below sphere and opposite to the source. In this position, the maximum error occurs as the scattering wave is dominant and thus the solution is most sensitive to the sphere surface discretization. The convergence results with all BEM methods are very similar.

The polar directivities at three frequencies shown in

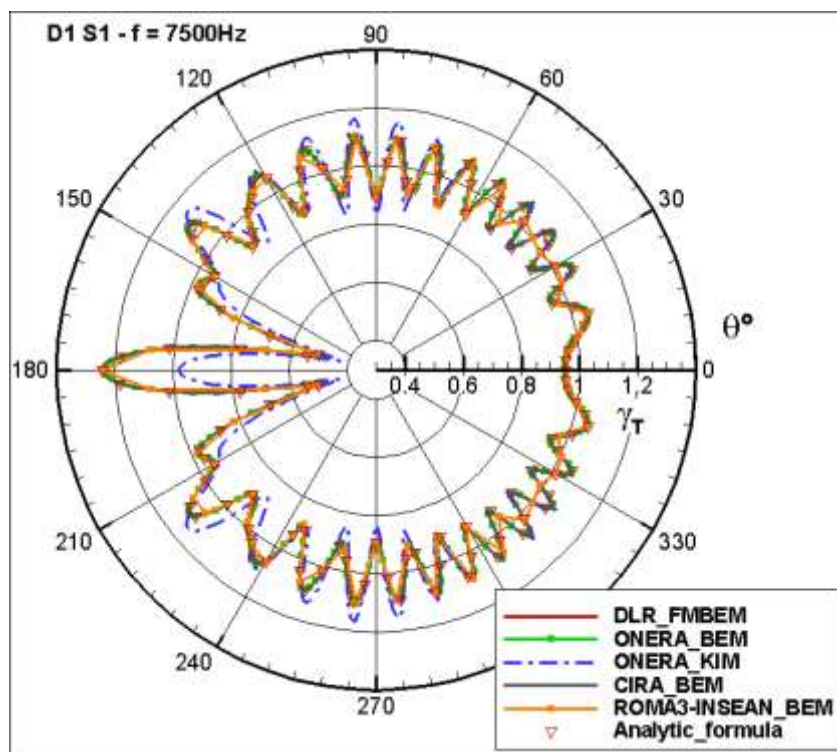
Figure 15 are computed for the observer positions on a circle of $r=0.6m$ with $\phi = 0^\circ$ and θ from 0 to 360° in one degree steps. The sphere surface is discretized with PPW=14. All methods give similar trends which are in good agreement with analytical results. This is especially true when considering the BEM results, which are very close and collapse on the analytical solution. As expected, somewhat poorer results are provided by the flat approximation (FSA) method of the ONERA_KIM code. Although the improvement at high frequency is observed, the area between approximately 120° and 240° (shadow zone) is always of poor accuracy. As mentioned before, FSA method only predicts reflection (by supposing a surface locally flat) and ignores refraction. Consequently, the sphere test case is particularly unsuitable for this approach. However, the rapidity of this approach has to be taken into account when looking at the accuracy.



f=2500Hz



f=5000Hz



f=7500Hz

Figure 15. Comparison of the scattering directivity from the sphere $D1=0.12m$ and source $S=0.32m$, at three different frequencies. PPW=14

For the large sphere ($D2=0.34m$), the scattering at 2500Hz is shown in Figure 16, where NLR CAA results are also included. The shielding factors exhibit a narrow shadow region and lower value of the shielding factor in comparison with the small sphere for this frequency as shown in

Figure 15.

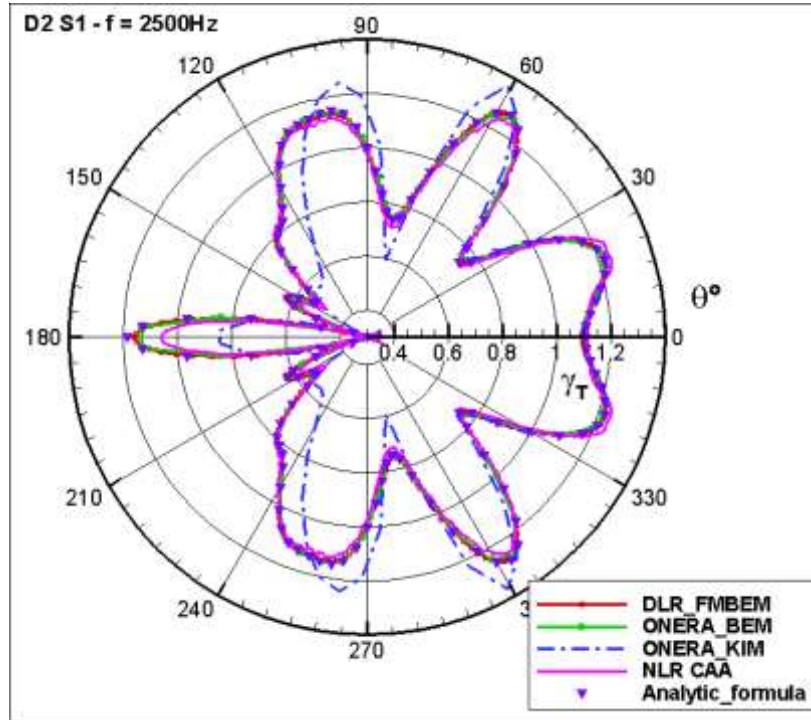


Figure 16. Comparison of the scattering directivity from the sphere $D2=0.34m$ and source $S=0.32m$, $f=2500Hz$. PPW=14

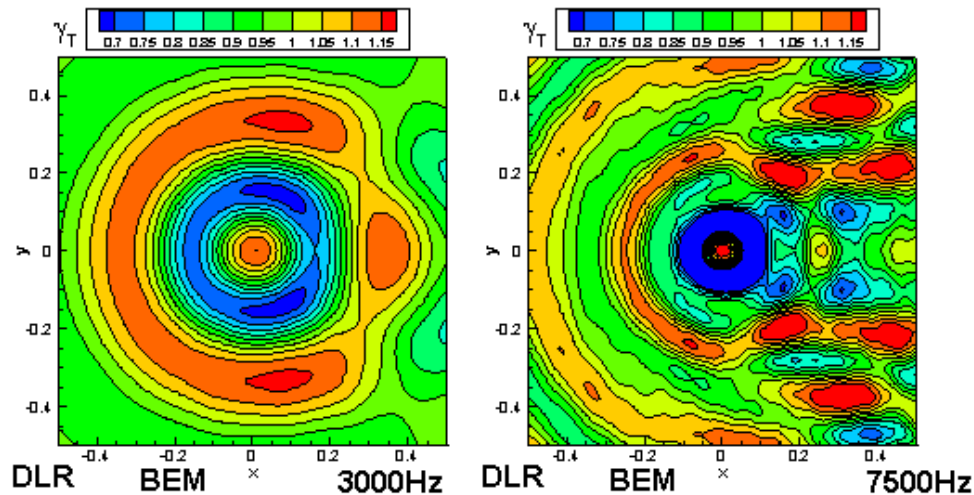
The study highlights again that all BEM methods show the general high level of accuracy of the acoustic scattering models in capturing the analytical solution in terms of magnitude and directivity. The CAA results from NLR show some amplitude error near the 180° angle. Such behavior may be caused by (1) the applied monopole source model, which smoothly distributes the forcing over a few cells and does not capture exactly the singular behavior of the monopole, and (2) the impact of artificial damping that was introduced to counteract spurious modes.

4.2.2 Scattering from Sphere + Sting

The numerical simulations for the configuration with the sting support, as shown in Figure 7, are conducted in order to demonstrate the influence of the sting and to compare with test results. Only the horizontal part of the sting with a

length 0.3867m and diameter ($D=0.028\text{m}$) is considered in the simulation. In order to avoid discrepancies in generating surface mesh with given mesh criteria defined by PPW, a common surface grid is used. The average grid resolution is about 0.00324m which corresponds to 14 PPW at 7500Hz. The source and microphone positions are shown in Figure 7. A point source is located at 0.32m on the z axis above the sphere and the size of the sphere chosen for this example is $D=0.12\text{m}$. The contour plots and the values taken from two dashed lines used in the measurements are compared.

Figure 17 shows the contour plot of the shielding factor on a receiving plane (microphones) given in Figure 7 for two different frequencies at 3000Hz and 7500Hz, respectively. The general shielding characteristics can be observed by the shielding pattern composed by the higher and lower levels in the plot. The higher and lower levels are represented by different colors. The “silent zone” directly below the sphere, where no incident wave can be propagated, is determined entirely by the diffracted waves, which have a small peak showing in red areas. Due to the contribution of the diffraction waves from the sting support, the shielding pattern is deviated from its symmetric circular patterns, especially for the area underneath the sting in positive x direction, where most of the deviations occur. In general, the complexity of the scattering pattern increases with increasing frequency. An increase of higher and lower shielding bands in lateral (y) direction of the sphere (negative x direction) is observed with increasing frequency. The results from BEM method show very good correlation among the partners. The FSA approach proposed by ONERA_KIM provides a good qualitative prediction.



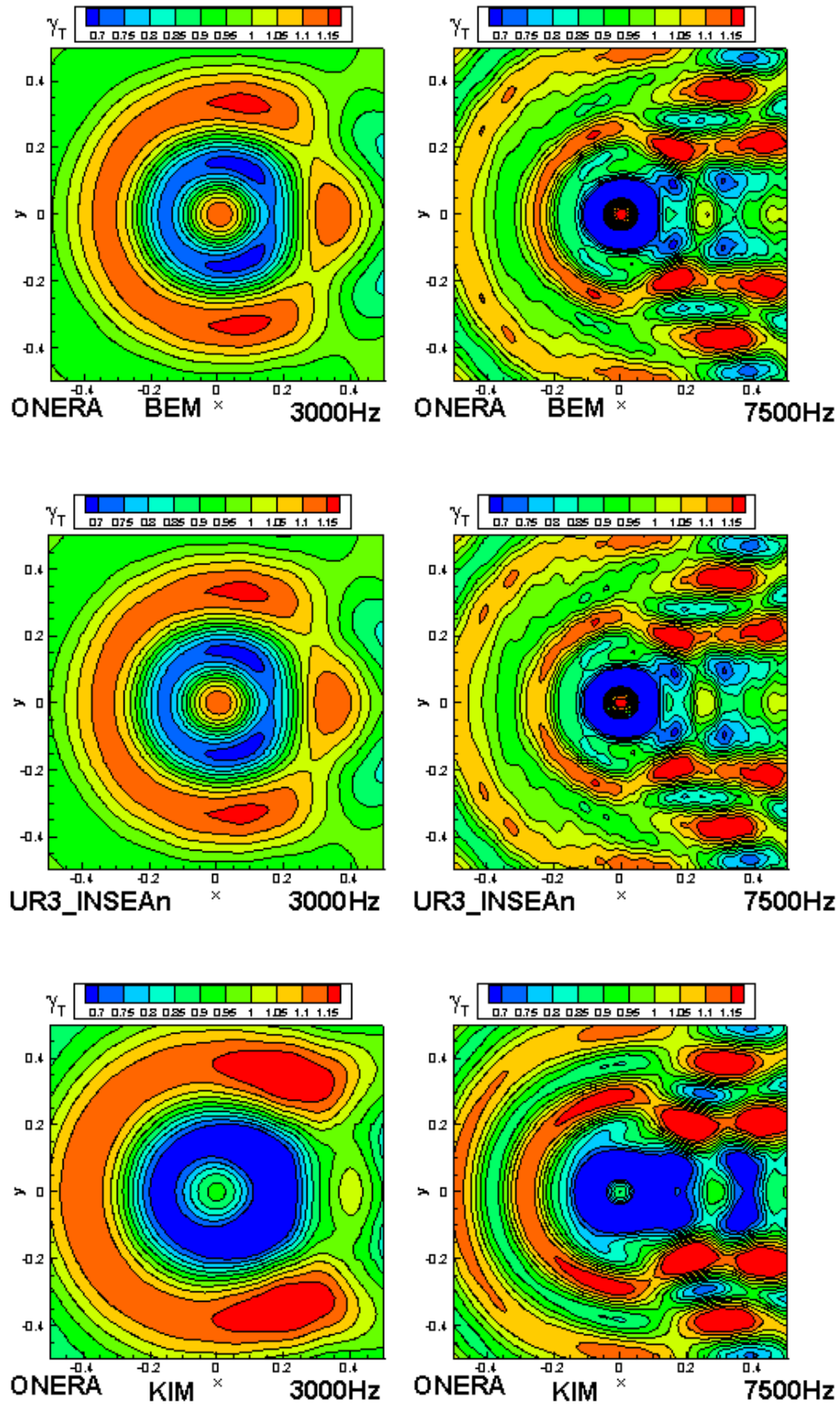
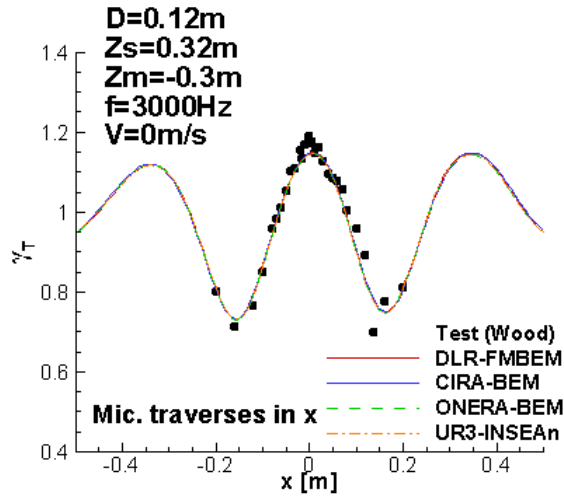
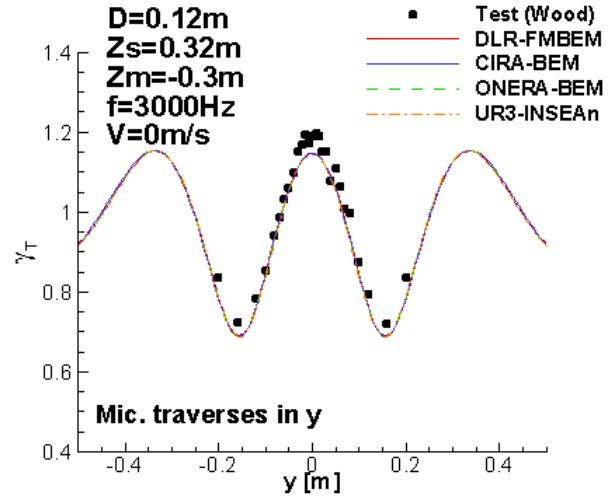


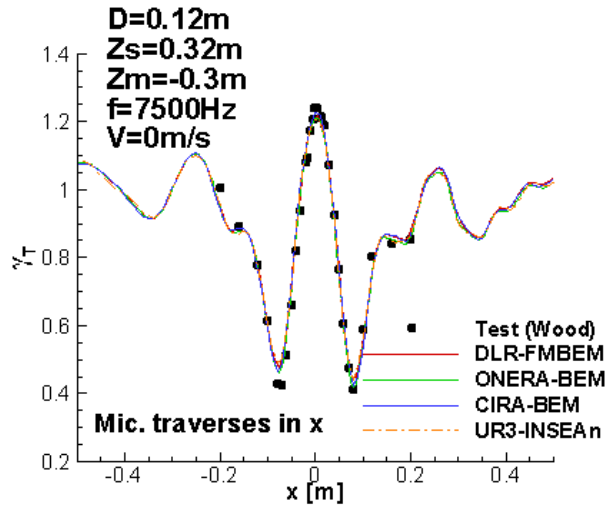
Figure 17. Contour plot of shield factor for the sphere+sting $D=0.12\text{m}$ at $f=3000\text{Hz}, 7500\text{Hz}$, with $V_0=0\text{ m/s}$



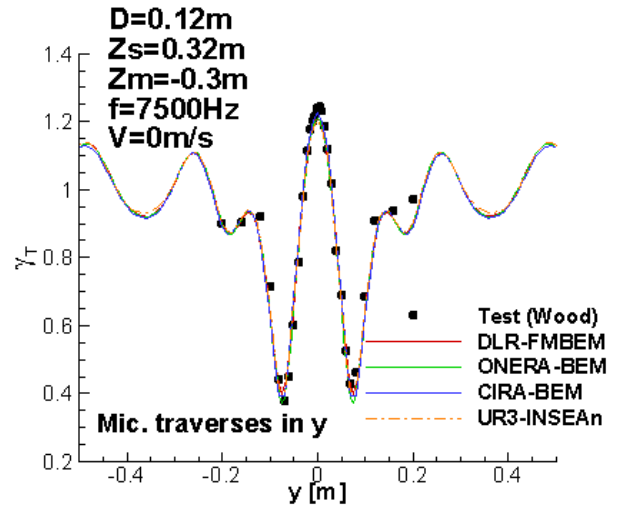
(a) shielding factor at 3000Hz,



Left: X-traverse, Right: Y-traverse



(a) shielding factor at 7500Hz,



Left: X-traverse, Right: Y-traverse

Figure 18. Comparison of the shielding factor with test for the sphere $D=0.12\text{m}$ with sting support

The comparison with the experiment results at two microphone arrays is given in Figure 18. The comparisons of the shielding factor with the experimental data show very good correlations in terms of amplitude and phase. The asymmetry of the scattering in x-direction under the influence of sting is captured by all participants. The agreement among partners is excellent in both traverse directions.

Figure 19 shows the comparison of the shielding factor at 7500Hz under influence of mean flow ($V=45\text{m/s}$). The comparison with the experimental data shows a reasonable good agreement, except the large differences occur

downstream of the sphere (positive x value) as shown in Figure 19 left, where the flow in the downstream of the sphere can be complicated and may contain large flow gradient due to possible separation of the flow field behind the sphere. In the simulations, both DLR and ONERA results consider a uniform mean flow effect, while a potential flow field is considered by UR3_INSEAN (pressure-based Ffowcs-Williams and Hawkings Equation (FWH)). The difference from the test indicates that the flow field used in the simulations may be quite different from the real flow field in the test, especially in the area behind the sphere. The potential flow treatment used by UR3_INSEAN slightly improves the correlation with the test in this area. All of the BEM codes can't consider large flow gradient. The agreement for the lateral array among the partners, as shown in Figure 19 right, is extremely good, indicating little flow effect in this radiation direction.

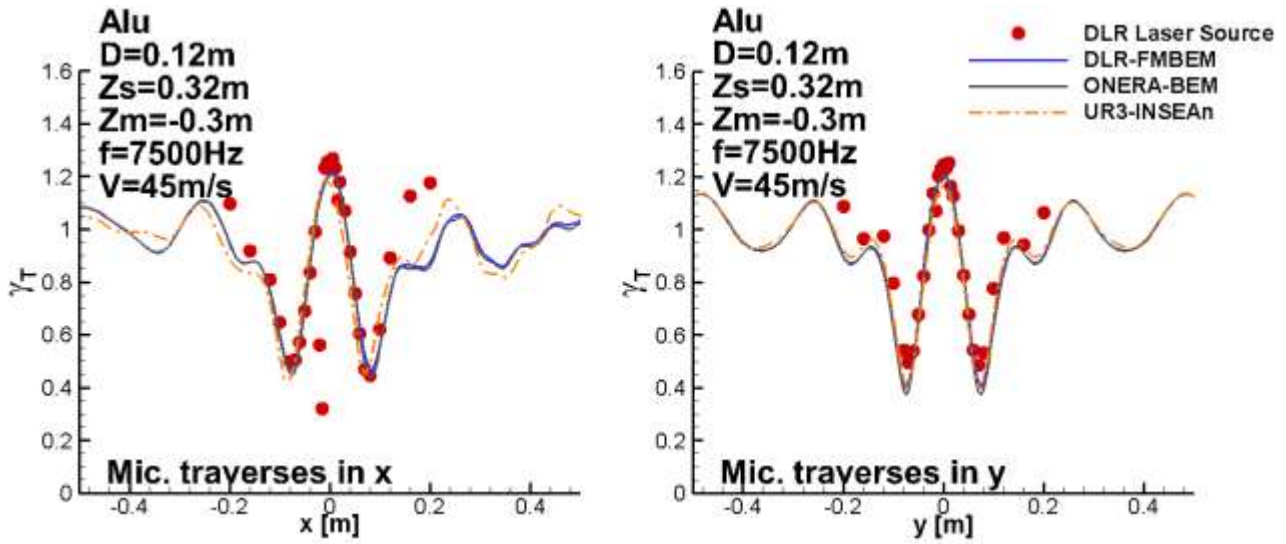
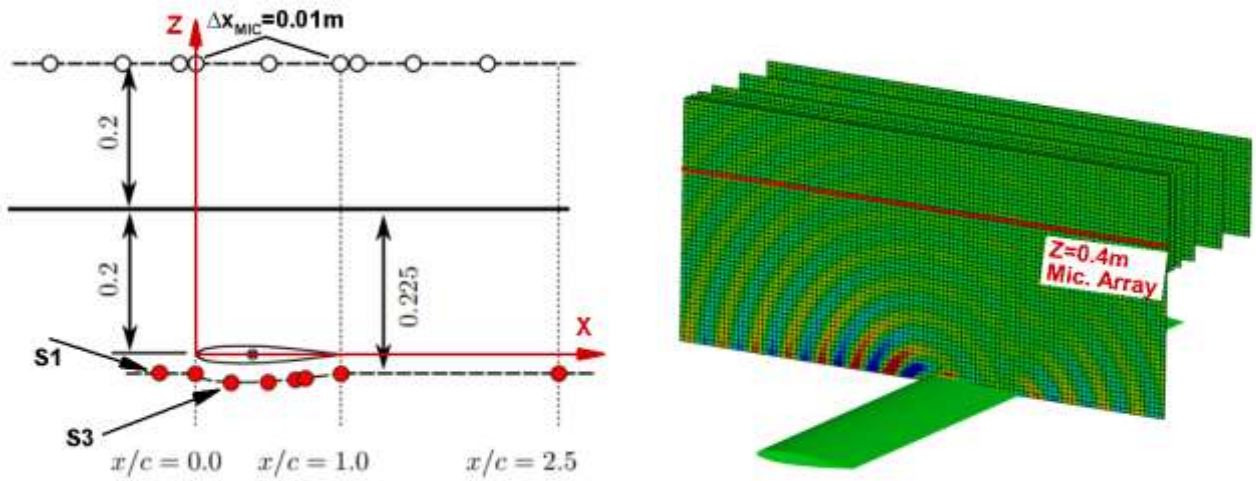


Figure 19. The comparison of the shielding factor with the test for the sphere $D=0.12\text{m}$ with mean flow 45m/s

4.2.3 Scattering from NACA 0012 wing

For a further assessment of the acoustic scattering prediction capabilities, the test cases conducted in the NATO STO (AVT 233 RTG-078) Group have been chosen for the predictions [20]. The experimental data are provided by STO group for the validation. The wind tunnel setup, the coordinate system as well as the relative position between the source position (solid red circles) and the microphones (black open circle) is shown in Figure 20. The microphones are located in the symmetry plane above the wing. For the region $0.0 < x/c < 1.0$, measurements were done with a spatial resolution of $\Delta x = 0.01\text{ m}$ in x , where c is the chord length $c=0.2\text{m}$. No dots are shown for clarity's sake. The selected results from source position S1 $(x,y,z)=(-0.05,0.0,-0.025)\text{m}$ and S3 $(x,y,z)=(0.05,0.0,-0.036841)\text{m}$, as indicated in

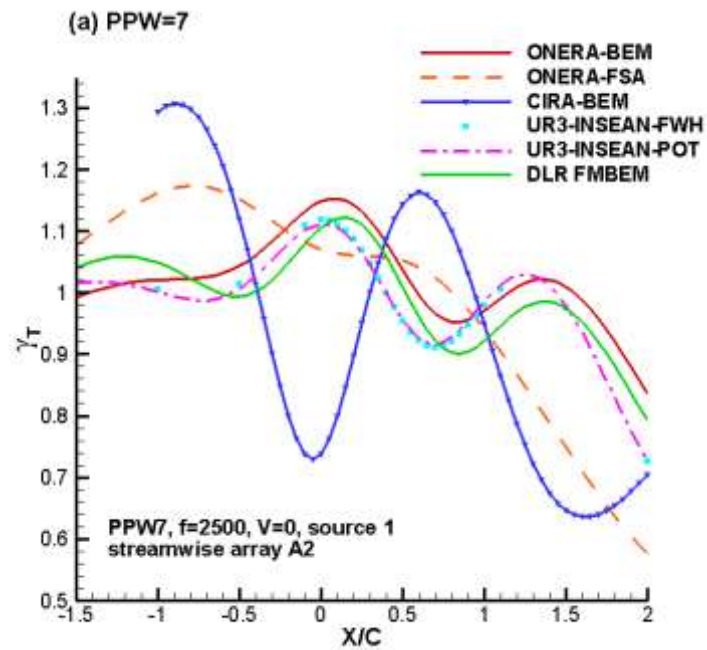
Figure 20a, will be compared with test results. The comparison will be made on the microphone array position, also shown with the red line in Figure 20b.



(a) Source and microphone positions

(b) perspective view of the microphone array position

Figure 20. Coordinate system, source position (S1,S3) and microphones (black open circle)



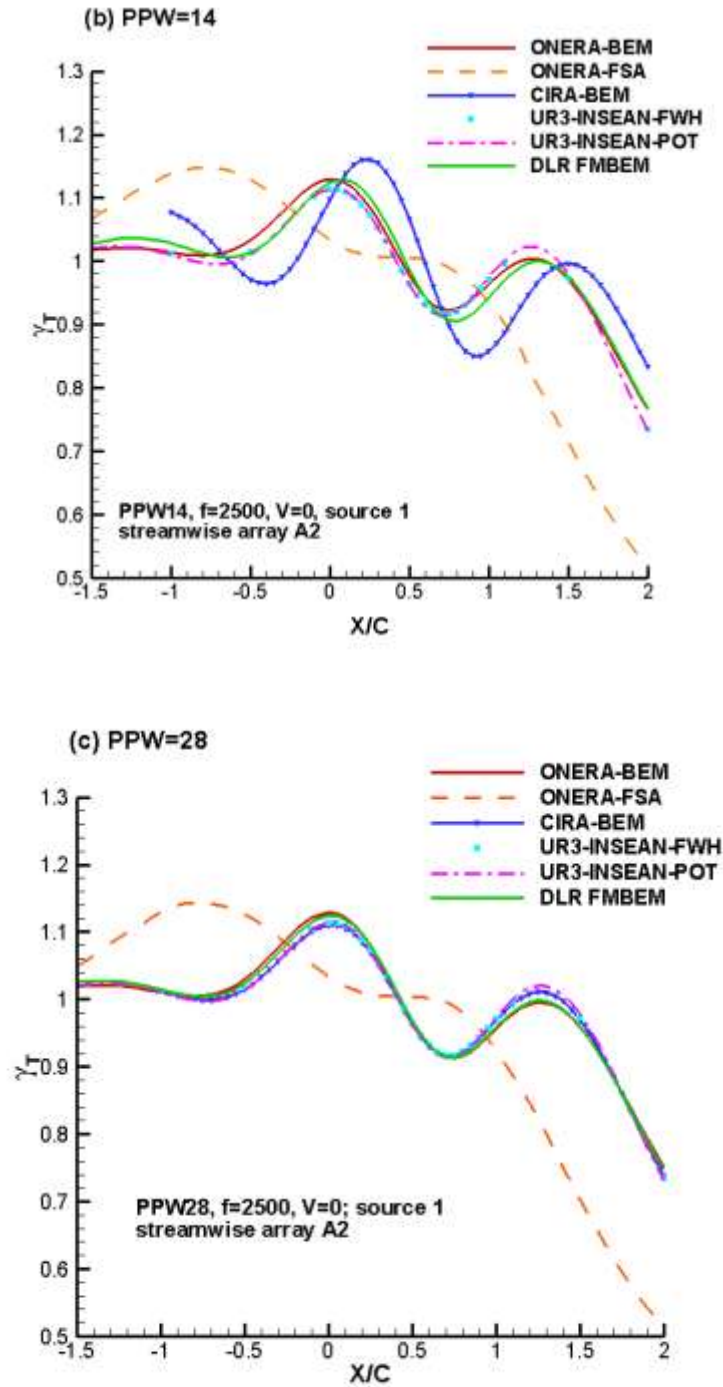
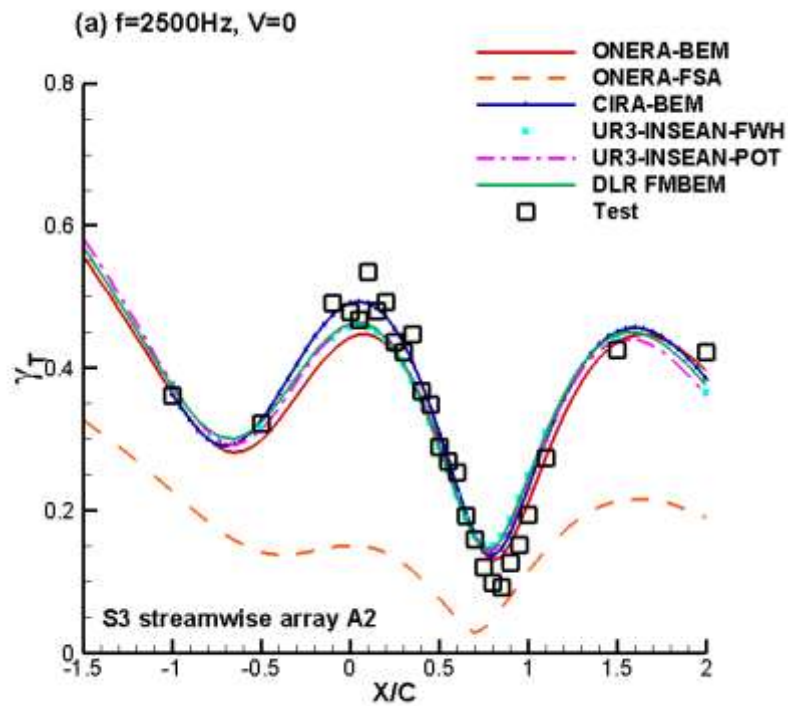


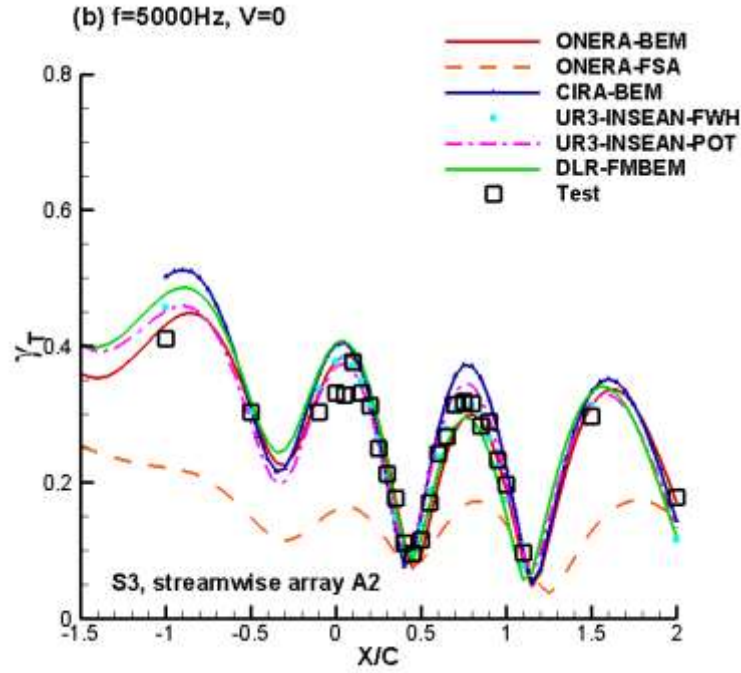
Figure 21. Shielding factor as function of PPW, Source at S1; $f=2500\text{Hz}$; $V=0.0\text{m/s}$

The Effect of the discretization is first studied by varying PPW. All partners use identical meshes with the exception of the University of Roma (UR3) using structured grids. Figure 21 shows the shielding factor at $f=2500\text{Hz}$ as function of PPW for noise source located at S1. No mean flow is considered in this case. The scatter of the results at the lower PPW indicates that the results are more sensitive to the PPW compared to the sphere case. It is obviously that 7 PPW is not

enough to discretize the leading edge of the wing. Almost all BEM formulations tend to coincide with increasing spatial resolution to PPW 28, as can be observed in Figure 21 (c). Although the structured surface mesh is used by UR3, the results from UR3 fit well with that of other partners. This indicates that requiring appropriate PPW to ensure a good representation of the scattering source on the wing surface is more important than the mesh structure. The FSA formulation gives good tendencies even if results are different from the BEM formulations. It has to be pointed out that the FSA method considers only reflections; therefore FSA should not be considered at the same level of the accuracy as the BEM.

The comparison of the numerical simulations with the experiment results for source position S3 (Figure 20) is given in Figure 22 for two frequencies. All methods give similar trends and good correlation with the experiment results. Differently from the source at S1, the simulation show relative large deviation around $x/c=0$ at 2500Hz among the partners although the high spatial resolution PPW=28 is used. For 5000Hz the deviations spread to almost all microphones and especially for far negative x . In comparison with the source position S1, S3 is much closer to the wing, therefore to ensure a good representation of the scattering source on the wing surface, the higher PPW, higher than 28, especially for 5000Hz is required. Due to limitation of different code capabilities, the comparison can only be conducted for PPW=28.





**Figure 22. Comparison of measured and simulated shield factor for Source S3 without mean flow $V=0\text{m/s}$,
PPW=28**

Figure 23 shows the comparison of the shielding factor for source position S3 with a mean flow speed $V=55\text{m/s}$ for two frequencies. All calculations assume the uniform flow, except in ONERA's simulation the mean flow is assumed with potential flow. The BEM results from CIRA, DLR and ONERA show similar characteristics as the results simulated without mean flow shown in Figure 22, indicating minor influence of the flow on the shielding factor. As CIRA, DLR and ONERA method take into account flow effect using the Taylor transformation as described in [14], the same correction is applied on the incident field and the total field. Therefore there is very little flow effect when looking at the shielding factor. The BEM code from UR3-INSEAN uses both pressure-based Ffowcs-Williams and Hawkings Equation (FWH) and velocity-potential-based Helmholtz equation. In the pressure-based FWH code the convective Green's function is applied, while in the potential-based formulation nonlinear effects due to the steady-state aerodynamic mean flow is included. Due to the different approximations on the mean flow effect, the higher discrepancies between UR3-INSEAN and other partners appear. For instance, those based on Taylor Transform neglect M_∞^2 terms affecting both the surface integral contribution and the acoustic delay. The Taylor transformation is clearly an approximation but when looking at the comparisons with CAA in Figure 24 the result is satisfactory for a uniform flow.

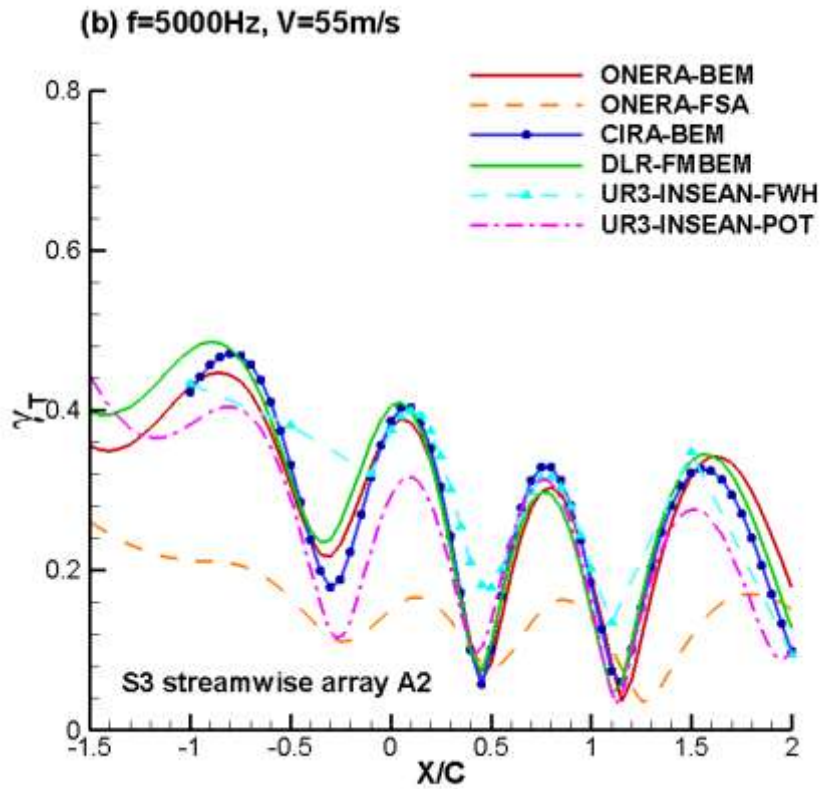
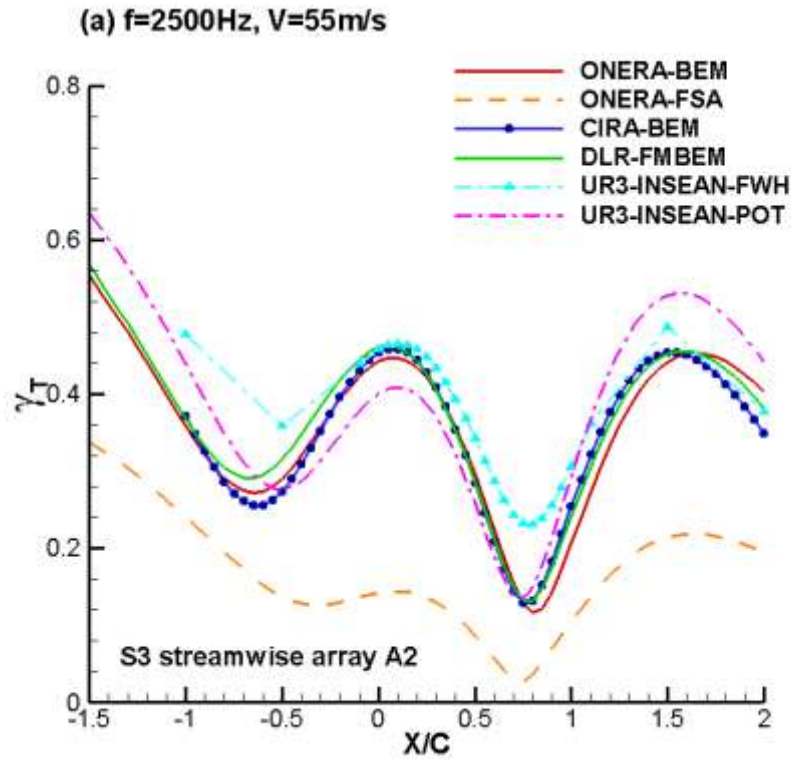
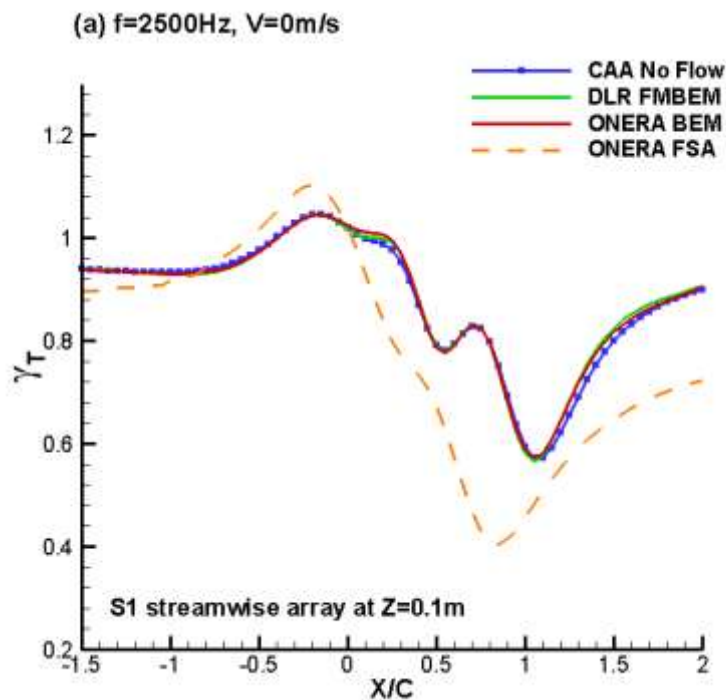


Figure 23. Simulated shield factor for Source S3 with mean flow $V=55\text{m/s}$, $\text{PPW}=28$

Further analyzes are proposed in Figure 24. BEM and FSA results are compared to CAA simulation performed by the ONERA sAbrinA solver which has the capacity to properly take into account non-uniform mean flow. It is important to notice that the comparison is made closer to the airfoil at $Z=0.1m$ to reduce CAA computational time. First of all, in Figure 24a, the comparison is performed without flow. A very good agreement is obtained when comparing BEM and CAA results. Once again, the FSA results are of poorer accuracy but capturing the general trends. In Figure 24b, flow effects are taken into account. When only a uniform flow is taken into account, the impact is weak for all methods involved and the agreement between BEM results are still accurate compared to CAA results. It is also noticeable that the ONERA BEM simulation taking into account potential flow reacts actually just like a uniform flow case. On the other hand, when a potential non-uniform flow is considered, CAA results appear to be impacted especially in the upstream direction ($x/c < 0$) indicated as blue dashed line in Figure 24b. This is again explained by the fact that the uniform flow does not change the way the acoustic waves are scattered. The effect is the same on both direct, incident and scattered wave. This is not the case when non-uniformity of the flow is encountered by acoustic waves in the vicinity of the airfoil.



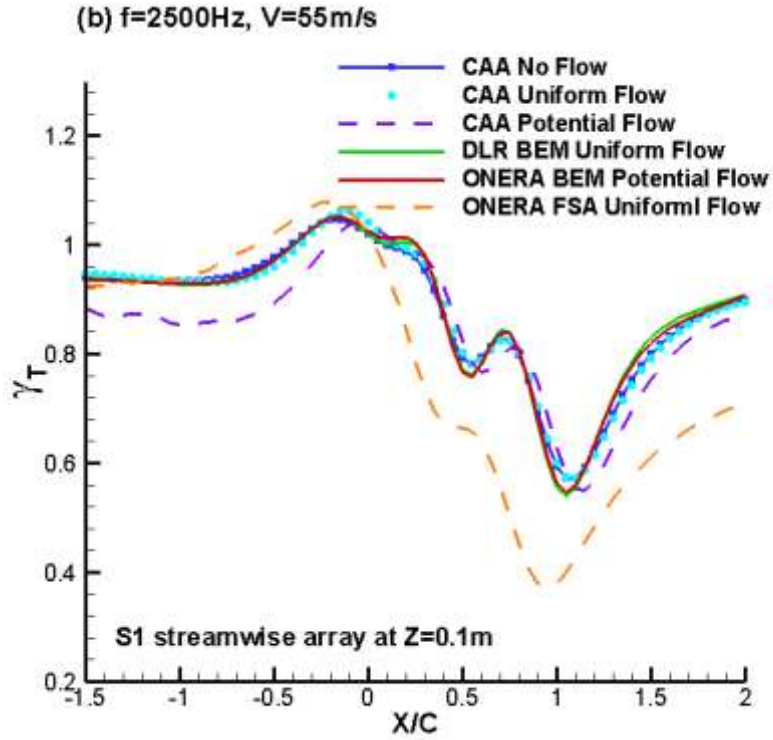


Figure 24. Comparison with ONERA CAA, for Source S1 with mean flow $V=55\text{m/s}$, $\text{PPW}=28$

CONCLUSION REMARKS

In this paper, experimental and numerical investigations of the shielding characteristics of both the sphere and the wing are presented. Comparisons of code-to-code and the code-to-test results or code-to-analytical solutions were carried out. The configurations, herein investigated, are the rigid nonmoving spheres and the wing impinged by the sound waves emitted by a monopole. The test results are derived from the noise source generated from either DLR laser pulse or ONERA SPARC. The numerical comparisons were conducted among different solvers available within the Action Group AG24.

Following concluding remarks can be drawn:

1. Test results from both DLR laser-based and ONERA SPARC noise source capture the general characteristics of the noise shielding effect from a point monopole. The noise shielding results using DLR laser-based non-intrusive sound source provide clear and consistent trends for all considered cases. As the intrusive characteristics of the ONERA SPARC source, the results from ONERA SPARC however indicate large deviation for the aluminum sphere. The possible reasons are (a) the interference of the support structure from the source probes on the sound propagation, (b) the disruption of the metal sphere on ionized electric field

which caused the signal deviation from the point source, and (c) relative lower signal to noise ratio at 3000Hz for the ONERA SPARC source.

2. The accuracy of the measurement results in comparing with the analytical one depends on (a) the position measurement; (b) the deviation of the test sphere from the analytical one; (c) the pulse signal post processing; (d) interference of the microphone and the source probe on the sound field and flow field.
3. The estimated value of the uncertainty on the measured shielding factors is in the range +/- 8% for the case without mean flow. For the case with mean flow, at $U_0=45\text{m/s}$, a slightly larger uncertainty of about +/- 10% is obtained. This slightly larger value is related to the fewer number of valid data blocks available for the Fourier analysis.
4. The numerical simulation results for the sphere scattering case indicate that the BEM methods achieve a high level of accuracy in compared to the analytical solution. The spatial convergence results with all BEM methods are very similar. The shielding factor with mean flow shows the large deviations from the test occur downstream of the sphere as the flow behind the sphere is no longer uniform. The influence of mean flow gradients on the directivity and strength of sound waves propagating can contribute to the large deviations.
5. The assessments of the acoustic scattering from the NACA0012 wing indicate the scattering solution is very sensitive to the source position relative to the wing surface. The comparison indicates that requiring appropriate PPW to ensure a good representation of the scattering source on the wing surface is more important than the mesh structure.
6. The comparison of CAA and BEM results for the NACA0012 wing case indicate a noticeable impact in the upstream direction when the potential non-uniform flow is considered. The approximation on the flow effect, using Tylor transformation, is not able to consider this effect.

ACKNOWLEDGMENTS

The research leading to the presented results has been addressed within the framework of the HC/AG-24 Helicopter Fuselage Scattering Effects for Exterior/Interior Noise Reduction, supported by GARTEUR.

REFERENCES

- [1]. J. Yin, M. Barbarino, H. Brouwer, G. Reboul, M. Gennaretti, G. Bernardini, C. Testa, L. Vigevano, "Helicopter Fuselage Scattering Effects for Exterior/Interior Noise Reduction", Terms of Reference for the GARTEUR Action Group HC/AG-24, April 2015.

- [2]. M. Barbarino, D. Bianco, J. Yin, M. Lummer, G. Reboul, M. Gennaretti, G. Bernardini, C. Testa, "Acoustical methods towards accurate prediction of rotorcraft fuselage scattering", 42nd European Rotorcraft Forum, September 5-8, Lille, France, Paper 62, 2016
- [3]. J. Yin, K-S. Rossignol, J. Bulté, "Acoustic scattering experiments on spheres for studying helicopter noise scattering", 42nd European Rotorcraft Forum, September 5-8, Lille, France, Paper 127, 2016
- [4]. J. Yin, K-S. Rossignol, M. Barbarino, D. Bianco, C. Testa, H. Brouwer S. R. Janssen, G. Reboul, L. Vigevano, G. Bernardini, M. Gennaretti, J. Serafini, C. Poggi, "Acoustical Methods and Experiments for Studying Rotorcraft Fuselage Scattering", 43rd European Rotorcraft Forum (ERF) 2017, 12-15 September, Milan, Italien, 2017.
- [5]. M. Barbarino, "Aeroacoustic Methods for Low-Noise Technologies Design", PhD Thesis, Federico II University, Naples, 2013.
- [6]. M. Barbarino, D. Bianco, "BEM-FMM simulation of uniform mean flows with a new internal-point algorithm for the CHIEF spurious solutions removal", Proceedings of the 23rd International Congress on Sound & Vibration, 10-14 July, 2016.
- [7]. M. Lummer, C. Richtery, C. Pröber, J. Delfs, "Validation of a Model for Open Rotor Noise Predictions and Calculation of Shielding Effects using a Fast BEM", 19th AIAA/CEAS Aeroacoustics Conference (34th AIAA Aeroacoustics Conference), 27 - 29 May 2013.
- [8]. J. C. Kok, "Computation of sound radiation from cylindrical ducts with jets using a high-order finite-volume method", 13rd AIAA/CEAS Aeroacoustics Conference, AIAA paper 2007-3489 (NLR-TP-2007-514), Rome, Italy, 21 - 23 May 2007.
- [9]. G. Rahier, and J. Prieur, "An efficient Kirchhoff integration method for rotor noise prediction starting indifferently from subsonically or supersonically rotating meshes", AHS forum 53, Virginia Beach, May 1997.
- [10]. Juvigny, X., "A Fast algebraic boundary integral solver", 8th World Congress on Computational Mechanics, Venice, Italy, June 2008.
- [11]. V. Rokhlin, "Rapid Solution of Integral Equations of Classical Potential Theory", Journal of Computational Physics, 60, 187–207, 1985.
- [12]. A. J. Burton, G. F. Miller, "The Application of Integral Equation Methods to the Numerical Solution of Some Exterior Boundary-Value Problems", Proc. R. Soc. Lond. A 1971 323 201-210; DOI: 10.1098/rspa.1971.0097. Published 8 June 1971.
- [13]. L. Grasedyck, "Adaptive Recompression of H-matrix for BEM". Technical Report 17, Max-Planck- Institut für Mathematik in den Naturwissenschaften, Leipzig, 2004.

- [14]. Agarwal and Dowling, "The Calculation of Acoustic Shielding of Engine Noise by the Silent Aircraft Airframe", 11th AIAA/CEAS Aeroacoustics Conference, AIAA 2005-2996, 2005
- [15]. S. Redonnet, E. Manoha and P. Sagaut, "Numerical Simulations of Propagation of Small Perturbations Interacting with Flows and Solid Bodies", Proceedings of 7th AIAA/CEAS Aeroacoustics Conference, May 2001.
- [16]. D. C. Mincu, T. Le Garrec, S. Péron and M. Terracol, "Immersed boundary conditions for high order CAA solvers - Aeroacoustics installation effects assessment", 23rd AIAA/CEAS Aeroacoustics Conference, 5-9 June 2017, Denver, Colorado.
- [17]. M. Gennaretti, C. Testa, "A Boundary Integral Formulation for Sound Scattered by Elastic Moving Bodies". JSV-D-06-00750, JOURNAL OF SOUND AND VIBRATIONS, 2008.
- [18]. M. Gennaretti, G. Bernardini, C. Poggi, C. Testa, "A Boundary-Field Integral Formulation for Sound Scattering of Moving Bodies", AIAA-2016-2715 – 22nd AIAA/CEAS Aeroacoustics Conference Lyon (Fr), June 2016.
- [19]. M. Gennaretti, G. Bernardini, C. Poggi, C. Testa, "Lighthill Equation-based Boundary Integral Formulations for Sound Scattering of Moving Bodies", AIAA-2017-3514 – 23rd AIAA/CEAS Aeroacoustics Conference Denver (USA), June 2017.
- [20]. K.-S. Rossignol, J. Delfs. "Analysis of the Noise Shielding Characteristics of a NACA0012 2D Wing", 22nd AIAA/CEAS Aeroacoustics Conference, Lyon, France, 2016
- [21]. K.-S. Rossignol, J. Delfs, F. Boden, "On the Relevance of Convection Effects for a Laser-Generated Sound Source", 21th AIAA/CEAS aeroacoustics conference, AIAA 2015-3146 Dallas, USA, June 2015
- [22]. P. Lebigot, J. Bulté, R. Davy, F. Desmerger, L. Coste, "SPARC: Source imPulsionnelle AéRoACoustique", ONERA Technical Report (in French), N°4/22699, 2015.
- [23]. N. Hosoya, M. Nagata, I. Kajiwara, "Acoustic testing in a very small space based on a point sound source generated by laser-induced breakdown: Stabilization of plasma formation", Journal of Sound and Vibration, Vol. 332, No. 19, 2013, pp. 4572-4583
- [24]. L. Radziemski, D. Cremers, "Laser induced plasmas and applications", Marcel Dekker Inc., New-York, June 1989