

A Novel Single-Inductor Injection-Locked Frequency Divider by Three With Dual-Injection Secondary Locking

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Abstract—The paper presents a comprehensive analysis of signal intermixing taking place across the injectors of frequency-divide-by-three circuits with divide-by-two secondary locking. The analytical results confirmed by circuit simulations provide an insightful understanding of the circuit operation, and inspire the design of a novel single-inductor injection-locked frequency divider (ILFD) by three, where injection is reinforced by a dual-injection scheme with no penalty in power dissipation. The novel circuit, when benchmarked against existing ILFD topologies, optimized in a 65-nm LP CMOS process, shows about a three-time larger locking range with respect to the single-inductor divider by three with a floating-source injector, and about a 40% improvement with respect to the single-inductor divider by three with divide-by-two locking, for the same power dissipation. The novel topology has been adopted in a 15-GHz divider by three for a 5G radio-frequency synthesizer, reaching a 23.6% locking range at 1.56-mW dc power, featuring one of the best performances among divide-by-three ILFDs and a compact size of only 0.09 mm².

Index Terms—CMOS, injection-locked frequency divider (ILFD), divide-by-3, locking range, low power, single inductor, radio-frequency (RF), frequency synthesis, phase-locked loop.

I. INTRODUCTION

IN RECENT years, wireless communications have experienced an incredible growth, and a clear trend exists towards higher working frequencies and millimeter-wave operating bands. In these applications, the frequency divider is a critical block and injection-locked frequency dividers (ILFDs) are attracting more interest than other kinds of architecture, thanks to their ability to obtain both low power consumption and low phase noise performance at high frequencies.

LC-based ILFD circuits are essentially LC-tank oscillators that are locked to an external reference by periodically injecting a current tone into the resonator. To this aim, the most used

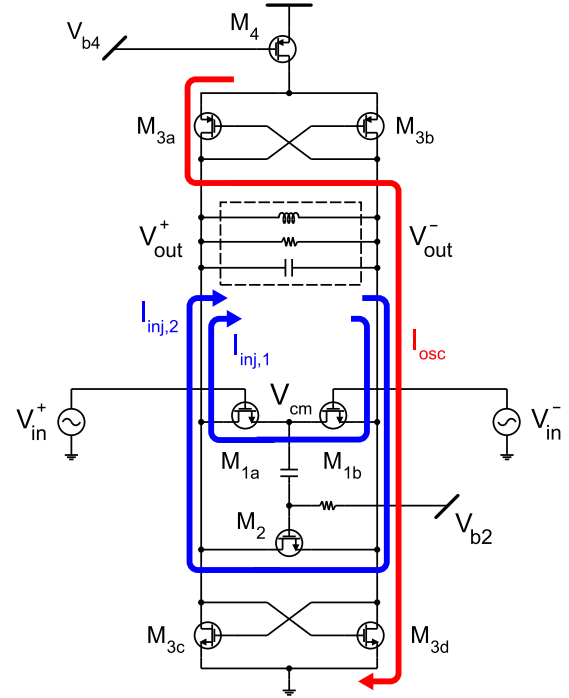


Fig. 1. ILFD by three with divide-by-two locking [2]. The arrows denote the injection currents $I_{inj,1}$ and $I_{inj,2}$, and the oscillation current I_{osc} , that is in phase with the output differential voltage ($V_{out}^+ - V_{out}^-$). The positions of the source terminals of M_{1a} , M_{1b} and M_2 refer to the case of a positive output differential voltage.

injection mechanism is the direct one, in which the injector is directly placed in parallel to the tank. To obtain a division factor of three, the injector is usually implemented with a floating-source differential structure [1].

Most of the improved ILFD topologies recently reported in literature increase performance by using additional inductors [3]–[5], however at the cost of larger area occupation, which is a limited resource in low-cost CMOS millimeter-wave radios. An alternative approach is to keep a single-inductor topology while increasing the injection current amplitude by suitable topological improvements. This is the case of the divide-by-three ILFD with divide-by-two locking, proposed by Wu *et al.* [2] and illustrated in Fig. 1. In this circuit, the floating-source injector (M_{1a} , M_{1b}) generates a first

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injection current, $I_{inj,1}$. A second injector, M_2 , is then added in parallel, driven by a down-converted voltage signal at the source terminal of the floating-source injector, thus generating a further injection current, $I_{inj,2}$, which adds in phase to the first one.

This paper presents a novel comprehensive analysis of the circuit in Fig. 1, describing the intermixing signal generated across both the floating-source and the divide-by-two injectors (Sect. II), first relying on a small-signal-injection approximation and then extending the analysis to large-signal injection. The results, confirmed by circuit simulations, inspire a new divider topology (Sect. III), where a pMOS tail transistor M_4 is used as an extra divide-by-two injection path [6]. A thorough comparison between the performance of conventional and novel divide-by-three ILFD topologies in 65-nm CMOS is provided in Sect. IV. The novel topology is then adopted to design a 15-GHz divide-by-three prescaler for a frequency synthesizer in a 5G wireless radio (Sect. V), reaching a remarkable improvement of the locking range and divider figure of merit (FoM).

II. INTERMIXING IN DIRECT-INJECTION ILFDS

Aim of this section is to highlight the most relevant harmonic terms generated by input-output intermixing across the injectors in Fig. 1. The ILFD will be considered in locking conditions, with the input radial frequency $\omega_{in} = 2\pi f_{in}$, equal to three times the output radial frequency $\omega_{osc} = 2\pi f_{osc}$ (i.e. $\omega_{osc} = \omega$ and $\omega_{in} = 3\omega$). The input and output differential signals, taken as harmonic signals with different phases, can be written as

$$V_{in,d} = V_{in}^+ - V_{in}^- = 2A_{inj} \sin(3\omega t + \gamma) \quad (1)$$

$$V_{out,d} = V_{out}^+ - V_{out}^- = 2A_{out} \sin(\omega t + \phi) \quad (2)$$

where the single-ended zero-peak amplitudes are denoted as A_{inj} and A_{out} , respectively.

The analysis is carried out in two steps. Calculations are first performed by considering the MOSFETs of the injectors as they were in ohmic region for the whole time, i.e. with an I_{ds} current given by

$$I_{ds} = K \cdot (2V_{ov}V_{ds} - V_{ds}^2) \quad (3)$$

where the constant K is $(1/2)\mu C'_{ox}(W/L)$, V_{ov} the overdrive voltage ($V_{gs} - V_T$), and V_T the threshold voltage. The analysis is then extended to the more realistic large-signal operation of the injectors.

A. Floating-Source Injector (Ohmic Regime)

Let us consider first the floating-source injector (M_{1a} and M_{1b} in Fig. 1), whose currents $I_{1,a}$ and $I_{1,b}$ can be calculated relying on (3). During the positive swing of the output voltage, the source terminals of M_{1a} and M_{1b} are oriented as in Fig. 1, so the overdrive voltages of the two MOSFETs are written as

$$V_{ov,1a} = V_{in,dc} + A_{inj} \sin(3\omega t + \gamma) - V_{cm} - V_T \quad (4)$$

$$V_{ov,1b} = V_{in,dc} - A_{inj} \sin(3\omega t + \gamma) - V_{out,dc} + A_{out} \sin(\omega t + \phi) - V_T \quad (5)$$

where $V_{in,dc}$ and $V_{out,dc}$ are the DC bias values of the input and output nodes, and V_{cm} denotes the potential of the common node between M_{1a} and M_{1b} . In a similar way, the drain-source voltages are given by

$$V_{ds,1a} = V_{out,dc} + A_{out} \sin(\omega t + \phi) - V_{cm} \quad (6)$$

$$V_{ds,1b} = V_{cm} - V_{out,dc} + A_{out} \sin(\omega t + \phi). \quad (7)$$

The voltage V_{cm} at the common node is derived, as in [7], by equating the two injectors' current ($I_{1a} = I_{1b}$), using the model in (3), and neglecting the term $(V_{cm} - V_{out,dc})^2$. The latter simplification corresponds to assume small signals across the injector, i.e. $A_{out}, A_{inj} \ll V_{ov}$. The resulting expression of V_{cm} is therefore given by

$$V_{cm} = \left[V_{out,dc} - \frac{A_{out}^2}{4V_{ov,dc}} \right] + \frac{A_{out}^2}{4V_{ov,dc}} \cos(2\omega t + 2\phi) + \frac{A_{inj}A_{out}}{2V_{ov,dc}} \cos(2\omega t + \gamma - \phi) - \frac{A_{inj}A_{out}}{2V_{ov,dc}} \cos(4\omega t + \gamma + \phi) \quad (8)$$

where $V_{ov,dc} = V_{in,dc} - V_{out,dc} - V_T$.

To make the reading easier, let us introduce a more compact notation highlighting the different frequency components of the various signals. For example, (8) will be rewritten as follows

$$V_{cm} = V_{cm}^{(0)} + V_{cm}^{(2^\circ)} + V_{cm}^{(2')} + V_{cm}^{(4')} \quad (9)$$

where $V_{cm}^{(0)}$ is the DC term, while for the harmonics, the number in the superscript refers to the harmonic order, the apex (') highlights that the term is dependent on the input signal phase, γ , and the apex ($^\circ$) means that the term is independent on γ . In (9), $V_{cm}^{(0)}$ and $V_{cm}^{(2^\circ)}$ do not depend on γ .

In a similar way, relying on (9), the harmonic expansion of $V_{ov,1a}$ in (4) can be written as

$$V_{ov,1a} = V_{ov,1a}^{(0)} + V_{ov,1a}^{(3')} - V_{cm}^{(2^\circ)} - V_{cm}^{(2')} - V_{cm}^{(4')} \quad (10)$$

including all the DC terms in $V_{ov,1a}^{(0)}$. Sorting the terms on the basis of the harmonic indexes, it can be rewritten as

$$V_{ov,1a} = V_{ov,1a}^{(0)} - V_{cm}^{(2^\circ)} - V_{cm}^{(2')} + V_{ov,1a}^{(3')} - V_{cm}^{(4')}. \quad (11)$$

Following the same procedure, (6) is rewritten as

$$V_{ds,1a} = V_{ds,1a}^{(0)} + V_{ds,1a}^{(1^\circ)} - V_{cm}^{(2^\circ)} - V_{cm}^{(2')} - V_{cm}^{(4')}. \quad (12)$$

The harmonics of the injector current I_{1a} can be computed combining (3), (11) and (12). Limiting our analysis to the first harmonic, $I_{1a}^{(1)}$, the relevant intermixing terms are those listed in the table in Fig. 2. They can be further divided into two groups, i.e. those retaining the phase γ of the input signal (highlighted by boxes in Fig. 2), and those independent of γ . Thus, using our notation, the first-order harmonic of I_{1a} is correspondingly written as

$$I_{1a}^{(1)} = I_{1a}^{(1')} + I_{1a}^{(1^\circ)} \quad (13)$$

$2 V_{ov,1a} V_{ds,1a}$	$-V_{ds,1a}^2$
$2 V_{ov,1a}^{(0)} V_{ds,1a}^{(1^\circ)}$	$-2 V_{ds,1a}^{(0)} V_{ds,1a}^{(1^\circ)}$
$-2 V_{cm}^{(2')} V_{ds,1a}^{(1^\circ)}$	$2 V_{cm}^{(2')} V_{ds,1a}^{(1^\circ)}$
$-2 V_{cm}^{(2^\circ)} V_{ds,1a}^{(1^\circ)}$	$2 V_{cm}^{(2^\circ)} V_{ds,1a}^{(1^\circ)}$
$-2 V_{ov,1a}^{(3')} V_{cm}^{(2')}$	
$-2 V_{ov,1a}^{(3')} V_{cm}^{(2^\circ)}$	
$-2 V_{ov,1a}^{(3')} V_{cm}^{(4')}$	

Fig. 2. Beating terms generating the harmonic component of the M_{1a} current at the ILFD output frequency. The terms highlighted by boxes are the only ones contributing to the first harmonic of the injector current component dependent on the phase γ of the input signal.

where $I_{1a}^{(1')}$ contributes to the injection current, being dependent on γ , while $I_{1a}^{(1^\circ)}$ is a resistive current independent of the input signal, in phase with $V_{out,d}$. From Fig. 2, it is easy to verify that the only term contributing to $I_{1a}^{(1')}$ is the one from $-2V_{ov,1a}^{(3')} V_{cm}^{(2^\circ)}$. Thus, the effective injection current $I_{inj,1}$, with the direction defined in Fig. 1 is given by

$$I_{inj,1} = -I_{1a}^{(1')} = A_{I,inj,1} \sin(\omega t + \gamma - 2\varphi) \quad (14)$$

where

$$A_{I,inj,1} = K \frac{A_{inj} A_{out}^2}{4V_{ov,dc}}. \quad (15)$$

Without loss of generality, we can assume that the current I_{osc} delivered by the cross-coupled pairs (M_{3a} , M_{3b}) and (M_{3c} , M_{3d}) in Fig. 1 follows the phase of $V_{out,d}$ (i.e. the transconductor introduces negligible delay). Thus, from (2),

$$I_{osc} = A_{I,osc} \sin(\omega t + \varphi). \quad (16)$$

If ω is exactly the resonance frequency of the LC tank, the oscillation current I_{osc} and the injection current $I_{inj,1}$ must have the same phase. Otherwise, the resulting tank current would be delayed with respect to $V_{out,d}$ and the oscillation frequency would depart from resonance [8]. As a result, combining (16) and (14), the following condition holds:

$$\gamma - 2\varphi = \varphi \rightarrow \gamma = 3\varphi. \quad (17)$$

The condition means that, at resonance, the leading edges of the two waveforms in (1) and (2) start synchronously, as it can be readily verified by circuit simulations.

B. Floating-Source Injector (Large-Signal Regime)

As the injectors are fully switched by large driving signals, we may wonder if the simplifications made so far are valid. To this purpose, we will now extend the previous results to large-signal regime and demonstrate that the main conclusions derived from the ohmic model still hold.

Since the injector circuit is symmetric and differentially driven by sine waveforms, the V_{cm} signal is the sum of cosine functions at even harmonics. Thus, (8) can be put in a more general form as follows

$$V_{cm} = V_{cm}^{(0)} + \sum_{n=1}^{\infty} V_{cm}^{(2n^\circ)} + \sum_{n=1}^{\infty} V_{cm}^{(2n')} \quad (18)$$

where $V_{cm}^{(2n^\circ)} \sim \cos(2n\omega t + 2n\varphi)$ and $V_{cm}^{(2n')} \sim \cos(2n\omega t + a\gamma + b\varphi)$ terms, with a and b relative integers.

In this frame, (4) and (6) are replaced by

$$V_{ov,1a} = V_{ov,1a}^{(0)} + A_{inj} \sin(3\omega t + \gamma) + \sum_{n=1}^{\infty} V_{cm}^{(2n^\circ)} - \sum_{n=1}^{\infty} V_{cm}^{(2n')} \quad (19)$$

$$V_{ds,1a} = V_{ds,1a}^{(0)} + A_{out} \sin(\omega t + \varphi) + \sum_{n=1}^{\infty} V_{cm}^{(2n^\circ)} - \sum_{n=1}^{\infty} V_{cm}^{(2n')} \quad (20)$$

As a final step, to be more general, the current flowing through M_{1a} may be written as

$$I_{1a} = G(V_{ov,1a}, V_{ds,1a}) \cdot V_{ds,1a} \quad (21)$$

where a non-linear conductance $G(V_{ov,1a}, V_{ds,1a})$ links the MOSFET current to $V_{ds,1a}$. To derive the harmonic components of I_{1a} , $G(V_{ov,1a}, V_{ds,1a})$ is expanded in Taylor's series

$$G(V_{ov,1a}, V_{ds,1a}) \approx G_0 + G'_x V_{ov,1a} + G'_y V_{ds,1a} + G'_{xx} V_{ov,1a}^2 + G'_{xy} V_{ov,1a} V_{ds,1a} + G'_{yy} V_{ds,1a}^2 + \dots \quad (22)$$

and inserted into (21), together with (19) and (20). Let's now focus on the beat tones at ω , generated by the intermixing terms $V_{ov,1a}^n V_{ds,1a}^m$ and contributing to the component $I_{1a}^{(1)}$. To this aim, note that: i) a beat tone at an odd frequency is generated by intermixing an odd number of harmonics at odd frequencies (e.g. $4\omega - 2\omega - \omega = \omega$); ii) the harmonics at odd frequencies in (19) and (20) are sine functions, while those at even frequencies are cosines. It follows that, since all intermixing terms contributing to $I_{1a}^{(1)}$ result from the product of an odd number of sine functions, they are sine functions. Moreover, as in (13), $I_{1a}^{(1)}$ can be split into a resistive term, $I_{1a}^{(1^\circ)}$, following $V_{out,d} \sim \sin(\omega t + \varphi)$, and an injection current given by tones at ω fulfilling the intermixing condition

$$h \cdot 3\omega t - k \cdot \omega t = \pm \omega t \rightarrow k = 3h \mp 1. \quad (23)$$

In the most general case, the effective injection current, $I_{inj,1}$ may be written as

$$I_{inj,1} = \sum_{h=1}^{\infty} A_{inj,1,h} \sin[\omega t + h\gamma - (3h-1)\varphi] + \sum_{h=1}^{\infty} B_{inj,1,h} \sin[\omega t + (3h+1)\varphi - h\gamma] \quad (24)$$

Note that the simpler (14) corresponds to the first term of (24). Despite the presence of more terms in (24), all

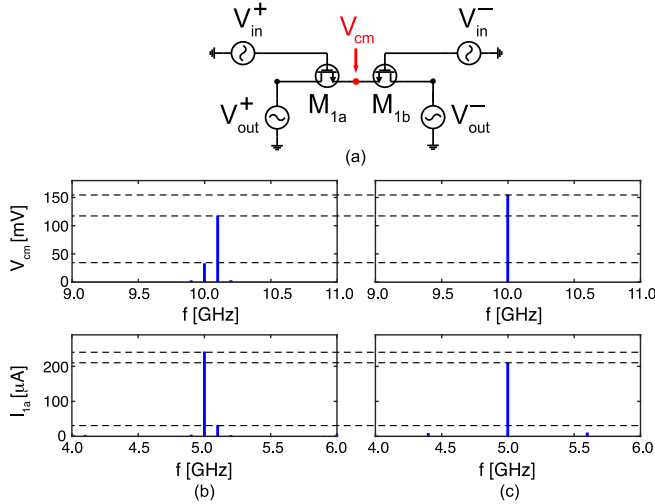


Fig. 3. Spectra of the common-mode voltage, V_{cm} , and of the floating-source injector current I_{1a} . The circuit in (a) shows the simulation setup. The DC bias, $V_{out,dc}$, of both the output nodes and of the body terminals is 450 mV. The DC bias of the input nodes is $V_{in,dc} = 700$ mV. The output nodes are driven by harmonic signals at $f_{out} = 5$ GHz, with opposite phases and a zero-peak voltage amplitude $A_{out} = 200$ mV. The input signals are also harmonic with an amplitude $A_{inj} = 300$ mV, opposite phases and: (b) $f_{in} = 15.1$ GHz, (c) $f_{in} = 15$ GHz, $\gamma = 3\phi$. The transistors' form factors are $(W/L)_{1a} = (W/L)_{1b} = (20\mu\text{m}/0.06\mu\text{m})$.

of them become synchronous with $(\omega t + \phi)$ for $\gamma = 3\phi$, as in the ohmic-regime approximation. The actual orientation of $I_{inj,1}$ depends instead on the magnitude and the signs of $A_{inj,1,h}$, $B_{inj,1,h}$. However, from a practical standpoint, since the amplitude of the beat tones quickly vanishes by increasing its order, the injection current is expected to retain the same orientation of (14). To clearly assess the orientation of $I_{inj,1}$, circuit simulations of the real floating-source injector were performed using the simulation set-up in Fig. 3(a). Two sinusoids (V_{in}^+ and V_{in}^-) with $A_{inj} = 300$ mV zero-peak amplitude drive in anti-phase the gate terminals of M_{1a} and M_{1b} , at frequency f_{in} , while two sinusoids (V_{out}^+ and V_{out}^-) with $A_{out} = 200$ mV at $f_{osc} = 5$ GHz drive in anti-phase the output terminals of the injector. The spectra in Fig. 3(b) refers to $f_{in} = 15.1$ GHz, where the 100-MHz offset between f_{in} and $3f_{osc}$ makes it possible to identify the signal components generated by intermixing with the input signal. In fact, the spectrum of V_{cm} in Fig. 3(b) shows a tone at $2f_{osc} = 10.0$ GHz [which is essentially due to $V_{cm}^{(2^\circ)}$ in (9)], and a tone at $f_{in} - f_{osc} = 10.1$ GHz, which is due to intermixing with the input signal [term $V_{cm}^{(2')}$ in (9)]. The injector current has a tone at $f_{osc} = 5.0$ GHz, resulting from resistive conduction, while intermixing generates the dominant component at $f_{in} - 2f_{osc} = 5.1$ GHz in (14). The other higher order beat tones at $[\dots, 4.8, 4.9, 5.2, \dots]$ GHz are hardly visible. To check for the relative phases, the simulation was repeated by shifting the input signal frequency to $f_{in} = 15$ GHz and taking $\gamma = 3\phi$, thus making the harmonics overlapping. The results are in Fig. 3(c). Note that the V_{cm} amplitude increases, thus confirming that the second-harmonic terms in (8) add up with phase coherence. The current tone at 5 GHz decreases, instead, meaning that the injection current is opposite to $V_{out,d}$

and to the resistive current, $I_{1a}^{(1^\circ)}$, in agreement with the sign in (14).

C. Divide-By-Two Locking

The concept behind the ILFD by three with divide-by-two locking [2] is to use the V_{cm} voltage tone at $f_{in} - f_{osc}$ to drive the additional direct injector M_2 . Figure 1 shows the resulting circuit and the additional injection current, $I_{inj,2}$.

To compute this term, let us apply the ohmic MOSFET model to M_2 , thus writing

$$I_2 = K_2(2V_{ov,2}V_{ds,2} - V_{ds,2}^2). \quad (25)$$

Note that, due to the capacitive coupling between the central node of the floating-source injector and the gate of M_2 , the DC term of V_{cm} (i.e. $V_{cm}^{(0)}$) does not contribute to the M_2 gate signal, $V_{g,2}$. Therefore, we may write

$$V_{g,2} = V_{b2} + (V_{cm} - V_{cm}^{(0)}) \quad (26)$$

leading to the M_2 overdrive voltage

$$V_{ov,2} = V_{b2} + (V_{cm} - V_{cm}^{(0)}) - V_{out,dc} + A_{out} \sin(\omega t + \phi) - V_T \quad (27)$$

and to

$$V_{ov,2} = V_{b2} + V_{cm}^{(2^\circ)} + V_{cm}^{(2')} + V_{cm}^{(4')} - V_{out,dc} + A_{out} \sin(\omega t + \phi) - V_T \quad (28)$$

$$V_{ds,2} = 2A_{out} \sin(\omega t + \phi). \quad (29)$$

Following the compact notation introduced before, we may order the harmonics and list them as

$$V_{ov,2} = V_{ov,2}^{(0)} + V_{ov,2}^{(1^\circ)} + V_{cm}^{(2^\circ)} + V_{cm}^{(2')} + V_{cm}^{(4')} \quad (30)$$

$$V_{ds,2} = V_{ds,2}^{(1^\circ)}. \quad (31)$$

Also in this case, the first harmonic $I_2^{(1)}$ of the total current I_2 of M_2 can be written as

$$I_2^{(1)} = I_2^{(1')} + I_2^{(1^\circ)}. \quad (32)$$

From the products in (25), it turns out that $I_2^{(1)}$ is generated by the following terms:

$$2K_2V_{ov,2}^{(0)}V_{ds,2}^{(1^\circ)}; \quad 2K_2V_{cm}^{(2^\circ)}V_{ds,2}^{(1^\circ)}; \quad 2K_2V_{cm}^{(2')}V_{ds,2}^{(1^\circ)} \quad (33)$$

where the only term contributing to the injection current is due to $2K_2V_{cm}^{(2')}V_{ds,2}^{(1^\circ)}$, which gives a down-converted component depending on the phase γ of the input signal. It turns out that the effective injection current $I_{inj,2}$ of the second injector is

$$I_{inj,2} = -I_2^{(1')} = A_{I,inj,2} \sin(\omega t + \gamma - 2\phi) \quad (34)$$

where

$$A_{I,inj,2} = K_2 \frac{A_{inj} A_{out}^2}{V_{ov,dc}}. \quad (35)$$

Also in this case, a large-signal analysis similar to the previous ones can be carried out. To check for large-signal operation, simulations were performed on the circuit in Fig. 4(a). Each output node is driven by a $A_{out} = 200$ mV zero-to-peak amplitude. The input voltage, V_{in} , driving the M_2 gate,

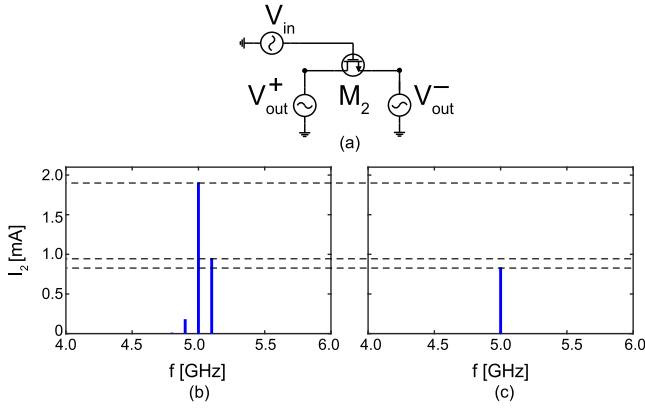


Fig. 4. Spectrum of the current I_2 flowing through the M_2 injector. The circuit in (a) shows the simulation setup. The DC bias, $V_{out,dc}$, of both the output nodes and of the body terminals is 450 mV. The DC bias of the input nodes is $V_{in,dc} = 700$ mV. The output nodes are driven by harmonic signals at $f_{out} = 5$ GHz, with opposite phases and a zero-peak voltage amplitude $A_{out} = 200$ mV. The input signal is also harmonic with a zero-peak voltage amplitude of 100 mV and a frequency: (b) $f_{in} = 10.1$ GHz, (c) $f_{in} = 10$ GHz. The transistor form factor is $(W/L)_2 = (60\mu\text{m}/0.06\mu\text{m})$.

has instead a 100-mV zero-peak amplitude. To be consistent with the relative phase, a 90° phase shift is kept between V_{in} , which is a cosine [see $V_{cm}^{(2)}$ in (8)], and V_{out} [see $V_{out,d}$ in (2)]. The first simulations were performed by using an input signal frequency $f_{in} = 10.1$ GHz, to separate the different current components [Fig. 4(b)]. Then, the simulations were repeated with $f_{in} = 10$ GHz, aligning the harmonic signals with $\gamma = 3\phi$, to verify the relative sign of the different terms [Fig. 4(c)]. Note that the amplitude of the tone at 5 GHz in Fig. 4(c) is equal to the difference between the amplitudes of $I_2^{(1^\circ)}$ at 5 GHz and $I_2^{(1')}$ at 5.1 GHz in Fig. 4(b). The effective injection current, $I_{inj,2}$ is therefore positive in the direction in Fig. 1, as predicted from the sign in (34).

III. NOVEL ILFD TOPOLOGY

The analysis proposed above brings to a key observation. The down-converted voltage tone, $V_{cm}^{(2)}$, can be also exploited to drive the gate terminal of the tail transistor M_4 (Fig. 5), thus generating an additional current component, $I_{inj,3}$, which can reinforce the injection. The injected current $I_{inj,3}$ can be computed by calculating $I_{3a}^{(1')}$, i.e. the component of the first harmonic of the current in M_{3a} that is dependent on the input phase γ .

For small V_{cm} signals, the tail current signal in M_4 can be written as

$$\begin{aligned} I_4 &= I_{dc} - g_{m,4} \left(V_{cm}^{(2^\circ)} + V_{cm}^{(2')} + V_{cm}^{(4')} \right) \\ &= I_4^{(0)} + I_4^{(2^\circ)} + I_4^{(2')} + I_4^{(4')}. \end{aligned} \quad (36)$$

The fundamental harmonic of the mixing transfer function due to the cross-coupled pairs oscillation is

$$X_{ccp}^{(1^\circ)} = \frac{4}{\pi} \sin(\omega t + \phi). \quad (37)$$

The harmonics of the current, I_4 , beat with $X_{ccp}^{(1^\circ)}$, leading to harmonics of the current I_{3a} , that flows via (M_{3a}, M_{3b}) to

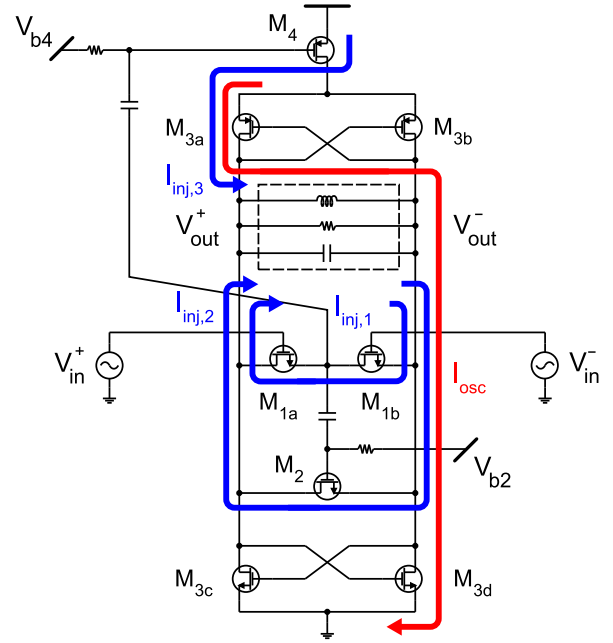


Fig. 5. Novel ILFD by three with dual-injection divide-by-two locking. The arrows denote the injected currents $I_{inj,1}$, $I_{inj,2}$, $I_{inj,3}$, and the oscillation current I_{osc} . The positions of the source terminals of M_{1a} , M_{1b} and M_2 refer to the case of a positive output differential voltage ($V_{out}^+ - V_{out}^-$).

the tank. The first harmonic component, $I_{3a}^{(1')}$, is generated by the following intermixing products:

$$I_4^{(0)} X_{ccp}^{(1^\circ)}; \quad I_4^{(2^\circ)} X_{ccp}^{(1^\circ)}; \quad I_4^{(2')} X_{ccp}^{(1^\circ)} \quad (38)$$

where the only term depending on the phase of the input signal, γ , is the last one:

$$I_4^{(2')} X_{ccp}^{(1^\circ)} = -g_{m,4} \frac{A_{inj} A_{out}}{2V_{ov,dc}} \cos(2\omega t + \gamma - \phi) \frac{4}{\pi} \sin(\omega t + \phi). \quad (39)$$

The expression of the effective injection current $I_{inj,3}$ follows directly from (39) taking the beat tone at ω

$$I_{inj,3} = I_{3a}^{(1')} = A_{I,inj,3} \sin(\omega t + \gamma - 2\phi) \quad (40)$$

where

$$A_{I,inj,3} = \frac{g_{m,4}}{\pi} \frac{A_{inj} A_{out}}{V_{ov,dc}} \sin(\omega t + \gamma - 2\phi). \quad (41)$$

The analysis shows that the tail path gives rise to an injection current which flows out of M_{3a} with the same orientation of I_{osc} , and adds in phase to $I_{inj,1}$ and $I_{inj,2}$, reinforcing the injection-locking mechanism.

Following the same approach used above, the result was checked by simulating the circuit in Fig. 6(a). The input and output voltage amplitudes were the same as in the analysis of the direct-injector M_2 , with a 90° phase shift between the signals. Two simulations were performed, with an input frequency f_{in} of 10.1 GHz and 10 GHz, respectively. Fig. 6(b) and (c) show the resulting spectra. Note that the sum of the amplitudes of the 5-GHz tone, which is in phase with $V_{out,d}$, and the 5.1-GHz injection tone in Fig. 6(b) is equal to the

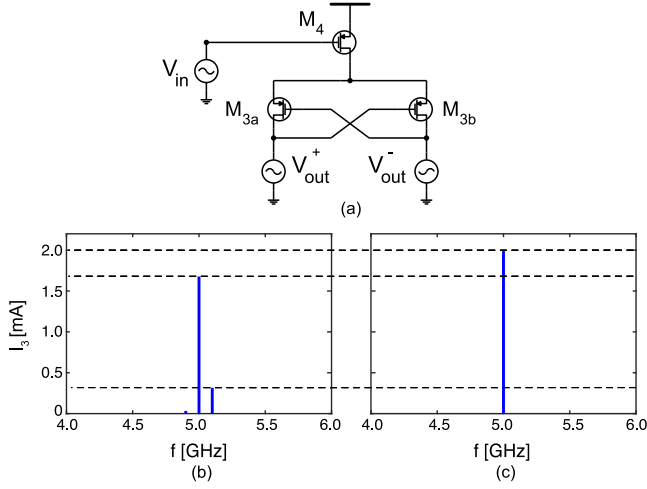


Fig. 6. Spectrum of the current I_3 , flowing via M_{3a} and M_{3b} to the tank. The circuit in (a) shows the simulation setup. The DC bias of the output nodes is $V_{out,dc} = 450$ mV, while the DC bias of the input node is $V_{in,dc} = 550$ mV. The output nodes are driven by harmonic signals at $f_{out} = 5$ GHz, with opposite phases and a zero-peak voltage amplitude $A_{out} = 200$ mV. The input signal is also harmonic with a zero-peak voltage amplitude of 100 mV and a frequency: (b) $f_{in} = 10.1$ GHz, (c) $f_{in} = 10$ GHz. The transistors' form factors are $(W/L)_4 = (56\mu\text{m}/0.06\mu\text{m})$ and $(W/L)_3 = (69\mu\text{m}/0.06\mu\text{m})$.

amplitude of the tone at 5 GHz in Fig. 6(c), in agreement with the analysis.

In the novel circuit, the overall injection current flowing through the tank is given by the coherent superposition of all the three terms, leading to a higher total injection current and, therefore, to a wider locking range [8]:

$$\Delta\omega_{max} \approx \frac{\omega_0}{2Q_{tot}} \frac{I_{inj,1} + I_{inj,2} + I_{inj,3}}{I_{osc}} \quad (42)$$

where Q_{tot} is the tank quality factor, when loaded by the injectors, and $\omega_0 = 2\pi f_0$ is the resonance radial frequency. The first term at the RHS of (42) arises from the injection through the floating-source injector and corresponds to the locking range of the conventional ILFD by three. The second and third terms are generated by the divide-by-two paths through M_2 and M_4 , respectively. Because of the presence of the third contribution, the proposed ILFD is therefore expected to feature a wider locking range, not only with respect to the conventional divide-by-three ILFD, but also compared to the ILFD with divide-by-two locking in Fig. 1, for the same power dissipation.

IV. PERFORMANCE COMPARISON

To quantitatively assess the potentials of the new topology, the schematic-level performance of the three single-inductor ILFD structures were compared, namely the conventional divide-by-three ILFD with floating-source injector, the divide-by-three ILFD with divide-by-two locking and the proposed ILFD. Each ILFD circuit was designed in a 65-nm LP CMOS technology, and, to perform a fair comparison, separately optimized to meet the same performance: (i) a free-running oscillation frequency of 5 GHz (i.e. the center frequency of the input locking range is 15 GHz), (ii) a DC current consumption of 2.2 mA, (corresponding to a DC power consumption of

2.64 mW for a 1.2 V voltage supply) and (iii) an output single-ended voltage amplitude, A_{out} , larger than 0.2 V.

The ILFDs were designed with complementary cross-coupled pairs to halve the DC power consumption of the circuit for the same oscillation amplitude, keeping the output voltage swing within the supply voltage rails, thus improving the circuit reliability. In all the three ILFDs, the tail current generators were implemented with p-type MOSFETs. Low-threshold-voltage devices were used for all the transistors. In this way, the cross-coupled pairs have enough voltage headroom despite the three stacked transistors, and the injectors have reduced switching times and higher current capacity. Further reduction of their threshold voltage was obtained by tying the body terminals to the center tap of the tank inductor, thus preventing body effect [9].

The target oscillation amplitude for a given power consumption sets the minimum load parallel resistance across the tank to $R_{tot} \approx 200 \Omega$. The latter value is given by the shunt composition of the injector resistance, R_{inj} , and of the resistance, R_L , accounting for the intrinsic tank losses.

To boost the injected currents, the injectors' width must be maximized, thus reducing R_{inj} , though keeping the R_{tot} requirement. Therefore, to leave room to injectors' conductivity, the R_L value must be maximized. Since $R_L = \omega_0 L Q_L$, this, in turn, calls for a large inductance, L . In practice, the inductor value was chosen as $L = 4.1$ nH with a quality factor $Q_L = 20$, corresponding to $R_L \approx 2.5$ k Ω at the 5-GHz resonance frequency.

In the conventional ILFD by three, the size of the injector was decided by sweeping the form factors of M_{1a} and M_{1b} , from $(W/L)_1 = (80\mu\text{m}/0.06\mu\text{m}) = 1333$ to $(96\mu\text{m}/0.06\mu\text{m}) = 1600$, and their gate bias, V_{b1} , from 550 mV to 850 mV. By increasing V_{b1} , the locking range increases since the MOSFETs are on for a longer time interval, thus resulting in a higher injected current. Simulations show that the maximum locking range is obtained for V_{b1} ranging from 650 mV to 750 mV, at the cost of a tolerable reduction of the output amplitude. Beyond this point, the locking range does not increase further, while the output voltage amplitude is significantly degraded. Based on these results, V_{b1} was set at 750 mV and $(W/L)_1$ was set to $(88\mu\text{m}/0.06\mu\text{m}) = 1466$ for both M_{1a} and M_{1b} .

For the ILFD with divide-by-two locking in Fig. 1, the gate bias of the floating-source injector was kept to $V_{b1} = 750$ mV, as above. To size the additional injector M_2 , a similar optimization procedure was followed. The form factor of the floating-source injector was progressively reduced to leave room to lower the resistance of the second injector, in parallel to the tank, for the same target R_{tot} . For each $(W/L)_1$ value, the dependence of the oscillation amplitude and the locking range vs. $(W/L)_2$ (i.e. the form factor of M_2) and V_{b2} were derived. The optimal values were identified as $(W/L)_1 = (20\mu\text{m}/0.06\mu\text{m}) = 333$, and $(W/L)_2 = (60\mu\text{m}/0.06\mu\text{m}) = 1000$ for $V_{b2} = 650$ mV.

Note that the optimal sizing is reached with M_2 three times bigger than M_{1a} and M_{1b} . This outcome is in line with the results of the harmonic analysis. In fact, by comparing (15) and (35) it turns out that for the same K value of the

Additional transistors (M_T in Fig. 8), switchable with a six-bits thermometric coding, were added in parallel to M_4 , to reach the target oscillation amplitude also on process corners, by properly changing the DC current value. Their gates are not modulated by V_{cm} , not to increase signal losses due to the higher parasitic capacitance in series to the AC coupling. They are instead connected to a fixed voltage bias, with a 6-pF C_F capacitance to filter noise and disturbances coming from the external bias network.

TABLE II
COMPARISON WITH THE STATE OF ART OF INJECTION-LOCKED FREQUENCY DIVIDERS BY THREE[‡]

Ref.	[4] ^a	[5] ^a	[10] ^a	[11] ^a	[12] ^a	[13] ^a	[14] ^a	[15] ^a	[2] ^a	This work ^b
Tech.	0.18 μm	0.13 μm	0.18 μm	0.18 μm	0.18 μm	0.18 μm	90 nm	0.18 μm	0.18 μm	65 nm
# of inductors	5	5 ^c	3	3	3	2	1	1	1	1
Area (mm^2) ^d	0.81	0.83 ^c	0.67	0.43	0.53	0.47	0.14	0.22	0.14	0.09
V_{DD} (V)	0.9	0.5	0.8	1.8	1.4	0.8	0.5	1.45	1.2	1.2
P_{diss} (mW)	6.76	2.05	7.72	3.90	5.60	4.90	2.85	5.13	4.20	1.56
f_{center} (GHz)	8.43	14.55	8.00	22.10	9.15	10.50	28.95	26.35	14.20	14.85
Lock Range (%)	84.2	35.0	50.0 ^f	15.4 ^f	53.6	47.6	15.5 ^f	12.5	34.3	23.6
FoM (%/mW)	12.5	17.1	6.5	3.9	9.6	9.7	5.4	2.4	8.2	15.1

[‡] All data refers to 0-dBm input power.

^a Measured results.

^b Post-layout simulation results @ $T = 100^\circ\text{C}$.

^c One inductor is implemented with external bondwire.

^d Estimated from chip size (if not explicitly reported).

^e Chip size.

^f No varactors used.

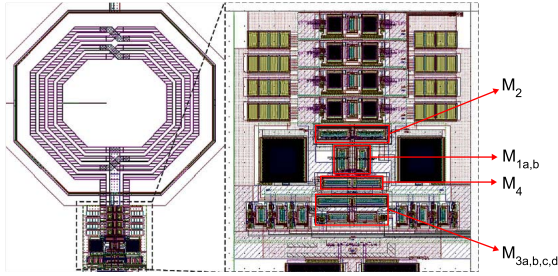


Fig. 9. Layout of the designed single-inductor ILFD (left) and zoomed view of the ILFD core (right).

Figure 9 shows the layout implementation of the designed ILFD. To minimize tank losses, the capacitor bank was placed as close as possible to the inductor. Since the M_2 injector has the largest injection strength, it is placed very close to the LC tank. The floating-source injector is beside it, and the tail transistor M_4 follows. With this choice, M_4 is located as close as possible to the p-type cross-coupled pairs (M_{3a} , M_{3b}), thus minimizing the stray capacitance at its drain node.

The netlist was first extracted from the layout and then simulated with the PSS analysis of Cadence SpectreRF[®]. To better account for the impact of the top metal levels on both the inductance and the quality factor values, the RC parasitics of the ILFD core were extracted with Mentor Graphics Calibre[®] xRC, while the RLC parasitics of the coil and its interconnections were achieved using Keysight Momentum[®] electromagnetic simulator. The simulations were carried out on the post-layout extracted netlist, considering a $T = 100^\circ\text{C}$ temperature, which is the worst case for thermal noise and tank quality factor.

The plot in Fig. 10 shows the input sensitivity curves of the ILFD at the DC power of 1.56 mW as a function of the input frequency f_{in} . The five curves correspond to the possible settings of the capacitive bank. The widest locking range of 28% (12.9 to 17.1 GHz) is reached for $A_{inj} = 0.7$ V. With $A_{inj} = 0.3$ V, the locking range is 23.6% (13.1 to 16.6 GHz), and, even with $A_{inj} = 0.15$ V, it still reaches a remarkable value of 19.7% (13.3 to 16.2 GHz).

Figure 11 shows the zero-peak amplitude of the single-ended output oscillation and the DC power, for $A_{inj} = 0.3$ V input voltage amplitude. The output differential amplitude is about 0.44 V, and it is rather constant along the

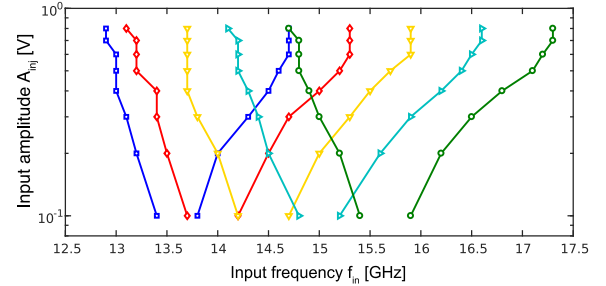


Fig. 10. Input sensitivity curves from post-layout simulations at $T = 100^\circ\text{C}$.

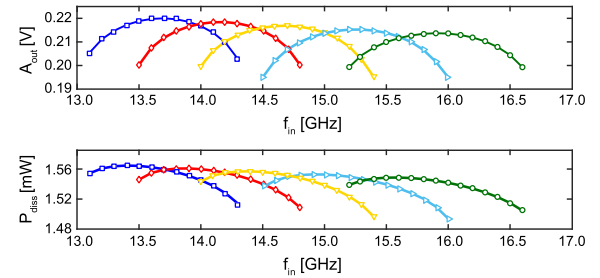


Fig. 11. Single-ended zero-peak output voltage amplitude, A_{out} , and DC power consumption with $A_{inj} = 0.3$ V, from post-layout simulation at $T = 100^\circ\text{C}$.

whole locking range, with proper setting of the capacitor bank. The same result holds for the dissipated power, which ranges between 1.52 and 1.56 mW.

Figure 12 shows the phase noise at the output of the ILFD, with $A_{inj} = 0.3$ V at 14.9 GHz, obtained from SpectreRF pnoise analysis. The white noise is -143.5 dBc/Hz, while the flicker has a corner frequency of 280 kHz. Finally, Table II compares the design figures with state-of-art divide-by-three ILFDs working with 0-dBm input power using the FoM values defined as in [10]

$$\text{FoM} = \frac{\text{LR}(\%) }{P_{diss}(\text{mW})}. \quad (43)$$

Note that the proposed divider has the best FoM among those using a single inductor (last four columns in Table II) and features, in general, one of the highest FoM values among multi-inductor stages. To the best of our knowledge, only the divider proposed in [5] shows a similar FoM, but it needs five inductors instead than one. Thanks to the use of a single

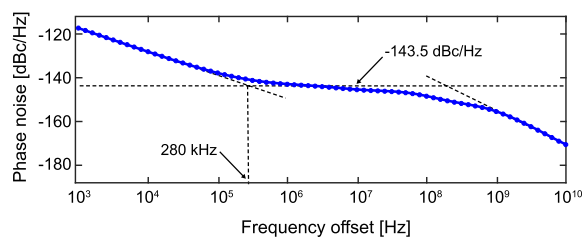


Fig. 12. Phase noise spectrum of the 4.96 GHz output signal with $A_{inj} = 0.3$ V, from post-layout simulations at $T = 100^\circ\text{C}$.

inductor, the novel circuit occupies, instead, a very small area of only $332\ \mu\text{m}$ by $274\ \mu\text{m}$, that is $0.09\ \text{mm}^2$.

VI. CONCLUSION

A detailed analysis of the signal intermixing taking place across the injectors of the divider by three with divide-by-two locking was presented, providing deeper insights in circuit operation and opening the way to the invention of a new divide-by-three ILFD. The latter widens by about 40% the typical locking range obtained with conventional divide-by-two locking in a 65-nm LP CMOS technology. The novel topology has also been adopted in the design of a 15-GHz divide-by-three for a frequency synthesizer targeting 5G specifications. In post-layout simulations at 100°C , the circuit reaches a 23.6% locking range at 1.56-mW DC power, featuring one of the best performance among divide-by-three ILFDs and, using just a single inductor, it occupies only $0.09\ \text{mm}^2$.

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